CMPT 379 Compilers

Anoop Sarkar http://www.cs.sfu.ca/~anoop

Parsing - Roadmap

- Parser:
 - decision procedure: builds a parse tree
- Top-down vs. bottom-up
- LL(1) Deterministic Parsing
 - recursive-descent
 - table-driven
- LR(k) Deterministic Parsing
 - LR(0), SLR(1), LR(1), LALR(1)
- Parsing arbitrary CFGs Polynomial time parsing

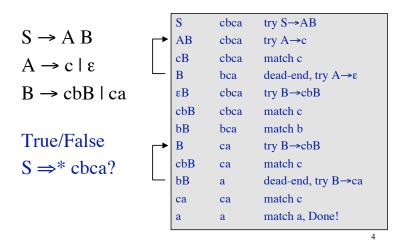
Top-Down vs. Bottom Up

Grammar: $S \rightarrow A B$ Input String: ccbca $A \rightarrow c \mid \epsilon$ $B \rightarrow cbB \mid ca$

Top-Down/leftmost		Bottom-Up/rightmost		
$S \Rightarrow AB$	S→AB	ccbca ← Acbca	A→c	
⇒cB	A→c	← AcbB	B→ca	
⇒ ccbB	B→cbB	←AB	B→cbB	
⇒ccbca	B→ca	← S	S→AB	

3

Top-Down: Backtracking

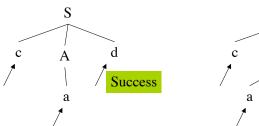


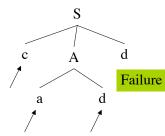
Backtracking

 $S \rightarrow cAd \mid c$ $A \rightarrow a \mid ad$

Input: cad

 $S \rightarrow cAd \mid c$ $A \rightarrow ad \mid a$





For some grammars, rule ordering is crucial for backtracking parsers, e.g $S \rightarrow aSa$, $S \rightarrow aa$

Predictive Top-Down Parser

- Knows which production to choose based on single lookahead symbol
- Need LL(1) grammars

First L: reads input Left to right
Second L: produce Leftmost derivation
1: one symbol of lookahead

- Can't have left-recursion
- Must be left-factored (no left-factors)
- Not all grammars can be made LL(1)

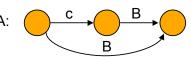
Transition Diagram

 $S \rightarrow cAa$

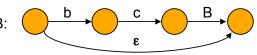
S:



 $A \rightarrow cB \mid B$



 $B \rightarrow bcB \mid \epsilon \quad B$:



Leftmost derivation for id + id * id

$$E \rightarrow E + E$$
 $E \Rightarrow E + E$ $E \rightarrow E * E$ $\Rightarrow id + E$ $E \rightarrow (E)$ $\Rightarrow id + E * E$ $E \rightarrow -E$ $\Rightarrow id + id * E$ $E \rightarrow id$ $\Rightarrow id + id * id$

$$E \Rightarrow^*_{lm} id + E \setminus^* E$$

6

5

Predictive Parsing Table

1	Productions		
1	T → F T'		
2	Τ' → ε		
3	T' → * F T'		
4	F → id		
5	$\mathbf{F} \rightarrow (\mathbf{T})$		

	*	()	id	\$
T		T → F T'		T → F T '	
T'	T' → * F T'		Τ' → ε		Τ' → ε
F		$\mathbf{F} \rightarrow (\mathbf{T})$		F → id	

 Stack
 Input
 Output

 \$T'
 *id\$

 \$T'F*
 *id\$

 \$T'F
 id\$

 \$T'id
 id\$

 \$T'
 \$

 \$
 \$

Trace "(id)*id"

T → FT'

T' → *FT'

T → FT'

T' → ε

T' → ε

9

Trace "(id)*id"

	*	()	id	\$
T		T → FT'		T → FT'	
T'	T' → *FT'		T' → ε		Τ' → ε
F		F → (T)		F → id	

Stack	Input	Output
\$T	(id)*id\$	
\$T'F	(id)*id\$	T → F T'
\$T')T((id)*id\$	$\mathbf{F} \rightarrow (\mathbf{T})$
\$T')T	id)*id\$	
\$T')T'F	id)*id\$	T → F T'
\$T')T'id	id)*id\$	F → id
\$T')T')*id\$	
\$T'))*id\$	Τ' → ε

