# CMPT-413: Computational Linguistics

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### **Spelling Correction**

- A look at how to correct spelling errors, but the approaches we will consider have connections with other topics of interest in this course:
  - finite-state transducers
  - probabilistic models of language (the noisy channel model)
  - dynamic programming algorithms for parsing sentence structure
  - phylogenetic trees in linguistics and in bioinformatics (tracing historical relationships between strings based on edit distance)

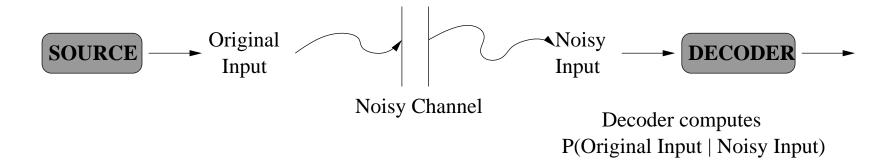
### **Spelling Correction**

- Types of spelling correction techniques
  - non-word error detection, e.g. hte for the
  - isolated word error detection
  - context dependent error detection (real word errors). *All I want is piece . . . a little piece of Poland, a little piece of France, . . .*

## **Spelling Correction**

- Types of single-error misspellings
  - insertion/addition: acress → cress
  - deletion: acress → actress
  - substitution: acress → access
  - transposition/reversal: acress → caress

## Noisy Channel Model: Bayesian Inference



### Noisy Channel Model for Spelling Correction:

(Kernighan, Church and Gale, 1990)

t is the typo (misspelled word) and c is the correct word

$$P(c \mid t) = P(t \mid c) \times P(c)$$

• Find the best candidate for the correct word,  $\hat{c}$ :

$$\widehat{c} = \underset{c \in \mathcal{C}}{\operatorname{arg max}} P(t \mid c) \times P(c)$$

$$P(c) = \frac{f(c)}{N}$$

$$P(t \mid c) = ??$$

### Noisy Channel Model for Spelling Correction:

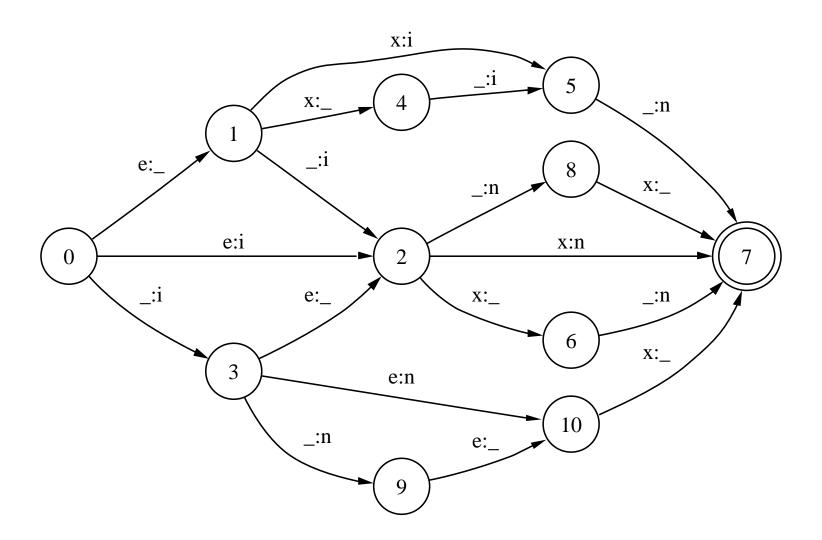
(Kernighan, Church and Gale, 1990): single error, condition on previous letter

$$P(t \mid c) = \begin{cases} \frac{del[c_{p-1}, c_p]}{chars[c_{p-1}, c_p]} & (xy)_c \text{ typed as } (x)_t \\ \frac{ins[c_{p-1}, t_p]}{chars[c_{p-1}]} & (x)_c \text{ typed as } (xy)_t \\ \frac{sub[t_p, c_p]}{chars[c_p]} & (y)_c \text{ typed as } (x)_t \\ \frac{rev[c_p, c_{p+1}]}{chars[c_p, c_{p+1}]} & (xy)_c \text{ typed as } (yx)_t \end{cases}$$

### Noisy Channel Model for Spelling Correction:

(Kernighan, Church and Gale, 1990)

- The del, ins, sub, rev matrix values need data in which errors are marked by a human (Key definition: **training data**)
- Accuracy on single errors on unseen data (test data): 87% accuracy vs. 98% avg. human accuracy.
- What are the limitations of this algorithm for correcting spelling?
   ... was called a "stellar and versatile acress whose combination of sass and glamour has defined her . . .
  - → KCG best guess is **acres**



