

PRACTICAL - 1

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basics of R software.

- 1). R is a software for statistical analysis and data computing.
- 2). It is an effective data handling software and outcome storage is possible.
- 3). It is capable of graphical display.
- 4). It is a free software.

solve the following

$$1). 4+6+8 :- 2-5$$

$$> 4+6+8/2-5$$

(1) 9

$$2). 2^2 + |-3| + \sqrt{15}$$

$$> 2^2 + \text{abs}(-3) + \sqrt{15}$$

(1) 13.7082

$$3). 5^3 + 7 \times 5 \times 8 + 46/5$$

$$> 5^3 + 7 \times 5 \times 8 + 46/5$$

(1) 414.2

$$4). \sqrt{4^2 + 5^3 + 7/6}$$
$$\therefore 4^2 + 5^3 + 7/6$$

Q5). round off

$$36 \quad 46 \div 7 + 9 \times 8$$

$$> \text{round} (46 / 7 + 9 * 8)$$

[1] 79.

Q2.

$$> C(2, 3, 5, 7) * 2$$

[1] 4 6 10 14

$$> C(2, 3, 5, 7) * C(2, 3, 6, 2)$$

[1] 4 9 30 14

$$> C(2, 3, 5, 7) ^ 2$$

[1] 4 9 25 49

$$> C(6, 2, 7, 5) / C(4, 5)$$

[1] 1.50 0.40 1.75 1.00

$$> C(2, 3, 5, 7) * C(2, 3)$$

[1] 4 9 10 21

$$> C(1, 6, 2, 3) * C(-2, -3, -4, -1)$$

[1] -2 -18 -8 -3

$$> C(4, 6, 8, 9, 4, 5) ^ 2 * C(1, 2, 3)$$

[1] 4 36 512 9162185

Q3.

$$> x = 20 \quad > y = 30 \quad > z = 2$$

$$> x^2 + y^3 + z$$

[1] 27402

$$> sqrt(x^2 + y^2 + z)$$

[1] 20.73694

$$> x^2 + y^2 + z$$

[1] 1300

Q4. > x <- matrix (nrow=4, ncol=2, data = c(1, 2, 3, 4, 5, 6, 7, 8))

> x

[1,] [2,]

[1]

[2]

1

5

2

6

[3,]

3

7

[4,]

4

8

Q9

Find $x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$

$$y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

$\Rightarrow x$ c-matrix (nrow=3, ncol=3, data=c(4, 7, 9, -2, 0, -5, 7, 3))

$$\begin{bmatrix} [1,] & 4 & -2 & 6 \\ [2,] & 7 & 0 & 7 \\ [3,] & 9 & -5 & 3 \end{bmatrix}$$

$\Rightarrow y$ c-matrix (nrow=3, ncol=3, data=c(10, 12, 15, -5, -4, -6, 7, 9, 5))

$$\begin{bmatrix} [1,] & 10 & -5 & 7 \\ [2,] & 12 & -4 & 9 \\ [3,] & 15 & -6 & 5 \end{bmatrix}$$

$\Rightarrow x+y$

$$\begin{bmatrix} [1,] & 14 & -7 & 13 \\ [2,] & 19 & -4 & 16 \\ [3,] & 24 & -11 & 8 \end{bmatrix}$$

$\Rightarrow 2*x + 3*y$

$$\begin{bmatrix} [1,] & 38 & -19 & 33 \\ [2,] & 50 & -12 & 41 \\ [3,] & 63 & -28 & 21 \end{bmatrix}$$

Marks of statistics of C.S batch A. 58

x = c(59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)

> x = c(data)

> break8 = seq(20, 60, 5)

> a = cut(x, break8, right = FALSE).

> b = table(a)

> c = transform(b)

> c

	a	freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

PRACTICAL -2

check whether the following is pmf or not:-

x	$p(x)$
0	0.1
1	0.2
2	0.5
3	0.4
4	0.3
5	0.5

Since $p(2) = -0.5$, if it can't be probability
pmf function $p(x)$ is greater than equal to zero.

It cannot be pmf as $\sum p(x) \neq 1$

i). Find C.d.f for the following P.N.F and sketch the graph.

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

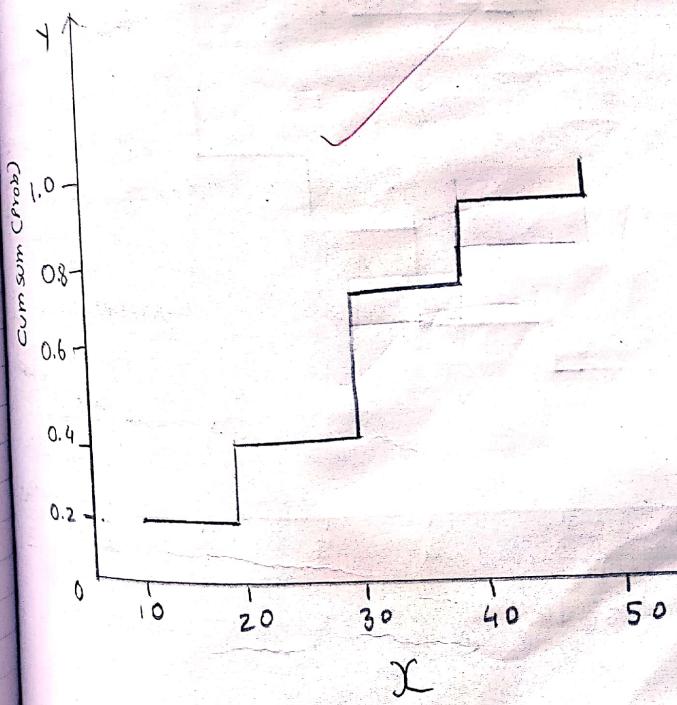
$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.95 & 40 \leq x < 50 \\ 1.00 & 50 \leq x < 60 \quad x \geq 50 \end{cases}$$

