



Mark Scheme (Results)

January 2021

Pearson Edexcel International A Level
in Statistics S2 (WST02/01)

Question Number	Scheme		Marks
1(a)	B(30, 0.05)		B1
			(1)
(b)	The probability (oe) of an <u>oyster</u> surviving/not surviving is constant		B1
	The survival of each <u>oyster</u> is independent of the others		(1)
(c)(i)	${}^{30}C_{24} (0.05)^6 (0.95)^{24}$ oe		M1
	= 0.002708...	awrt 0.0027	A1
(ii)	$P(Y \geq 3) = 1 - P(Y \leq 2)$ from $Y \sim B(30, 0.05)$ or $P(X \leq 27)$ from $X \sim B(30, 0.95)$		M1
	= $1 - 0.8122$		
	= 0.1878	awrt 0.188	A1
			(4)
(d)	$A \sim \text{Po}(10)$		B1
	$P(A \geq n) > 0.8$		
	$P(A \leq n-1) < 0.2$ or $P(A \leq 6) = 0.1301$awrt 0.13 or $P(A \geq 7) = 0.8699$awrt 0.87		M1
	$n = 7$		A1cao
			(3)
(e)	$H_0 : p = 0.05, H_1 : p > 0.05$		B1
	Using $C \sim B(25, 0.05)$ and $P(C \geq 4)$	Using $D \sim B(25, 0.95)$ and $P(D \leq 21)$	M1
	$P(C \geq 4) = 0.0341 / \text{CR } C \geq 4$	$P(D \leq 21) = 0.0341 / \text{CR } D \leq 21$	A1
	Evidence to reject H_0 , in the CR, significant		dM1
	There is evidence that the proportion of oysters not surviving has increased (oe)/ Jim's belief is supported.		A1cso
			(5)
			Total 14
Notes			
(a)	B1	Must include B(inomial), $n = 25$ and $p = 0.05$. Do not allow $p = 0.95$ in part (a)	
(b)	B1	For either correct assumption in context. Ignore extraneous non-contradicting comments.	
(c)(i)	M1	allow ${}^{30}C_6$ oe or $P(X \leq 6) - P(X \leq 5)$ with one correct probability	
	A1	awrt 0.0027 (correct answer scores 2 out of 2)	
(ii)	M1	Writing/using $1 - P(Y \leq 2)$ with $B(30, 0.05)$ or writing/using $P(X \leq 27)$ with $B(30, 0.95)$	
	A1	awrt 0.188 (correct answer scores 2 out of 2)	
(d)	B1	Writing or using $\text{Po}(10)$ (sight of 0.1301 or 0.8699 can imply this mark)	
	M1	Allow $P(A < n) < 0.2$ or $P(A < 7) = \text{awrt } 0.13$ or $P(A > 6) = \text{awrt } 0.87$	
	A1cao	$n = 7$ which must come from use of $\text{Po}(10)$ or $N(10, 9.5)$	
	Note:	Use of normal approx. with $\mu = 10$ and $\sigma^2 = 9.5$ leading to $n < 7.4$...can score M1 Exact binomial gives $P(A \leq 6) = 0.14 / P(A \geq 7) = 0.86$ scores B0M0A0	
(e)	B1	Both hypotheses correct (allow use of p or π). Allow $H_0 : p = 0.95, H_1 : p < 0.95$	
	M1	Using $B(25, 0.05)$ and writing/using $P(C \geq 4)$ or if CR given $P(C \geq 3)$ using $B(25, 0.95)$ and writing/using $P(D \leq 21)$ or if CR given $P(D \leq 20)$	
	A1	Correct probability to 3sf (must not go on and give incorrect CR) or correct CR (ignore upper tail)	
	dM1	(dep on 1 st M1) A correct non-contextual statement (do not allow contradicting non-contextual comments) which is consistent with their prob and 0.05 (If not stated, may be implied by A1)	
	A1cso	All previous marks must be awarded. Correct contextual conclusion with bold words (oe)	
SC:	2-tail	Use of two-tailed test can score max: B1M1A1M1A0, but must not reject H_0 for 2 nd M1	

