

### Feature 0: average\_near\_price\_per\_stock

- **DSL expression:** `groupby(key=stock_id, value=ask_price, statistic_operator=mean)`
- **Thought:** Considering the data distribution, especially the potential issue of uneven grouping due to a small number of stocks, we can add a new grouping criterion, 'date\_id', to the existing feature 'average\_ask\_price\_per\_stock'. This will allow for further refinement when calculating the average ask price for each stock, breaking it down by date to reduce the imbalance caused by having a small number of stocks in each group. Specifically, the implementation will involve using both 'stock\_id' and 'date\_id' as grouping criteria in the 'groupby' operation.

### Feature 1: average\_ask\_price\_per\_stock\_per\_date

- **DSL expression:** `groupby(key=[stock_id, date_id], value=ask_price, statistic_operator=mean)`
- **Thought:** We can further reduce the noise in the results by introducing a moving average to smooth the ask price. Specifically, when calculating 'average\_ask\_price\_per\_stock\_per\_date', we will first apply a moving average to the near\_price and then compute the mean of that.

### Feature 2: average\_ask\_price\_per\_stock\_per\_date\_smoothed

- **DSL expression:** `groupby(key=[stock_id, date_id], value=moving_average(ask_price, window_size=5), statistic_operator=mean)`
- **Thought:** Given that the current feature 'average\_ask\_price\_per\_stock' is calculated based on the mean of the ask price, we could attempt to introduce a combination of price-related features to enhance the diversity and robustness of the feature. Based on the data distribution, it is recommended to replace ask\_price with a combination of bid\_price and ask\_price, calculating their difference. This would provide a more comprehensive reflection of market price dynamics.

### Feature 3: average\_ask\_bid\_price\_per\_stock\_per\_date\_smoothed

- **DSL expression:** `groupby(key=[stock_id, date_id], value=moving_average(ask_price-bid_price, window_size=5), statistic_operator=mean)`
- **Thought:** Since the calculation of the bid-ask spread may not be significantly affected by extreme values, we can introduce additional statistical measures to more comprehensively reflect the characteristics of the spread. Specifically, when calculating the bid-ask spread, in addition to using the mean, we can also introduce quartiles (Q1 and Q3) to capture the distribution characteristics of the spread. We can calculate the quartiles (Q1 and Q3) of the ask\_price and bid\_price for each stock on each date and use Q3 - Q1 to represent the range of changes in the spread.

### Feature 4: iqr\_ask\_bid\_price\_per\_stock\_per\_date\_smoothed

- **DSL expression:** `groupby(key=[stock_id, date_id], value=(ask_price - bid_price), statistic_operator=IQR)`, where IQR represents the interquartile range.
- **Thought:** In order to capture more distribution patterns, we can attempt additional price-related feature combinations such as near\_price, wap, far\_price, etc.

### Feature 5: iqr\_prices\_per\_stock\_per\_date\_smoothed

- **DSL expression:** `groupby(key=[stock_id, date_id], value=price for price in [near_price, wap, far_price], statistic_operator=IQR)`

- **Thought:** To capture additional price dynamics, we could explore combinations of different price metrics, such as near\_price, weighted average price (wap), and far\_price. The IQR of these prices will provide insight into the spread and variation of prices over time.