

# Assignment 10-Probability and Random Variable

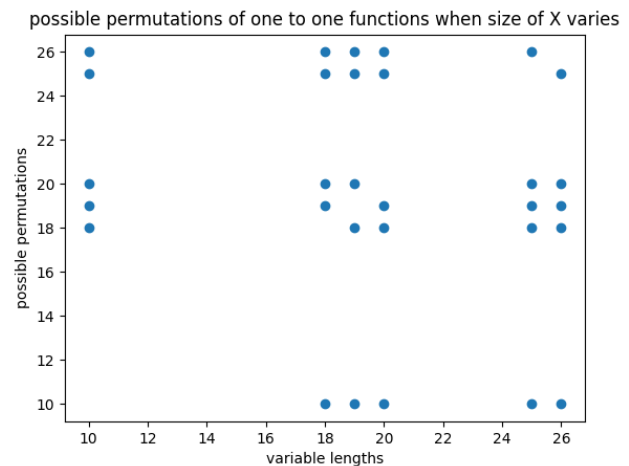
Annu-EE21RESCH01010

Download latex code from here-

[https://github.com/annu100/AI5002-Probability-and-Random-variables/tree/main.tex/ASSIGNMENT\\_10](https://github.com/annu100/AI5002-Probability-and-Random-variables/tree/main.tex/ASSIGNMENT_10)

## I. PROBLEM STATEMENT-GATE 10

Let  $X$  and  $Y$  denote the sets containing 2 and 20 distinct objects respectively and  $F$  denote the set of all possible functions defined from  $X$  to  $Y$ . Let  $f$  be randomly chosen from  $F$ . The probability of  $f$  being one-to-one is .....



## II. SOLUTIONS

Function:  $X \rightarrow Y$

$|Y|=20$

$|X|=2$

total number of functions:  $= 20^2 = 400$

total number of one-one functions:

$$\begin{aligned} {}^{|Y|}P_{|X|} &= {}^{20}P_2 \\ &= 380. \end{aligned}$$

Probability  $= \frac{380}{400} = 0.95$ .

**Another way to see this:**

Every element of  $X$  can take any of the 20 values.

Total  $= 20 \times 20 = 400$ .

For one-one function, Every element of  $X$  takes a different value.

so, total one to one functions are  $= 20 \times 19 = 380$ .

And thus probability is

Probability  $= \frac{380}{400} = 0.95$