

APPENDIX

Due to the page limit, the current submission of Paper 327 does not include the detailed algorithm with updating rules, the dataset statistics about Foursquare-LA, or its experiment results. They are all listed in this supplementary material.

Detailed Algorithm

The detailed algorithm with the parameter updating rules is shown in **Algorithm 1**.

Algorithm 1 Our Proposed Methodology

- 1: **Input:** check-in data D
 - 2: **repeat**
 - 3: **E-Step:**
 - 4: $\langle z_{u,i,j} \rangle \leftarrow \frac{\sigma_1^2 w (\chi_{u,i,j} - \hat{\chi}_{u,i,j} - \rho d_{i,j}^{-1}) + \hat{z}_{u,i,j}^{-1} \sigma_2^2}{w^2 \sigma_1^2 + \sigma_2^2}$
 - 5: $\langle z_{u,i,j}^2 \rangle \leftarrow \frac{\sigma_1^2 \cdot \sigma_2^2}{\sigma_2^2 + w^2 \cdot \sigma_1^2} + \langle z_{u,i,j} \rangle^2$
 - 6: **M-Step:**
 - 7: $\sigma_1^2 \leftarrow \frac{1}{N_{u,d}} \sum_{u,d} (\langle z_{u,i,j}^2 \rangle - 2 \langle z_{u,i,j} \rangle \cdot \hat{z}_{u,i,j}^{-1} + \hat{z}_{u,i,j}^{-2})$
 - 8: $\sigma_2^2 \leftarrow \frac{1}{N_{u,d}} \sum_{u,d} (w^2 \cdot \langle z_{u,i,j}^2 \rangle + (\hat{\chi}_{u,i,j} + \rho d_{i,j}^{-1})^2 + \chi_{u,i,j}^2 + 2w \cdot \langle z_{u,i,j} \rangle \cdot (\hat{\chi}_{u,i,j} + \rho d_{i,j}^{-1}) - 2w \cdot \chi_{u,i,j} \cdot \langle z_{u,i,j} \rangle) - 2 \chi_{u,i,j} \cdot (\hat{\chi}_{u,i,j} + \rho d_{i,j}^{-1})$
 - 9: $\rho \leftarrow \frac{\sum_d d_{i,j}^{-1} (\chi_{u,i,j} - w \langle z_{u,i,j} \rangle) - \sum_d d_{i,j}^{-1} \cdot \hat{\chi}_{u,i,j}}{\sum_d d_{i,j}^{-2}}$
 - 10: $w \leftarrow \frac{\sum_{u,d} \langle z_{u,i,j} \rangle (\chi_{u,i,j} - \hat{\chi}_{u,i,j} - \rho d_{i,j}^{-1})}{\sum_{u,d} \langle z_{u,i,j}^2 \rangle}$
 - 11: $\gamma_1 \leftarrow \hat{\chi}_{u,i,j} + \rho \cdot d_{i,j}^{-1} + w \langle z_{u,i,j} \rangle - \chi_{u,i,j}$
 - 12: $\mathbf{v}_u^{U,J} \leftarrow \mathbf{v}_u^{U,J} + \alpha (2 \mathbf{v}_j^{J,U} \cdot \gamma_1)$
 - 13: $\mathbf{v}_j^{J,U} \leftarrow \mathbf{v}_j^{J,U} + \alpha (2 \mathbf{v}_u^{U,J} \cdot \gamma_1)$
 - 14: $\mathbf{v}_j^{J,I} \leftarrow \mathbf{v}_j^{J,I} + \alpha (2 \mathbf{v}_i^{I,J} \cdot \gamma_1)$
 - 15: $\mathbf{v}_i^{I,J} \leftarrow \mathbf{v}_i^{I,J} + \alpha (2 \mathbf{v}_j^{J,I} \cdot \gamma_1)$
 - 16: $\mathbf{e}_u^{U,J} \leftarrow \mathbf{e}_u^{U,J} + \alpha (2 \mathbf{e}_j^{J,U} \cdot (\hat{z}_{u,i,j} - \langle z_{u,i,j} \rangle^{-1}))$
 - 17: $\mathbf{e}_j^{J,U} \leftarrow \mathbf{e}_j^{J,U} + \alpha (2 \mathbf{e}_u^{U,J} \cdot (\hat{z}_{u,i,j} - \langle z_{u,i,j} \rangle^{-1}))$
 - 18: $\mathbf{e}_j^{J,I} \leftarrow \mathbf{e}_j^{J,I} + \alpha (2 \mathbf{e}_i^{I,J} \cdot (\hat{z}_{u,i,j} - \langle z_{u,i,j} \rangle^{-1}))$
 - 19: $\mathbf{e}_i^{I,J} \leftarrow \mathbf{e}_i^{I,J} + \alpha (2 \mathbf{e}_j^{J,I} \cdot (\hat{z}_{u,i,j} - \langle z_{u,i,j} \rangle^{-1}))$
 - 20: **until** convergence
 - 21: **Return:** Θ
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Experiments

