

Lecture 3

Module 08

Q. Find the zeroes of the following quadratics Polynomials.

(1) $x^2 - 5x + 6$

Sol.

$$\begin{aligned} & x^2 - 5x + 6 \\ = & 1x^2 - (3x + 2x) + 6 \\ = & x^2 - 3x - 2x + 6 \\ = & x(x - 3) - 2(x - 3) \\ = & (x - 3)(x - 2) \end{aligned}$$

$\therefore (x - 3)$ and $(x - 2)$ are the factors of $x^2 - 5x + 6$

So, the value of $x^2 - 5x + 6$ is zero

When $(x - 3) = 0$ or $(x - 2) = 0$

$$\therefore x - 3 = 0 \quad \text{or} \quad x - 2 = 0$$

$$\therefore x = 3 \quad \text{or} \quad x = 2$$

\therefore The zeroes of $x^2 - 5x + 6$ are 3 and 2.

$$\begin{array}{c} 6 \\ \swarrow \quad \searrow \\ 6 \quad + \quad 1 \quad \neq \quad 1 \\ 3x \quad + \quad 2x \quad = \quad 5x \end{array}$$

Q. Find the zeroes of the following quadratics Polynomials.

(2) $x^2 - 13x - 30$

Sol.

$$x^2 - 13x - 30$$
$$= 1x^2 - (15x - 2x) - 30$$

$$= x^2 - 15x + 2x - 30$$

$$= x(x - 15) + 2(x - 15)$$

$$= (x - 15)(x + 2)$$

$\therefore (x - 15)$ and $(x + 2)$ are the factors of $x^2 - 13x - 30$

So, the value of $x^2 - 13x - 30$ is zero

When $(x - 15) = 0$ or $(x + 2) = 0$

$$\therefore x - 15 = 0 \quad \text{or} \quad x + 2 = 0$$

$$\therefore x = 15 \quad \text{or} \quad x = -2$$

\therefore The zeroes of $x^2 - 13x - 30$ are 15 and -2.

$$\begin{array}{r} 30 \\ \swarrow \quad \searrow \\ 30 \quad - \quad 1 \end{array} \neq 13$$
$$15x - 2x = 13x$$

Module 09

Q. Find the zeroes of the following quadratics Polynomials.

(1) $x^2 - 17x + 60$

Sol.

$$x^2 - 17x + 60$$

$$= 1x^2 - (12x + 5x) + 60$$

$$= x^2 - 12x - 5x + 60$$

$$= x(x - 12) - 5(x - 12)$$

$$= (x - 12)(x - 5)$$

\therefore $(x - 12)$ and $(x - 5)$ are the factors of $x^2 - 17x + 60$

So, the value of $x^2 - 17x + 60$ is zero

When $(x - 12) = 0$ or $(x - 5) = 0$

$$\therefore x - 12 = 0 \text{ or } x - 5 = 0$$

$$\therefore x = 12 \text{ or } x = 5$$

\therefore The zeroes of $x^2 - 17x + 60$ are 12 & 5

$$\begin{array}{c} 60 \\ \swarrow \quad \searrow \\ 10 \quad + \quad 6 \quad \neq \quad 17 \\ 12x + 5x = 17x \end{array}$$

Q. Find the zeroes of the following quadratics Polynomials.

(2) $2x^2 - 5x - 3$

Sol.

$$2x^2 - 5x - 3$$
$$= 2x^2 - (6x - x) - 3$$

$$= 2x^2 - 6x + x - 3$$

$$= 2x(x - 3) + 1(x - 3)$$

$$= (x - 3)(2x + 1)$$

$\therefore (x - 3)$ and $(x + 1)$ are the factors of $2x^2 - 5x - 3$

So, the value of $2x^2 - 5x - 3$ is zero

$$\text{When } (x - 3) = 0 \text{ or } (x + 1) = 0$$

$$\therefore x - 3 = 0 \text{ or } x + 1 = 0$$

$$\therefore x = 3 \text{ or } x = -1$$

\therefore The zeroes of $2x^2 - 5x - 3$ are 3 and -1.

$$\begin{array}{r} 6 \\ \swarrow \quad \searrow \\ 3 \quad - \quad 2 \\ 6x \quad - \quad 1x = 5x \end{array} \neq 5$$

Module 10

Q. Find the zeroes of the following quadratics Polynomials.

(1) $3x^2 - 10x + 8$

Sol.

$$\begin{aligned} & 3x^2 - 10x + 8 \\ = & 3x^2 - (6x + 4x) + 8 \\ = & 3x^2 - 6x - 4x + 8 \\ = & 3x(x - 2) - 4(x - 2) \\ = & (x - 2)(3x - 4) \end{aligned}$$

\therefore $(x - 2)$ and $(3x - 4)$ are the factors of $3x^2 - 10x + 8$

So, the value of $3x^2 - 10x + 8$ is zero

When $(x - 2) = 0$ or $(3x - 4) = 0$

$$\therefore x - 2 = 0 \text{ or } 3x - 4 = 0$$

$$\therefore x = 2 \text{ or } 3x = 4$$

$$\therefore x = 2 \text{ or } 3x = \frac{4}{3} \therefore$$

$$\begin{array}{rcccl} & 24 & & & \\ & \swarrow & & \searrow & \\ 8 & + & 3 & \neq & 10 \\ 6x & + & 4x & = & 10x \end{array}$$

The zeroes of $3x^2 - 10x + 8$ are 2 and $\frac{4}{3}$

Q. Find the zeroes of the following quadratics Polynomials.

(2) $6x^2 - 7x - 13$

Sol.

