

Assignment 13-Probability and Random Variable

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Download latex code from here-

https://github.com/annu100/AI5002-Probability-and-Random-variables/tree/main.tex/ASSIGNMENT_13

$$Pr(y_1|x_1) \times Pr(x_1) = \frac{7}{8} \times \frac{1}{10} \quad (7)$$

$$= \frac{7}{80} \quad (8)$$

Now according to M.A.P criteria at receiver -

$$Pr(y_0|x_0) \times Pr(x_0) > Pr(y_0|x_1) \times Pr(x_1) \quad (9)$$

So, when a symbol is received is received as y_0 , the decision can be made in favour of x_0 in an optimum way.

$$Pr(y_0|x_0) \times Pr(x_0) > Pr(y_0|x_1) \times Pr(x_1) \quad (10)$$

So, when a symbol is received is received as y_0 , the decision can be made in favour of x_0 in an optimum way.

As

$$Pr(y_0|x_0) * Pr(x_0) > Pr(y_0|x_1) * Pr(x_1) \quad (11)$$

So, when a symbol is received is received as y_0 , the decision can be made in favour of x_0 in an optimum way.

$$Pr(y_1|x_0) \times Pr(x_0) > Pr(y_1|x_1) \times Pr(x_1) \quad (12)$$

So, when a symbol is received is received as y_1 , the decision can be made in favour of x_0 in an optimum way.

So, for the given BSC channel, with optimum receiver, both the received symbols will be decoded as x_0 .

Hence, the probability of error is equal to probability of transmitting x_1 .

so, $Pr(error) = Pr(x_1) = \frac{1}{10}$

$$Pr(y_0|x_0) \times Pr(x_0) = \frac{7}{8} \times \frac{9}{10} \quad (1)$$

$$= \frac{63}{80} \quad (2)$$

$$Pr(y_0|x_1) \times Pr(x_1) = \frac{1}{8} \times \frac{1}{10} \quad (3)$$

$$= \frac{1}{80} \quad (4)$$

$$Pr(y_1|x_0) \times Pr(x_0) = \frac{1}{8} \times \frac{9}{10} \quad (5)$$

$$= \frac{9}{80} \quad (6)$$

I. GATE-24 SOLUTION

A binary symmetric channel (BSC) has a transition probability of $\frac{1}{8}$. If the binary transmit symbol X is such that $Pr(X = 0) = \frac{9}{10}$, then the probability of error for an optimum receiver will be-

II. SOLUTIONS

Let x_0 and x_1 are two binary transmitted symbols. y_0 and y_1 are received symbols. transition probability = $Pr(y_1|x_0) = Pr(y_0|x_1)$ Given data-

$$Pr(x_0) = \frac{9}{10}$$

$$Pr(x_1) = 1 - \frac{9}{10} = \frac{1}{10}$$

$$Pr(y_1|x_0) = \frac{1}{8}$$

$$Pr(y_0|x_1) = \frac{1}{8}$$

$$Pr(y_0|x_0) = 1 - \frac{1}{8} = \frac{7}{8}$$

$$Pr(y_1|x_1) = 1 - \frac{1}{8} = \frac{7}{8}$$

Calculating probability values for MAP criteria -