CODE :-

```

> prob = c(0.2, 0.2, 0.35, 0.15, 0.1)
> sum(prob)
[1] 1.0
> cumsum(prob)
[1] 0.2 0.4 0.75 0.95 1.00
> x = c(10, 20, 30, 40, 50)
> plot(x, cumsum(prob), "S")

```

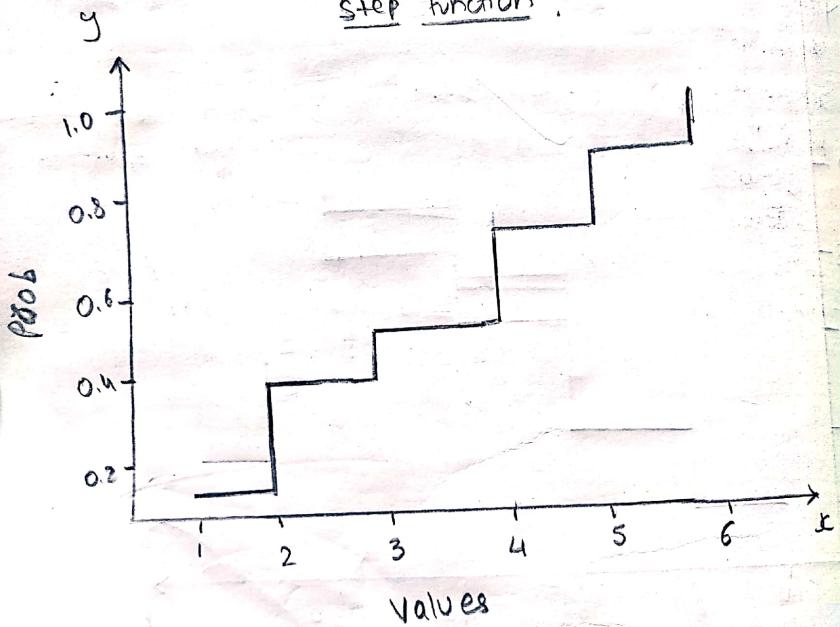


09-

CODE:-

```
> x = c(1, 2, 3, 4, 5, 6)
> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
> cumsum(prob)
> plot(x, cumsum(prob), "s", main = "Step function",
xlab = "values", ylab = "prob", col = "green")
```

Step function.



Q8)

x	prob
1	0.15
2	0.25
3	0.1
4	0.2
5	0.02
6	0.1

CODE :-

Q1). $> \text{dbinom}(10, 100, 0.1)$

[A] 0.1318653.

Q2). $> \text{dbinom}(4, 12, 0.2)$

[A] 0.1328756.

Q3). $> \text{pbinom}(4, 12, 0.2)$

[A] 0.927445.

Q4). $> 1 - \text{pbinom}(5, 12, 0.2)$

[A] 0.01940528.

Q5). $> \text{dbinom}(0.5, 5, 0.1)$

[A] 0.59049 0.32805 0.07290 0.00810 0.00045
0.00001

Q6). Q. $> \text{dbinom}(5, 12, 0.25)$

[A] 0.1032414

Q7). $> \text{pbinom}(5, 12, 0.25)$

[A] 0.9455978

Q8). $> 1 - \text{pbinom}(7, 12, 0.25)$

[A] 0.00278151

Q9). $> \text{dbinom}(6, 12, 0.25)$

[A] 0.04014945

(Practical - 3).

Formulae (Common).

i). $P(X=x) = \text{dbinom}(x, n, p)$.

ii). $P(X \leq x) = \text{pbinom}(x, n, p)$.

iii). $P(X > x) = 1 - \text{pbinom}(x, n, p)$.

iv). If x is unknown and $p_1 = P(X \leq x) = \alpha$

Q1). Find the probability of exactly 10 success in trials with $p = 0.1$.

Q2). Suppose there are 12 MCQ. Each question has 5 options out of which correct. find the probability of having :-

i). Exactly 4 correct answers $P(X=4)$

ii). At most 4 correct answers $P(X \leq 4)$

iii). More than 5 correct answers. $P(X > 5)$

Q3). Find the complete distribution when $n=12$, $p=0.25$.

i). $P(X=5)$

ii). $P(X \leq 5)$

iii). $P(X > 7)$

iv). $P(5 < X < 7)$

Q4). Probability of a salesman making sales is 0.15. Find the probability of

i). No sales out of 10 customers.