$$6x^2 - 7x - 13$$

$$= 6x^2 - (13x - 6x) - 13$$

$$= 6x^2 - 13x + 6x - 13$$

$$= x(6x - 13) + 1(6x - 13)$$

$$= (6x - 13)(x + 1)$$

\therefore $(6x - 13)$ and $(x + 1)$ are the factors of $6x^2 - 7x - 13$

So, the value of $6x^2 - 7x - 13$ is zero

When $(6x - 13) = 0$ or $(x + 1) = 0$

$$\therefore 6x - 13 = 0 \text{ or } x + 1 = 0$$

$$\therefore 6x = 13 \text{ or } x = -1$$

$$\therefore 6x = \frac{13}{6} \text{ or } x = -1 \therefore$$

$$\begin{array}{c} 78 \\ \swarrow \quad \searrow \end{array}$$

$$13x - 6x = 7x$$

The zeroes of $6x^2 - 7x - 13$ are $\frac{13}{6}$ and -1

Module 11

Q. Find the zeroes of the following quadratics Polynomials.

(1) $3x^2 - 11x + 6$

Sol.

$$\begin{aligned} & 3x^2 - 11x + 6 \\ = & 3x^2 - (9x + 2x) + 6 \\ = & 3x^2 - 9x - 2x + 6 \\ = & 3x(x - 3) - 2(x - 3) \\ = & (x - 3)(3x - 2) \end{aligned}$$

\therefore $(x - 3)$ and $(3x - 2)$ are the factors of $3x^2 - 11x + 6$

So, the value of $3x^2 - 11x + 6$ is zero

When $(x - 3) = 0$ or $(3x - 2) = 0$

$\therefore x - 3 = 0$ or $3x - 2 = 0$

$\therefore x = 3$ or $3x = 2$

$\therefore x = 3$ or $3x = \frac{2}{3}$

\therefore The zeroes of $3x^2 - 11x + 6$ are 3 and $\frac{2}{3}$

$$\begin{array}{rcccl} & 18 & & & \\ & \swarrow & \searrow & & \\ 6 & + & 3 & \neq & 11 \\ 9x & + & 2x & = & 11x \end{array}$$

Q. Find the zeroes of the following quadratics Polynomials.

(2) $10x^2 + 3x - 4$

Sol.

$$10x^2 + 3x - 4$$

$$= 10x^2 + (8x - 5x) - 4$$

$$= 10x^2 + 8x - 5x - 4$$

$$= 2x(5x + 4) - 1(5x - 4)$$

$$= (5x + 4)(2x - 1)$$

\therefore $(5x + 4)$ and $(2x - 1)$ are the factors of $10x^2 + 3x - 4$

So, the value of $10x^2 + 3x - 4$ is zero

$$\text{When } (5x + 4) = 0 \text{ or } (2x - 1) = 0$$

$$\therefore 5x + 4 = 0 \text{ or } 2x - 1 = 0$$

$$\therefore 5x = -4 \text{ or } 2x = -1$$

$$\therefore x = \frac{-4}{5} \text{ or } 2x = -1$$

\therefore The zeroes of $10x^2 + 3x - 4$ are $\frac{-4}{5}$ and -1 .

$$\begin{array}{c} 40 \\ \swarrow \quad \searrow \\ 10 \quad - \quad 4 \end{array} \neq 3$$
$$8x - 5x = 3x$$

Module 12

Q. Find the zeroes of the following quadratics Polynomials.

(1) $x^2 - x - 132$

Sol.

$$\begin{aligned} & x^2 - x - 132 \\ = & 1x^2 - (12x - 11x) - 132 \\ = & x^2 - 12x + 11x - 132 \\ = & x(x - 12) + 11(x - 12) \\ = & (x - 12)(x + 11) \end{aligned}$$

\therefore $(x - 12)$ and $(x + 11)$ are the factors of $x^2 - x - 132$

So, the value of $x^2 - x - 132$ is zero

When $(x - 12) = 0$ or $(x + 11) = 0$

$$\therefore x - 12 = 0 \text{ or } x + 11 = 0$$

$$\therefore x = 12 \text{ or } x = -11$$

\therefore The zeroes of $x^2 - x - 132$ are 12 and -11.

$$\begin{array}{r} 132 \\ \swarrow \quad \searrow \\ 132 - 1 \neq 1 \\ 12x - 11x = 1x \end{array}$$

Q. Find the zeroes of the following quadratics Polynomials.

(2) $x^2 - 3\sqrt{3}x + 6$

Sol.

$$x^2 - 3\sqrt{3}x + 6$$

$$= 1x^2 - (2\sqrt{3}x + \sqrt{3}x) + 6$$

$$= x^2 - 2\sqrt{3}x - \sqrt{3}x + 6$$

$$= x(x - 2\sqrt{3}) - \sqrt{3}(x - 2\sqrt{3})$$

$$= (x - 2\sqrt{3})(x - \sqrt{3})$$

$\therefore (x - 2\sqrt{3})$ and $(x - \sqrt{3})$ are the factors of $x^2 - 3\sqrt{3}x + 6$

So, the value of $x^2 - 3\sqrt{3}x + 6$ is zero

$$(x - 2\sqrt{3}) = 0 \quad \text{or} \quad (x - \sqrt{3}) = 0$$

$$x = 2\sqrt{3} \quad \text{or} \quad x = \sqrt{3}$$

\therefore The zeroes of are $x^2 - 3\sqrt{3}x + 6$ and $\sqrt{3}$.

$$\begin{array}{c} 6 \\ \swarrow \quad \searrow \\ 2\sqrt{3}x + \sqrt{3}x = 3\sqrt{3}x \end{array}$$

$$\begin{array}{l} 6 = 2 \times 3 \\ = 2 \times \sqrt{3} \times \sqrt{3} \end{array}$$

Thank You