$\epsilon \asymp \log(\log(n))$