

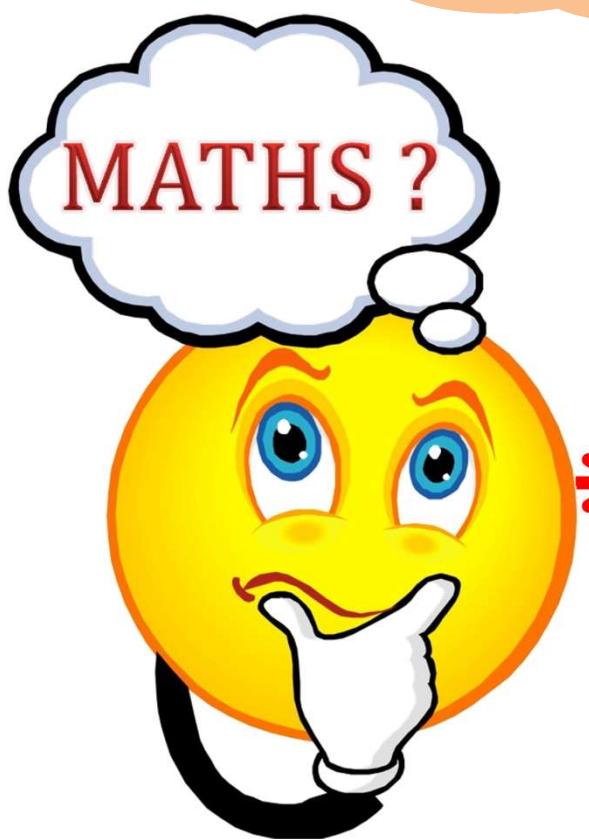
# **Lecture 01**

# Module 01

6 7 5 4  
-8 3 6 7  
3 9 5 -53

# RATIONAL NUMBERS

9 4 7 6 3 5 3 →  
6 5 3

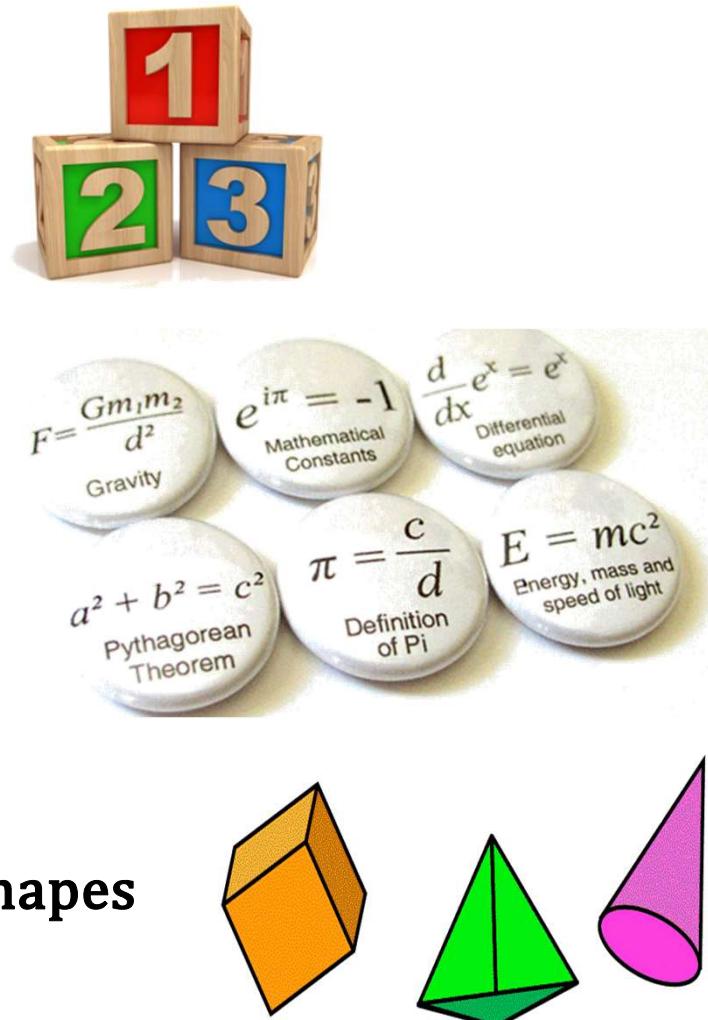


Maths is the study of ?