Question Number	Scheme		Marks
2(a)	$1 - F(3.5) = 1 - 0.97127\dots$		M1
	$= 0.028727\dots$	awrt 0.0287	A1
			(2)
(b)	$W \sim B(30, "0.0287")$		M1
	$1 - P(W \leq 1) = 1 - \left((1 - "0.0287")^{30} + {}^{30}C_1 ("0.0287")^1 (1 - "0.0287")^{29} \right)$ oe		M1
	$= 1 - 0.78748 \dots = 0.2125\dots$	awrt 0.213 to awrt 0.216	A1
			(3)
(c)	$\frac{dF(w)}{dw} = \frac{1}{3} \left(1 - \frac{w^3}{64} \right)$		M1
	$E(W^2) = \int_0^4 \frac{1}{3} \left(w^2 - \frac{w^5}{64} \right) dw = \frac{1}{3} \left[\frac{w^3}{3} - \frac{w^6}{384} \right]_0^4$		dM1
	$= \frac{32}{9}$		A1
	$\text{Var}(W) = \frac{32}{9} - 1.6^2$		M1
	$= \frac{224}{225}$		A1
			(5)
			Total 10
Notes			
(a)	M1	For writing or using $1 - F(3.5)$ Implied by correct answer	
	A1	awrt 0.0287	
(b)	M1	For writing or using $B(30, "0.0287")$ allow $n("their\ 0.0287")^1 (1 - "their\ 0.0287")^{29}$ ignore any number for n (allow their p to 2sf)	
	M1	For $1 - \left((1 - "0.0287")^{30} + {}^{30}C_1 ("0.0287")^1 (1 - "0.0287")^{29} \right)$ Allow ${}^{30}C_{29}$ in any form	
	A1	allow answer in the range awrt 0.213 to awrt 0.216	
(c)	M1	Differentiating $F(w)$ at least one term correct	
	dM1	(Dep on previous M1). Attempting to integrate expanded $w^2 f(w)$. At least one $w^n \rightarrow w^{n+1}$ Ignore limits for this M mark.	
	A1	awrt 3.56 must come from correct algebraic integration (may be embedded)	
	M1	Use of correct formula with values substituted. Must see the subtraction of 1.6^2	
	A1	Dependent upon 2 nd M1 awrt 0.996 (A correct answer with no algebraic integration seen may score M1M0A0M1A0)	

Question Number	Scheme		Marks
3(a)	$P(X \neq 4) = 1 - P(X = 4)$ oe $\left(= 1 - \frac{e^{-7} 7^4}{4!} \quad \text{or} \quad 1 - (0.1730 - 0.0818)\right)$		M1
	$= 0.90877\dots$	awrt 0.909	A1
			(2)
(b)	$P(Y=1) = (1 - "0.90877\dots") ("0.90877\dots")^4 \times {}^5C_1$		M1M1
	$= 0.311\dots$		A1
			(3)
(c)(i)	$\lambda = 0.07n$		B1
	$A \sim N(0.07n, 0.07n)$		M1
	$\frac{3.5 - "0.07n"}{\sqrt{"0.07n"}}$		M1
	$\frac{3.5 - 0.07n}{\sqrt{0.07n}} = -1.55$ or $"0.07n" - (1.55\sqrt{0.07})\sqrt{n} - 3.5 = 0$		B1
	$n - \left(\frac{1.55}{0.07}\sqrt{0.07}\right)\sqrt{n} - \frac{3.5}{0.07} = 0 \Rightarrow n - 1.55\sqrt{\frac{n}{0.07}} - 50 = 0$		A1cso
			(5)
(ii)	$\sqrt{n} = \frac{\frac{1.55}{\sqrt{0.07}} \pm \sqrt{\left(\frac{1.55}{\sqrt{0.07}}\right)^2 + 4 \times 50}}{2} = \text{awrt } -4.72\dots \text{ or awrt } 10.6\dots (4\sqrt{7})$		M1
	$n = 112$		A1cao
			(2)
(d)	$H_0: \lambda = 7 \quad H_1: \lambda > 7$		B1
	$P(X \geq 15) = 1 - P(X \leq 14)$	$P(X \geq 14) = 0.0128$	M1
	$= 1 - 0.9943$	$P(X \geq 15) = 0.0057$	
	$= 0.0057$	CR $X \geq 15$	A1
	Reject H_0 , in the CR, Significant		dM1
	There is evidence that the number of water fleas per 100 ml of the pond water has increased		A1
			(5)
Total 17			
Notes			
(a)	M1	For $1 - P(X = 4)$ or $1 - P(X \leq 4) + P(X \leq 3)$ oe	
(b)	M1	$(1 - "their 0.909")^4 ("their 0.909")$ or $(1 - "their 0.909") ("their 0.909")^4$ allow their values to 2s.f.	
	M1	$P(Y=1) = (1 - "their 0.909") ("their 0.909")^4 \times {}^5C_1$ allow their values to 2s.f.	
	A1	awrt 0.312 or awrt 0.311	
(c)(i)	B1	Writing or using mean as $0.07n$	
	M1	Normal with the mean = variance which must be in terms of n (may be implied by correct standardisation).	
	M1	Standardising with their mean and their $\sqrt{\text{var}}$. If not stated they must be correct. Allow 2.5, 3, 3.5, 4, 4.5 (A correct standardisation implies B1M1M1)	
	B1	Their standardisation = ± 1.55	
	A1cso	Must come from compatible signs in standardisation. Need at least one step between standardisation indicating division by 0.07 and correct equation.	
(ii)	M1	Correct method to solve given quadratic <u>or</u> sight of awrt -4.72 or awrt 10.6	
	A1cao	112 only (must reject 2nd answer if found) (an answer of 112 only scores M1A1)	
(d)	B1	Both hypotheses correct in terms of λ or μ [using p scores B0]	
	M1	For $1 - P(X \leq 14)$ or for CR: one of $P(X \geq 14) = 0.0128$ or $P(X \geq 15) = 0.0057$	
	A1	awrt 0.0057 or correct CR allow $X > 14$	
	dM1	(dep on 1 st M1) A correct non-contextual statement (do not allow contradicting non-contextual comments) which is consistent with their prob and 0.01. (If not stated, may be implied by A1)	
	A1	All previous marks must be awarded. Correct context. conclusion with increase(oe) and fleas	

