

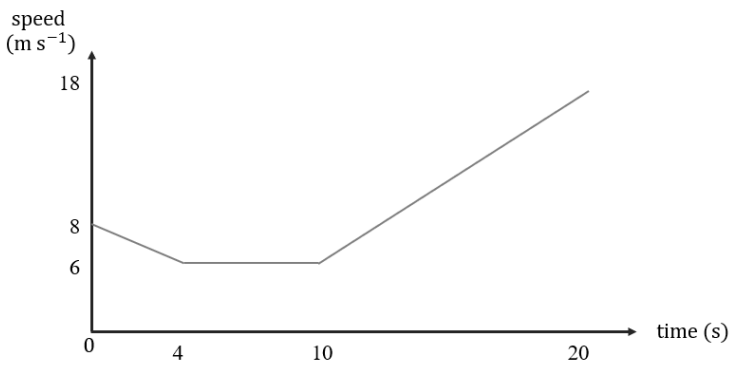


Mark Scheme (Results)

October 2023

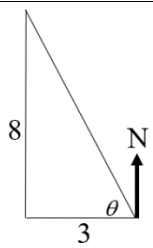
Pearson Edexcel International Advanced Level
in Mechanics (WME01) Paper 01

QUESTION NUMBER	SCHEME	MARKS
1	<p>Diagram description: A horizontal beam AB of length 6. A downward force of 24 acts at G, the midpoint. An upward force of 2T acts at C, and an upward force of T acts at D. The distance from A to C is x, and from C to D is 2. The distance from G to D is 3, and from G to B is 3.</p>	
	Form a moments equation M(A): $(2T \times x) + T(x + 2) = (24 \times 3)$	M1 A1
	Form a second equation vert $3T = 24$	M1
	Alternative moments equations in x and T M(C): $24(3 - x) = T \times 2$ M(G): $2T(3 - x) = T(x - 1)$ M(D): $(2T \times 2) = 24 \times (x - 1)$ M(B): $2T(6 - x) + T(4 - x) = (24 \times 3)$ M(C): $\frac{24x}{6} \times \frac{x}{2} + 2T = \frac{24(6 - x)}{6} \times \frac{(6 - x)}{2}$	
	$T = 8(\text{N})$	A1
	$x = \frac{7}{3}$ accept 2.3 or better	A1
		(5)
	Notes for question 1	
M1	Forms a moments equation in x and T only with the correct no. of terms. Allow consistent extra g's. M0 if no x .	
A1	Correct unsimplified moments equation. Where two moments equations are used, award this mark for the first correct equation.	
M1	Resolves vertically to give equation in T only or a second moments equation in x and T (M0 if no x). Must be dimensionally correct with the correct no. of terms.	
A1	Correct value for tension at D	
A1	Correct value for x . Accept 2.3 or better	
	N.B. If T and $2T$ the wrong way round or they use $24g$, can score max M1A0M1A0A0.	

QUESTION NUMBER	SCHEME	MARKS
2(a)	$v = u + at : w = 8 + (-0.5)(4)$ (the value of w may not be seen)	M1
	$v = u + at : v = w + (1.2)(10)$	M1
	$v = 18^*$	A1*
		(3)
2(b)		B1 shape B1 time labels 4,10,20 B1 speed labels 6, 8, 18
		(3)
2(c)	Clear attempt to find distance using the area under their graph from $t = 0$ to $t = 20$ or another suitable method, <u>even if they are using the wrong shapes.</u> $\text{Distance} = \frac{(8 + "6") \times 4}{2} + (6 \times "6") + \frac{("6" + 18) \times 10}{2}$ $\text{OR } = (6 \times 4) + \frac{1}{2} \times 4 \times (8 - 6) + (6 \times 6) + (6 \times 10) + \frac{1}{2} \times 10 \times (18 - 6)$	M1 A1ft A1ft
	$= 184 \text{ (m)}$	A1
		(4)
		(10)
	Notes for question 2	
(a) M1 M1 A1*	Complete method for finding the velocity (w) when $t = 4$ M0 if $u = 0$. N.B. 6 on its own can imply this mark. Method completed to show the speed when $t = 20$ M0 if initial speed is not w . Fully correct solution leading to given answer	
(b) B1 B1 B1	Correct shape of graph Correct time labels Correct speed labels N.B. Solid vertical line(s) B0 for the shape.	
(c) M1 A1ft A1ft A1	Complete method to find distance travelled in 20 seconds. May use speed-time graph or <i>suvat</i> equations for three sections (28m, 36m, 120m) of the journey. Award this mark for a clear attempt to find the area and penalise errors in the A marks. M0 if graph does not have three sections. Equation with at most one error, ft their "6" Correct equation, ft their "6" Correct final answer	

