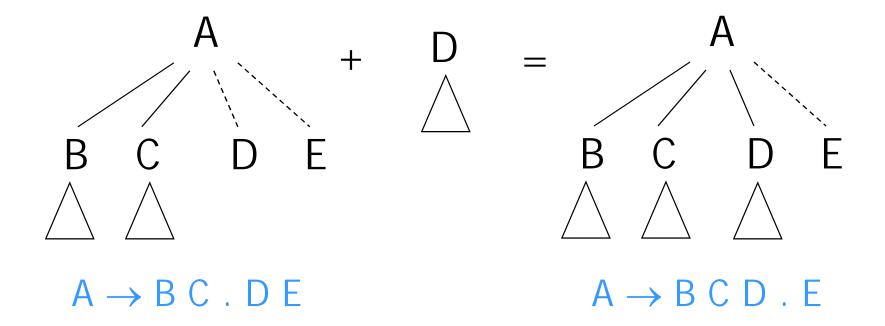
Earley's Algorithm (1970)

Nice combo of our parsing ideas so far:

- no restrictions on the form of the grammar:
 - $-A \rightarrow B C spoon D x$
- incremental parsing (left to right, like humans)
- left context constrains parsing of subsequent words
 - so waste less time building impossible things
 - makes it faster than O(n³) for many grammars

Overview of Earley's Algorithm

- Finds constituents and <u>partial</u> constituents in input
 - A \rightarrow B C . D E is partial: only the first half of the A



Overview of Earley's Algorithm

- Proceeds <u>incrementally</u>, left-to-right
 - Before it reads word 5, it has already built all hypotheses that are consistent with first 4 words
 - Reads word 5 & attaches it to immediately preceding hypotheses. Might yield new constituents that are then attached to hypotheses immediately preceding them ...
 - E.g., attaching D to A \rightarrow B C . D E gives A \rightarrow B C D . E
 - Attaching E to that gives $A \rightarrow B C D E$.
 - Now we have a complete A that we can attach to hypotheses immediately preceding the A, etc.

Our Usual Example Grammar

```
ROOT \rightarrow S
          \rightarrow NP VP
                               NP \rightarrow Papa
         \rightarrow Det N
NP
                               N \rightarrow caviar
NP \rightarrow NP PP
                               N \rightarrow spoon
VP
         \rightarrow VP PP
                               V \rightarrow ate
                               P \rightarrow with
VP
         \rightarrow V NP
PP
         \rightarrow P NP
                               Det \rightarrow the
                               Det \rightarrow a
```

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

```
0 \text{ ROOT} \rightarrow .S 0
```

• $0 \text{ S} \rightarrow . \text{ NP VP } 0$

"goal stack"

```
• 0 \text{ NP} \rightarrow . \text{ Papa } 0
```

•
$$0 \text{ NP} \rightarrow \text{Papa}$$
 . 1

$$-$$
 0 S \rightarrow NP . VP 1

- 1 VP
$$\rightarrow$$
 . VP PP 1

- 1 VP
$$\rightarrow$$
 . VP PP 1

• 1 VP
$$\rightarrow$$
 . VP PP 1
1 VP \rightarrow . VP PP 1

oops, stack overflowed

- OK, let's pretend that didn't happen.
- Let's suppose we didn't see VP \rightarrow VP PP, and used VP \rightarrow V NP instead.

