110-1 ENGINEERING MATHEMATICS HW2

Due Date: 2021/11/03 (2pages)

Part I: Find the general solution of the given differential equation.

1.
$$y' + 3x^2y = x^2$$

Part II: Bernoulli equation

2.
$$x \frac{dy}{dx} + y = x^2 y^2$$

Part III: Solve by substitution

3.
$$(y^2 + yx)dx - x^2dy = 0$$

Part IV: Find a member of the family that is a solution of the initial-value problem.(find c_1,c_2)

4.
$$y = c_1 e^x + c_2 e^{-x}$$
, $(-\infty, \infty)$; $y'' - y = 0$,

$$y(0) = 0, y'(0) = 1$$

Part V: Reduction of Order(find a second solution y_2)

5.
$$y'' + 16y = 0$$
, $y_1 = \cos 4x$

6.
$$xy'' + y' = 0$$
, $y_1 = \ln x$

Part VI: Homogeneous Linear Equation with Constant

Coefficients(find the general solution, e.g. $y = c_1 e^{?x} + c_2 e^{?x} +$

…)

7.
$$y'' - y' - 6y = 0$$

8.
$$y''' + 3y'' + 3y' + y = 0$$

Part VII: Undetermined Coefficients

9.
$$\frac{1}{4}y'' + y' + y = x^2 - 2x$$

10.
$$y'' + 2y' + y = \sin x + 3\cos 2x$$