Datasets

Besides the two datasets Foursquare(NYC) and Gowalla which are provided by [Bao *et al.*, 2012] and [Cheng *et al.*, 2012] respectively, we also evaluate the models on Foursquare(LA) which is provided by [Bao *et al.*, 2012]. The statistics of the three datasets are listed in Table 1. Each dataset is split into two non-overlapping subsets to evaluate the model performance (for each user, the earliest 80% of check-ins as training set, and the remaining 20% check-ins as test set).

Table 1: Dataset Statistics

	#User	#POI	#Check-in
Foursquare-LA	2470	81361	123782
Foursquare-NYC	3401	106974	178143
Gowalla	1488	92679	226116

Performance Comparison on Next POI Recommendation (Foursquare-LA)

Fig.2(a) and Fig.2(b) show the experimental results for the “exact” next POI recommendation and the “exact” next new POI recommendation on Foursquare-LA dataset. The observations are consistent with that of the other two datasets described in the current submission (See Sec.4.3).

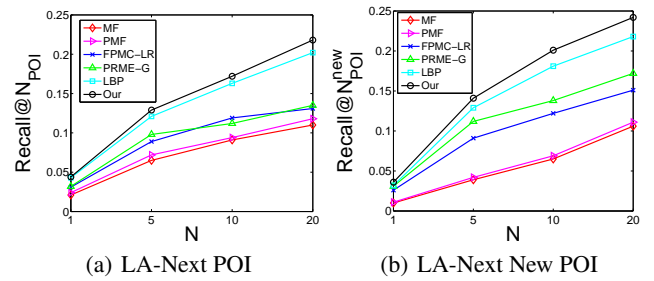


Figure 1: Performance Comparison on Next POI Recommendation

Performance Comparison on γ -hour Next POI Recommendation (Foursquare-LA, $\gamma = 6$)

To make a fair comparison with the existing work, we further evaluate the performance of next POI recommendation by considering consecutive next check-ins within γ hours as the next location set (γ is set to 6 following [Cheng *et al.*, 2013] and [Feng *et al.*, 2015]).

Fig.2 depicts the comparison on Foursquare-LA dataset when considering the next POI as a set of locations. Similar outcomes to that in paper for the other two datasets can be observed. It is evident that our proposed model consistently outperforms other baselines.

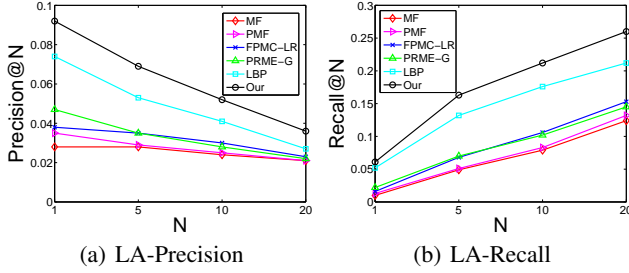


Figure 2: Performance Comparison on γ -hour Next POI Recommendation($\gamma = 6$)

Performance Comparison on Transition Interval Prediction (Foursquare-LA)

Fig.3 shows the performance comparison on transition interval predictions. The results show that the proposed model always achieves the highest precision over baselines, which proves that our model is capable of providing effective POI recommendations to users as well as predicting when it will happen. We also compute MAPE between the predicted transition intervals and the ground truth of the test set (See Table 2). Lower values indicate more accurate predictions. It is evident that the proposed model outperforms the baselines by a significant margin. Fig.4 shows the performance comparison by relaxing the threshold T , and our method outperforms all the baselines again. The observations are consistent with that in the submitted paper.

Table 2 tabulates the MAPE between the predicted transition intervals and the ground truth of the test set. Our proposed model achieves more accurate predictions than other baselines on the three datasets.