Table-Driven Parsing

```
stack.push($); stack.push(S);
a = input.read();
forever do begin

X = stack.peek();
if X = a and a = $ then return SUCCESS;
elsif X = a and a != $ then
pop X; a = input.read();
elsif X != a and X ∈ N and M[X,a] then
pop X; push right-hand side of M[X,a];
else ERROR!
end
```

Predictive Parsing table

- Given a grammar produce the predictive parsing table
- We need to to know for all rules $A \rightarrow \alpha \mid \beta$ the lookahead symbol
- Based on the lookahead symbol the table can be used to pick which rule to push onto the stack
- This can be done using two sets: FIRST and FOLLOW

13

FIRST and FOLLOW

```
a \in \text{FIRST}(\alpha) \text{ if } \alpha \Rightarrow^* a\beta

if \alpha \Rightarrow^* \epsilon \text{ then } \epsilon \in \text{FIRST}(\alpha)

a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A a\beta

a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A \gamma a\beta

and \gamma \Rightarrow^* \epsilon
```

Conditions for LL(1)

- Necessary conditions:
 - no ambiguity
 - no left recursion
 - Left factored grammar
- A grammar G is LL(1) iff whenever $A \rightarrow \alpha \mid \beta$
 - 1. First(α) \cap First(β) = \emptyset
 - 2. $\alpha \Rightarrow^* \epsilon$ implies !($\beta \Rightarrow^* \epsilon$)
 - 3. $\alpha \Rightarrow * \epsilon \text{ implies First}(\beta) \cap \text{Follow}(A) = \emptyset$

15

ComputeFirst(α : string of symbols)

```
// assume \alpha = X_1 \ X_2 \ X_3 \dots X_n

if X_1 \in T then First[\alpha] := \{X_1\}

else begin

i:=1; First[\alpha] := ComputeFirst(X_1) \setminus \{\epsilon\};

while X_i \Rightarrow^* \epsilon do begin

if i < n then

First[\alpha] := First[\alpha] \cup ComputeFirst(X_{i+1}) \setminus \{\epsilon\};

else

First[\alpha] := First[\alpha] \cup \{\epsilon\};

i:=i+1;

end

end
```

ComputeFirst(α : string of symbols)

ComputeFirst; modified

17

18

```
foreach X \in T do First[X] := X;

foreach p \in P : X \rightarrow \epsilon do First[X] := \{\epsilon\};

repeat foreach X \in N, p : X \rightarrow Y_1 Y_2 Y_3 ... Y_n do

begin i:=1;

while Y_i \Rightarrow^* \epsilon and i <= n do begin

First[X] := First[X] \cup First[Y_i] \setminus \{\epsilon\};

i := i+1;

end

if i = n+1 then First[X] := First[X] \cup \{\epsilon\};

else First[X] := First[X] \cup First[Y_i];

until no change in First[X] for any X;
```

ComputeFirst; modified

```
foreach X \in T do First[X] := X;

foreach p \in P : X \to \epsilon do First[X] := \{\epsilon\};

repeat foreach X \in N, p : X \to Y_1 Y_2 Y_3 ... Y_n do

begin i:=1;

while Y_i \Rightarrow^*

First[X] := Computes a fixed point for FIRST[X]

i := i+1; for all non-terminals X in the grammar.

end But this algorithm is very inefficient.

if i = n+1 then First[X] := First[X] \cup \{\epsilon\};

else First[X] := First[X] \cup First[Y_i];

until no change in First[X] for any X;
```

ComputeFollow

```
\label{eq:follow} \begin{split} & \text{Follow}(S) \coloneqq \{\$\}; \\ & \textbf{repeat} \\ & \textbf{foreach} \ p \in \textbf{P} \ \textbf{do} \\ & \textbf{case} \ p = A \rightarrow \alpha B \beta \ \textbf{begin} \\ & \text{Follow}[B] \coloneqq \text{Follow}[B] \ \cup \ \text{ComputeFirst}(\beta) \backslash \{\pmb{\epsilon}\}; \\ & \textbf{if} \ \epsilon \in \text{First}(\beta) \ \textbf{then} \\ & \text{Follow}[B] \coloneqq \text{Follow}[B] \ \cup \ \text{Follow}[A]; \\ & \textbf{end} \\ & \textbf{case} \ p = A \rightarrow \alpha B \\ & \text{Follow}[B] \coloneqq \text{Follow}[B] \ \cup \ \text{Follow}[A]; \\ & \textbf{until} \ \text{no} \ \text{change} \ \text{in} \ \text{any} \ \text{Follow}[N] \end{split}
```