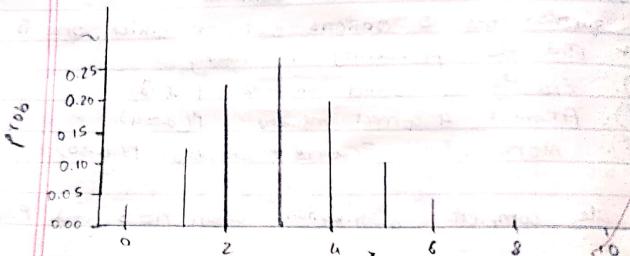
ii). ...

Q6] A Salesman has a 20% probability of making a sale to a customer, out of 30 customers. what minimum no. of sales he can make with 88% probability.

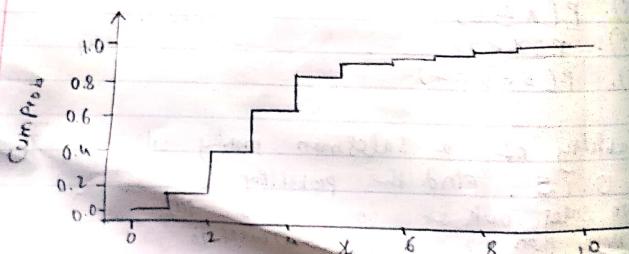
Q7]. X follows binomial distribution with $n=10$, $p=0.3$. plot the graph of p.m.f. and c.d.f

GRAPH.

P.M.F.



C.d.f.



Q8]. i) $> \text{dbinom}(0, 10, 0.15)$
 (i) 0.1968744 .

ii) $> 1 - \text{pbinom}(3, 20, 0.15)$
 (ii) 0.3522748 ..

Q9]. $> \text{qbinom}(0.88, 30, 0.2)$
 (iii) 9 .

Q10].
 $> n = 10$

$> p = 0.3$

$> x = 0:n$

$> \text{prob} = \text{dbinom}(x, n, p)$

$> \text{cumprob} = \text{pbinom}(x, n, p)$

$> d = \text{data.frame}("x.values" = x, "Probability" = prob)$

$> \text{print}(d)$

$\rightarrow x.values \quad \text{Probability}$

1	0	0.0282475249
2	1	0.1210608210
3	2	0.2334744405
4	3	0.2668277320
5	4	0.2001209490
6	5	0.1029193452
7	6	0.0367569090
8	7	0.0090016920
9	8	0.001446
10	9	0.0001
11	10	A.

PRACTICAL-4

6.5

(Q). $> p_1 = \text{pnorm}(15, 12, 3)$

$> p_1$

[1] 0.8413447

$> p_2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$

$> p_2$

[1] 0.3480661

$> p_3 = 1 - \text{pnorm}(14, 12, 3)$

$> p_3$

[1] 0.2524925.

$> p_4 = rnorm(5, 12, 3)$

$> p_4$

[1] 10.299518

13.439425

11.956763

12.190045

18.976714

$> cat("P(x=5) =", p_1)$

$> cat("P(10 \leq x \leq 13) =", p_2)$

$> cat("P(x > 14) =", p_3)$

A random variable x follows normal distribution with mean = 12 = μ and $SD = 3 = \sigma$. Find:

- 1). $P(x \leq 15)$
- 2). $P(10 \leq x \leq 13)$
- 3). $P(x > 14)$
- 4). Generate 5 observations (random numbers)

x follows normal distribution with $\mu = 10$, $\sigma = 3$. Find i). $P(x \leq 7)$

ii). $P(5 < x < 12)$

iii). $P(x > 12)$

iv). Generate 10 observations.

v). Find n such that probability $P(x < n) = 0.4$

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- (Q) Generate 5 random nos from a N(10, 4) with
mean = 15 (μ) and s.d = 4 (σ).
Find sample mean, median, s.d, and
print it.

```
> p1 = rnorm(7, 10, 2)
> p1
[1] 0.0668072
```

```
> p2 = rnorm(12, 10, 2) - rnorm(5, 10, 2)
> p2
[1] 0.8351351
```

```
> p3 = rnorm(12, 10, 2)
> p3
[1] 0.1586553
```

```
> p4 = rnorm(10, 10, 2)
```

```
> p4
[1] 9.592804
```

```
10.300246
```

```
10.737278
```

```
11.991047
```

```
12.28 11.55417
```

```
> p5 = rnorm(0, 4, 10, 2)
> p5
```

```
[1] 9.493306
```

- (Q) Plot the standard normal graph.

```
> x = rnorm(15, 0)
```

```
> xm = mean(x)
```

```
[1] 17.52547
```

```
> median = median(x)
```

```
[1] 17.02539
```

```
> sdev = sd(x)
```

```
> variance = (n-1)*var(x)/n
```

```
[1] 2.916316
```

```
> sd = sqrt(variance)
[1] 5.567117
```

PRACTICAL - 5

*TOPIC:- NORMAL & t-Test

Q1. Test the hypothesis $H_0: \mu = 15$
 $H_1: \mu \neq 15$.