QUESTION NUMBER	SCHEME	MARKS
3	<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> <p>Before</p> <p>10 ↓</p> <p>0</p> </div> <div style="text-align: center;"> </div> <div style="text-align: center;"> <p>After</p> <p>↓ v</p> </div> </div>	
3(a)	$10 \times 1.8 = (0.2 + 1.8)v$	M1
	$v = 9$ (positive)	A1
		(2)
3(b)	For tent peg, $I = \pm 0.2(v - 0)$ or For hammer, $-I = \pm 1.8(v - 10)$	M1 A1
	1.8Ns OR 1.8 kgms ⁻¹ units needed.	A1
		(3)
3(c)	$0 = 9^2 + 2a(0.12)$ OR $0 = 9^2 - 2a(0.12)$	M1A1
	$2g - R = 2a$ $R - 2g = 2a$	M1 A1
	$R = 690$ or 695	A1
		(5)
	N.B. Using $u = 10$ for 9 can score M0A0M1A1A0 max	
	Using $s = 12$, can score M1A0M1A1A0 max	(10)
ALT 1	$0.12 = \frac{(9+0)}{2}t$	M1A1
	$(R - 2g)t = 2 \times 9$	M1A1
	$R = 690$ or 695	A1
ALT 2	$0.12R = \frac{1}{2} \times 2 \times 9^2 + 2g \times 0.12$	M2A2
	$R = 690$ or 695	A1
	Notes for question 3	
(a)		
M1	Forms CLM equation, condone sign errors and extra g's and any correct cancellation	
A1	cao	
(b)		
M1	Impulse-momentum equation, dimensionally correct, correct no. of terms. Condone sign errors.	
	N.B. M0 if g is included.	
A1	A1 correct unsimplified equation	
A1	A1 cao must include units.	
(c)		
M1	Equation formed to find the acceleration. Must be dimensionally correct and have the correct no. of terms.	
A1	Correct unsimplified equation. Note $a = -337.5$	

M1	Use of $F=ma$. Must be dimensionally correct and have the correct no. of terms.	
A1	Correct equation, a does not need to be substituted but should be consistent with their a from first equation.	
A1	N.B. Use the equation for a to define the positive direction. cao	
	ALT 1	
M1	Equation(s) formed to find the time	
A1	Correct unsimplified equation. Note $t = \frac{2}{75} = 0.02666\ldots$	
M1	Use of imp-mom equation. Must be dimensionally correct and have the correct no. of terms.	
A1	Correct equation, t does not need to be substituted but should be consistent with their t from first equation.	
A1	cao	
	ALT 2	
M2	Use of work-energy equation. Must be dimensionally correct and have the correct no. of terms.	
A2	Correct unsimplified equation, -1 each error.	
A1	cao	

QUESTION NUMBER	SCHEME	MARKS
4(a)	$(5\mathbf{i} - 8\mathbf{j}) + 5(-\lambda\mathbf{i} + 2\lambda\mathbf{j})$ (m s ⁻¹) isw	M1 A1
		(2)
4(b)	$13 = \sqrt{(5 - 5\lambda)^2 + (-8 + 10\lambda)^2}$	M1 A1
	$169 = 25 - 50\lambda + 25\lambda^2 + 64 - 160\lambda + 100\lambda^2$	
	$25\lambda^2 - 42\lambda - 16 = 0^*$	A1* cso
		(3)
4(c)	$(-2\mathbf{i} + 4\mathbf{j})$ seen or implied	B1
	$(5\mathbf{i} - 8\mathbf{j}) + (-2\mathbf{i} + 4\mathbf{j})4$	M1A1
	 <p>e.g. $\tan^{-1}\left(\pm\frac{8}{3}\right), \tan^{-1}\left(\pm\frac{3}{8}\right), \sin^{-1}\left(\pm\frac{8}{\sqrt{73}}\right), \dots$</p>	M1
	339°	A1
		(5)
		(10)
	Notes for question 4	
(a) M1 A1	Use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ to form a vector expression in λ and t Correct unsimplified expression with $t = 5$ N.B. Allow use of column vectors for the M mark but not for the A mark.	
(b) M1 A1 A1*	Collect \mathbf{i} 's and \mathbf{j} 's and correct use of Pythagoras to form an equation in λ Correct equation cso. Expand brackets and correctly reach the GIVEN answer. N.B. Allow $0 = 25\lambda^2 - 42\lambda - 16$	
(c) B1 M1 A1 M1 A1	Or column vector Complete method to find the velocity when $t = 4$. Correct unsimplified expression. Note the correct velocity is $\mathbf{v} = -3\mathbf{i} + 8\mathbf{j}$ Use their velocity vector at $t = 4$ with trig to find a relevant angle. Cao. Degrees sign not required. N.B. if they work with both values of λ , can score max all the marks except the last one.	