Table 2: MAPE for our model and baselines on three datasets

	MF	PMF	FPMC	Our
Foursquare-LA	13.79	11.45	5.68	1.75
Foursquare-NYC	14.87	12.64	6.72	1.84
Gowalla	16.95	14.12	7.89	2.15

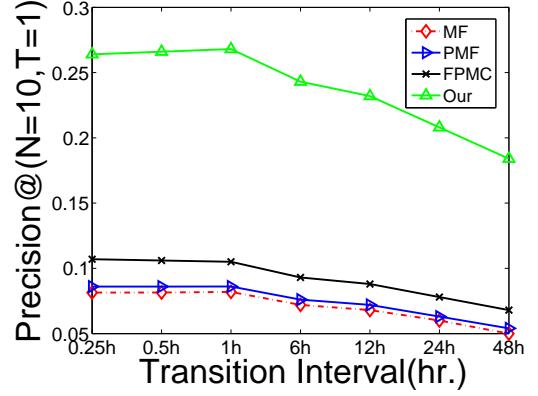


Figure 3: Performance Comparison for Transition Interval Prediction (Foursquare-LA)

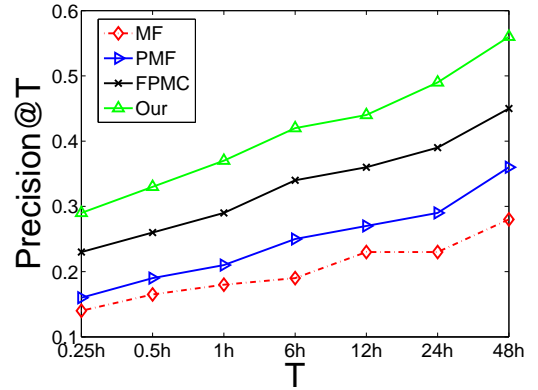


Figure 4: Transition interval prediction v.s. T (Foursquare-LA)

Detailed Performance Comparisons on Specific Time Period for Next POI Recommendation

In this section, we report the detailed performance comparisons for different settings of future time period. For example, the setting of $TP = [0.5, 1]$ denotes that we consider the next check-ins between 0.5 to 1 hour since the current time point as the next location set. In contrast to MF and PFM, FPMC-LR, PRME-G and LBP are more competitive baselines. To present a more clear comparison, we only report the performance comparisons on recall for the three datasets. The detailed performance comparisons are tabulated in Table 3- Table 8.

Please note that, in general, with the setting of time interval increasing, the number of check-in within the time interval increases which lead the upper bound of recall@N to decrease. Again, our proposed method consistently outperforms the competitive baselines by a large margin for all three datasets.

Table 3: Performance Comparison for Next POI Recommendation, $TP = [0.5, 1]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.030 96.7%	0.027 119%	0.045 31.1%	0.059	0.042 78.6%	0.043 74.4%	0.062 21.0%	0.075	0.011 72.7%	0.011 72.7%	0.013 46.2%	0.019
top5 Improve	0.099 158%	0.098 160%	0.197 29.4%	0.255	0.143 62.9%	0.152 53.3%	0.187 24.6%	0.233	0.146 84.2%	0.164 64.0%	0.179 50.3%	0.269
top10 Improve	0.142 130%	0.145 126%	0.265 23.4%	0.327	0.181 68.0%	0.178 70.8%	0.235 29.4%	0.304	0.223 92.4%	0.237 81.0%	0.276 55.4%	0.429
top20 Improve	0.201 98.5%	0.226 76.5%	0.316 26.3%	0.399	0.205 86.8%	0.209 83.3%	0.306 25.2%	0.383	0.304 82.2%	0.318 74.2%	0.368 50.5%	0.554

Table 4: Performance Comparison for Next POI Recommendation, $TP = [1, 2]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.021 143%	0.022 132%	0.042 21.4%	0.051	0.027 66.7%	0.026 73.1%	0.037 21.6%	0.045	0.009 88.9%	0.010 70.0%	0.012 41.7%	0.017
top5 Improve	0.085 133%	0.091 118%	0.158 25.3%	0.198	0.126 64.3%	0.130 59.2%	0.168 23.2%	0.207	0.083 89.2%	0.092 70.7%	0.104 51.0%	0.157
top10 Improve	0.133 135%	0.141 121%	0.246 26.8%	0.312	0.167 79.0%	0.171 74.9%	0.243 23.0%	0.299	0.161 87.0%	0.159 89.3%	0.203 48.3%	0.301
top20 Improve	0.202 89.6%	0.216 77.3%	0.298 28.5%	0.383	0.219 76.7%	0.225 72.0%	0.301 28.6%	0.387	0.231 87.4%	0.228 89.9%	0.301 43.9%	0.433