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

- $0 \text{ ROOT} \rightarrow .S 0$
 - $0 \text{ S} \rightarrow . \text{ NP VP } 0$
 - $0 \text{ NP} \rightarrow . \text{ Papa } 0$
 - $0 \text{ NP} \rightarrow \text{Papa} . 1$
 - 0 S \rightarrow NP . VP 1
 - $-1 \text{ VP} \rightarrow . \text{ V NP 1}$
 - 1 V \rightarrow . ate 1
 - 1 V \rightarrow ate . 2
 - \bullet 1 VP \rightarrow V . NP 2
 - $\stackrel{\bullet}{}$ 2 NP \rightarrow 2
 - $\stackrel{\bullet}{}$ 2 NP \rightarrow 7
 - 1 VP \rightarrow V NP . 7

- after dot = nonterminal, so recursively look for it ("predict")
- after dot = nonterminal, so recursively look for it ("predict")
- after dot = terminal, so look for it in the input ("scan")
- after dot = nothing, so parent's subgoal is completed ("attach")
- predict (next subgoal)
- do some more parsing and eventually ...
- we complete the parent's NP subgoal, so attach
- attach again
- 600.\$465 NPro VPNL7 J. Eisner attach again

^oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

S() calls NP() and VP(), which recurse

First Try: Recursive Descent

```
NP \rightarrow Papa
ROOT \rightarrow S
               VP \rightarrow V NP
                                                                          V \rightarrow ate
                                                                          P \rightarrow with
        \rightarrow NP VP VP PP
                                                  N \rightarrow caviar
                           PP \rightarrow P NP
                                                                          Det \rightarrow the
NP \rightarrow Det N
                                                  N \rightarrow spoon
NP \rightarrow NP PP
                                                                           Det \rightarrow a
```

implement by function calls:

- $0 \text{ ROOT} \rightarrow . S 0$
 - $0 S \rightarrow . NP VP 0$
 - $0 \text{ NP} \rightarrow . \text{ Papa } 0$
 - $0 \text{ NP} \rightarrow \text{Papa}$. 1
 - $0 S \rightarrow NP . VP 1$
 - (VP → . V NP 1) must backtrack to try predicting a different VP rule here instead
 - 1 $V \rightarrow$. ate 1
 - 1 $V \rightarrow ate$. 2
 - 1 VP \rightarrow V . NP 2
 - $\stackrel{\bullet}{}$ 2 NP \rightarrow 2
 - 2 NP $\rightarrow \dots$ 7
- But how about the other parse?
- 1 VP \rightarrow V NP . 7

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

- $0 \text{ ROOT} \rightarrow .S 0$
 - $0 \text{ S} \rightarrow . \text{ NP VP } 0$
 - $0 \text{ NP} \rightarrow . \text{ Papa } 0$
 - $0 \text{ NP} \rightarrow \text{Papa} . 1$
 - $0 S \rightarrow NP . VP 1$
 - $1 \text{VP} \rightarrow . \text{VP PP}$
 - (VP → . V NP) we'd better backtrack here too!
 - 1 V \rightarrow . ate 1

(why?)

- 1 V \rightarrow ate . 2
- \bullet 1 VP \rightarrow V . NP 2
 - $-2 \text{NP} \rightarrow \dots 2$
- do some more parsing and eventually ...
- $\stackrel{\bullet}{}$ 2 NP \rightarrow 4
 - ... the correct NP is from 2 to 4 this time (but might we find the one from 2 to 7 instead?)

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

```
0 \text{ ROOT} \rightarrow . S 0
   • 0 \text{ S} \rightarrow . \text{ NP VP } 0
            • 0 \text{ NP} \rightarrow . \text{ Papa } 0
            • 0 \text{ NP} \rightarrow \text{Papa} . 1
      0 \text{ S} \rightarrow \text{NP} \cdot \text{VP} 1
             \bullet (VP \rightarrow . VP PP)
                      \blacksquare VP \rightarrow . VP PP
                                • 1 VP \rightarrow . VP PP 1
                                          1 \text{ VP} \rightarrow . \text{ VP PP } 1
                                                 1 \text{ VP} \rightarrow \text{. VP PP } 1
                                                        oops, stack overflowed
                                                        no fix after all
```

600,465 - Intro to NLP - J. Eisner — must transform grammar to eliminate left-recursive rules