Formulae

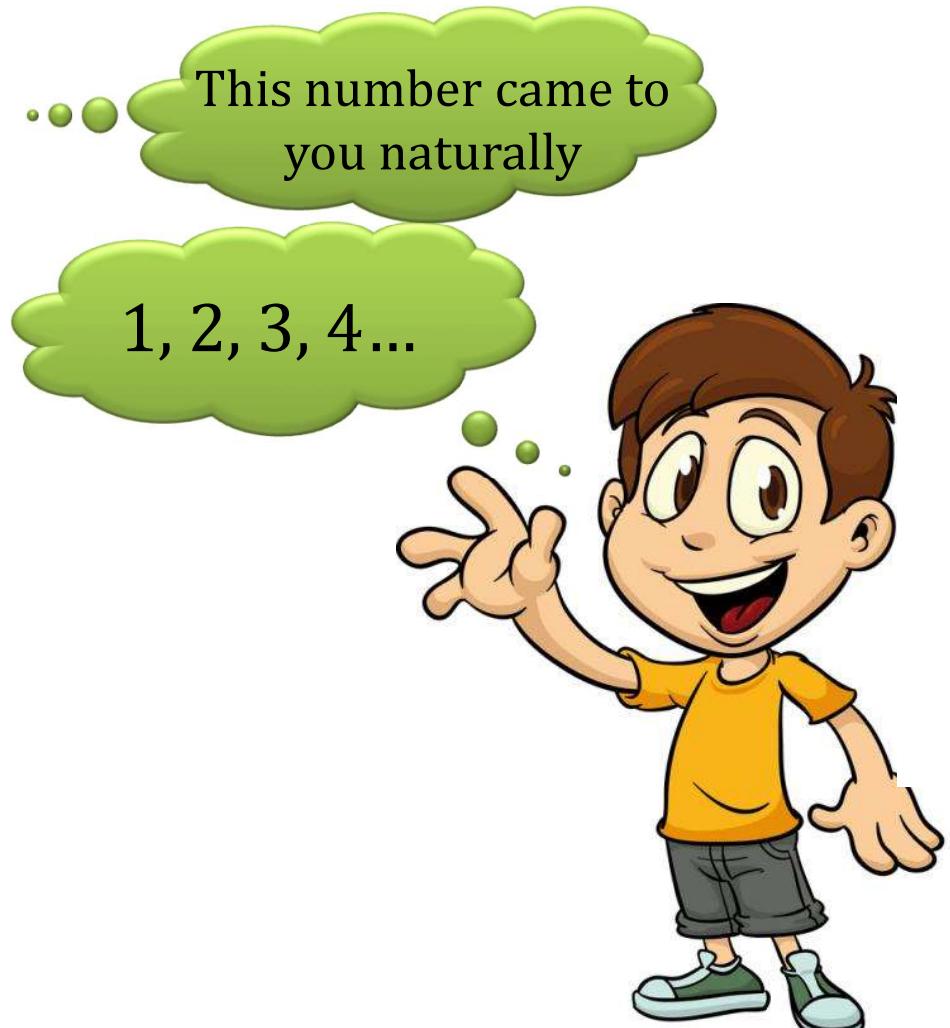


Geometric Shapes



## ⦿ Natural Number

Natural Numbers :      1, 2, 3, 4 , 5 .....



## ⦿ Whole Number

Natural Numbers :  $1, 2, 3, 4, 5 \dots$

Whole Numbers :  $0, 1, 2, 3, 4, 5 \dots$

The collection of number which includes all the natural number and zero



## ⌚ Integers Number

Natural Numbers :  $1, 2, 3, 4, 5 \dots$

Whole Numbers :  $0, 1, 2, 3, 4, 5 \dots$

Integers :  $\dots -3, -2, -1, 0, 1, 2, 3, 4, 5 \dots$

The slide features a dark blue background with two examples of integer addition on the left. Each example has a light green thought bubble on the right containing two statements: "It is a Natural Number" and "It is a Whole Number". The first example shows  $3 + 4 = 7$ . The second example shows  $2 - 3 = -1$ .

$3$   
+  $4$   
—  
 $7$

It is a Natural Number ✓  
It is a Whole Number ✓

$2$   
-  $3$   
—  
 $-1$

It is a Natural Number ✗  
It is a Whole Number ✗

## COMMUTATIVITY

Two rational numbers can be added in any order

Operation	Numbers	Remarks
Addition	<p>What do you observe ?</p> <p>And <math>7 = \boxed{7}</math>; <math>7 + 0 = \boxed{7}</math></p> <p><math>i.e., 0 + 7 = \boxed{7} + \boxed{0}</math></p> <p>Lets take an example</p> <p>Take two numbers a and b,</p> $a + b = b + a$	Addition is commutative

## COMMUTATIVITY

Operation	Numbers	Remarks
Subtraction	<p>What do you observe ?</p> <p>And</p> $0 = \boxed{7}; 0 - 7 = \boxed{-7}$ <p>I 7 - 0 <math>\neq</math> 0 - 7 an example</p>	Subtraction is not commutative

## COMMUTATIVITY

Two rational numbers can be multiplied in any order

Operation	Numbers	Remarks
Multiplication	<p>What do you observe ?</p> <p>And <math>7 \times 0 = 0</math>; <math>0 \times 7 = 0</math></p> <p>Lets take an example</p> <p>Take two rational numbers a and b,</p> $a \times b = b \times a$	Multiplication is commutative

## COMMUTATIVITY

Operation	Numbers	Remarks
Division	<p>What do you observe ?</p> <p>And <math>0 = \boxed{N.d};</math> <math>0 \div 7 = \boxed{0}</math></p> <p>I <math>7 \div 0 \neq 0 \div 7</math> an example</p>	Division is not commutative

## Module 02

## ASSOCIATIVITY

Three rational numbers can be grouped in any order

Operation	Numbers	Remarks
Addition	<p>What do you observe ?</p> <p>And <math>(2+5) + 7 = 14</math> <math>(7+2) + 5 = 14</math></p> <p>i.e. <math>(a+b)+c = a+(b+c)</math></p> <p>Lets take an example... Whole numbers and c</p> $a + (b + c) = (a + b) + c$	Addition is associative

## ASSOCIATIVITY

Operation	Numbers	Remarks
Subtraction	<p>What do you observe ?</p> <p>And</p> $7 - (2 - 5) = 10$ $(7 - 2) - 5 = 0$ <p><math>7 - (2 - 5) \neq (7 - 2) - 5</math></p> <p>an example</p>	Subtraction is not associative

## ASSOCIATIVITY

Three rational numbers can be grouped in any order

Operation	Numbers	Remarks
Multiplication	<p>What do you observe ?</p> <p>And <math>(2 \times 5) = 10</math>   <math>(7 \times 2) \times 5 = 70</math></p> <p>i.e. <math>7 \times (2 \times 5) = (7 \times 2) \times 5</math></p> <p>Let's take</p> <p>For any two whole numbers a, b and c</p> $a \times (b \times c) = (a \times b) \times c$	Multiplication is associative

## ASSOCIATIVITY

Operation	Numbers	Remarks
Divide	<p>What do you observe ?</p> <p>And</p> $(2 \div 5) = 17.5$ $(7 \div 2) \div 5 = 0.7$ <p><math>7 \div (2 \div 5) \neq (7 \div 2) \div 5</math></p> <p>an example</p>	Subtraction is not associative

## Additive Inverse

Q.1) Write the additive inverse of each of the following.

Examples:

(i)  $\frac{2}{8}$

Negative of  
Integers

Sol.

$$\frac{2}{8} \times -1 = \frac{-2}{8}$$

(ii)  $\frac{-5}{9}$

Sol.

$$\frac{-5}{9} \times -1 = \frac{5}{9}$$

## Additive Inverse

Q.1) Write the additive inverse of each of the following.

Examples:

(iii)  $\frac{-6}{-5}$

Negative of  
Integers

Sol.

$$\frac{-6}{-5} = \frac{6}{5} \times -1 = \frac{6}{-5}$$

## Multiplicative Inverse

Q.2) Write the multiplicative inverse of each of the following.