Question Number	Scheme		Marks
4(a)	$\int_0^a k(a-x)^2 dx = \left[k \left(a^2 x - ax^2 + \frac{x^3}{3} \right) \right]_0^a$ or $\left[\frac{-k(a-x)^3}{3} \right]_0^a$		M1 A1
	$k \left(a^3 - a^3 + \frac{a^3}{3} \right) = 1$ or $\frac{ka^3}{3} = 1 \Rightarrow ka^3 = 3$		A1 cso
			(3)
(b)	$\int_0^a kx(a-x)^2 dx = \left[k \left(\frac{a^2 x^2}{2} - \frac{2ax^3}{3} + \frac{x^4}{4} \right) \right]_0^a$ or $\left[\frac{-kx(a-x)^3}{3} + \frac{k(a-x)^4}{12} \right]_0^a$		M1A1
	$k \left(\frac{a^2 a^2}{2} - \frac{2aa^3}{3} + \frac{a^4}{4} \right) = 1.5$ or $\left[\frac{ka(a)^3}{3} - \frac{k(a)^4}{12} \right]_0^a = 1.5$ or $ka^4 = 18$ oe		dM1
	$\frac{ka^4}{ka^3} = 6$ or $\frac{18}{3} = 6$ [$\therefore a = 6$]		A1cso
			(4)
(c)	$F(x) = \frac{1}{72} \left(36x - 6x^2 + \frac{x^3}{3} \right)$	$\frac{1}{72} \left(36x - 6x^2 + \frac{x^3}{3} \right) = 0.5$ oe	M1
	F(1.15)(= 0.47...) and F(1.25) (= 0.5038...)	1.2377...	M1
	F(1.15) = awrt 0.47, F(1.25) = awrt 0.504 (0.47(18...) < 0.5 < 0.503(8...)) therefore the median is 1.2 to 1 decimal place.	therefore the median is 1.2 to 1 decimal place.	A1
			(3)
			Total 10
Notes			
(a)	M1	Integrating f(x) at least 1 term correct. For M1 allow $\frac{\pm k(a-x)^3}{3}$	
	A1	Correct integration (ignore limits)	
	A1cso	Substitute limits and equating to 1 to form one expression in terms of k and a leading to $ka^3 = 3$	
(b)	M1	Indicating that they are integrating xf(x) with an attempt at integrating $x^n \rightarrow x^{n+1}$	
	A1	Correct integration	
	dM1	(dep on previous M1). Substitute limits and equating to 1.5 to form a 2 nd expression in terms of k and a	
	A1cso	Correct method shown to solve their 2 equations to eliminate k and show a=6	
(c)	M1	Finding correct F(x). Allow $F(x) = 1 - \frac{(6-x)^3}{216}$ but $F(x) = \frac{(6-x)^3}{216}$ is M0 Allow in terms of k for this mark	
	M1	For attempting their F(1.15) and their F(1.25) or a suitable tighter interval or for ‘solving’ cubic leading to a value awrt 1.24	
	A1	Both correct values and correct conclusion (allow $x = 1.2$) or awrt 1.24 and correct conclusion (allow $x = 1.2$). Allow change of sign argument if they have subtracted 0.5 (i.e. $-0.028... < 0 < 0.0038...$).	