Use a Parse Table

- Earley's algorithm resembles recursive descent, but solves the left-recursion problem. No recursive function calls.
- Use a parse table as we did in CKY, so we can look up anything we've discovered so far.
 "Dynamic programming."
- Entries in column 5 look like $(3, S \rightarrow NP . VP)$

(but we'll omit the \rightarrow etc. to save space)

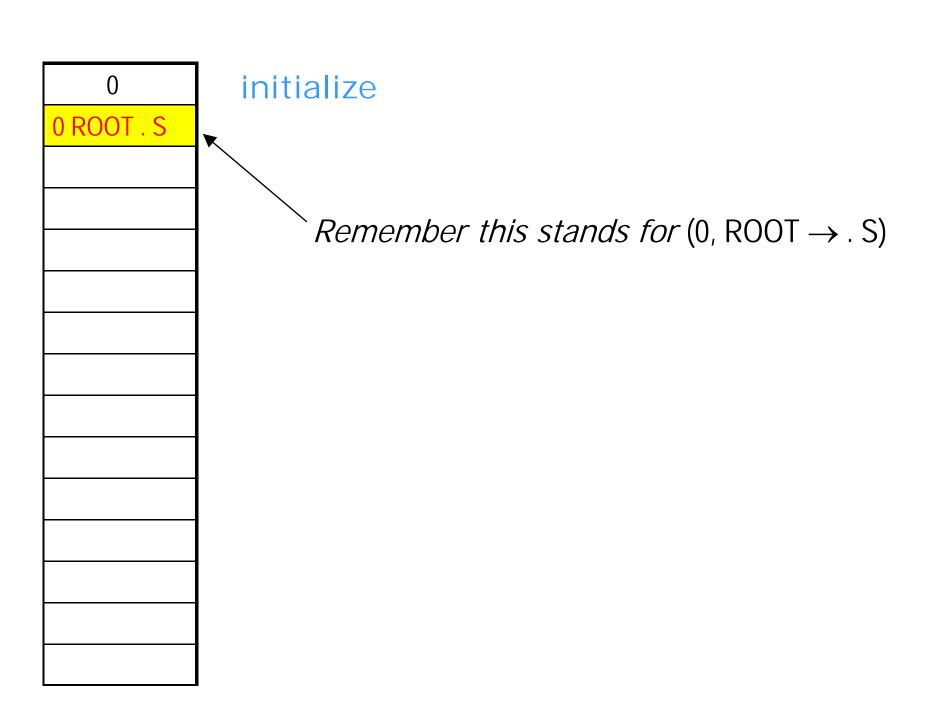
- Built while processing word 5
- Means that the input substring from 3 to 5 matches the initial NP portion of a S → NP VP rule
- Dot shows how much we've matched as of column 5
- Perfectly fine to have entries like $(3, S \rightarrow is it . true that S)$

Use a Parse Table

- Entries in column 5 look like $(3, S \rightarrow NP . VP)$
- What does it mean if we have this entry?
 - Unknown right context: Doesn't mean we'll necessarily be able to find a VP starting at column 5 to complete the S.
 - Known left context: Does mean that some dotted rule back in column 3 is looking for an S that starts at 3.
 - So if we actually do find a VP starting at column 5, allowing us to complete the S, then we'll be able to attach the S to something.
 - And when that something is complete, it too will have a customer to its left ... just as in recursive descent!
 - In short, a top-down (i.e., goal-directed) parser: it chooses to start building a constituent not because of the input but because that's what the left context needs. In the spoon, won't build spoon as a verb because there's no way to use a verb there.
 - So any hypothesis in column 5 could get used in the correct parse, if words 1-5 are continued in just the right way by words 6-n.