A random sample of size 400 is drawn and it
 is calculated as sample mean = 14 and s.d = 3.
 Test the hypothesis at 5% level of significance.

$$\text{Formula } Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

In R software $m_0 = 15$, $m_x = 14$, $s_d = 3$, $n = 400$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / (\sqrt{n}))$$

$$p\text{value} = 1 - pnorm(abs(z_{\text{cal}})) * 2$$

$$p\text{value} = 2 * (1 - pnorm(abs(z_{\text{cal}})))$$

$$p\text{value} = 2 * 0.616796 e^{-11}$$

$$p\text{value} = ((1 - pnorm(abs(z_{\text{cal}}))) * 2)$$

Since pvalue is less than 0.05, we aren't accepting $H_0: \mu = 15$.

2] CODE :-

```
> m0 = 10
> mK = 10.2
> n = 400
> sd = 2.25
> zcal = (mK - m0) / (sd / (sqrt(n)))
> zcal
```

```
[2] 1.7777777777777777
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
```

```
[2] 0.07544036
```

test the hypothesis $H_0: \mu = 10$
 $H_1: \mu \neq 10$
 A random sample of size 400 is drawn with
 sample mean 10.2 and s.d = 2.25. Test the
 hypothesis at 5% level of significance.

[Q3]

Test the Hypothesis $H_0: p = 0.2$
 proportion of smokers in our college is 0.2
 The sample is collected and sample proportion = 0.125
 Test the Hypothesis at 5% level of significance
 (sample size = 400).

\Rightarrow Since the value is less than 0.05, we reject
 H_0 : proportion = 0.2.

CODE :-
 $> n = 400$
 $> p = 0.2$
 $> \hat{p} = 0.125$
 $> Q = 1 - p$
 $> Z_{\text{cal}} = (p - \hat{p}) / (\sqrt{p * Q / n})$

$$> Z_{\text{cal}} = -3.75$$

$$(1) > p\text{value} = 2 * (1 - \text{norm}(\text{abs}(Z_{\text{cal}})))$$

$$> \text{pvalue}$$

$$(1) 0.0001768346$$

[Q4]

Last year \rightarrow the farmers lost 20% of their crop.
 A random sample of 60 fields are collected and it
 is found that 9 fields crops are ~~greatly~~ polluted
 Test the Hypothesis at 1% levels of significance.

$$H_0: p = 0.2$$

$$H_1: p = 9/60$$

\Rightarrow since p value is greater than 0.01, we ~~ref~~
 accept the H₀: $p = 0.2$.

CODE :-
 $> n = 60$
 $> P = 0.2$
 $> p = 0.15$
 $> Q = 1 - p$
 $> Z_{\text{cal}} = (p - \hat{p}) / (\sqrt{p * Q / n})$

$$> p\text{value} = 2 * (1 - \text{norm}(\text{abs}(Z_{\text{cal}})))$$

$$(1) -0.9682458$$

$$> \text{pvalue}$$

$$(1) 0.3329216$$

[Q3] Test the Hypothesis $H_0: p = 0.2$
 Proportion of smokers in our college is 0.2
 The sample is collected and sample proportion = 0.125
 Test the hypothesis at 5% level of significance
 (sample size = 400).

\Rightarrow Since the value is less than 0.05, we reject
 $H_0: \text{proportion} = 0.2$.

[Q4] Last year \rightarrow the farmers lost 20% of their crop.
 A random sample of 60 fields are collected and it
 is found that 9 fields crops are insect polluted
 Test the hypothesis at 1% levels of significance.
 $H_0: P = 0.2$
 $H_1: P = \frac{9}{60}$

\Rightarrow Since p-value is greater than 0.01, we ~~reject~~
 accept the value $H_0: P = 0.2$.

CODE :-
 $> n = 400$
 $> p = 0.2$
 $> q = 0.125$
 $> q = 1 - p$
 $> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$

$\Rightarrow z_{\text{cal}} = -3.75$

$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $> \text{pvalue}$
 $[1] 0.0001768346$

CODE :-
 $> n = 60$
 $> P = 0.2$
 $> p = 0.15$
 $> q = 1 - p$
 $> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$
 $> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $> z_{\text{cal}}$
 $\Rightarrow z_{\text{cal}} = -0.9682458$
 $> \text{pvalue}$
 $[1] 0.3329216$

PRACTICAL - 06

Large sample test

(Q) Let the population mean [the amount spent by customers in a restaurant] for 250. A sample of 100 customers selected. The sample mean is calculated as 245 and s.d is 50. Test the hypothesis that population means 250 or not. The level of significance is 5%.

$$H_0: \mu_1 = \mu_2 \text{ against } H_1: \mu_1 \neq \mu_2$$

Since the p-value is less than 0.05, we reject the p-value $H_0: \mu_1 = \mu_2$.

CODE :-

```
[1] zcal = (mx-mo)/(csd/sqrt(n))
[1] n = 100
[1] m = 250
[1] mx = 245
[1] sd = 50
[1] zcal = (mx-mo)/(csd/sqrt(n))
[1] 8.3333333
```

[1] pvalue = (1 - pnorm(abs(zcal)))*2
 [1] pvalue
 [1] 0.05

[1] cat ("zcal is:", zcal)

[1] zcal is : 8.333333

[1] cat ("pvalue is:", pvalue)
 pvalue is : 0.

