Table 1: Time costs (Seconds) for querying $Q_1 - Q_4$ included in this paper

		Genera	ted by OpenI	RuleBench Ge	nerator	Stanford Large Network Dataset Collection				
		G_{a1}	G_{a2}	G_{a3}	G_{a4}	S_{l1}	S_{l2}	S_{l3}	S_{l4}	
	DLV	0.12984	0.19448	0.26517	0.41013	7.32432	7.69948	17.87713	11.92344	
Q_1	IRIS	0.88169	2.35286	4.27499	9.01246	9.95180	3438.38439	5827.55796	4184.18595	
	XSB	2.04782	1.02391	1.58240	1.86165	121.00725	140.80500	381.64770	399.81060	
	Yap	11.60403	9.20487	10.32242	15.98619	58.45222	220.02794	21.30200	25.55715	
	$ASLOG_d$	0.02312	0.06436	0.08600	0.07172	1.60079	1.71433	2.87502	2.60274	
	$ASLOG_d^{\star}$	0.01317	0.01981	0.02334	0.01830	1.01537	1.02508	1.42151	1.32121	
	$RDFox_n$	0.01744	0.03288	0.04570	0.07468	1.33415	1.38628	1.69490	1.80259	
	$RDFox_c$	0.00473	0.00553	0.00830	0.01275	0.28660	0.30369	0.15630	0.43000	
Q_1	FI_c	0.00001	0.00012	0.00050	0.00784	0.23739	0.24299	0.53447	0.26522	
	$AMEM_c$	0.00002	0.00015	0.00044	0.00654	0.24319	0.24672	0.56235	0.27770	
	$ASLOG_m$	0.02274	0.06384	0.08543	0.07123	1.57175	1.68752	2.79670	2.54502	
	$ASLOG_{m}^{\star}$	0.01279	0.01929	0.02278	0.01714	1.01088	1.02010	1.40726	1.31201	
	$ASLOG_c$	0.00002	0.00009	0.00017	0.00162	0.01932	0.02030	0.05711	0.04034	
	DLV	0.21667	0.35725	0.47180	0.80445	15.64693	16.46927	50.22032	26.09315	
	IRIS	1.01871	2.49934	4.67151	10.73180	3182.16654	3487.82112	6138.22010	4401.22505	
Q_{21}	XSB	2.04782	1.02391	1.58240	1.86165	121.00725	140.80500	544.08375	403.60950	
46 Z I	Yap	12.29143	16.33546	13.12378	30.19559	239.01375	930.10586	29.21770	44.67015	
	$ASLOG_d$	0.03187	0.12228	0.14953	0.09231	2.48819	2.56458	3.87450	3.60232	
	$ASLOG_d^{\star}$	0.02513	0.10093	0.10207	0.03094	1.07181	1.07643	1.49052	1.39624	
	$RDFox_c$	0.00597	0.00759	0.01029	0.02191	0.55871	0.61738	1.03897	0.73780	
Q_{21}	FI_c	0.00002	0.00059	0.00060	0.00956	0.46744	0.50259	1.04877	0.48627	
*C 21	$AMEM_{c}$	0.00001	0.00057	0.00060	0.00876	0.47195	0.50253	1.09286	0.50428	
	$ASLOG_c$	0.00002	0.00023	0.00023	0.00191	0.03732	0.04049	0.11656	0.07537	
	$RDFox_c$	0.00470	0.00492	0.00867	0.01870	0.57462	0.78155	1.70478	0.66072	
Q_{22}	FI_c	0.00002	0.00034	0.00323	0.01470	1.16574	1.20741	2.50247	1.52633	
~22	$AMEM_{c}$	0.00003	0.00039	0.00341	0.01606	1.15008	1.20390	2.67054	1.59411	
	$ASLOG_c$	0.00067	0.00070	0.00125	0.00127	0.08287	0.08963	0.24401	0.03383	
	$RDFox_c$	0.00385	0.00540	0.00795	0.01244	0.82856	0.89026	1.32037	1.15546	
Q_{23}	FI_c	0.00006	0.00070	0.00710	0.03077	2.32470	2.43427	5.04603	2.94793	
	$AMEM_c$	0.00009	0.00088	0.00753	0.03117	2.30070	2.44790	5.30436	3.08169	
	$ASLOG_c$	0.00014	0.00232	0.00064	0.00121	0.11890	0.12661	0.28241	0.21225	
	$RDFox_c$	0.00699	0.00677	0.00915	0.02432	1.15619	1.20550	2.24636	1.73744	
Q_{24}	FI_c	0.00019	0.00115	0.01271	0.05209	3.48033	3.67300	7.51618	4.06213	
	$AMEM_c$	0.00017	0.00103	0.01284	0.05465	3.46279	3.70579	7.85370	4.00548	
	$ASLOG_c$	0.00044	0.00020	0.00018	0.00126	0.12787	0.13315	0.30374	0.21819	
		G_{c1}	G_{c2}	G_{c3}	G_{c4}	S_{s1}	S_{s2}	S_{s3}	S_{s4}	
	BTC	0.03466	0.17051	20.59905	158.12764	1.98426	9.98626	88.30648	136.86502	
	$COMP_TC$	0.01899	0.08048	20.70697	30.03981	0.54494	1.79537	8.28847	10.80741	
	DLV	0.56851	6.31600	606.85556	473.17643	37.53294	80.03073	359.94785	401.87129	
	IRIS	1.96919	16.87184	error	error	error	error	error	error	
	XSB	0.89303	2.52032	135.92171	82.13846	39.76907	83.00565	369.67424	430.85889	
	Yap	0.11661	0.23228	0.63504	0.22869	7.91457	23.61215	543.31414	23.82326	
Q_3	$RDFox_n$	0.04506	0.21504	43.77177	170.84027	2.85925	12.29743	127.70164	135.39372	
	$RDFox_{c}$	0.03829	0.18253	43.68946	170.81856	2.83979	12.25151	127.67461	135.36936	
	$ASLOG_d$	0.03351	0.09277	7.50731	4.36236	0.35976	1.56511	2.25546	3.05115	
	$ASLOG_d^{\star}$	0.01116	0.08626	7.46008	4.32180	0.35012	1.52450	2.22049	3.03434	
	$ASLOG_m$	0.01300	0.08111	10.20640	3.20158	0.31613	1.43020	1.56191	2.07024	
	$ASLOG_m^{\star}$	0.00944	0.07903	10.20209	3.17017	0.29783	1.38960	1.52693	2.05343	
	$ASLOG_c$	0.00528	0.05427	7.13642	3.14163	0.27201	1.32862	1.50017	2.02024	
	BTC	0.00004	0.00032	0.03979	0.17233	3.91256	22.67666	219.46325	344.81091	
	$COMP_TC$	0.00001	0.00010	0.01121	0.14951	1.13801	6.78766	64.46893	99.65049	
Q_4	$RDFox_c$	0.00004	0.00012	0.04843	0.22452	2.44854	7.98440	76.17953	121.59931	
	$ASLOG_TC$	0.00002	0.00013	0.01605	0.01090	0.74572	4.66900	6.64818	8.36974	
	$ASLOG_c$	0.00001	0.00005	0.00084	0.00128	0.15678	1.24576	0.76468	0.05352	