Operation of the Algorithm

- Process all hypotheses one at a time in order.
 (Current hypothesis is shown in blue.)
- This may add new hypotheses to the end of the to-do list, or try to add old hypotheses again.
- Process a hypothesis according to what follows the dot – just as in recursive descent:
 - If a word, scan input and see if it matches
 - If a nonterminal, predict ways to match it
 (we'll predict blindly, but could reduce # of predictions by
 looking ahead k symbols in the input and only making
 predictions that are compatible with this limited right context)
 - If nothing, then we have a complete constituent, so attach it to all its customers



0 ROOT . S 0S.NPVP

predict the kind of S we are looking for

Remember this stands for $(0, S \rightarrow . NP VP)$

0 ROOT . S 0S.NPVP 0 NP . Det N 0 NP . NP PP 0 NP . Papa

predict the kind of NP we are looking for (actually we'll look for 3 kinds: any of the 3 will do)

0 ROOT . S 0S.NPVP 0 NP . Det N 0 NP . NP PP 0 NP . Papa 0 Det . the 0 Det . a

predict the kind of Det we are looking for (2 kinds)

0 ROOT . S 0S.NPVP 0 NP . Det N 0 NP . NP PP 0 NP . Papa 0 Det . the 0 Det . a

predict the kind of NP we're looking for

but we were already looking for these so don't add duplicate goals! Note that this happened when we were processing a left-recursive rule.

0 Pa	pa 1		
0 ROOT . S	0 NP Papa.		
0 S . NP VP			
0 NP . Det N			
0 NP . NP PP			
0 NP . Papa	scan: the	e desired wo	ord is in the input
0 Det . the			•
0 Det . a			

0 Pa	pa 1	
0 ROOT . S	0 NP Papa .	
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the	scan: f	ailure
0 Det . a		

0 Pa	pa 1	
0 ROOT . S	0 NP Papa .	
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a	scan: f	ailure

0 Papa 1		
0 ROOT . S	0 NP Papa.	
0S.NPVP	0SNP.VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

attach the newly created NP (which starts at 0) to its customers (incomplete constituents that *end* at 0 and have NP after the dot)

0 Pa	pa 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	OSNP.VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	
0 Det . a	

0 Papa 1		
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0SNP.VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a		

0 Papa 1		
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0SNP.VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	

0 Papa 1		
0 NP Papa .		
0 S NP . VP		
0 NP NP . PP		
1 VP . V NP		
1 VP . VP PP		
1 PP . P NP		
1 V . ate		

0 Papa 1	
0 ROOT . S	0 NP Papa .
0 S . NP VP	0 S NP . VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	1 PP . P NP
0 Det . a	1 V . ate
	1 P . with

0 Pa	pa 1 ate	2	
0 ROOT . S	0 NP Papa .	1 V ate.	
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate	scan: su	ccess
	1 P . with		

0 Pa	pa 1 ate	2	
0 ROOT . S	0 NP Papa .	1 V ate.	
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate		
	1 P . with	scan: fai	lure

0 Papa 1 ate 2		
0 ROOT . S	0 NP Papa .	1 V ate.
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 P . with	

attach

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate.
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 P . with	

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate.
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

predict (these next few steps
should look familiar)

0 Papa 1 ate 2				
0 ROOT . S	0 NP Papa .	1 V ate.		
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate.
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

scan (this time we fail since Papa is not the next word)

0 Pa	pa 1 ate	e 2 the	3	
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the	scan: su	ccess
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Pa	pa 1 ate	e 2 the	3
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Pa	pa 1 ate	e 2 the	3
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Pa	pa 1 ate	e 2 the	3
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Pa	pa 1 ate	e 2 the	: 3 ca\	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Pa	pa 1 ate	e 2 the	e 3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Pa	pa 1 ate	e 2 the	3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar.
0S.NPVP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach

0 Pa	pa 1 ate	2 the	a 3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach (again!)

0 Pa	pa 1 ate	e 2 the	a 3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	OSNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		OSNPVP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach (again!)

0 Pa	pa 1 ate	e 2 the	e 3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			

0 Pa	pa 1 ate	e 2 the	a 3 cav	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		OSNPVP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.

attach (again!)