CODE :-

n = 1000

p = 0.8

Q = 1 - p

z = p - Q / 100

zcal = (p - Q) / sqrt(p * Q / n)

zcal

-3.952847

Since the p-value $\cancel{is} (7.72268e-05)$ is less than 0.01, we reject the p-value

$$H_0: \mu_1 = \mu_2$$

CODE :-

[1] -3.952847

[1] pvalue = 2 * (1 - pnorm(abs(zcal)))

[1] pvalue

[1] -7.72268e-05

[1] cat ("zcal is:", zcal)

[1] zcal is : -3.952847

CODE :-

```

> n1=1000
> n2=2000
> mu=67.5
> mx2=68
> sd1=2.5
> sd2=2.5
> zcal=(mx1-mx2)/sqrt((sd1^2/n1)+(sd2^2/n2))
> zcal
[1] -5.163978
> pvalue = (1-pnorm(abs(zcal)))*2
> pvalue
[1] 2.417564e-07
> cat ("zcal ps:", zcal)
zcal ps: -5.163978
> cat ("pvalue ps:", pvalue)
pvalue ps: 2.417564e-07

```

Two random samples of size 1000 and 2000 are drawn from two population with the same S.D i.e. 2. The sample means are 67.5 and 68 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

$$\mu_0: \mu_1 = \mu_2 \text{ against } \mu_1: \mu_1 \neq \mu_2$$

$$n_1 = 1000$$

$$n_2 = 2000$$

$$mx_1 = 67.5$$

$$mx_2 = 68$$

$$sd_1 = 2.5$$

$$sd_2 = 2.5$$

\therefore since pvalue ps less than 0.05, we reject the pvalue $H_0: \mu_1 = \mu_2$.

(Q4)

A study of noise level σ^2 in 2 hospitals is given below. Test the claim that the 2 hospitals have same level of noise at 1% level of significance
 $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

	Hospital A	Hospital B
Size	84	34
Mean	61.2	59.4
S.D.	7.9	7.45

\therefore Since the p-value is greater than 0.01, we accept the H₀: $\mu_1 = \mu_2$

(Q5)

In a sample of 600 students, in a college, 400 use blue ink in another college from a sample of 900 students, 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in 2 colleges are equal or not. at 1% level of significance.

$H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$.

$H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

Since p-value is less than 0.01 we reject the p-value & $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$.

$$\begin{aligned} p_1 &= 84 \\ p_2 &= 34 \\ m\bar{x}_1 &= 61.2 \\ z_{cal} &= 7.9 \\ s.d. &= 7.5 \\ z_{cal} &= (m\bar{x}_1 - m\bar{x}_2) / \sqrt{(s^2 d_1 / n_1) + (s^2 d_2 / n_2)} \\ z_{cal} &= 1.162528 \end{aligned}$$

$$\begin{aligned} p-value &= 1 - \text{pnorm}(abs(z_{cal})) * 2 \\ p-value &= 0.2450211 \end{aligned}$$

$$\begin{aligned} z_{cal} &= 1.162528 \\ p-value &= \text{pnorm}(abs(z_{cal})) * 2 \end{aligned}$$

$$\begin{aligned} p-value &= 0.2450211 \\ \text{Code :-} & \end{aligned}$$

```

> n1=600
> n2=900
> p1=400/600
> p2=450/900
> p=(n1*p1+n2*p2)/(n1+n2)
> p=1-p
> zcal=(p1-p2)/sqrt(p*p*(1/n1+1/n2))
> pvalue=1-pnorm(abs(zcal))*2

```

$$\begin{aligned} z_{cal} &= (p_1 - p_2) / \sqrt{p_1 * p_2 * (1/n_1 + 1/n_2)} \\ p-value &= (1 - \text{pnorm}(abs(z_{cal}))) * 2 \end{aligned}$$

p-value

1.753222 e-10

zcal

is : 1.162528

p-value

is : 0.2450211

Scanned with CamScanner

$\rightarrow \rho$

[1] 0.56666667

$> \text{cat}(" \rho \neq \rho_s:", \rho)$

$\rho \neq \rho_s : 0.56666667.$

CODE :-

$\rightarrow n_1 = 200$

$\rightarrow n_2 = 200$

$\rightarrow p_1 = 44 / 200$

$\rightarrow p_2 = 30 / 200$

$\rightarrow \rho = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

$\rightarrow q = 1 - \rho$

$\rightarrow z_{\text{cal}} = (\rho_1 - \rho_2) / \sqrt{p * q * (1 * n_1 + 1 * n_2)}$

$\rightarrow \text{pvalue} = 1 - \text{pnorm}(\text{abs}(z_{\text{cal}})) * 2$

$\rightarrow z_{\text{cal}}$

(D) 1.802741

$\rightarrow \text{pvalue}$

[1] 0.0742888

$\rightarrow \rho$

(D) 0.185.

$\rightarrow \text{cat}(" z_{\text{cal}} \neq_s:", z_{\text{cal}})$

$z_{\text{cal}} \neq_s : 1.802741$

$> \text{cat}(" \rho \neq \rho_s:", \rho)$

$\rho \neq \rho_s : 0.185$

$> \text{cat}(" \text{pvalue} \neq_s:", \text{pvalue})$

$\text{pvalue} \neq_s : 0.0742888$

$$\begin{aligned} n_1 &= 200 \\ n_2 &= 200 \\ p_1 &= 44 / 200 \\ p_2 &= \frac{30}{200} \end{aligned}$$

$H_0: \rho_1 = \rho_2 \text{ against } H_1: \rho_1 \neq \rho_2$

Since pvalue \neq_s greater than 0.05, we reject accept the pvalue:

$H_0: \rho_1 = \rho_2$

$\frac{\rho}{2} = 0.185$

PRACTICAL - 7

One sample t-test

Ques. Small sample space.