Examples:

(i)  $-13$

Reciprocal of  
Integers

Sol.

$$-13 = \frac{1}{-13}$$

(ii)  $\frac{-13}{19}$

Sol.

$$\frac{-13}{19} = \frac{19}{-13}$$

## Module 03



Find using distributivity

$$\text{Q. } \left\{ \frac{7}{5} \times \left( \frac{-3}{12} \right) \right\} + \left\{ \frac{7}{5} \times \frac{5}{12} \right\}$$

Since denominator  
is same

Sol.

$$\begin{aligned} \left\{ \frac{7}{5} \times \left( \frac{-3}{12} \right) \right\} + \left\{ \frac{7}{5} \times \frac{5}{12} \right\} &= \frac{7}{5} \times \left\{ \frac{-3}{12} + \frac{5}{12} \right\} \\ &= \frac{7}{5} \times \left\{ \frac{-3 + 5}{12} \right\} \\ &= \frac{7}{5} \times \frac{2}{12} \\ &= \frac{7}{30} \end{aligned}$$



Using appropriate properties find:

Q.  $\frac{2}{5} \times \left( -\frac{3}{7} \right) - \frac{1}{6} \times \frac{1}{2} + \frac{1}{14} \times \frac{2}{5}$

Sol.  $= \frac{2}{5} \times \left( -\frac{3}{7} \right) + \frac{1}{14} \times \frac{2}{5} - \frac{1}{4}$  (Using commutativity)

What are the  
uncommon factors?

$$= \frac{2}{5} \left( \frac{-3}{7} + \frac{1}{14} \right) - \frac{1}{4}$$
 (Using distributivity)

$$= \frac{2}{5} \left( \frac{-42 + 7}{98} \right) - \frac{1}{4}$$

$$= \frac{2}{5} \times \frac{-35}{98} - \frac{1}{4}$$

$$= \frac{-1}{7} - \frac{1}{4}$$

$$= \frac{-4 - 7}{28}$$

$$= \frac{-11}{28}$$

## Module 04

**Q. Using appropriate properties find**

$$-\frac{2}{3} \times \frac{3}{5} + \frac{5}{2} - \frac{3}{5} \times \frac{1}{6}$$

Sol.

$$-\frac{2}{3} \times \frac{3}{5} + \frac{5}{2} - \frac{3}{5} \times \frac{1}{6}$$

$$= -\frac{2}{3} \times \frac{3}{5} + \frac{3}{5} \times \frac{1}{6} + \frac{5}{2}$$

What are the  
uncommon factors?

(Using associativity)

$$= \frac{3}{5} \left( -\frac{2}{3} - \frac{1}{6} \right) + \frac{5}{2} \quad \text{(using distributivity)}$$

$$= \frac{3}{5} \left( -\frac{4}{6} - \frac{1}{6} \right) + \frac{-2 \times 2}{3 \times 2} - \frac{1}{6}$$

$$= \frac{3}{5} \times \frac{-5}{6} + \frac{5}{2}$$

$$= -\frac{1}{2} + \frac{5}{2}$$

= 2

**Q. Name the property under multiplication used in each of the following:**

Sr. No.	Rational number	Multiplication	Is this in the form of $a \times 1 = 1 \times a = a$	Yes!
(i)	$\frac{-4}{5} \times 1 = 1 \times \frac{-4}{5}$	$= -\frac{4}{5}$ 1 is the multiplier	When we multiply rational number with 1, we get that rational number as the product	

## **Lecture 02**

## Module 05



Q. Write five rational numbers which are smaller than 2.

Sol.

$\frac{1}{3}$ ,  $\frac{1}{4}$ ,  $\frac{1}{2}$ ,  $\frac{-1}{2}$ ,  $\frac{-1}{5}$ , and so on.

**Q.** Find ten rational numbers between:

**Q.**  $\frac{-2}{5}$  and  $\frac{1}{2}$

**Sol.**

$$\frac{-2}{5} = \frac{-2 \times 2}{5 \times 2} = \frac{-4}{10}$$

$$\frac{1}{2} = \frac{1 \times 5}{2 \times 5} = \frac{5}{10}$$

Converting  $\frac{-2}{5}$  and  $\frac{1}{2}$  having same

denominators such that difference

between the numerators is less than 10

The difference between  
the numerators is not  
more than 10

Ten rational numbers between  $\frac{-2}{5}$  and  $\frac{1}{2}$  are

$$\frac{-7}{20}, \frac{-6}{20}, \frac{-5}{20}, \frac{-4}{20}, \frac{-3}{20}, \frac{-2}{20}, \frac{-1}{20}, 0, \frac{1}{20}, \frac{2}{20}$$

**Q.** Find five rational numbers between:

**Q.**  $\frac{1}{4}$  and  $\frac{1}{2}$

**Sol.**

$$\frac{1}{4} = \frac{1 \times 8}{4 \times 8} = \frac{8}{32}$$

$$\frac{1}{2} = \frac{1 \times 4}{2 \times 4} = \frac{4}{8}$$

Converting  $\frac{1}{4}$  and  $\frac{1}{2}$  having same denominators such that difference between the numerators is more than 5.

difference between the numerators is not more than 5.