Question Number	Scheme		Marks
5(a)	U[0, 3]		M1
	$\frac{3-1.8}{3} = 0.4$		A1
			(2)
(b)	$X^2 = W^2 + (3-W)^2$		M1
	$X^2 = W^2 + 9 + W^2 - 6W \Rightarrow X^2 = 2W^2 - 6W + 9$		A1
			(2)
(c)	$E(W) = 1.5$		B1
	$\text{Var}(W) = \frac{9}{12} = \frac{3}{4}$		B1
	$E(W^2) = \frac{3}{4} + "1.5"^2$		M1
	$E(W^2) = 3$		A1
	So $E(X^2) = 2 \times "3" - 6 \times "1.5" + 9 = 6$		M1A1
			(6)
(d)	$P(X^2 > 5) = P(2W^2 - 6W + 4 > 0)$		M1
	$= P((2W - 2)(W - 2) > 0)$		M1
	$= P(W > 2) + P(W < 1)$		dM1
	$= \frac{2}{3}$ oe		A1
			(4)
			Total 14
Notes			
(a)	M1	Writing or using the correct distribution	Allow: $\frac{1.8}{3}$ for M1A0
	A1	0.4 oe	
(b)	M1	Using Pythagoras to find the length	Note: $X^2 = W^2 + (W - 3)^2$ scores M1A0
	A1	Brackets multiplied seen leading to $X^2 = 2W^2 - 6W + 9$ with no incorrect working	
(c)	B1	1.5	
	B1	$\text{Var}(W) = 0.75$	Using integration: $E(W^2) = \int_0^3 \frac{1}{3} w^2 dw$ (ignore limits)
	M1	Writing or using $E(W^2) = \text{Var}(W) + [E(W)]^2$	$\left[\frac{1}{9} w^3\right]_0^3$ (correct integration with correct limits)
	A1	3	
	M1	Use of $E(X^2) = 2E(W^2) - 6E(W) + 9$ with their values.	
	A1	6 An answer of 6 from correct working implies all previous marks.	
(d)	M1	For realising they need to find the probability of $2W^2 - 6W + 4 > 0$ (condone =)	
	M1	Solving their 3-term quadratic ($W = 1$ and $W = 2$ implies 1 st two M marks)	
	dM1	(dep on 2 nd M1) Realising they need to add the 2 outer areas	
	A1	awrt 0.667	

Question Number	Scheme						Marks													
6(a)	Taking a random sample is quicker/cheaper/easier (compared to asking all of the youth club members).						B1													
							(1)													
(b)	A <u>list/register/database</u> of <u>all</u> the youth club <u>members</u>						B1													
							(1)													
(c)	The <u>members</u>						B1													
							(1)													
(d)	$p^2 = \frac{25}{64}$						M1													
	$p = \frac{5}{8}$						A1													
	$\frac{5}{8} + q + r = 1$ or $2qr = \frac{1}{16}$ or $\frac{25}{64} + 2\frac{5}{8}q + 2\frac{5}{8}r + q^2 + \frac{1}{16} + r^2 = 1$						B1													
	Any two equations from above						B1													
	$\frac{3}{8}q - q^2 = \frac{1}{32}$						dM1													
	$q = \frac{1}{4}$						A1													
	$P(M = 50) = \frac{1}{4} \times \frac{1}{4} = \frac{1}{16}$ *						A1cso*													
							(7)													
						Total 10														
Notes																				
(a)	B1	Any one of the given reasons. Ignore extraneous non-contradictory reasons.																		
(b)	B1	Idea of list(oe). Need all (oe) (eg complete list) and members.																		
(c)	B1	The members/a member																		
(d)	M1	Correct method, may be implied																		
	A1	$p = \frac{5}{8}$ or $P(X = 20) = \frac{5}{8}$																		
	B1	One equation in q and r from use of $p + q + r = 1$, $P(M = 60)$ or $\sum P(M=m) = 1$ see Note (allow ft on their value of p)																		
	B1	Two correct equations in q and r Some will substitute directly into the third equation so may see: $\frac{25}{64} + \frac{5}{4}q + \frac{5}{128q} + q^2 + \frac{1}{16} + \frac{1}{1024q^2} = 1$ which is correct and scores B1B1																		
	dM1	(dep on 1 st B1) Correct method to solve simultaneous equation leading to a probability for q or r (may be implied by $q = \frac{1}{4}$ or $r = \frac{1}{8}$ provided B1B1 scored)																		
	A1	Correct probability for q (dependent on all previous marks in part (d))																		
	A1cso*	Correct solution with use of $P(M = 50) = q^2$ and all previous marks awarded.																		
	Note:	<table><tr><td>m</td><td>20</td><td>35</td><td>45</td><td>50</td><td>60</td><td>70</td></tr><tr><td>$P(M=m)$</td><td>$\frac{25}{64}$</td><td>$2pq$</td><td>$2pr$</td><td>q^2</td><td>$\frac{1}{16}$</td><td>r^2</td></tr></table>					m	20	35	45	50	60	70	$P(M=m)$	$\frac{25}{64}$	$2pq$	$2pr$	q^2	$\frac{1}{16}$	r^2
m	20	35	45	50	60	70														
$P(M=m)$	$\frac{25}{64}$	$2pq$	$2pr$	q^2	$\frac{1}{16}$	r^2														
		$\frac{25}{64} + 2pq + 2pr + q^2 + \frac{1}{16} + r^2 = 1$																		