0 Pa	0 Papa 1 ate 2 the 3 caviar 4					
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		
	1 P . with			0 ROOT S.		

0 Pa	pa 1 ate	e 2 the	: 3 ca\	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

0 Pa	pa 1 ate	e 2 the	3 ca\	viar 4
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P. with

0 Pa	pa 1 ate	e 2 the	e 3 cav	∕iar <mark>4</mark> wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P. with	

0 Pa	pa 1 ate	e 2 the	: 3 ca\	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	pa 1 ate	e 2 the	: 3 ca\	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0SNPVP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	pa 1 ate	e 2 the	3 cav	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	pa 1 ate	e 2 the	3 ca\	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	pa 1 ate	e 2 the	3 cav	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	pa 1 ate	e 2 the	: 3 ca\	viar 4 wit	h 5
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P. with	

ate	2 the	a 3 cav	viar 4 wit	h 5 a	a 6
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a.
C	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	
эΡ	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
ъЬ	2 NP . Papa		0 S NP VP.	5 NP . Papa	
)	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P . with		

ate	2 the	a 3 cav	viar 4 wit	h 5 a	a 6
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a.
)	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N
эР	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
ъЬ	2 NP . Papa		0 S NP VP.	5 NP . Papa	
)	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P. with		

ate	2 the	e 3 cav	viar 4 wit	h 5 a	a 6
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .
)	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N
эР	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
ъЬ	2 NP . Papa		0SNPVP.	5 NP . Papa	
)	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P. with		

ate	2 the	a 3 cav	viar 4 wit	h 5 a	a 6
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .
)	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N
эΡ	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
эÞ	2 NP . Papa		0SNPVP.	5 NP . Papa	
)	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P . with		

ate	ate 2 the 3 caviar 4 with 5 a 6 spoon 7					oon 7
	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
C	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N	
эР	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
ъЬ	2 NP . Papa		0 S NP VP.	5 NP . Papa		
)	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P . with			

ate 2 the 3 caviar 4 with 5 a 6 sp					a 6 spo	oon 7
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
)	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N	5 NP Det N.
эЬ	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
ъЬ	2 NP . Papa		0 S NP VP.	5 NP . Papa		
)	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P . with			

ate	2 the	e 3 cav	viar 4 wit	h 5	a 6 spo	oon 7
•	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
)	1 VP V . NP	2 NP Det . N	2 NP Det N.	4 PP P . NP	5 NP Det . N	5 NP Det N.
эЬ	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	4 PP P NP.
)	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	5 NP NP . PP
ъЬ	2 NP . Papa		0 S NP VP.	5 NP . Papa		
)	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P . with			

0 Pa	pa 1 ate	2 the	3 cav	riar 4 with	as	spoon 7
0 ROOT . S	0 NP Papa.	1 V ate.	2 Det the .	3 N caviar .]	6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP.
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		
	1 P . with			0 ROOT S.		
				4 P . with		

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7							
0 ROOT . S	0 NP Papa.	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP		
	1 P . with			0 ROOT S.				
				4 P . with				

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7							
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .] 	6 N spoon.		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP.		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP		
	1 P . with			0 ROOT S.		1 VP V NP.		
				4 P . with		2 NP NP . PP		

0 Pa	pa 1 ate	2 the	3 cav	riar 4 with	as	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP
						OSNPVP.
						1 VP VP . PP

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP	
	1 P . with			0 ROOT S.		1 VP V NP.	
				4 P . with		2 NP NP . PP	
						0SNPVP.	
						1 VP VP . PP	
						7 P . with	

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7							
0 ROOT . S	0 NP Papa.	1 V ate.	2 Det the .	3 N caviar .]	6 N spoon.		
0 S . NP VP	OSNP.VP	1 VP V . NP 2 NP Det . N 2 NP Det N .			5 NP Det N.			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP		
	1 P . with			0 ROOT S.		1 VP V NP.		
				4 P . with		2 NP NP . PP		
						0SNPVP.		
						1 VP VP . PP		
						7 P . with		