Five rational numbers between  $\frac{1}{4}$  and  $\frac{2}{4}$  having same denominators such that difference between the numerators is more than 5.

$$\frac{9}{32}, \frac{10}{32}, \frac{11}{32}, \frac{12}{32}, \frac{13}{32}$$

## Module 06



Q. Verify that  $-(-x) = x$  for :

Sol.

$$x = \left( -\frac{13}{17} \right)$$

$$x = -\frac{13}{17} \dots(i)$$

Multiplying  $\begin{array}{c} - \\ - \\ - \end{array} = +$  on both the sides

$$-1 \times x = -1 \times \left( -\frac{13}{17} \right)$$

$$-x = +\frac{13}{17}$$

Multiplying  $-1$  on both the sides

$$\begin{array}{c} - \\ + \\ - \end{array} = -$$

$$-1 \times (-x) = -1 \times \left( +\frac{13}{17} \right)$$

$$-(-x) = x$$

we need to prove

In order to find  $-x$

$$-(-x) = -\frac{13}{17} \dots(ii)$$

But  $\frac{-13}{17}$  is the value of  $x$

In order to find  $-(-x)$

[ From (i) and (ii)]



Q. Find five rational numbers between:

Q.  $\frac{2}{3}$  and  $\frac{4}{5}$

Sol.

$$\frac{2}{3} = \frac{2 \times 20}{3 \times 20} = \frac{40}{60}$$

$$\frac{4}{5} = \frac{4 \times 12}{5 \times 12} = \frac{48}{60}$$

What are next number between 40 to 48?

$$\frac{41}{60}, \frac{42}{60}, \frac{43}{60}, \frac{44}{60}, \frac{45}{60}$$

Converting  $\frac{2}{3}$  and  $\frac{4}{5}$  having same denominators such that difference between denominators is more than 5.

Now, any five rational numbers are  $\frac{41}{60}, \frac{42}{60}, \frac{43}{60}, \frac{44}{60}, \frac{45}{60}$



Q. Find five rational numbers between:

Q.  $\frac{-3}{2}$  and  $\frac{5}{3}$

Sol.

$$\frac{-3}{2} = \frac{-3 \times 3}{2 \times 3} = \frac{-9}{6}$$

$$\frac{5}{3} = \frac{5 \times 2}{3 \times 2} = \frac{10}{6}$$

What are next number between -9 to -10 ?

$$\frac{-8}{6}, \frac{-7}{6}, \frac{-6}{6}, \dots, \frac{1}{6}, \frac{2}{6}$$

Count

denominators. we have

Same denominators

$\therefore$  Five rational numbers are  $\frac{-8}{6}, \frac{-7}{6}, \frac{-6}{6}, \frac{1}{6}, \frac{2}{6}$



Q. Find five rational numbers between  $\frac{3}{5}$  and

Q.  $\frac{3}{5}$  and  $\frac{3}{4}$

Sol.

$$\frac{3}{5} = \frac{3 \times 20}{5 \times 20} = \frac{60}{100}$$

$$\frac{3}{4} = \frac{3 \times 25}{4 \times 25} = \frac{75}{100}$$

What are numbers between 60 to 75 ?

$$\frac{61}{100}, \frac{62}{100}, \frac{63}{100}, \frac{64}{100}, \frac{65}{100}$$

$$\frac{66}{100}, \frac{67}{100}, \frac{68}{100}, \frac{69}{100}, \frac{70}{100} \dots$$

$\therefore$  Ten rational numbers are  $\frac{61}{100}, \frac{62}{100}, \frac{63}{100}, \frac{64}{100}, \frac{65}{100}, \frac{66}{100}, \frac{67}{100}, \frac{68}{100}, \frac{69}{100}, \frac{70}{100}$

## Module 07

**Q. Find the multiplicative inverse of the following**

Sr. No.	Rational number	M
(i)	$-1 \times \frac{-2}{5} = \frac{2}{5}$	$\frac{5}{2}$
(ii)	$-1$	$\frac{5}{2}$

What is the reciprocal of  $\frac{2}{5}$

$$\frac{-1}{1} = -1$$

**Q. Verify that  $-(-x) = x$  for :**

$$x = \frac{11}{15}$$

Sol.

$$x = \frac{11}{15} \dots(i)$$

Multiplying  $-1$  on both the sides

$$-1 \times x = -1 \times \frac{11}{15}$$

$$-x = -\frac{11}{15}$$

Multiplying  $-1$  on both the sides

$$- \times - = +$$

$$-1 \times (-x) = -1 \times \left( -\frac{11}{15} \right)$$

We need to prove  
 $-(-x) = x$

$$-(-x) = \frac{11}{15} \dots(ii)$$

But  $\frac{11}{15}$  is the value of  $x$

In order to find  $-(-x)$

[ From (i) and (ii)]

## Module 08



Q. Find the multiplicative inverse of the following

Sr. No.	Rational number	Multiplicative inverse
(i)	- 13	What is the reciprocal of $\frac{-13}{1}$
(ii)	$\frac{-13}{19}$	What is the reciprocal of $\frac{-13}{19}$
(iii)	$\frac{1}{5}$	What is the reciprocal of $\frac{1}{5}$
(iv)	$\frac{-5}{8} \times \frac{-3}{7} = \frac{15}{56}$ $(-5) \times (-3)$ $8 \times 7$ $= \frac{15}{56}$	$\frac{56}{15}$ What is the reciprocal of $\frac{15}{56}$

What is the reciprocal of  $\frac{-13}{1}$

What is the reciprocal of  $\frac{-13}{19}$

What is the reciprocal of  $\frac{1}{5}$

What is the reciprocal of  $\frac{15}{56}$

$\frac{56}{15}$



Q. Name the property under multiplication.

Sr. No. Multiplicative

(i) 
$$-\frac{13}{17} \times \frac{-2}{7} = \frac{-2}{7} \times -\frac{13}{17}$$

(ii) 
$$a \times b = b \times a$$

Property

Commutativity

Multiplicative inverse

What is the reciprocal of  $\frac{-19}{29}$

$a \times b = b \times a$

YES!

Whenever a number multiplied by its reciprocal then which property is used?

Com

Multiplicative  
inverse



Q. Multiply  $\frac{6}{13}$  by the reciprocal of  $\frac{-7}{16}$ .

What is the reciprocal of  $\frac{-7}{16}$

$$\therefore \frac{6}{13} \times \left( \text{Reciprocal of } \frac{-7}{16} \right)$$
$$\therefore \frac{6}{13} \times \left( \frac{-16}{7} \right)$$
$$= \frac{6 \times (-16)}{13 \times 7}$$
$$= \frac{-96}{91}$$

## **Lecture 03**

## Module 09

Q. Tell what property allows you to compute

$$\left(\frac{1}{3} \times 6 \times \frac{4}{3}\right) \text{ as } \left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$$

Is this in the form of  $a \times (b \times c) = (a \times b) \times c$  

So what is the property called as ?

