Please check the examination details below before entering your candidate information		
Candidate surname		Other names
Centre Number Candidate Nu	ımber	
Pearson Edexcel International Advanced Level		
Time 1 hour 30 minutes	Paper reference	WFM02/01
Mathematics		
International Advanced Subsidiary/Advanced Level		
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Further Pure Mathematics F2		
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(M. 1)		
You must have:  Mathematical Formula a and Statistical Tables (Vallous), salsulators  Total Marks		
Mathematical Formulae and Statistical Tables (Yellow), calculator		
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Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
- use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

  Turn over





- 1. Given that  $y = \ln(5 + 3x)$ 
  - (a) determine, in simplest form,  $\frac{d^3y}{dx^3}$

(3)

(b) Hence determine the Maclaurin series expansion of ln(5 + 3x), in ascending powers of x up to and including the term in  $x^3$ , giving each coefficient in simplest form.

**(2)** 

(c) Hence write down the Maclaurin series expansion of ln(5-3x), in ascending powers of x up to and including the term in  $x^3$ , giving each coefficient in simplest form.

**(1)** 

(d) Use the answers to parts (b) and (c) to determine the first 2 non-zero terms, in ascending powers of x, of the Maclaurin series expansion of

$$\ln\left(\frac{5+3x}{5-3x}\right)$$

**(2)** 

Question 1 continued



Question 1 continued

Question 1 continued	
(To	otal for Question 1 is 8 marks)
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2. (a) Express

$$\frac{1}{(2n-1)(2n+1)(2n+3)}$$

in partial fractions.

**(2)** 

(b) Hence, using the method of differences, show that for all integer values of n,

$$\sum_{r=1}^{n} \frac{1}{(2r-1)(2r+1)(2r+3)} = \frac{n(n+2)}{a(2n+b)(2n+c)}$$

where a, b and c are integers to be determined.

**(4)** 

Question 2 continued



Question 2 continued

Question 2 continued	
(Total for Questi	ion 2 is 6 marks)



3. (a) Show that the transformation  $y = \frac{1}{z}$  transforms the differential equation

$$x^2 \frac{\mathrm{d}y}{\mathrm{d}x} + xy = 2y^2 \tag{I}$$

into the differential equation

$$\frac{\mathrm{d}z}{\mathrm{d}x} - \frac{z}{x} = -\frac{2}{x^2} \tag{II}$$

(b) Solve differential equation (II) to determine z in terms of x.

**(4)** 

(c) Hence determine the particular solution of differential equation (I) for which  $y = -\frac{3}{8}$ at x = 3

Give your answer in the form y = f(x).

**(2)** 



Question 3 continued



Question 3 continued

Question 3 continued
(Total for Orestion 2 is 0 months)
(Total for Question 3 is 9 marks)



$$\frac{\mathrm{d}^4 y}{\mathrm{d}x^4} = Ay \frac{\mathrm{d}^3 y}{\mathrm{d}x^3} + B \frac{\mathrm{d}y}{\mathrm{d}x} \frac{\mathrm{d}^2 y}{\mathrm{d}x^2}$$

where A and B are integers to be determined.

**(4)** 

Given that y = 1 at x = -1

4.

(b) determine the Taylor series solution for y, in ascending powers of (x + 1) up to and including the term in  $(x + 1)^4$ , giving each coefficient in simplest form.

**(3)** 



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Question 4 continued	
(To	otal for Question 4 is 7 marks)



5.	In this question you must show all stages of your working.
	Solutions relying entirely on calculator technology are not acceptable.

Use algebra to determine the set of values of x for which

$$\frac{x^2 - 9}{|x + 8|} > 6 - 2x$$

**(6)** 

Question 5 continued



Question 5 continued

Question 5 continued	
(Tota	al for Question 5 is 6 marks)
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**6.** A complex number z is represented by the point P in an Argand diagram.

Given that

$$|z - 2i| = |z - 3|$$

(a) sketch the locus of P. You do **not** need to find the coordinates of any intercepts.

**(2)** 

The transformation T from the z-plane to the w-plane is given by

$$w = \frac{iz}{z - 2i} \qquad z \neq 2i$$

Given that T maps |z - 2i| = |z - 3| to a circle C in the w-plane,

(b) find the equation of C, giving your answer in the form

$$\left| w - \left( p + qi \right) \right| = r$$

where p, q and r are real numbers to be determined.

**(6)** 



Question 6 continued	



Question 6 continued

Question 6 continued	
(Total for Question 6 is 8 marks)	



## 7. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(a) Use de Moivre's theorem to show that

$$\cos 5x \equiv \cos x \left( a \sin^4 x + b \sin^2 x + c \right)$$

where a, b and c are integers to be determined.

**(4)** 

(b) Hence solve, for  $0 < \theta < \frac{\pi}{2}$ 

$$\cos 5\theta = \sin 2\theta \sin \theta - \cos \theta$$

giving your answers to 3 decimal places.

**(4)** 



Question 7 continued



Question 7 continued

Question 7 continued	
Γ)	Cotal for Question 7 is 8 marks)



$$r = 1 - \sin \theta \qquad 0 \leqslant \theta < \frac{\pi}{2}$$

The point *P* lies on *C*, such that the tangent to *C* at *P* is parallel to the initial line.

(a) Use calculus to determine the polar coordinates of P

**(4)** 

The finite region R, shown shaded in Figure 1, is bounded by

- the line with equation  $\theta = \frac{\pi}{2}$
- the tangent to *C* at *P*
- part of the curve C
- the initial line
- (b) Use algebraic integration to show that the area of R is

$$\frac{1}{32}\Big(a\pi+b\sqrt{3}+c\Big)$$

where a, b and c are integers to be determined.

**(6)** 

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Question 8 continued



Question 8 continued	
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Question 8 continued	
	(Total for Question 8 is 10 marks)



- **9.** (a) Given that  $x = t^{\frac{1}{2}}$ , determine, in terms of y and t,
  - (i)  $\frac{\mathrm{d}y}{\mathrm{d}x}$
  - (ii)  $\frac{d^2y}{dx^2}$

**(5)** 

(b) Hence show that the transformation  $x = t^{\frac{1}{2}}$ , where t > 0, transforms the differential equation

$$x\frac{d^{2}y}{dx^{2}} - (6x^{2} + 1)\frac{dy}{dx} + 9x^{3}y = x^{5}$$
 (I)

into the differential equation

$$4\frac{\mathrm{d}^2 y}{\mathrm{d}t^2} - 12\frac{\mathrm{d}y}{\mathrm{d}t} + 9y = t \tag{II}$$

(2)

(c) Solve differential equation (II) to determine a general solution for y in terms of t.

**(5)** 

(d) Hence determine the general solution of differential equation (I).

**(1)** 

Question 9 continued



Question 9 continued	
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Question 9 continued



(Total for Question 9 is 13 marks)
TOTAL FOR PAPER IS 75 MARKS