Table 5: Performance Comparison for Next POI Recommendation, $TP = [2, 3]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.024 41.7%	0.022 54.5%	0.026 30.8%	0.034	0.031 51.6%	0.032 46.9%	0.039 20.5%	0.047	0.011 63.6%	0.012 50.0%	0.013 38.5%	0.018
top5 Improve	0.132 63.6%	0.126 71.4%	0.173 24.9%	0.216	0.138 60.9%	0.141 57.4%	0.179 24.0%	0.222	0.069 62.3%	0.072 55.6%	0.082 36.6%	0.112
top10 Improve	0.187 47.1%	0.171 60.8%	0.213 29.1%	0.275	0.189 55.0%	0.194 51.0%	0.231 26.8%	0.293	0.132 65.2%	0.143 52.4%	0.163 33.7%	0.218
top20 Improve	0.234 44.9%	0.216 56.9%	0.265 27.9%	0.339	0.221 66.5%	0.226 62.8%	0.291 26.5%	0.368	0.193 68.9%	0.192 69.8%	0.243 34.2%	0.326

Table 6: Performance Comparison for Next POI Recommendation, $TP = [3, 6]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.023 65.2%	0.025 52.0%	0.031 22.6%	0.038	0.015 46.7%	0.014 57.1%	0.018 22.2%	0.022	0.011 63.6%	0.012 50.0%	0.015 20.0%	0.018
top5 Improve	0.081 50.6%	0.078 56.4%	0.101 20.8%	0.122	0.071 47.9%	0.072 45.8%	0.085 23.5%	0.105	0.062 69.4%	0.068 54.4%	0.081 29.6%	0.105
top10 Improve	0.122 41.8%	0.119 45.4%	0.142 21.8%	0.173	0.115 44.3%	0.112 48.2%	0.131 26.7%	0.166	0.116 64.7%	0.124 54.0%	0.148 29.1%	0.191
top20 Improve	0.168 43.5%	0.171 40.9%	0.200 20.5%	0.241	0.143 48.3%	0.141 50.4%	0.173 22.5%	0.212	0.169 68.6%	0.176 61.9%	0.224 27.2%	0.285

Table 7: Performance Comparison for Next POI Recommendation, $TP = [6, 12]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.021 57.1%	0.025 32.0%	0.027 22.2%	0.033	0.018 44.4%	0.017 52.9%	0.021 23.8%	0.026	0.010 60.0%	0.011 45.5%	0.013 23.1%	0.016
top5 Improve	0.086 65.1%	0.078 82.1%	0.113 25.7%	0.142	0.073 45.2%	0.072 47.2%	0.087 21.8%	0.106	0.054 63.0%	0.061 44.3%	0.069 27.5%	0.088
top10 Improve	0.125 73.6%	0.119 82.4%	0.176 23.3%	0.217	0.99 52.5%	0.101 49.5%	0.124 21.8%	0.151	0.106 60.4%	0.105 61.9%	0.134 26.9%	0.170
top20 Improve	0.165 67.3%	0.171 61.4%	0.221 24.9%	0.276	0.145 51.0%	0.151 45.0%	0.178 23.0%	0.219	0.164 62.8%	0.162 64.8%	0.216 23.6%	0.267

Table 8: Performance Comparison for Next POI Recommendation, $TP = [12, 24]$

Metrics	Foursquare-LA				Foursquare-NYC				Gowalla			
	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our	F-LR	P-G	LBP	Our
top1 Improve	0.019 63.2%	0.018 72.2%	0.024 29.2%	0.031	0.017 52.9%	0.018 44.4%	0.021 23.8%	0.026	0.013 61.5%	0.014 50.0%	0.017 23.5%	0.021
top5 Improve	0.072 79.2%	0.073 76.7%	0.098 31.6%	0.129	0.068 47.1%	0.067 49.3%	0.079 26.6%	0.100	0.068 69.1%	0.073 57.5%	0.089 29.2%	0.115
top10 Improve	0.107 72.0%	0.099 85.9%	0.146 26.0%	0.184	0.104 55.8%	0.109 48.6%	0.131 23.7%	0.162	0.113 66.4%	0.118 59.3%	0.151 24.5%	0.188
top20 Improve	0.151 61.6%	0.144 69.4%	0.201 21.4%	0.244	0.147 53.7%	0.143 58.0%	0.186 21.5%	0.226	0.168 65.5%	0.172 61.6%	0.224 24.1%	0.278