Example First/Follow

$$S \rightarrow AB$$

 $A \rightarrow c \mid \epsilon$ Not an LL(1) grammar
 $B \rightarrow cbB \mid ca$
First(A) = {c, \epsilon} Follow(A) = {c}
First(B) = {c} Follow(A) \cap First(cbB) = First(c) = {c}
First(ca) = {c} Follow(B) = {\$}
First(S) = {c} Follow(S) = {\$}

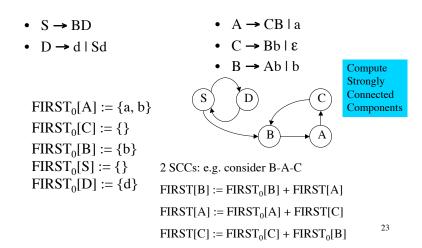
ComputeFirst on Left-recursive Grammars

- ComputeFirst as defined earlier loops on leftrecursive grammars
- Here is an alternative algorithm for ComputeFirst
 - 1. Compute non-recursive cases of FIRST
 - 2. Create a graph of recursive cases where FIRST of a non-terminal depends on another non-terminal
 - 3. Compute Strongly Connected Components (SCC)
 - 4. Compute FIRST starting from root of SCC to avoid cycles

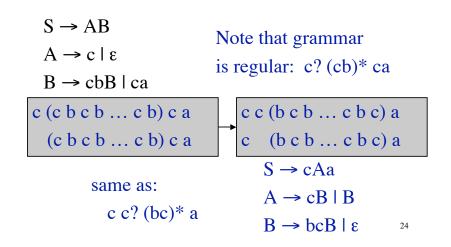
22

 Unlike top-down LL parsing, bottom-up LR parsing allows left-recursive grammars, so this algorithm is useful for LR parsing

ComputeFirst on Left-recursive Grammars



Converting to LL(1)



Verifying LL(1) using F/F sets

$$S \rightarrow cAa$$

 $A \rightarrow cB \mid B$
 $B \rightarrow bcB \mid \epsilon$
First(A) = {b, c, \varepsilon} Follow(A) = {a}
First(B) = {b, \varepsilon} Follow(B) = {a}
First(S) = {c} Follow(S) = {\$}

Revisit conditions for LL(1)

- A grammar G is LL(1) iff whenever $A \rightarrow \alpha \mid \beta$
 - 1. $First(\alpha) \cap First(\beta) = \emptyset$
 - 2. $\alpha \Rightarrow^* \epsilon \text{ implies } !(\beta \Rightarrow^* \epsilon)$
 - 3. $\alpha \Rightarrow * \epsilon \text{ implies First}(\beta) \cap \text{Follow}(A) = \emptyset$
- No more than one entry per table field

25

Building the Parse Table

- Compute First and Follow sets
- For each production $A \rightarrow \alpha$
 - foreach a ∈ First(α) add A \rightarrow α to M[A,a]
 - If ε ∈ First(α) add A → α to M[A,b] for each b in Follow(A)
 - If ε ∈ First(α) add A → α to M[A,\$] if \$ ∈ Follow(α)
 - All undefined entries are errors

Error Handling

- Reporting & Recovery
 - Report as soon as possible
 - Suitable error messages
 - Resume after error
 - Avoid cascading errors
- Phrase-level vs. Panic-mode recovery

Panic-Mode Recovery

- Skip tokens until synchronizing set is seen
 - Follow(A)
 - garbage or missing things after
 - Higher-level start symbols
 - First(A)
 - · garbage before
 - Epsilon
 - if nullable
 - Pop/Insert terminal
 - · "auto-insert"
- Add "synch" actions to table

29

Summary so far

- LL(1) grammars, necessary conditions
 - No left recursion
 - Left-factored
- Not all languages can be generated by LL(1) grammar
- LL(1) Parsing: O(n) time complexity
 - recursive-descent and table-driven predictive parsing
- LL(1) grammars can be parsed by simple predictive recursive-descent parser
 - Alternative: table-driven top-down parser