Associativity

In computing  $\frac{1}{3} \times \left(6 \times \frac{4}{3}\right)$  as  $\left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$   
we use the **associativity property**.

Q. Is  $\frac{8}{9}$  the multiplicative inverse of  $-1\frac{1}{8}$  why or why not ?

Sol.

$$\frac{8}{9} \times \left(-1\frac{1}{8}\right)$$

$$= \frac{\cancel{8}}{\cancel{9}} \times \frac{-9^{-1}}{8}$$

$$= -1$$

$$\neq 1$$

The product of a rational number and its multiplicative inverse is equal to 1.

$\therefore \frac{8}{9}$  is not the multiplicative inverse of  $-1\frac{1}{8}$  because the product is not 1.

Q. Is 0.3 the multiplicative inverse of  $3\frac{1}{3}$  why or why not ?

Sol.

$$\begin{aligned} & 0.3 \times 3\frac{1}{3} \\ &= \frac{3}{10} \times \frac{10}{3} \\ &= 1 \end{aligned}$$

$\therefore$  0.3 is the multiplicative inverse of  $3\frac{1}{3}$  as the product is 1.

The product of a rational number and its multiplicative inverse is equal to 1.

# Module 10

**Q. Write.**

1

**The rational number that does not have a reciprocal**

**Sol.**

0

2

**The rational numbers that are equal  
to their reciprocals.**

**Sol.**

1 and -1

3

**The rational number that is equal to its negative.**

**Sol.**

0

### Q. Fill in the blanks:

- (i) Zero has No reciprocal.
- (ii) The numbers 1 and -1 are their own reciprocals.
- (iii) The reciprocal of - 5 is  $\frac{-1}{5}$ .
- (iv) Reciprocal of  $\frac{1}{x}$ , where  $x \neq 0$  is  $x$ .
- (v) The product of two rational numbers is always a Rational Number
- (vi) The reciprocal of a positive rational number is Positive.

# Module 11

Q. Simplify  $\frac{8}{-15} + \frac{4}{-3}$

Sol.

$$\begin{aligned}\frac{8}{-15} + \frac{4}{-3} &= \frac{8 \times -1}{-15 \times -1} + \frac{4 \times -1}{-3 \times -1} \\&= \frac{-8}{15} + \frac{-4}{3} \dots \text{Denominators are equal} \\&= \frac{-8}{15} + \frac{-4 \times 5}{3 \times 5} \\&= \frac{-8}{15} + \frac{-20}{15} \dots \text{Denominators are equal} \\&= \frac{-8 + (-20)}{15} \\&= \frac{-8 - 20}{15} \\&= \frac{-28}{15}\end{aligned}$$

Denominators of both rational numbers are not positive

Q. Add  $\frac{5}{12}$  and  $\frac{3}{8}$

Sol.

$$\begin{aligned} & \frac{5}{12} + \frac{3}{8} \\ &= \frac{5 \times 2}{12 \times 2} + \frac{3 \times 3}{8 \times 3} \\ &= \frac{10}{24} + \frac{9}{24} \\ &= \frac{10 + 9}{24} \\ &= \frac{19}{24} \end{aligned}$$

$$12 \times 2 = 24$$

$$8 \times 3 = 24$$

Denominators of both rational numbers are positive

Denominators of both rational numbers are not equal

Lets add the numerators

make them equal by taking L.C.M

2	12, 8
2	6, 4
2	3, 2
3	3, 1
1, 1	

LCM of 12 and 8  
=  $2 \times 2 \times 2 \times 3$   
=  $\boxed{24}$

Q. Simplify  $\frac{7}{-26} + \frac{16}{39}$

Sol.

$$\begin{aligned}
 & \frac{7}{-26} + \frac{16}{39} \\
 &= \frac{7 \times -1}{-26 \times -1} + \frac{16}{39} \\
 &= \frac{-7}{26} + \frac{16}{39} \\
 &= \frac{-7 \times 3}{26 \times 3} + \frac{16 \times 1}{39 \times 1} \\
 &= \frac{-21}{78} + \frac{32}{78} \\
 &= \frac{-21+32}{78} \\
 &= \frac{11}{78}
 \end{aligned}$$

Multiply & divide by -1

$$39 \times 2 = 78$$

Denominators are same  
Let's add the numerators

Lets make  
taking LCM

13	26, 39
2	2, 3
3	1, 3
	1, 1

LCM of 26 and 39  
 $= 13 \times 2 \times 3$   
 $= 78$

## Module 12

Q.

$$4 \times ? = 3 \times 6 \times ? = 12$$

Denominators of eq 1

$$2 \times ? =$$

Sol.

$$\frac{-7}{4} + \frac{5}{3} + \frac{-5}{6} + \frac{1}{3} + \frac{-1}{2}$$

Lets find L.C.M of 4, 3, 6 & 2

2	2, 3, 3, 1
3	1, 3, 3, 1
	1, 1, 1, 1

LCM of 4,3,6,2

$$= 2 \times 2 \times 3 \\ = [12]$$

$$= \frac{-7 \times 3}{4 \times 3} + \frac{5 \times 4}{3 \times 4} + \frac{-5 \times 2}{6 \times 2} + \frac{1 \times 4}{3 \times 4} + \frac{-1 \times 6}{2 \times 6}$$

$$= \frac{-21}{12} + \frac{20}{12} + \frac{-10}{12} + \frac{4}{12} + \frac{-6}{12}$$

$$= \frac{-21 + 20 + (-10) + 4 + (-6)}{12}$$

$$= \frac{-37 + 24}{12}$$

$$= \frac{-13}{12}$$

Denominators of eq. 1

Let's n

$$Q. \text{ Evaluate } \frac{-12}{5} + \frac{-7}{20} + \frac{3}{14} + \frac{1}{7} + \frac{-1}{10}$$

$$= \frac{-12 \times 28}{5 \times 28} + \frac{-7 \times 7}{20 \times 7} + \frac{3 \times 10}{14 \times 10} + \frac{1 \times 20}{7 \times 20} + \frac{-1 \times 14}{10 \times 14}$$

$$= \frac{-336}{140} + \frac{-49}{140} + \frac{30}{140} + \frac{20}{140} + \frac{-14}{140}$$

$$= \frac{-336 + (-49) + 30 + 20 + (-14)}{140}$$

$$= \frac{-399 + 50}{140}$$

$$= \frac{-349}{140}$$

Sol.