1. The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from the population with the average 66.

$$H_0: \mu = 66$$

Ans. — Since p-value is less than 0.05, we reject the hypothesis $H_0: \mu = 66$ at 5% level of significance.

If (p-value > 0.05) \Rightarrow cat("accept H₀") Else \Rightarrow cat("reject H₀")

2. Two groups of students scored the following marks. Test the hypothesis that there is no significant difference between the two groups.

Group 1 — 18, 22, 21, 17, 20, 23, 20, 22, 21,

Group 2 — 16, 20, 14, 21, 20, 18, 13, 15, 17,

21.

Welch two sample t-test

data : x and y

$t = 2.2573$, $df = 16.376$, $p\text{-value} = 0.03749$

Alternative hypothesis: true difference in mean is not equal to 0
is percent confidence interval:

$0.1628205 \leq \bar{x} \leq 5.037145$

Simple estimates :

mean of x mean of y

20.1 17.5

(value > 0.05) \Rightarrow cat("accept H₀") Else \Rightarrow cat("reject H₀")

Ans. — Since p-value is less than 0.05, we reject the hypothesis $H_0: \mu$ no difference at 5% level of significance.

data : x
 $x = [63, 63, 66, 67, 68, 69, 70, 70, 71, 72]$
t-test(x)

alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:

65.65171 70.14829

4. Two medicines are applied to groups of patient respectively

Group 1 - 10, 12, 13, 11, 14.

Group 2 - 8, 9, 12, 14, 15, 10, 9.

Is there any significant difference between the two medicines?

Ans → Since the p-value is greater than 0.05, we accept the hypothesis.

H₀: no significant difference between these medicines.

5. The following are the weights before and after the diet program. Is the diet program effective?

Before - 120, 125, 115, 130, 123, 119.

After - 100, 114, 95, 90, 115, 99.

Ans → Since the p-value is greater than 0.05, we accept the hypothesis.

H₀: no significant difference.

R code:
x = c(10, 12, 13, 11, 14)
y = c(8, 9, 12, 14, 15, 10, 9).
t.test(x, y)

welch two sample t-test

data: x and y
 $t = 0.80384$, $df = 9.7594$, $p\text{-value} = 0.4406$
mean of x mean of y 2 sample estimate.
12 11

~~alternative hypothesis: true difference in mean is not zero~~
95 percent confidence interval:
-1.7810245 -1.281173 3.281173

sample estimates:

~~mean~~
t-test (pvalue > 0.05) {cat("accept H₀")}
accept H₀.

b. Paired t-test
data: b and a
 $t = 4.3488$, $df = 5$, $p\text{-value} = 0.9963$
alternative hypothesis: true difference in means is not zero
95 percent confidence interval:
-1.7810245 2.9.0295

paired t-test
data: b and a
 $t = 4.3488$, $df = 5$, $p\text{-value} = 0.9963$
alternative hypothesis: true difference in means is not zero
95 percent confidence interval:
-1.7810245 2.9.0295

Not effective

Ques:-

1. CODE:-

```

> n = 100
> mx = 52
> mo = 55
> sd = 7
> zcal = (mx - mo) / (sd / (sqrt(n)))
> Pvalue = 1 - pnorm(abs(zcal)) * 2
[1] -4.285714
> Pvalue
[1] 1.92153e-05
    
```

Ans → we reject the Pvalue at $H_0: \mu = 55$ at ~~H₀: μ ≠ 55~~.

2. CODE:-

```

> n = 400
> p = 350/400
> P = 0.5
> Q = 1 - P
> zcal = (p - P) / (sqrt(Q/n))
> zcal
[1] 0.
    
```

Ans → we accept the Pvalue at $H_0: p = 1/2$ at 1%.

(1) i.

(Q3) Ans \rightarrow we accept/reject the p-value

(Q3). Ans \rightarrow we reject the p-value at $H_0: \mu = 0.05$ at 5% level of significance.

(Q4). Ans \rightarrow we reject the p-value at $H_0: \mu = 100$ at 5% level of significance

$\begin{aligned} & z_{\text{cal}} = \frac{(p_1 - p_2)}{\sqrt{p_1(1-p_1)/n_1 + p_2(1-p_2)/n_2}} \\ & z_{\text{cal}} = \frac{(0.1 - 0.05)}{\sqrt{0.1(0.9)/100 + 0.05(0.95)/150}} \\ & z_{\text{cal}} = \frac{0.05}{\sqrt{0.001 + 0.000333}} \\ & z_{\text{cal}} = \frac{0.05}{0.014842} \\ & p\text{-value} = 1 - \text{pnorm}(\text{abs}(z_{\text{cal}})) * 2 \\ & p\text{-value} = 1 - \text{pnorm}(0.08364) * 2 \\ & p\text{-value} = 0.014 \end{aligned}$