Table 2: Overhead of ASLOG included in this paper

		Generated by OpenRuleBench Generator				Stanford Large Network Dataset Collection				
		G_{a1}	G_{a2}	G_{a3}	G_{a4}	S_{l1}	S_{l2}	S_{l3}	S_{l4}	
	ASLOG-AI	0.004(26)	0.008(27)	0.012(27)	0.020(27)	1.164(53)	1.216(54)	2,026(60)	1,927(60)	
Time(s)	ASLOG-SI	0.011(74)	0.022(73)	0.033(73)	0.054(73)	1.015(47)	1.021(46)	1,345(40)	1,289(40)	
1 time(s)	Average	0.000001	0.000001	0.000001	0.000001	0.000002	0.000002	0.000002	0.000003	
	FI	0.017	0.031	0.043	0.079	2.071	2.164	3.291	2.985	
Size (kb)	ASLOG-AI	268(64)	423(58)	576(56)	884(53)	15,722(53)	16,494(53)	25,076(57)	23,477(59)	
	ASLOG-SI	154(36)	307(42)	461(44)	769(47)	13,936(47)	14,598(47)	19,007(43)	16,160(41)	
	Average	0.042	0.036	0.034	0.033	0.032	0.032	0.035	0.037	
	FI	671	840	1,044	1,530	27,814	29,307	48,470	54,422	

