

Mark Scheme (Results)

January 2024

Pearson Edexcel International Advanced Level in Mechanics M2 (WME02) Paper 01

Q	Scheme	Mark	Notes
1a	Use of $v = \frac{dx}{dt}$	M1	At least 2 powers going down by 1.
	dt		Clear division by t is M0
	$v = 6t^2 - 42t + 60$	A1	Correct only
	Set $v = 0$ and correctly solves to	M1	Complete method to obtain both
	obtain 2 values for <i>t</i>		values
			(implied by correct answers seen)
			$(0 = t^2 - 7t + 10 = (t - 2)(t - 5))$
	Obtain $t = 2$ and $t = 5$	A1	Correct only. Allow 2.0, 5.0
		[4]	
1b	Distance = $ x_2 - x_1 + x_3 - x_2 $	M1	Correct strategy dependent on their <i>t</i>
	(= 45-52 + 52-41)		being in $1 < t < 3$
	=11+7=18 (m)	A1	Correct only
		[2]	
1c	$\int_{\text{Lice of } a} dv$	M1	Differentiate their <i>v</i> .
	Use of $a = \frac{dv}{dt}$		Clear division by t is M0.
			A power going down by 1
			$\left(a=12t-42\right)$
	Obtain 6 (ms ⁻²)	A1	Must be positive – the Q asks for
	\ /		magnitude
		[2]	
		(8)	

Q	Scheme	Mark	Notes
2a	Use of $\mathbf{I} = m\mathbf{v} - m\mathbf{u}$	M1	NB: Column vectors are acceptable.
			Condone wrong order but must be
			subtracting.
			Condone 5 in place of 0.5.
	$2\mathbf{i} + 5\mathbf{j} = 0.5(\mathbf{v} - (3\mathbf{i} + \mathbf{j}))$	A1	Correct unsimplified equation
			Accept as a vector equation or as a
	$(\mathbf{v} = 7\mathbf{i} + 11\mathbf{j})$		pair of equations, one for each
	$(\mathbf{v} - \mathbf{h} + \mathbf{h})$		component.
			Accept alternative notations
			provided the meaning is clear.
	Use of Pythagoras	M1	For their v
			Independent M1 but they must have
			a v
	$ v = \sqrt{121 + 49} = \sqrt{170} (\text{m s}^{-1})$	A1	$13(m s^{-1})$ or better. (13.038)
		[4]	
2b	Correct use of trigonometry e.g.	M1	Condone subtraction in either order.
	$\theta = \tan^{-1} \frac{11}{7} - \tan^{-1} \frac{1}{3}$		Allow if both fractions are the other
	$\frac{0-\tan \frac{\pi}{7}-\tan \frac{\pi}{3}}{1}$		way up.
	(=57.5-18.4)		Alternatives:
	,		scalar product
			$\theta = \cos^{-1}\left(\frac{21+11}{\sqrt{10}\sqrt{170}}\right)$
			cosine rule
			$4 \times 29 = 10 + 170 - 2\sqrt{10}\sqrt{170}\cos\theta$
	$\theta = 39.1$	A1	Accept ±39 or better (39.0938)
			0.68(2) radians is M1A0
			Accept $\pm (360-39) = \pm 321$ or better
		[2]	
		(6)	

Q	Scheme	Mark	Notes
3a	$E = \frac{1}{2} \sqrt{2} \cos \alpha \left(-5.00\right)$	M1	Use of $F = \mu R$
	$F_{\text{max}} = \frac{1}{3} \times 2g \cos \alpha \ (= 5.90)$		Seen or implied.
			Condone sine / cosine confusion
			Condone <i>g</i> missing
	WD against friction = $6 \times their F_{max}$	M1	(=35.4(J)) Seen or implied as
			part of the 4 th M mark
	PE gain = $2g \times 6 \times \sin \alpha$	M1	dimensionally correct. Condone
	$\left(=6 \times \frac{42}{5} = 50.4\right)$		sine / cosine confusion
	Total WD = WD against friction + WD		Dependent on the 3 preceding M
	against gravity (gain in PE)	DM1	marks. Require both terms and no extras
	Total WD = $85.8(J)$ or $86(J)$	A1	3 sf or 2 sf only
	Total (1) of so (1)		$\left(8\sqrt{10} + 36\right)\frac{g}{7}$ is A0 (incorrect
			units)
	NB a candidate who resolves parallel to	the slope	but never multiplies either
	component by 6 will score the first M1 o	nly	
		[5]	
3b	Work-energy equation	M1	Must be using work-energy.
	(KE gained = loss in GPE - WD		Need all terms, no extras and
	against friction)		dimensionally correct.
			Condone sign errors
	1 2	A1	Condone sine / cosine confusion.
	$\frac{1}{2} \times 2v^2 = 2g \times 6\sin\alpha - 6 \times \frac{2}{3}g\cos\alpha$	AI	Unsimplified equation with at most one error
	2 3	A1	Correct unsimplified equation.
			They must have started with
			correct expressions, but follow
			through on any calculation errors
	$v = 3.87 (\text{m s}^{-1}) or 3.9 (\text{m s}^{-1})$	A1	3 sf or 2 sf only
		[4]	
		(9)	

