# Data Structures and Algorithms in Java<sup>™</sup>

**Sixth Edition** 

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**Study Guide: Hints to Exercises** 

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## Chapter

## 10

## Maps, Hash Tables, and Skip Lists

## Hints

#### Reinforcement

**R-10.1**) The first insertion is O(1), the second is O(2), ...

**R-10.2**) Use the PositionalList.remove method to delete an entry from the map.

**R-10.3**) Take advantage of the existing findIndex method.

**R-10.4**) Think about which of the schemes use the array supporting the hash table exclusively and which of the schemes use additional storage external to the hash table.

**R-10.5**) There is a lot of symmetry and repetition in this string, so avoid a hash code that would not deal with this.

**R-10.6**) Try to mimic the figure in the book.

**R-10.7**) Try to mimic the figure in the book.

**R-10.8**) The failure occurs because no empty slot is found. For the drawing, try to mimic the figure in the book.

**R-10.9**) Try to mimic the figure in the book.

**R-10.10**) Think of the worst-case time for inserting every entry in the same cell in the hash table.

**R-10.11**) Mimic the way the figure is drawn.

**R-10.12**) Combine the hash values of the two components to make a hash value for the pair.

**R-10.13**) There is a subtle flaw—but can you find it?

**R-10.14**) The load factor can be controlled from within the abstract class, but there must be means for setting the parameter (either through the constructor, or a new method).

**R-10.15**) It is okay to insert a new entry on "top" of the deactivated entry object.

- **R-10.16**) You will need to keep track of the number of probes in order to apply quadratic probing.
- **R-10.17**) Think of where the entry with minimum key is stored.
- **R-10.18**) Since the map will still contain n entries at the end, you can assume that each remove() operation takes the same asymptotic time.
- **R-10.19**) Take advantage of the existing findIndex method.
- **R-10.20**) The crucial methods are get and put.
- **R-10.21**) In the new code, what happens when key equals table.get(mid)?
- **R-10.22**) Assume that a skip list is used to implement the sorted map.
- **R-10.23**) Mimic the style of the figures in the book.
- **R-10.24**) You must link out the removed entry's tower from all the lists it belongs to.
- **R-10.25**) Compare to the implementation of the addAll method given in Section 10.5.1.
- **R-10.26**) Compare to the implementation of the addAll method given in Section 10.5.1.
- **R-10.27**) Recall that most skip-list operations run in  $O(\log k)$  time for a set with size k.
- **R-10.28**) Recall that most hash-table operations run in O(1) expected time.
- **R-10.29**) Recall that most hash-table operations run in O(1) expected time.
- **R-10.30**) Recall that most hash-table operations run in O(1) expected time
- **R-10.31**) Something from this chapter should be helpful!

## Creativity

- C-10.32) Consider a bootstrapping method for finding the primes up to  $\sqrt{2M}$ .
- C-10.33) Your solution should make a single call to findIndex.
- **C-10.34**) You may assume that such a method is supported by the auxiliary UnsortedTableMap
- C-10.35) You must only call the findSlot utility once.
- **C-10.36**) Model your solution after the existing support for other map methods.
- **C-10.37**) You may assume that such a method is supported by the auxiliary UnsortedTableMap

**C-10.38**) The heart of the process can be performed by the findSlot utility.

**C-10.39**) When might the load factor fall below the threshold, and how can you detect this from within AbstractHashMap?

**C-10.40**) Start by defining an appropriate subclass of AbstractMap.MapEntry that includes the new next field that is desired.

**C-10.41**) You need to do some shifting of entries to close up the "gap" just made, but you should only do this for entries that need to move.

**C-10.42**) For part a, note that the symmetry will halve the range of possible values. For part b, note that such automatic collisions will not occur.

**C-10.43**) Perhaps borrow techniques from the Progression hierarchy of Chapter 2, or use Java's iterators.

**C-10.44**) Maintain a secondary PositionalList instance that represents the FIFO order, and store positions within that list with each entry of the hash table.

C-10.45) Each map entry instance should store its current index within the table.

**C-10.46**) Each map entry instance should store its current index within the table.

**C-10.47**) Each map entry instance should store its position within the bucket list.

C-10.48) Try out some examples.

C-10.49) Do a "double" binary search.

C-10.50) Dovetail two binary searches.

C-10.51) Do a lazy iteration through indices of the underlying array list.

**C-10.52**) Manage a primary iteration through all nonempty buckets, and then a secondary iteration through each element of a bucket.

C-10.53) Do a lazy iteration through the nonempty cells of the table.

C-10.54) Think about first sorting the pairs by cost.

**C-10.55**) In the insertion algorithm, first repeatedly flip the coin to determine the level where you should start inserting the new entry.

C-10.56) Consider augmenting each node v in a higher level with the number of missing entries in the gap from v to the next node over.

C-10.57) Consider augmenting each node v in a higher level with the number of missing entries in the gap from v to the next node over.

**C-10.58**) Think first about how you can determine the number of 1's in any row in  $O(\log n)$  time.

C-10.59) Consider a two-pass solution, with use of an auxiliary structure.

**C-10.60**) Think of describing your algorithms in terms of boolean operations on the bit vectors.

**C-10.61**) Think of how you could transform *D* into *L*.

**C-10.62**) Consider the way subMap was implemented for Sorted TableMap.

**C-10.63**) You need some way of grouping together entries with the same key.

**C-10.64**) You need some way of grouping together elements with the same key.

## **Projects**

**P-10.65**) The biggest challenge is detecting the case of an infinite loop.

**P-10.66)** When searching for an existing key, make sure to consider both of the possible buckets.

**P-10.67**) Maintain a secondary PositionalList instance that represents the FIFO order, and store positions within that list with each entry of the hash table.

**P-10.68)** We've already implemented them for you; all that's left is the experiments.

**P-10.69**) In a Unix/Linux system, a good place to start is /usr/dict.

**P-10.70**) It is okay to generate these phone numbers more-or-less at random.

**P-10.71**) Sentinels can be used in place of the theoretical  $-\infty$  and  $+\infty$ .

**P-10.72**) Try to make your screen images mimic the skip list figures in the book.

**P-10.73**) You need to find some way to let the intermediate nodes in the skip list keep track of the number of elements that have been skipped over.

**P-10.74)** For each word t that results from a minor change to s, you can test if t is in W in O(1) time.