QUESTION NUMBER	SCHEME	MARKS
5		
5(a)	$F = 10\cos\theta - 0.2g$ or $F = 0.2g - 10\cos\theta$	M1 A1
	$ F = 1.9$ or 1.89 (N)	A1
		(3)
5(b)	Friction acts downwards or down.	A1
	A0 for anything else.	
		(1)
5(c)	$R = T \sin\theta$ $\left(R = \frac{12T}{13}\right)$	M1 A1
	$F = \frac{1}{4}R$	B1
	Resolve vertically For min value $T \cos\theta = 0.2g - F$ For max value $T \cos\theta = 0.2g + F$	M1 A1 A1
(i)	Min T 3.2 or 3.19 (N)	A1
(ii)	Max T 13 or 12.7 (N)	A1
	N.B. Penalise over accuracy once for the whole question and penalise the FIRST time it is seen.	
	N.B. If 2 instead of 0.2 is used throughout the WHOLE question, treat as a MR.	
		(8)
		(12)
	Notes for question 5	
(a) M1	Resolve vertically, dimensionally correct, condone sin/cos confusion and sign errors.	
A1	Correct unsimplified equation.	
A1	Correct value for Friction, must be positive	
	N.B. If they use μR as their notation for F and never separate μ and R , allow M1A1A1. If, however, they do separate them, give M1A1A0.	
(b) A1	Correct direction from a correct, but possibly unrounded, answer to part (a).	
(c) M1	Resolve perpendicular to the rod. Must be dimensionally correct and have correct no of terms. Condone sin/cos confusion.	
	N.B. M0 if they use $T = 10$	
A1	Correct unsimplified equation	
B1	$F = \frac{1}{4}R$ seen or implied	
M1	Resolve parallel to the rod for either case. Must be dimensionally correct and have correct no of terms. Condone sin/cos confusion.	
	N.B. M0 if they use $T = 10$ or if they use F from part (a).	
A1	Correct minimum case equation	
A1	Correct maximum case equation	
(i)A1	cao for min T . Allow 0.325g	
(ii)A1	cao for max T Allow 1.3g	
	N.B. If only one found and no labels, allow the A mark for the equation but must state which one it is to score the A mark for the answer.	
	N.B. If both correctly found and no labels, allow all the marks.	
	N.B. If both correctly found but the answers are labelled wrongly, lose the final two A marks.	

QUESTION NUMBER	SCHEME	MARKS
6(a)	$\frac{(20\mathbf{i} + 34\mathbf{j}) - (15\mathbf{i} + 36\mathbf{j})}{0.5} \text{ oe}$	M1
	$(10\mathbf{i} - 4\mathbf{j})^*$	A1*
		(2)
6(b)	$(15\mathbf{i} + 36\mathbf{j}) + t(10\mathbf{i} - 4\mathbf{j})$	M1 A1
		(2)
6(c)(i)	Verify using $t = 1.5$ in p or q $\mathbf{p} = (15\mathbf{i} + 36\mathbf{j}) + 1.5(10\mathbf{i} - 4\mathbf{j}) = 30\mathbf{i} + 30\mathbf{j}$ $\mathbf{q} = (42 - 8 \times 1.5)\mathbf{i} + (9 + 14 \times 1.5)\mathbf{j} = 30\mathbf{i} + 30\mathbf{j}$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
	N.B. The A mark for (ii) is now to be treated as a B mark.	
		(4)
ALT1 (i)	Find t by equating i or j components of p and q Equate i 's $15 + 10t = 42 - 8t \rightarrow t = 1.5$ j 's $36 - 4t = 9 + 14t \rightarrow t = 1.5$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
ALT2 (i)	Uses ratio: $\frac{15 + 10t}{36 - 4t} = \frac{42 - 8t}{9 + 14t}$ $\rightarrow t = 1.5$ or -8.5 verifies that components are both 30 at $t = 1.5$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
		(4)
6(d)	Position of P at 14:30 is $40\mathbf{i} + 26\mathbf{j}$	B1
	Position of Q when $t = 0.5$ $\mathbf{q} = (42 - 8 \times 0.5)\mathbf{i} + (9 + 14 \times 0.5)\mathbf{j}$ $= (38\mathbf{i} + 16\mathbf{j})$	M1
	$15\mathbf{j}$ seen or implied	B1
	New position of Q at time 14:30 $\mathbf{q} = (38\mathbf{i} + 16\mathbf{j}) + 2(15\mathbf{j})$ N.B. M0 if 2.5 is used.	M1
	$\mathbf{q} = 38\mathbf{i} + 46\mathbf{j}$	A1
	$ PQ = \sqrt{(40 - 38)^2 + (26 - 46)^2}$	dM1
	$= \sqrt{404} \text{ or } 2\sqrt{101} \text{ (km)}$	A1
		(7)
		(15)