4a				Mark	Notes
	If the division of the shape involves non-stan		tandard sha	pes (e.g. a trapezium) the centres of	
	mass must be quoted correctly or a correct method used to marks.				ed to find the position to score any
	rectangle	-triangle	+triangle		Correct mass ratios for a correct
	$20a^{2}$	$-\frac{9}{2}a^{2}$	$\frac{9}{2}a^{2}$	B1	division of the folded template and
	2a	3 <i>a</i>	$\frac{2}{2a}$		correct total of $20a^2$
	or			B1	Correct distances from AD seen or
	rectangle	rectangle	Double triangle] ^{D1}	implied. B0B1 is possible if they have incorrect masses but a full set of
	$3a^2$	$8a^2$	$9a^2$		correct distances. e.g. if they use the
	$\frac{1}{2}a$	2 <i>a</i>	2 <i>a</i>		second alternative but have not doubled the triangle. Or they might
	or	T	T	1	have a correct split with an error in
	rectangle	trapezium	triangle		one of the areas or an incorrect (or
	$5a^2$	$\frac{21}{2}a^{2}$	$\frac{9}{2}a^{2}$		missing) total
	$\frac{1}{2}a$	$\frac{48}{21}a$	2 <i>a</i>		or equivalent
	Moments abo	out AD or a par	allel axis.	M1	Dimensionally consistent. All terms for a correct division of <i>L</i>
					and no extras.
					Accept as part of a vector equation
	$40a^3 - \frac{27}{2}a^3$	$+9a^3 = 20a^2a$	d	A1	Correct unsimplified equation for
	or $\frac{3}{5}a^3 + 16a$	$^3 + 18a^3 = 20a$	a^2d		their axis. Allow for correct
	or $\frac{2}{2}a^3 + \frac{48}{2}a^3 + 9a^3 = 20a^2d$			component in a vector equation.	
	$d = \frac{71}{40}a *$		A1*	Obtain given answer from correct working. Need at least one line of working to collect like terms e.g. $20d = \frac{71}{2}a$ Final answer must be as printed i.e. $d = \dots$	
				[5]	
4b	Moments about S			M1	A complete method to get an equation in <i>W</i> and <i>F</i> only. Need all terms and no extras. Dimensionally consistent.
NB If	they start by fir	nding the centi	re of mass for t	he system t	hey do not score marks until they
If they		ng moments a			as distances in their equation) this is
					he required equation. incorrect distance allow M1A1A0A0
n mey	2.1			A1	Unsimplified equation with at most
	$4W \times \frac{31}{40}a + W \times 3a = F \times 5a$ or $(4W + W)(2.22a - a) = 5aF$			111	one error
	or $(4W+W)$	(2.22a-a)=	= 5 <i>aF</i>	A1	Correct unsimplified equation
	$F = \frac{61}{50}V$	V		A1	Accept 1.22W or 1.2W
				[4]	
1				1 171	

Q	Scheme	Mark	Notes
5a	Use of $P = Fv$	M1	$\frac{10000}{16}$ (= 625) o.e. seen or
			implied in the working.
			Allow for $\frac{10}{16}$
	Equation of motion for the system	M1	Dimensionally correct. Need all terms and no extras. Condone sign errors and sine/cosine confusion If they start with separate equations for the van and trailer,
	E 400 900 a sin at 900 a	A1	just mark the combined equation.
	$F - 400 - 800g\sin\alpha = 800a$	AI	Unsimplified equation in <i>P</i> or <i>F</i> with a most one error
		A1	Correct unsimplified equation in <i>P</i> or <i>F</i>
			Use of cosine in place of sine for both vehicles counts as a repeated error and only loses 1 mark
	Obtain deceleration	A1	3 sf or 2 sf only
	$0.419 (m s^{-2}) \text{ or } 0.42 (m s^{-2})$	711	Answer must be positive.
		[5]	
5b	Equation of motion for the van or the trailer	M1	Dimensionally correct. Need all terms and no extras. Condone sign errors and sine/cosine confusion Use the mass in the <i>ma</i> term to decide which part of the system they are using.
	$T - 150 - 200g\sin\alpha = 200a$	A1	Unsimplified equation with at
	or $F - T - 250 - 600g \sin \alpha = 600a$	A1	most one error Correct unsimplified equation
	Obtain tension 206(N) or 210(N)	A1	3 sf or 2 sf only
	200(11) 01 210(11)	[4]	
		(9)	
		(3)	