0 Pa	pa 1 ate	2 the	3 cav	iar 4 with	as	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with

0 Pa	pa 1 ate	2 the	3 cav	iar 4 with	as	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .]	6 N spoo
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP De
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P
	1 P . with			0 ROOT S.		1 VP V N
				4 P . with		2 NP NP
						0 S NP V
						1 VP VP
						7 P . with
						0 ROOT

spoon . IP Det N. PPPNP. IP NP . PP IP NP PP . P VP PP . P. P.NP PVNP. IP NP . PP NP VP. P VP . PP . with 00T S .

0 Pa	pa 1 ate	2 the	3 cav	iar 4 with	as	poon
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N s
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP
	1 P . with			0 ROOT S.		1 VP
				4 P . with		2 NP
						0 S N
						1 VP
						7 P .
						0 RO
					- '	

•	6 N spoon.
	5 NP Det N.
	4 PP P NP .
	5 NP NP . PP
	2 NP NP PP.
	1 VP VP PP.
	7 PP . P NP
	1 VP V NP .
	2 NP NP . PP
	0SNPVP.
	1 VP VP . PP
	7 P . with
	0 ROOT S.

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0S.NPVP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PF
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PF
						0 S NP VP.
						1 VP VP . PP
						7 P . with
						0 ROOT S .
						_

NP NP . PP

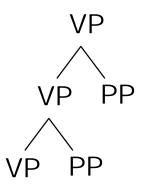
0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
]	7 P . with
						0 ROOT S .

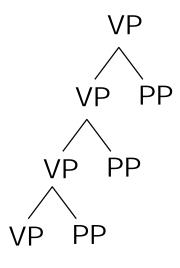
•

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .	• • •	6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	_	7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
					•	7 P . with
						0 ROOT S.
					'	

VP



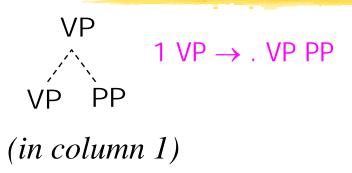


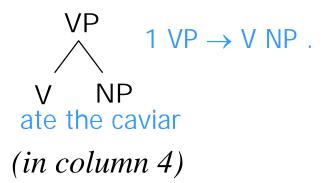


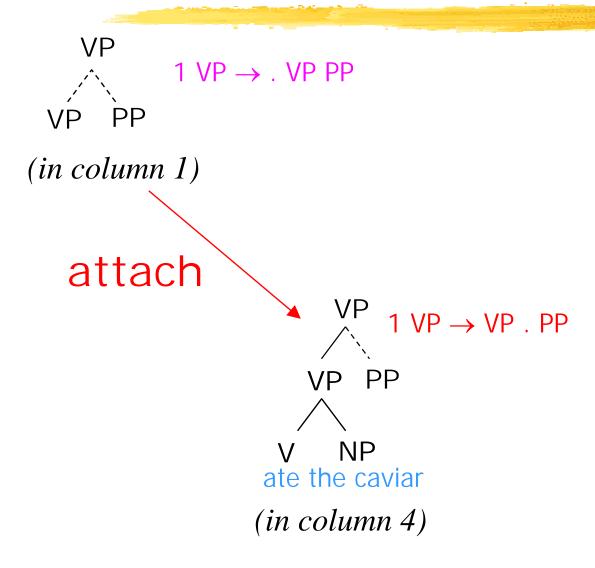
makes new hypotheses ad infinitum before we've seen the PPs at all

hypotheses try to predict in advance how many PP's will arrive in input

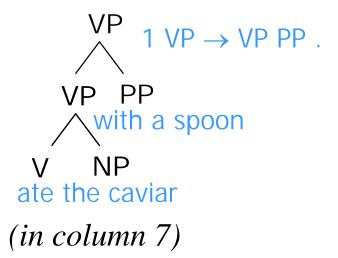
```
VP
\uparrow
VP \rightarrow . VP PP
VP PP
(in \ column \ 1)
```