	<p align="center">Notes for question 6</p> <p>N.B. Allow use of column vectors throughout apart from the A marks in (a) and (b).</p>	
(a)		
M1	Complete method to find an expression for the velocity. Allow if they use 30 minutes. Give M1A0, if there are missing brackets.	
A1*	Reaches the given answer from fully correct working.	
(b)		
M1	Finds an expression for p in terms of t with the correct structure	
A1	Correct answer in terms of i, j and t .	
(c)		
(i) M1	Substitutes $t = 1.5$ into the given q or their p	
A1	P equation correct	
A1	Q equation correct N.B. p or q = $30\mathbf{i} + 30\mathbf{j}$ alone can imply a correct equation in each case.	
(ii) A1(B1)	$30\mathbf{i} + 30\mathbf{j}$ seen	
	ALT 1	
(i) M1	Equates coefficients of i or j using the given q and their p	
A1	Correct equation for i leading to $t = 1.5$	
A1	Correct equation for j leading to $t = 1.5$ N.B. Allow both A marks if they only write $t = 1.5$ once.	
(ii) A1(B1)	$30\mathbf{i} + 30\mathbf{j}$ seen	
	ALT 2	
(i) M1	Uses ratio of components to form equation.	
A1	Two t values	
A1	Verifies that components are both 30 at $t = 1.5$	
(ii) A1(B1)	$30\mathbf{i} + 30\mathbf{j}$ seen	
(d)		
B1	Position of P at 14:30	
M1	Use $t = 0.5$ to find the new position of Q at 12:30	
B1	Correct expression seen for new velocity of Q	
M1	Complete method to find the new position of Q at 14:30, using their new v for Q .	
A1	Correct position,	
dM1	Use of Pythagoras to find the distance. Dependent on both previous M marks.	
A1	Correct surd answer	

QUESTION NUMBER	SCHEME	MARKS
7(a)(i)	For A: $\frac{4mg}{3} - mg \sin \alpha - F = ma$	M1A1
	$R = mg \cos \alpha$	M1 A1
	Use of $F = \frac{1}{3} R$ in an equation.	M1
	$a = \frac{11g}{15}$ or $0.73g$ or better	A1
(ii)	For B: $kmg - \frac{4mg}{3} = kma$	M1 A1
	$k = 5$	A1
	N.B. Either equation of motion could be replaced by a whole system equation: $kmg - mg \sin \alpha - F = (k+1)ma$	
		(9)
7(b)	Complete method to find resultant force $2T \cos\left(\frac{90^\circ - \alpha}{2}\right)$	M1 A1
	Substitute $T = \frac{4mg}{3}$ and trig	dM1
	$\frac{32mg}{15}$ or $2.1mg$ or better.	A1
ALT 1	Use of cosine rule: $\sqrt{T^2 + T^2 - 2(T)(T) \cos(90 + \alpha)}$	M1 A1
ALT 2	Use of vert and horiz components to find the resultant: $\sqrt{(T \cos \alpha)^2 + (T + T \sin \alpha)^2}$	M1 A1
		(4)
		(13)
	Notes for question 7	
(a) M1	For A use $F=ma$ parallel to the plane. Must be dimensionally correct and have correct no of terms. Condone sin/cos confusion.	
A1	N.B. If they use T in this equation and never replace it, allow M1.	
M1	Correct unsimplified equation.	
M1	N.B. a could be replaced by $-a$	
A1	Resolve perpendicular to the plane Must be dimensionally correct and have correct no of terms. Condone sin/cos confusion.	
M1	Correct equation	
A1	Use of $F = \frac{1}{3} R$	
M1	Correct answer	
	For B use $F=ma$ vertically. Must be dimensionally correct and have correct no of terms. Condone sin/cos confusion.	
	N.B. Must have km on <i>both</i> sides for this mark.	
	N.B. If they use T in this equation and never replace it, allow M1.	
A1	Correct unsimplified equation	
	N.B. a could be replaced by $-a$, but must be consistent with the equation for A.	
A1	correct answer	

(b) M1	Complete method to find resultant force on pulley , allow sin/cos confusion
A1	Correct expression
dM1	Substitute $T = \frac{4mg}{3}$ and trig, dependent on previous M mark
A1	Correct answer.
(b) ALT1	
M1	Complete method – must involve α or its numerical value
A1	Correct expression
dM1	Substitute $T = \frac{4mg}{3}$ and trig, dependent on previous M mark
A1	Correct answer. Allow $\sqrt{\frac{1024m^2g^2}{225}}$ or similar.
(b) ALT2	
M1	Complete method, allow sin/cos confusion
A1	Correct expression
dM1	Substitute $T = \frac{4mg}{3}$ and trig, dependent on previous M mark
A1	Correct answer. Allow $\sqrt{\frac{1024m^2g^2}{225}}$ or similar.