Q4. CODE :-

```

> mx = 99
> mo = 100
> sd = 8
> n = 400
> zcal = (mx - mo) / (sd / sqrt(n))
> pvalue = 1 - pnorm(abs(zcal)) * 2
> zcal
[1] -2.5
> pvalue
[1] 0.01241933

```

CODE:-

```
> x=c(63,63,68,69,71,71,72)  
> t.test(x)
```

One sample t-test

data : x

t = 47.94 , df = 6 , p-value = 5.522e-09

alternative hypothesis: true mean is not

equal to 0

95 percent confidence interval:

64.66474 71.62092

Sample estimates:

mean of x

68.14286

CODE:-

```
> x=c(66,67,75,76,82,84,88,90,92)
```

```
> y=c(69,66,76,78,82,85,87,92,93,95,97)
```

```
> var.test(x,y)
```

F test to compare two variances

data: x and y

F = 0.70686 , num df = 8 , denom df = 10 , p-value = 0.6369

alternative hypothesis: true ratio of variances is not equal to 1

95 percent confidence interval:

0.1833662 3.0360393

Sample estimates:

ratio of variances

0.7068567.

Ans? we reject the p-value at 1% level of significance.

H₀: $\mu = 66$ against $\mu \neq 66$.

Ans? we accept the p-value at 5% level of significance.

H₀: $61 = 62$ against $\mu_1 \neq \mu_2$

(Q3)

$H_0: \mu_1 = \mu_2 = 100$ against $H_A: \mu_1 \neq \mu_2$

Ans \rightarrow We reject the P -value if at $H_0: \mu_1 = \mu_2$

$$P_{\text{value}} = (1 - \text{norm}(\text{abs}(z_{\text{test}}))) * 2$$

(Q3) Ans \rightarrow we accept the H_0 if $|z| < 1.96$. Here

of significance

$H_0: \mu_1 = \mu_2$ against $H_A: \mu_1 \neq \mu_2$

$$\begin{aligned} n_1 &= 300 \\ n_2 &= 300 \\ p_1 &= 124/300 \\ p_2 &= 54/300 \end{aligned}$$

$$z_{\text{test}} = (p_1 - p_2) / \sqrt{(p_1 * p_2) / (n_1 + n_2)}$$

$$p_1 = 1 - p_2$$

$$\begin{aligned} z_{\text{test}} &= (p_1 - p_2) / \sqrt{\text{sqrt}((p_1 * p_2) * ((1 - p_1) / (n_1 + n_2)))} \\ p_1 &= (1 - \text{norm}(\text{abs}(z_{\text{test}}))) * 2 \end{aligned}$$

$$p_1 = 0.9128704$$

$$p_2 = 0.1343104$$

i). code

```
> x=c(70, 80, 35, 50, 20, 45)
> m=3
> n=n=2
> y=matrix(x, nrow=m, ncol=n)
> y
```

[1,1]	[1,2]
[2,1]	70 50
[2,2]	80 20
[3,1]	35 45

```
> pV=chisq.test(y)
> pV
```

Person's chi-squared test

data: y

$\chi^2 = 25.646$, df = 2, p-value = 2.698×10^{-6}

PRACTICAL - 9

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Chi-square Test and ANOVA

Use the following data to find whether the condition of the home and the condition of the child are independent or not.

Condition of Home

	Clean	Dirty
Clear	10	10
Fairly clear	10	10
Dirty	10	10

H₀: Condition of home and child are independent

Since p-value is less than 0.05, we reject H₀ at 5% level of significance.

- Q2. Test the hypothesis that the ~~vaccination~~ and the disease are independent or not.

		Vaccine	
		Affection	Not Affection
Disease	Aff.	70	46
	N.Aff.	35	37

Ans: Disease and the vaccine are independent.

\Rightarrow Since p-value is greater than 0.05, we accept H_0 at 5% level of significance

CODE :-

`x = c(70, 35, 46, 37)`

`m = 2`

`n = 2`

`y = matrix(x, nrow = m, ncol = n)`

`y`

`[1,1] [1,2]`

`[1,1] 70 46`

`[2,1] 35 37`

`pv = chisq.test(y)`

`pv`

Pearson's Chi-Squared test with Yates' continuity correction

`data: y`

`X-squared = 2.0275, df = 1, p-value = 0.1545`

3. Code

```
> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 58, 57, 56)
> x4 = c(52, 54, 54, 55)
> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))
> names(d)
[1] "values" "ind"
> oneway.test(values ~ ind, data = d, var.equal = T)
    one-way analysis of means
    data: values and ind
    F = 11.735, num df = 3, denom df = 9, p-value = 0.00183
> anova = aov(values ~ ind, data = d)
> summary(anova)
    Df Sum Sq Mean Sq F value Pr(>F)
ind      3 21.06   7.02   11.73 0.00183 ***
Residuals 9 18.17   2.019
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
```

perform an ANOVA on the following data.

Type	Observations
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

H₀: the means are equal for A, B, C, D.

Since the p-value is less than 0.05 we reject H₀ at 5% level of significance.

4.