Table 3: Test data not included in this paper

Time costs (Seconds) for querying Q_1 – Q_{21}

		Generated by OpenRuleBench Generator			Stanford Large Network Dataset Collection				
		G_{a1}	G_{a2}	G_{a3}	G_{a4}	S_{l1}	S_{l2}	S_{l3}	S_{l4}
	$RDFox_n$	0.02705	0.03374	0.05146	0.07768	1.54245	1.62663	2.48222	1.99229
Q_{21}	$ASLOG_m$	0.03151	0.12194	0.14918	0.09115	2.48370	2.55960	3.86025	3.59312
	$ASLOG_{m}^{\star}$	0.02478	0.10059	0.10172	0.03045	1.04541	1.05282	1.41912	1.34455
		Stanford Large Network Dataset Collection							
		G_{s1}	G_{s2}	G_{s3}	G_{s4}	-			
	DLV	0.24120	0.36213	0.27824	0.29937				
	IRIS	20.63938	20.80443	77.11381	12.36146				
	XSB	3.41463	14.27357	3.09483	4.14362				
	Yap	3.85925	5.79252	4.45129	4.78462				
	$ASLOG_d$	0.04590	0.08680	0.04328	0.05221				
Q_1	$ASLOG_d^{\star}$	0.02876	0.06360	0.03114	0.03502				
	RDFoxn	0.06032	0.06895	0.03463	0.04360				
	RDFoxc	0.03668	0.01894	0.00604	0.00551				
	$ASLOG_m$	0.04590	0.08614	0.04226	0.05096				
	$ASLOG_{m}^{\star}$	0.02810	0.06259	0.02989	0.03374				
	$ASLOG_c$	0.00078	0.00217	0.00067	0.00072				
	DLV	0.39743	0.59617	0.43714	0.55541				
	IRIS	27.98543	30.78394	97.94891	20.07562				
	XSB	3.69223	15.13727	4.06125	4.87380				
	Yap	25.90356	36.26428	27.19815	65.77262				
	$ASLOG_d$	0.06011	0.13834	0.06181	0.07390				
Q_{21}	$ASLOG_d^{\star}$	0.02917	0.06945	0.03032	0.03688				
	RDFoxn	0.06109	0.07585	0.03818	0.04818				
	RDFoxc	0.03449	0.02038	0.00669	0.01008				
	$ASLOG_m$	0.05970	0.13698	0.06111	0.07327				
	$ASLOG_{m}^{\star}$	0.02877	0.06809	0.02962	0.03625				
	$ASLOG_c$	0.00145	0.00357	0.00130	0.00113				

	Overhead of $ASLOG$ and $AMEM$									
		Generated by OpenRuleBench Generator				Stanford Large Network Dataset Collection				
	=	G_{c1}	G_{c2}	G_{c3}	G_{c4}	S_{s1}	S_{s2}	S_{s3}	S_{s4}	
	$ASLOG_AI$	0.005(62)	0.008(29)	0.016(15)	0.029(48)	0.012(34)	0.025(31)	0.028(52)	0.012(30)	
Time(s)	$ASLOG_SI$	0.003(38)	0.019(71)	0.095(85)	0.031(52)	0.023(66)	0.055(69)	0.026(48)	0.027(70)	
	Average	0.000002	0.000001	0.000001	0.000002	0.000001	0.000001	0.000002	0.000001	
	ASLOG_AI	62(52)	379(51)	1520(51)	479(57)	399(51)	924(51)	440(55)	544(56)	
Size~(kb)	$ASLOG_SI$	59(48)	369(49)	1476(49)	369(43)	378(49)	884(49)	357(45)	428(44)	
	Average	0.030	0.030	0.030	0.034	0.030	0.030	0.033	0.034	
		G_{a1}	G_{a2}	G_{a3}	G_{a4}	S_{l1}	S_{l2}	S_{l3}	S_{l4}	
AMEM	Time(s)	0.01703	0.03804	0.04649	0.09743	2.02214	2.12656	3.29796	3.03510	
AMEM	Size(kb)	631	764	935	1372	46,610	52,202	25,095	26,454	