

Selected exercises for Chapter 3: 3.3 from 4th edition. 3.20, 3.21, 3.22, 3.23, 3.24, 3.27, 3.29, 3.41, 3.42, 3.43

3.20

$0C000000_{16} = 0000\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000_2$

$201326592_{10} =$

in both cases.

3.21 jal 0x00000000

3.22

$0x0C000000 = 0000\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000$

$= 0\ 0001\ 1000\ 0000\ 0000\ 0000\ 0000\ 000$

sign is positive

$\text{exp} = 0 \times 18 = 24 - 127 = -103$

there is a hidden 1

mantissa = 0

answer = 1.0×2^{-103}

3.23 $63.25 = 10^0 = 111111.01 \times 2^0$

normalize, move binary point 5 to the left

1.1111101×2^5

sign = positive, $\text{exp} = 127 + 5 = 132$

Final bit pattern: 0 1000 0100 1111 1010 0000 0000 0000 000

$= 0100\ 0010\ 0111\ 1101\ 0000\ 0000\ 0000\ 0000 = 0x427D0000$

3.24 $63.25 \times 100 = 111111.01 \times 2^0$

normalize, move binary point 5 to the left

1.1111101×2^5

sign = positive, $\text{exp} = 1023 + 5 = 1028$

Final bit pattern:

0 100 0000 0100 1111 1010 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000

0000

$= 0x404FA00000000000$

3.27 [20] <§3.5> IEEE 754-2008 contains a half precision that is only 16 bits wide. The leftmost bit is still the sign bit, the exponent is 5 bits wide and has a bias of 15, and the mantissa is 10 bits long. A hidden 1 is assumed. Write down the bit pattern to represent -1.5625×10^{-1} assuming a version of this format, which uses

an excess-15 (not excess-16 in the textbook) format to store the exponent. Comment on how the range and accuracy of this 16-bit floating point format compares to the single precision IEEE 754 standard.

3.27 Given $= 1.5625 \times 10^{-1} = 0.15625_{10} \Rightarrow 0.15625 \times 2 = 0.3125 \text{ (0)}$

$$0.3125 \times 2 = 0.625 \text{ (0)}$$

$$0.625 \times 2 = 1.25 \text{ (1)}$$

$$0.25 \times 2 = 0.5 \text{ (0)}$$

$$0.5 \times 2 = 1 \text{ (1)}$$

Hence, $= -0.15625_{10} = -0.00101_2$

$= -1.01 \times 2^{-3}$ <Hidden 1 => 1.XXXXX>

Sign = 1

Exponent $= -3+15 = 12 = 01100_2$

Fraction = 0100,0000,00₂

IEEE Representation: 1 01100 0100,0000,00

3.29 $2.6125 \times 10^1 + 4.150390625 \times 10^{-1}$

$2.6125 \times 10^1 = 26.125 = 11010.001 = 1.1010001000 \times 2^4$

$4.150390625 \times 10^{-1} = .4150390625 = .011010100111 = 1.1010100111 \times 2^{-2}$

For the second number, shift binary point 6 to the left to align exponents,

GR

1.1010001000 00

0.0000011010 10 0111 (Guard bit = 1, Round bit = 0, Sticky bit = 1)

1.1010100010 101 (Guard bit = 1, Round bit = 0, Sticky bit = 1)

In this case, the extra bit (G,R,S) is more than half of the least significant bit (0).

Thus, the value is rounded up.

$1.1010100011 \times 2^4 = 11010.100011 \times 2^0 = 26.546875 = 2.6546875 \times 10^1$

3.41

Answer	sign	exp	Exact?
1 01111101 000000000000000000000000	—	-2	Yes

3.42 $b+b+b+b=-1$

$b \times 4 = -1$

They are the same

3.43

$0.3333333333 \times 2 = 0.66666666666666$ the digit is 0

$0.6666666666 \times 2 = 1.33333333333333$ the digit is 1

$0.3333333333 \times 2 = 0.66666666666666$the digit is 0

$0.666666666666 * 2 = 1.333333333333333$...the digit is 1

..... keep going.

$1/3 = 0.0101\ 0101\ 0101\ 0101\ 0101\ 0101....._2$

The representation is not exact since $1/3$ is not totally represented.