The following data gives the life of the tire of 4 brands

- (Q).
Type Life
A 20, 23, 18, 17, 18, 22, 24
B 19, 15, 17, 20, 16, 17
C 21, 19, 22, 17, 20
D 15, 14, 16, 18, 14, 16

→ H₀: the avg. life of A, B, C, D are equal

Since the p-value is less than 0.05, we reject H₀

at 5% level of significance

(Q).

Type Life
values "Ind"
names "Ind"

library (car)
one-way.test (values ~ Ind, data = d, var.equal = T)

One-way analysis of means
values and Ind

data: values and Ind
p: 6.84e-5, num df = 3, denom df = 20, p-value = 0.00000005
anova = ANOVA (values ~ Ind, data = d)

summary (anova)

Q1 code :-

```

> x=read.csv("C:/Users/Administrator/Desktop/math.csv", CSV)
> print(x)

> om=mean(x$statistics)
> om

(1) 52

> n=length(x$statistics)
> n

(1) 10

> sd=sqrt((n-1)*var(x$statistics)/n)
> sd

[1] 12.64911

> om=mean(x$maths)
> om

[1] 39.6

> n=length(x$maths)
> n

[1] 10

> sd=sqrt((n-1)*var(x$maths)/n)
> sd

[1] 15.2

> cov(x$d$statistics, x$maths)

[1] 0.0830618
  
```

To import excel file in R software,

	statistics	maths
1	40	60
2	45	48
3	42	47
4	15	20
5	37	25
6	36	27
7	49	57
8	59	58
9	20	25
10	27	27

Ay
2022

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PRACTICAL-10

Aims

Non-parametric test.

- Q.1) Following are the amounts of sulphur oxide emitted by some industry in 20 days.

Applied sign test to test the hypothesis that population median is 21.5 at 5% LOS.

$$X = 17, 15, 20, 20, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.$$

\rightarrow H_0 : population median is 21.5.

H_1 : less than 21.5

\Rightarrow Since the P-value is greater than 0.05, we accept H_0 at 5% LOS.

* NOTE :- If the alternative (H_1) is $m_e \neq z$ or $m_e < z$ then the used formula

Else, if $m_e > z$

$$PV = P \text{binom}(sn, n, 0.5).$$

CODE :-

$$x = C(\dots)$$

$$m_e = 21.5$$

$$sp = \text{length}(x[x > m_e])$$

$$sn = \text{length}(x[x < m_e])$$

$$n = sp + sn$$

$$PV = P \text{binom}(sp, n, 0.5)$$

$$PV$$

$$[1] 0.4119015$$

$$n$$

$$[2] 20.$$

✓

#28 CODE :-

```
>x=CC...  
>me=625  
>sp=length(x[x>me])  
>sn=length(x[x<=me])  
>n=sp+sn  
>pv=pbinom(sn,n,0.5)  
>n  
[1] 10  
>pv  
(1) 0.0546875
```

(Q2). ~~While~~ the following is the data ~~of~~ apply sign test to test the hypothesis population median is 625 against ~~that~~ it is more than 625.

$x = 612, 619, 631, 628, 643, 640, 655, 663$.

$\Rightarrow H_0$: Population mean is 625
 H_1 : greater than 625
 \Rightarrow Since the p-value is greater than 0.05,
 H_0 at 5% LOS.

THE NO. CODE:-

```
>x=c(12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66)
```

```
>wilcox.test(x, alternative = "less", mu=12)
```

data: x

v=66, p-value = 0.9986

alternative hypothesis: true location is less than 12

Using W.S.R.T. Test the population median is
or less than 12.

x= 15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 2

H₀: population median is 12.

H₁: greater than 12

since p-value is greater than 0.05, we

H₀ at 5%.

- Q5) The weights of students before and after they stopped smoking are given below w.r.t. Test that there is no significant change.

Weights

before	After
65	72
75	74
75	72
62	66
72	73

→ H_0 : before and after there is no change.
 H_1 : there is change.

⇒ Since the p-value is ~~not~~ greater than 0.05, we accept H_0 at s.y. level of 0.05.

Q5. CODE :-

> x = c(65, 75, 75, 62, 72)

> y = c(72, 74, 72, 66, 73)

> d = x - y

> wilcox.test(d, after = "two.sided", mu = 0)

data: d

V = 4, S, p-value = 0.4982

alternative hypothesis: true location is not equal to 0

0.4982
2

- Q3. The following are the values of a sample. Test the hypothesis that the population median is 60 against the alternative it is more than 60 at 5%. LOS using Wilcoxon Signed Rank Test.

$$x = 63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 87, 69.$$

$\rightarrow H_0: \text{population median} = 60$.
 $H_1: \text{greater than } 60$
 \Rightarrow Since p-value is less than 0.05, we reject H_0 at 5% LOS.

* NOTE:- If alternative is less $\text{alter} = \text{"less"}$.
If alternative is not equal to, then $\text{alter} = \text{"two sided"}$.

#3 Wilcoxon Signed Rank Test
 $x = c(\dots)$
 $\rightarrow \text{wilcox.test}(x, \text{alter} = \text{"greater"}, \text{mu} = 60)$

Wilcoxon Signed rank test with continuity
data: x
 $N = 14.5$, p-value = 0.02298.
alternative hypothesis: true location is greater than