2	5, 20, 14, 7, 10
5	5, 10, 7, 7, 5
7	1, 2, 7, 7, 1
2	1, 2, 1, 1, 1
	1, 1, 1, 1, 1

LCM of 5, 20, 14, 7, 10

$$= 2 \times 5 \times 7 \times 2 \\ = \boxed{140}$$

## Module 13



Prove that :

Q.  $\left( \frac{-3}{16} \times \frac{8}{15} \right) = \left( \frac{8}{15} \times \frac{-3}{16} \right)$

Sol.

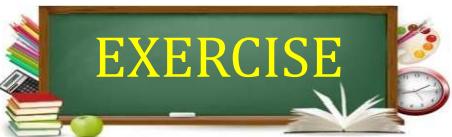
$$\text{LHS} = \left( \frac{\boxed{-3}}{\boxed{16}} \times \frac{\boxed{8}}{\boxed{15}} \right) = \frac{(-3) \times 8}{16 \times 15} = \frac{\cancel{1}^{-24}}{\cancel{10}^{240}} = \frac{-1}{10}$$

$$\text{RHS} = \left( \frac{\boxed{8}}{\boxed{15}} \times \frac{\boxed{-3}}{\boxed{16}} \right) = \frac{8 \times (-3)}{15 \times 16} = \frac{\cancel{1}^{-24}}{\cancel{10}^{240}} = \frac{-1}{10}$$

$$\therefore \text{LHS} = \text{RHS}$$

Hence,  $\left( \frac{-3}{16} \times \frac{8}{15} \right) = \left( \frac{8}{15} \times \frac{-3}{16} \right)$

Now open the  
Bracket



Solve :

Q.  $\frac{3}{5} + \frac{7}{3} + \frac{-11}{5} + \frac{-2}{3}$

Let us group the term with same denominator

Sol.

$$\begin{aligned}\frac{3}{5} + \frac{7}{3} + \frac{-11}{5} + \frac{-2}{3} &= \left( \frac{3}{5} + \frac{-11}{5} \right) + \left( \frac{7}{3} + \frac{-2}{3} \right) \\&= \frac{\{3 + (-11)\}}{5} + \frac{\{7 + (-2)\}}{3} \\&= \frac{-8}{5} + \frac{5}{3} \\&= \frac{(-24 + 25)}{15} \\&= \frac{1}{15}\end{aligned}$$

Since there are  
equal denominator

## **Lecture 04**

## Module 14

Q. Solve  $\left(\frac{-3}{2} \times \frac{4}{5}\right) + \left(\frac{9}{5} \times \frac{-10}{3}\right) - \left(\frac{1}{2} \times \frac{3}{4}\right)$

Sol.

$$\begin{aligned}& \left(\frac{-3}{2} \times \frac{4}{5}\right) + \left(\frac{9}{5} \times \frac{-10}{3}\right) - \left(\frac{1}{2} \times \frac{3}{4}\right) \\&= \frac{-3 \times 4}{2 \times 5} + \frac{9 \times -10}{5 \times 3} - \frac{1 \times 3}{2 \times 4} \\&= \frac{-3 \times 2}{1 \times 5} + \frac{2 \times 2}{5 \times 1} - \frac{1 \times 8}{2 \times 5} \quad \text{L.C.M of } 5, 1, 8 \text{ is } 40 \\&= \frac{-6}{5} + \frac{4}{1} - \frac{3}{8} = 40 \\&= \frac{-6 \times 8}{5 \times 8} + \frac{-6 \times 40}{1 \times 40} - \frac{3 \times 5}{8 \times 5} \\&= \frac{-48}{40} - \frac{240}{40} - \frac{15}{40} \\&= \frac{-48 - 240 - 15}{40} \\&= \frac{-303}{40}\end{aligned}$$

Q.  $\left(\frac{-7}{18} \times \frac{15}{-7}\right) - \left(1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times \frac{1}{4}\right)$

Sol.

$$\begin{aligned}
 & \left(\frac{-7}{18} \times \frac{15}{-7}\right) - \left(1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times \frac{1}{4}\right) \\
 &= \frac{1}{6} \cancel{18} \times \cancel{-7}^5 - \frac{1 \times 1}{1 \times 4} + \frac{1 \times 1}{2 \times 4} \\
 &= \frac{1 \times 5}{6 \times 1} - 4 \times ? + 8 \times ? = 24 \\
 &= \frac{5}{6} - 4 - 8 \\
 &= \frac{5 \times 4}{6 \times 4} - \frac{1 \times 6}{4 \times 6} + \frac{1 \times 3}{8 \times 3} \\
 &= \frac{20}{24} - \frac{6}{24} + \frac{3}{24} \\
 &= \frac{20 - 6 + 3}{24} \\
 &= \frac{23 - 6}{24} \\
 &= \frac{17}{24}
 \end{aligned}$$

L.C.M of 6, 4, 8

2	6, 4, 8
2	3, 2, 4
2	3, 1, 2
3	3, 1, 1
1	1, 1, 1

=  $2 \times 2 \times 2 \times 3$   
=  $\boxed{24}$

## Module 15



Q. Fill in the blanks :

$$\frac{27}{16} \div (\dots) = \frac{-15}{8}$$

Let us assume  $\frac{a}{b}$

Sol.

To convert  
÷ to ×

But, we have to  
find the value  
of  $\frac{a}{b}$

$$\frac{27}{16} \div \left( \frac{a}{b} \right) = \frac{-15}{8}$$

$$\frac{27}{16} \times \frac{b}{a} = \frac{-15}{8}$$

What is the  
reciprocal of  $\frac{a}{b}$ ?

$$= \frac{b}{a}$$

$$\therefore \frac{b}{a} = \frac{-15}{8} \times \frac{16}{27}$$

$$\therefore \frac{b}{a} = \frac{10}{9}$$

$$\therefore \frac{a}{b} = \frac{-9}{10}$$

What is the  
reciprocal of  $\frac{-10}{9}$ ?

$$= \frac{-9}{10}$$

Hence, the missing number is

$$\boxed{\frac{-9}{10}}$$





Q. What number should be added to  $\frac{-7}{8}$  to get  $\frac{4}{9}$ ?

Sol.