Q	Scheme	Mark	Notes
ба	$ \begin{array}{c} P \\ 2m \end{array} $ $ \begin{array}{c} A \\ \theta \\ H \end{array} $		
	Moments about <i>A</i> :	M1	Dimensionally correct. Condone sine / cosine confusion
	$5P = 40 \times \frac{7}{2} \cos \theta$ $P = 22.4 *$	A1	Correct unsimplified equation
	P = 22.4 *	A1*	Obtain given answer from correct working. Need to see evidence of $\cos \theta = \frac{4}{5}$
		[3]	
6b	Two equations required. M1A1 for the first equation seen, M1A1 for the second equation. If more than 2 equations mark the two equations used to obtain the resultant, or the best 2 if they do not go on to find the resultant. First equation M1 e.g. Resolve horizontally		
	$H = P\sin\theta (=13.44)$	A1	Condone sine / cosine confusion Correct unsimplified equation
	Second equation	M1	e.g. Resolve vertically Condone sine / cosine confusion
	$V + P\cos\theta = 40 \left(V = 22.08\right)$	A1	Correct unsimplified equation
	$ R = \sqrt{H^2 + V^2}$	DM1	solve for $ R $ Dependent on the 2 preceding Ms
	R = 26 (N)	A1	Or better (25.84879) Accept $\frac{24\sqrt{29}}{5}$
		[6]	
	Two alternatives on	followin	ng page

6balt	First equation	M1	e.g. Resolve parallel Condone sine		
			/ cosine confusion		
	$X = 40\sin\theta (= 24)$	A1	Correct unsimplified equation		
	Second equation	M1	e.g. Resolve perpendicular		
			Condone sine / cosine confusion		
	$Y + P = 40\cos\theta (Y = 9.6)$ $ R = \sqrt{X^2 + Y^2}$	A1	Correct unsimplified equation		
	$ R = \sqrt{X^2 + Y^2}$	DM1	solve for $ R $		
		DIVIT	Dependent on the 2 preceding Ms		
	R = 26(N)	A1	Or better (25.84879)		
			Accept $\frac{24\sqrt{29}}{5}$		
		[6]			
	Alternative equations:				
	$M(C)$ $40 \times 1.5 \cos \theta + H \times 5 \sin \theta = V \times 5$	$5\cos\theta$			
	$M(B)$ $2P + 7\cos\theta \times V = 7\sin\theta \times H + 3.5 \times 40\cos\theta$				
	$M(G) 1.5P + 3.5\sin\theta \times H = 3.5\cos\theta \times V$				
6balt		M1	3 force diagram seen or implied		
	θ 22.4 N				
	40 N	A1	Forces and angle in correct		
	40 N		positions		
	RN				
	Use Cosine Rule	M1	Correct formula used		
	$(R)^2 = 40^2 + 22.4^2 - 2 \times 40 \times 22.4 \cos \theta$	A1	Correct unsimplified equation		
	Substitute for trig and solve for $ R $	DM1	Dependent on the 2 preceding Ms		
	R = 26 (N)		Or better (25.84879)		
		A1	$24\sqrt{29}$		
			Accept $\frac{21\sqrt{25}}{5}$		
		[6]			
		(9)			