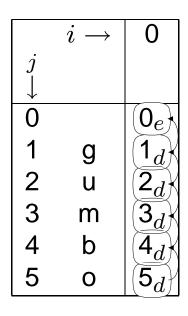
```
1 function MinEditDistance (target, source) returns min-distance:
   n = length(target)
   m = length(source)
   Create distance matrix distance of size (n+1, m+1)
   indexed from 0 to n and 0 to m
   distance[0,0] = 0
 7
    for each column i from 1 to n do:
      distance[i,0] = distance[i-1,0] + ins-cost(target i)
 8
    for each row j from 1 to m do:
10
      distance[0,j] = distance[0,j-1] + del-cost(source j)
11
    for each column i from 1 to n do:
12
      for each row j from 1 to m do:
        distance[i,j] =
13
14
          MIN ( distance[i-1,j] + ins-cost(target_i),
15
                distance[i-1,j-1] + subst-cost(source j, target i),
16
                distance[i,j-1] + del-cost(source j) )
17
    return distance[n,m]
```

#### Levenshtein Distance

- Cost is fixed across characters ins-cost is 1 del-cost is 1
- Levenshtein proposed two different costs for substitutions:
   subst-cost is 1 (a character transformation is equal to ins/del)
   subst-cost is 2 (one deletion plus one insertion)

```
7 for each column i from 1 to n do:
8   distance[i,0] = i

9 for each row j from 1 to m do:
10   distance[0,j] = j
```



Levenshtein distance between and *gumbo* = 5

	$i \rightarrow$	0	1
$\downarrow^j$			g
0		$0_e$	$1_i$
1	g	$1_d$	$\langle 0_e \rangle$
2 3	u	$2_d$	$(1_d)$
	m	$3_d$	$(2_d)$
4 5	b	$egin{array}{c} 2_d \ 3_d \ 4_d \ 5_d \end{array}$	$(3_d)$
5	0	$5_d$	$(4_d)$

Levenshtein distance between g and gumbo = 4

	$i \rightarrow$	0	1	2
j			g	а
0		$\bigcap$	<u>9</u> 1.	
U		$\bigcup e$	$\overline{}$	$2_i$
1	g	$\mid$ 1 $_d$ $\mid$	$\{0_e\}$	$1_i$
2	u	$2_d$	$(1_d)$	$2_s$
3	m	$3_d$	$(2_d)$	$3_{s}$
4	b	$4_d$	$(3_d)$	$4_s$
5	0	$5_d$	$4_{d}$	$\sqrt{5_s}$

Levenshtein distance between *ga* and *gumbo* = 5

	$i \rightarrow$	0	1	2	3
j			g	а	m
<u></u>			9		
0		$ 0_{e}\rangle$	$1_i$	${\bf 2}_i$	$3_i$
1	g	$1_d$	$\langle 0_e \rangle$	$1_i$	$2_i$
2	u	$2_d$	$\overline{1_d}$	2s	$3_s$
3	m	$3_d$	$2_d$	$3_{s}$	$\langle 2_e \rangle$
4	b	<b>4</b> <sub>d</sub>	$3_d$	$4_{s}$	$(3_d)$
5	0	$5_d$	<b>4</b> <sub>d</sub>	$5_{s}$	$\langle 4_d \rangle$

Levenshtein distance between *gam* and *gumbo* = 4

	$i \rightarrow$	0	1	2	3	4
$\downarrow^j$			g	а	m	b
0		$0_e$	$1_i$	$2_i$	$3_i$	<b>4</b> <sub>i</sub>
1	g	$1_d$	$\langle 0_e \rangle$	$1_i$	$2_i$	$3_i$
2	u	$2_d$	$\widecheck{1_d}$	2s	$3_{\scriptscriptstyle S}$	$4_{s}$
3	m	$3_d$	$2_d$	$\widetilde{3_s}$	$\langle 2_e \rangle$	$3_i$
4	b	<b>4</b> <sub>d</sub>	$3_d$	$4_{s}$	$\widetilde{3_d}$	$\langle 2_e \rangle$
5	0	$ $ 5 $_d$	<b>4</b> <sub>d</sub>	$5_{s}$	<b>4</b> <sub>d</sub>	$(3_d)$

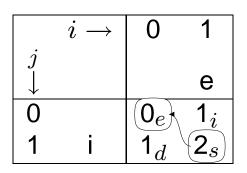
Levenshtein distance between *gamb* and *gumbo* = 3