Let the other number to be added be  $x$

We have to find the value of  $x$



$$\begin{aligned}x + \frac{-7}{8} &= \frac{4}{9} \\ \therefore x &= \frac{4}{9} - \left( \frac{-7}{8} \right) \\ \therefore x &= \frac{4+7}{9+8} \\ \therefore x &= \frac{(32+63)}{72} \\ \therefore x &= \frac{95}{72}\end{aligned}$$

Hence, the required number is





Q. What number should be subtracted from  $\frac{-5}{7}$  to get  $\frac{-7}{16}$

Since x is subtracted  
from  $\frac{-7}{16}$

Sol.

Let the other number to be subtracted be  $x$

$$\begin{aligned}\frac{-5}{7} - x &= -1 \\ \therefore -x &= -1 - \left( \frac{-5}{7} \right) \\ \therefore -x &= \frac{-1 + 5}{7} \\ \therefore -x &= \frac{(-7 + 5)}{7} \\ \therefore -x &= \frac{-2}{7} \\ \therefore x &= \frac{2}{7}\end{aligned}$$



We have to find the value of  $x$

Hence, the required number is

$$\frac{2}{7}$$





Q. The sum of two rational numbers is  $-5$ . If one of them is  $\frac{-13}{6}$ . Find the other

Sol.

Let the other number be  $x$ .

$$\begin{aligned}x + \frac{-13}{6} &= -5 \\ \therefore x &= -5 - \left( \frac{-13}{6} \right) \\ \therefore x &= \left( \frac{-5}{1} + \frac{13}{6} \right) \\ \therefore x &= \frac{(-30 + 13)}{6} \\ \therefore x &= \frac{-17}{6}\end{aligned}$$

Hence, the required number is  $\frac{-17}{6}$



## Module 16



Q. Tell what property allows you to compute

$$\frac{1}{3} \times 6 \times \frac{4}{3}$$
 as  $\left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$

Is this in the form of  $a \times (b \times c) = (a \times b) \times c$  **Yes!**

In computing  $\frac{1}{3} \times \left(6 \times \frac{4}{3}\right)$  as  $\left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$   
we use the **associativity**

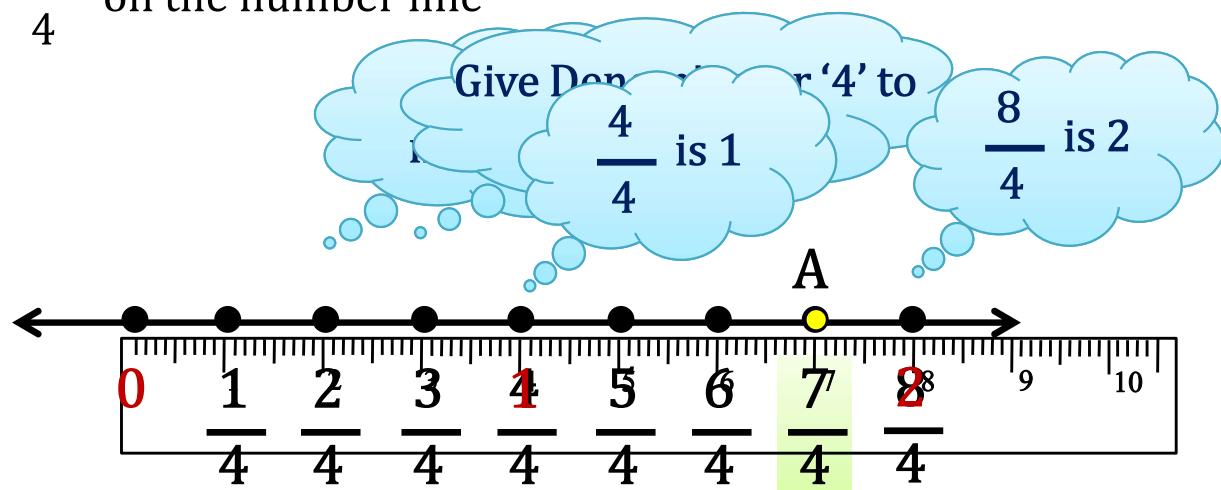
So what is the property called as ?

**Associativity**



Q. Represent  $\frac{7}{4}$  on the number line

Q.  $\frac{7}{4}$



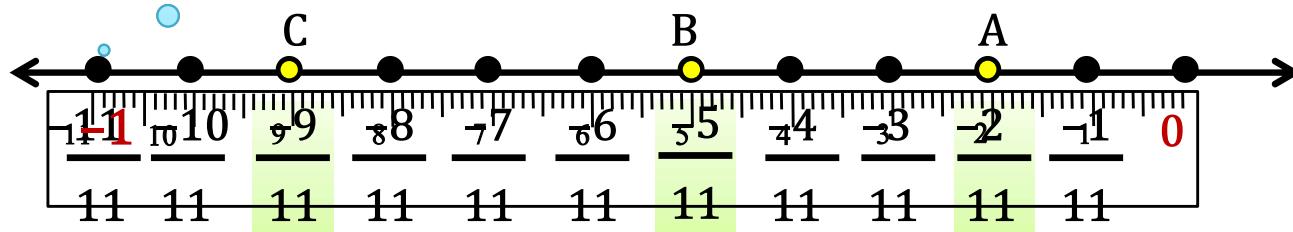


Q. Represent  $\frac{-2}{11}, \frac{-5}{11}, \frac{-9}{11}$  on the number line

Q.  $\frac{-2}{11}, \frac{-5}{11}, \frac{-9}{11}$

$\frac{-11}{11}$  is -1

Give Denominator '11' to each number

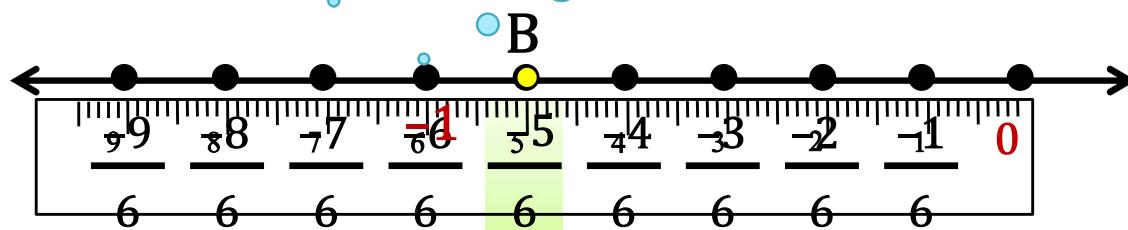




Q. Represent  $\frac{-5}{6}$  on the number line

Q.  $\frac{-5}{6}$

Give Dev  
e.  
 $\frac{-6}{6}$  is -1



## Module 17

## Example 1

Which of the numbers  $\frac{3}{-4}$  and  $\frac{-5}{6}$  is greater ?

