# Assignment 3 -Probability and Random Variable

### Annu-EE21RESCH01010

#### Download Python code from here

https://github.com/annu100/AI5002-Probabilityand-Random-variables/blob/main/ ASSIGNMENT 3/Assignment 3 Bayes.py

## Download latex code from here-

https://github.com/annu100/AI5002-Probabilityand-Random-variables/blob/main/ ASSIGNMENT 3/main.tex

#### I. Problem Statement-Problem 2.10

Bag I contains 3 red and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transferred ball is black.

#### II. Solutions

Bag 1 contains 3 red and 4 black balls. Bag 2 contains 4 red and 5 black balls.

let C1: Event of transferring black ball from bag 1 to 2

let C1: Event of transferring red ball from bag 1 to 2

let A: Event that the ball drawn from 2 is red after the transfer of a ball from bag 1 to bag 2.

$$Pr(C1) = \frac{4}{7}$$

$$Pr(C2) = \frac{3}{7}$$

$$Pr(A|C1) = \frac{4}{10} = \frac{2}{5}$$

$$Pr(A|C2) = \frac{5}{10} = \frac{1}{2}$$

From Baye's theoram

$$Pr(\text{Drawn ball is red}) = P(A)$$

$$= Pr(\frac{A}{C1}) \times Pr(C1) + PrC2 \times Pr(\frac{A}{C2})$$

$$= \frac{4}{10} \times \frac{4}{7} + \frac{5}{10} \times \frac{3}{7}$$

$$= \frac{16 + 15}{70}$$

$$= \frac{31}{10}$$

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The probability that the transferred ball is black It is equal to conditional probability of C1 when event A has already happened The desired probability is given by

$$Pr(\frac{C1}{A}) = \frac{Pr(C1 \cap A)}{Pr(A)}$$

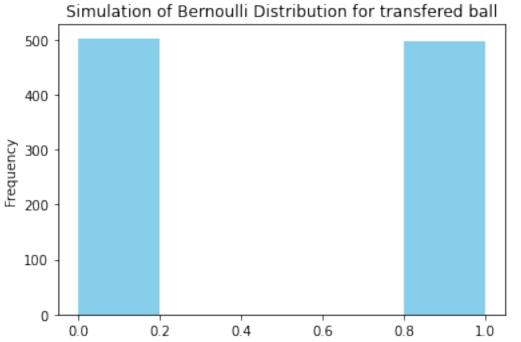
$$= \frac{Pr(\frac{A}{C1})Pr(C1)}{Pr(A)}$$

$$= \frac{\frac{4}{10} \times \frac{4}{7}}{\frac{31}{70}}$$

$$= \frac{16}{31}$$

Hence the desired probability is

$$\frac{16}{31} = 0.516$$



Probability such that transferred ball is black from bag 1 given drawn ball from bag 2

Figure 1: simulation of bernaulli distribution for transferred ball

#### III. SIMULATION PART

Using random variable simulation, bernaulli random variables are generated for the two cases:- P(X=0)=probability for drawnball P(X=1)=probability for transferred ball