

Assignment 10-Probability and Random Variable

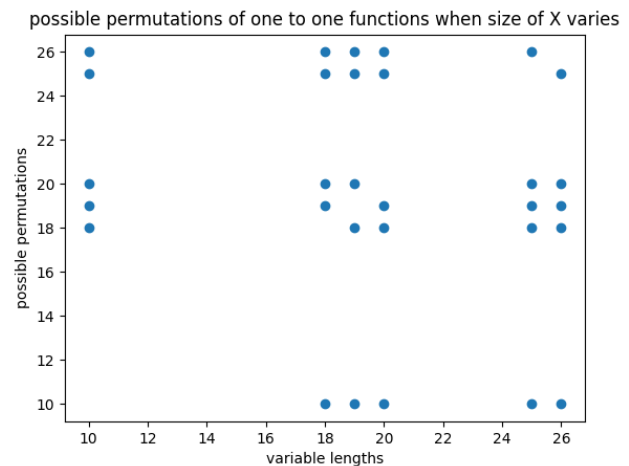
Annu-EE21RESCH01010

Download latex code from here-

https://github.com/annu100/AI5002-Probability-and-Random-variables/tree/main.tex/ASSIGNMENT_10

Download python code from here-

https://github.com/annu100/AI5002-Probability-and-Random-variables/tree/main.py/ASSIGNMENT_10



I. PROBLEM STATEMENT-GATE 10

Let X and Y denote the sets containing 2 and 20 distinct objects respectively and F denote the set of all possible functions defined from X to Y. let f be randomly chosen from F. The probability of f being one-to-one is

II. SOLUTIONS

Function: $X \rightarrow Y$

$|Y|=20$

$|X|=2$

total number of functions: $= 20^2 = 400$

total number of one-one functions:

$${}^{|Y|}P_{|X|} = {}^{20}P_2 \\ = 380.$$

Probability $= \frac{380}{400} = 0.95$.

Another way to see this:

Every element of X can take any of the 20 values.

Total $= 20 \times 20 = 400$.

For one-one function, Every element of X takes a different value.

so, total one to one functions are $= 20 \times 19 = 380$.

And thus probability is

Probability $= \frac{380}{400} = 0.95$