**Sol.**

$$\text{One number} = \frac{3}{-4} = \frac{3 \times (-1)}{-4 \times (-1)} = -\frac{3}{4}$$

Which is the negative sign?

- 5  
—  
6

## LCM of 4 and 6

$$\therefore \frac{-3}{4} = \frac{(-3) \times \text{First}}{4 \times \text{Second}}$$

To copy  
Fire each

Multiply the fraction by  $\frac{1}{6}$  to get 12 ?

$$\therefore \frac{-5}{6} = -\underline{3}$$

# 12 denominator

$$\therefore -9 > -10$$

$$\therefore \text{Hence, } \frac{3}{-4} > \frac{-5}{6}$$

**Example 2**

Arrange the numbers  $\frac{-3}{5}$ ,  $\frac{7}{-10}$  and  $\frac{-5}{8}$  in ascending order.

**Sol.**

We have  $\frac{7}{-10} = \frac{7 \times (-1)}{(-10) \times (-1)} = -\frac{7}{10}$

Thus, the given numbers are  $\frac{-3}{5}$ ,  $\frac{7}{-10}$  and  $\frac{-5}{8}$ .

LCM of 5, 10 and 8 is 40.

$\therefore \frac{-3}{5} = \frac{(-3) \times 8}{5 \times 8} = \frac{-24}{40}$

First we make the denominators same by multiplying by -1.

$\therefore \frac{-7}{10} = \frac{(-7) \times 4}{10 \times 4} = \frac{-28}{40}$

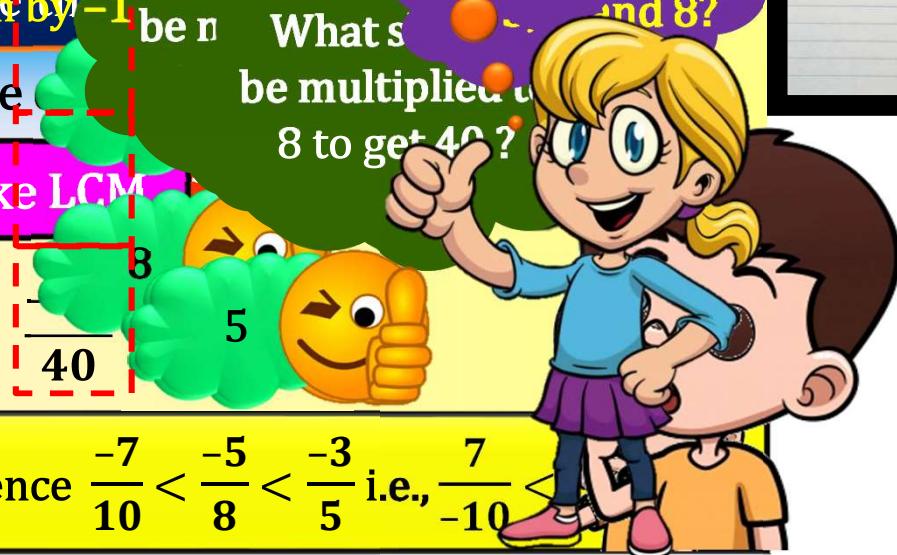
$\therefore \frac{-5}{8} = \frac{(-5) \times 5}{8 \times 5} = \frac{-25}{40}$

$\therefore \frac{-28}{40} < \frac{-25}{40} < \frac{-24}{40}$

Hence  $\frac{-7}{10} < \frac{-5}{8} < \frac{-3}{5}$  i.e.,  $\frac{7}{-10} < \frac{-5}{8} < \frac{-3}{5}$

Let us compare three of the numerators

Working		
5	5, 8, 10	
2	1, 8, 2	
2	1, 4, 1	
2	1, 2, 1	
	1, 1, 1	



## Module 18

Q.) Which of the following is greater:

(i)  $\frac{4}{-5}, \frac{-7}{10}$

Sol. We have,  $= \frac{4}{-5} = \frac{4 \times (-1)}{-5 \times (-1)} = \frac{-4}{5}$

LCM of 5 and 10 is 10. To make the denominator 10, we multiply the numerator and denominator by 2.  
 $\therefore \frac{-4}{5} = \frac{-4 \times 2}{5 \times 2} = \frac{-8}{10}$   
 $\therefore -\frac{7}{10} < -\frac{8}{10}$   
 $\therefore -8 < -7$

Hence,  $\frac{4}{-5} < \frac{-7}{10}$

Which is the smaller number from - 8 & - 7 ?



Q.) Arrange the following rational numbers in descending order :

(ii)  $\frac{-5}{6}, \frac{-7}{12}, \frac{-13}{18}, \frac{23}{-24}$

Sol.

We know,  $\frac{23}{-24} = \frac{23 \times (-1)}{-24 \times (-1)} =$

What should be multiplied to 18 to get 144?

∴

∴

$$\frac{-13}{18} = \frac{(-13) \times 6}{18 \times 6} = \frac{-78}{144}$$

positive denominator  
make LCM

$$\therefore -84 > -104 > -120 > -138$$

∴

$$\text{Hence, } \frac{-7}{12} > \frac{-13}{18} > \frac{-5}{6} > \frac{23}{-24}$$



Which is the greater number from  $-120, -84, -104$  &  $-138$  ?