Q	Scheme	Mark	Notes
7a	$ \begin{array}{cccc} & \longrightarrow & u \\ & & & Q \\ & & & & M \end{array} $		If 6 <i>u</i> and <i>u</i> are in opposite directions, mark as a sign error.
	Use of CLM	M1	Need all 4 terms. Dimensionally consistent. Condone sign errors Condone <i>x</i> in the wrong direction
	6mu + 5mu = 5my - mx $(11u = 5y - x)$	A1	Correct unsimplified equation
	Use of impact law	M1	Used correctly. Dimensionally correct. Condone sign errors
	x + y = 5eu	A1	Correct unsimplified equation. Signs consistent with their CLM equation
	Solve for x in terms of e and u : 6x = 25eu - 11u or solve for e in terms of y and u : $e = \frac{6y - 11u}{5u}$	DM1	Dependent on the first 2 M marks. As far as $kx =$ Dependent on the previous 2 M marks
	Use $x > 0 \ (\Rightarrow y > \frac{11}{5}u)$: $25e > 11$	DM1	Use correct inequality for their <i>x</i>
	$\frac{11}{25} < e (\leqslant 1)$	A1	Or equivalent. Condone if 1 not mentioned. Allow with <1. A0 if incorrect upper limit. cso
		[7]	
7b	$x = \frac{2}{3}u \text{ and } y = \frac{7}{3}u$	B1	Seen or implied
	Total KE lost $= \left(\frac{1}{2}m \times 36u^2 + \frac{1}{2}5m \times u^2\right)$ $-\left(\frac{1}{2}m \times x^2 + \frac{1}{2}5m \times y^2\right)$	M1	Complete expression. Dimensionally correct. Correct masses connected to correct speeds. Condone subtraction in the wrong order. Allow in <i>x</i> and <i>y</i>
	$= \left(\frac{1}{2}m \times 36u^2 + \frac{1}{2}5m \times u^2\right)$ $-\left(\frac{1}{2}m \times \frac{4}{9}u^2 + \frac{1}{2}5m \times \frac{49}{9}u^2\right)$	A1ft	Correct unsimplified expression in m and u . Follow their x , y with e substituted
	$=\frac{20}{3}mu^2$	A1	Or single term equivalent.
	3	F 47	Accept 6.7mu ² or better
7c	velocity of Q after collision with wall	[4]	
	$= \pm fy \left(= \pm f \times \frac{7}{3}u \right)$	B1ft	Follow their y (in terms of u)
	Second collision if $fy > x$ $\frac{7}{3} fu > \frac{2}{3} u$	DM1	Correct inequality for their <i>x</i> , <i>y</i> Dependent on the B1 and <i>P</i> moving away from the wall
	$\frac{2}{7} < f \leqslant 1$	A1	Correct only Need both limits
		[3]	
		(14)	

Q	Scheme	Mark	Notes
8a	Use symmetry to find time taken: $-7 = 7 - gt$	M1	Or equivalent complete method using <i>suvat</i> to find the time taken e.g. find the time for vertical distance = 0
	$t = \frac{14}{g} \left(= 1.428 \right)$	A1	Correct value seen or implied
	Horizontal distance $=4t$	DM1	Complete method using <i>suvat</i> to find the distance. Dependent on the preceding M1
	=5.71(m) or 5.7(m)	A1	3 sf or 2 sf only $\frac{40}{7}$ scores A0
			$\frac{56}{g}$ scores A0 (incorrect units)
		[4]	
8a alt	Find speed and angle of projection	M1	Correct use of Pythagoras and trig.
	Speed = $\sqrt{16 + 49} = \sqrt{65} (\text{m s}^{-1})$	A1	Both values seen or implied.
	Direction = $\tan^{-1} \frac{7}{4}$ (= 60.3°)		
	Use of $R = \frac{u^2 \sin 2\alpha}{g}$	DM1	Or equivalent. Dependent on the preceding M1
	g = 5.71(m) or 5.7(m)	A1	3 sf or 2 sf only
		[4]	
8b	$ \mathbf{v} = 5 \Rightarrow \mathbf{v} = 4\mathbf{i} + 3\mathbf{j} \text{ or } \mathbf{v} = 4\mathbf{i} - 3\mathbf{j}$	B1	Correct vertical component seen or implied
	-3=3-gT	M1	Complete method to find T
			e.g. $T = \frac{14}{g} - 2 \times \frac{4}{g}$
	T = 0.612 or $T = 0.61$	A1	3 sf or 2 sf only $\frac{30}{49}$ scores A0
			$\frac{6}{g}$ scores A0 (incorrect units)
		[3]	
8c	$\begin{pmatrix} 4 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ p \end{pmatrix} = 0$	M1	Or equivalent method to find perpendicular velocity
	$\Rightarrow p = -\frac{16}{7}, \mathbf{v} = 4\mathbf{i} - \frac{16}{7}\mathbf{j}$	A1	Correct vertical component Allow -2.28
	$\Rightarrow p = -\frac{16}{7}, \mathbf{v} = 4\mathbf{i} - \frac{16}{7}\mathbf{j}$ $\left(\left(-\right)\frac{16}{7}\right)^2 = 7^2 - 2gh$	DM1	Complete method using <i>suvat</i> or energy to form an equation in <i>h</i> only. Dependent on the preceding M1
	h = 2.23 or $h = 2.2$	A1	3 sf or 2 sf only cso (negative vertical component seen at some point)
		[4]	
8c alt	$\begin{pmatrix} 4 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 7 - gt \end{pmatrix} = 0$	M1	Or equivalent method to find time when velocity perpendicular
	$ \begin{pmatrix} 4 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 7 - gt \end{pmatrix} = 0 $ $ t = \frac{65}{7g} (= 0.947) $	A1	Correct time
	$h = 7t - \frac{1}{2}gt^2$	DM1	Complete method using <i>suvat</i> to form an equation in <i>h</i> only.
	h = 2.23 or $h = 2.2$	A1	3 sf or 2 sf only cso
		[4]	
		(11)	