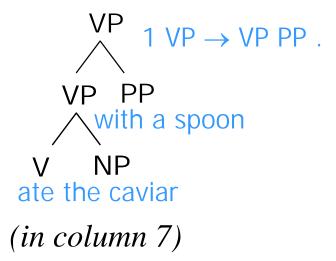


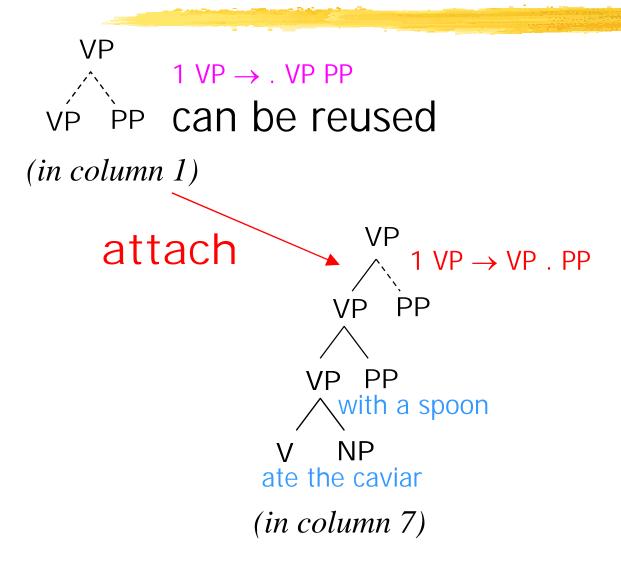


```
VP
\uparrow
VP \rightarrow . VP PP
VP PP
(in \ column \ 1)
```



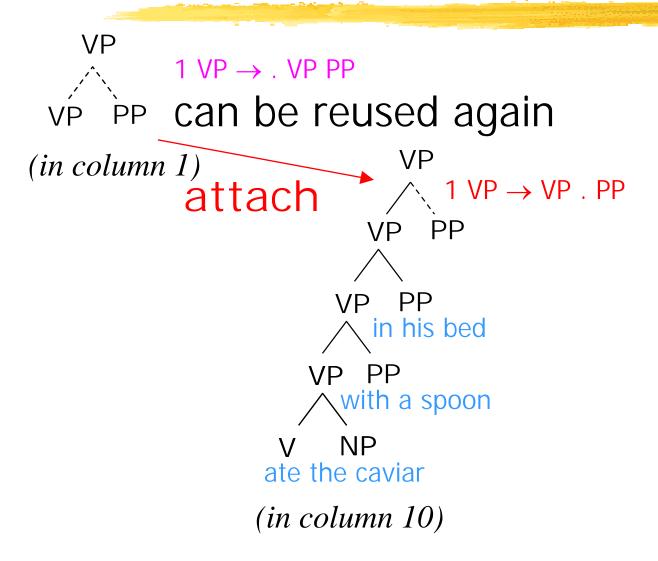
```
VP 1 \text{ VP} \rightarrow . \text{ VP PP}
VP PP can be reused (in column 1)
```





```
VP 1 \text{ VP} \rightarrow . \text{ VP PP}
VP PP can be reused (in column 1)
```

```
VP 1 VP \rightarrow . VP PP \stackrel{\frown}{\text{VP PP}} can be reused again (in column 1)
```



0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
		_				0 S NP VP.
completed a VP in col 4						1 VP VP . PP
col 1 lets us use it in a VP PP structure						7 P . with
						0 ROOT S.

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
_						0 S NP VP.
$\overline{}$ completed that VP = VP PP in col 7						1 VP VP . PP
col 1 would let us use <i>it</i> in a VP PP structure						7 P . with
can reuse col 1 as often as we need						0 ROOT S.

What's the Complexity?