Please check the examination details below before entering your candidate information			
Candidate surname		Other names	
Centre Number Candidate N	umber		
Pearson Edexcel Inter	nation	al Advance	ed Level
Time 1 hour 30 minutes	Time 1 hour 30 minutes Paper reference WMA 14/01		
Mathematics			
International Advanced Le	aval		
	evei		
Pure Mathematics P4			
You must have: Mathematical Formulae and Statistical	al Tables (Ye	ellow), calculator	Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
- use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶







1. The binomial expansion of

$$(3+kx)^{-2} \qquad |kx| < 3$$

where k is a non-zero constant, may be written in the form

$$A + Bx + Cx^2 + Dx^3 + \dots$$

where A, B, C and D are constants.

(a) Find the value of A

(1)

Given that C = 3B

(b) show that

$$k^2 + 6k = 0$$

(3)

- (c) Hence (i) find the value of k
 - (ii) find the value of D

(3)



Question 1 continued	
	(Total for Question 1 is 7 marks)



2. (a) Express $\frac{1}{(1+3x)(1-x)}$ in partial fractions.

(3)

(b) Hence find the solution of the differential equation

$$(1+3x)(1-x)\frac{dy}{dx} = \tan y - \frac{1}{3} < x \le \frac{1}{2}$$

for which $x = \frac{1}{2}$ when $y = \frac{\pi}{2}$

Give your answer in the form $\sin^n y = f(x)$ where *n* is an integer to be found.

(6)

Question 2 continued



Question 2 continued

Question 2 continued	
	(Total for Question 2 is 9 marks)



Figure 1

A tablet is dissolving in water.

The tablet is modelled as a cylinder, shown in Figure 1.

At t seconds after the tablet is dropped into the water, the radius of the tablet is x mm and the length of the tablet is 3x mm.

The cross-sectional area of the tablet is decreasing at a constant rate of $0.5\,\mathrm{mm}^2\,\mathrm{s}^{-1}$

(a) Find
$$\frac{dx}{dt}$$
 when $x = 7$

(4)

(b) Find, according to the model, the rate of decrease of the volume of the tablet when x = 4

(4)

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(Total for Question 3 is 8 marks)	Question 3 continued	
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4. In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

A curve has equation

$$16x^3 - 9kx^2y + 8y^3 = 875$$

where k is a constant.

(a) Show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{6kxy - 16x^2}{8y^2 - 3kx^2}$$

(4)

Given that the curve has a turning point at $x = \frac{5}{2}$

(b) find the value of k

(4)



Question 4 continued



Question 4 continued

Question 4 continued	
(Total	for Question 4 is 8 marks)



5. In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

(a) Use the substitution $x = 2 \sin u$ to show that

$$\int_{0}^{1} \frac{3x+2}{(4-x^{2})^{\frac{3}{2}}} dx = \int_{0}^{p} \left(\frac{3}{2}\sec u \tan u + \frac{1}{2}\sec^{2} u\right) du$$

where p is a constant to be found.

(4)

(b) Hence find the exact value of

$$\int_{0}^{1} \frac{3x+2}{(4-x^2)^{\frac{3}{2}}} \, \mathrm{d}x$$

(4)

Question 5 continued



Question 5 continued		

Question 5 continued		
	(Total for Question 5 is 8 marks)	
	(10tai 101 Vucsuon 2 is 6 marks)	



- **6.** Relative to a fixed origin *O*,
 - the point A has position vector $\mathbf{i} 4\mathbf{j} + 3\mathbf{k}$
 - the point B has position vector $5\mathbf{i} + 3\mathbf{j} 2\mathbf{k}$
 - the point C has position vector $3\mathbf{i} + p\mathbf{j} \mathbf{k}$

where p is a constant.

The line l passes through A and B.

(a) Find a vector equation for the line l

(3)

Given that \overrightarrow{AC} is perpendicular to l

(b) find the value of p

(3)

(c) Hence find the area of triangle ABC, giving your answer as a surd in simplest form.

(3)



Question 6 continued		

Question 6 continued		
(Total for Question	on 6 is 9 marks)	



7. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

The curve C has parametric equations

$$x = \sin t - 3\cos^2 t \qquad y = 3\sin t + 2\cos t \qquad 0 \leqslant t \leqslant 5$$

(a) Show that
$$\frac{dy}{dx} = 3$$
 where $t = \pi$

(4)

The point *P* lies on *C* where $t = \pi$

(b) Find the equation of the tangent to the curve at P in the form y = mx + c where m and c are constants to be found.

(3)

Given that the tangent to the curve at P cuts C at the point Q

(c) show that the value of t at point Q satisfies the equation

$$9\cos^2 t + 2\cos t - 7 = 0$$

(2)

(d) Hence find the exact value of the y coordinate of Q

(3)

Question 7 continued		



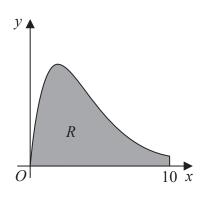
Question 7 continued		

Question 7 continued		
(Total	for Question 7 is 12 marks)	



8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.



20 cm

Figure 2

Figure 3

Figure 2 shows the curve with equation

$$y = 10xe^{-\frac{1}{2}x}$$

$$0 \leqslant x \leqslant 10$$

The finite region R, shown shaded in Figure 2, is bounded by the curve, the x-axis and the line with equation x = 10

The region R is rotated through 2π radians about the x-axis to form a solid of revolution.

(a) Show that the volume, V, of this solid is given by

$$V = k \int_{0}^{10} x^{2} e^{-x} dx$$

where k is a constant to be found.

(2)

(b) Find
$$\int x^2 e^{-x} dx$$

(3)

Figure 3 represents an exercise weight formed by joining two of these solids together.

The exercise weight has mass 5 kg and is 20 cm long.

Given that

density =
$$\frac{\text{mass}}{\text{volume}}$$

and using your answers to part (a) and part (b),

(c) find the density of this exercise weight. Give your answer in grams per cm³ to 3 significant figures.

(5)

Question 8 continued		



Question 8 continued		

Question 8 continued		
(Total	for Augstian & is 10 marks)	
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9.	Use proof by contradiction to show that, when n is an integer,		
	n^2-2		
	is never divisible by 4		
		(4)	

Question 9 continued



Question 9 continued	
	(Total for Question 9 is 4 marks)
	TOTAL FOR PAPER IS 75 MARKS