	$i \rightarrow$	0	1	2	3	4	5
$\left  egin{array}{c} j \ \downarrow \end{array}  ight.$			g	а	m	b	ı
0		$(0_e)$	$\overline{1_i}$	$2_i$	$3_i$	<b>4</b> <sub>i</sub>	$5_i$
1	g	$1_d$	$\langle 0_e \rangle$	$1_i$	$2_i$	$3_i$	$4_{i}$
2	u	$2_d$	$\widecheck{1_d}$	2s	$3_s$	$4_{s}$	$5_{s}$
3	m	$3_d$	$2_d$	$\widetilde{3_s}$	$\langle 2_e \rangle$	$3_i$	$4_i$
4	b	$4_d$	$3_d$	$4_{s}$	$\widecheck{3_{d}}$	$\langle 2_e \rangle$	$3_i$
5	0	$5_d$	<b>4</b> <sub>d</sub>	$5_s$	<b>4</b> <sub>d</sub>	$\widecheck{3_d}$	$\langle 4_{s} \rangle$

Levenshtein distance between *gambl* and *gumbo* = 4

	$i \rightarrow$	0	1	2	3	4	5	6
$\downarrow j$			g	а	m	b	I	е
0		$\left( 0_{e} ight)$	$1_i$	$2_i$	$3_i$	$4_{i}$	$5_{i}$	$6_i$
1	g	$1_d$	$\langle 0_e \rangle$	$1_i$	$2_i$	$3_i$	$4_i$	$5_{i}$
2	u	$2_d$	$1_d$	$\langle 2_s \rangle$	$3_{s}$	$4_{s}$	$5_{s}$	$6_s$
3	m	$3_d$	$2_d$	$\widetilde{3_s}$	2e	$3_i$	$4_i$	$5_{i}$
4	b	<b>4</b> <sub>d</sub>	$3_d$	$4_{s}$	$\widecheck{3_d}$	$\langle 2_e \rangle$	$+3_i$	$4_{i}$
5	0	$5_d$	<b>4</b> <sub>d</sub>	$5_{s}$	<b>4</b> <sub>d</sub>	$\widecheck{3_d}$	$\overbrace{4_s}$	5s

Levenshtein distance between *gamble* and *gumbo* = 5



Levenshtein distance between e and i = 2

	$i \rightarrow$	0	1	2
$\downarrow$ $\downarrow$			е	x
0		$(0_e)$	$\overline{1_i}$	$2_i$
1	i	$\mid$ 1 $_d$	$\langle 2_s \rangle$	$\left  3_{\mathcal{S}}^{^{v}} \right $
2	n	$2_d$	$\overset{\smile}{3_{s}}$	4s

Levenshtein distance between ex and in = 4

	$i \rightarrow$	0	1	2	3
$\downarrow j$			е	X	е
0		$(0_e)$	$1_i$	$2_i$	$\overline{3_i}$
1	i	$1_d$	$\langle 2_s \rangle$	$3_s$	$4_{s}$
2	n	$2_d$	$\overset{\smile}{3_{s}}$	$\langle 4_s \rangle$	$5_{s}$
3	t	$3_d$	<b>4</b> <sub>s</sub>	$\overset{\smile}{5_{s}}$	$\sqrt{6s}$

Levenshtein distance between exe and int = 6

	$i \rightarrow$	0	1	2	3	4
$\downarrow$			е	X	е	С
0		$(0_e)$	$\overline{1_i}$	$2_i$	$\overline{3_i}$	<b>4</b> <sub>i</sub>
1	i	$ 1_d\rangle$	$2_s$	$3_s$	$4_s$	$5_{s}$
2	n	$\widetilde{2_d}$	$\langle 3_s \rangle$	$4_s$	$5_s$	6s
3	t	$3_d$	$\widecheck{4_{s}}$	5s	$6_s$	$7_s$
4	е	<b>4</b> <sub>d</sub>	$3_e$	$\widecheck{4_{i}}$	5e	$-(6_i)$

Levenshtein distance between *exec* and *inte* = 6

	$i \rightarrow$	0	1	2	3	4	5
$\downarrow$ $j$			е	X	е	С	u
0		$(0_e)$	$1_i$	$2_i$	$3_i$	$4_{i}$	$5_{i}$
1	i	$ (1_d) $	$2_s$	$3_s$	$4_s$	$5_{s}$	$6_s$
2	n	$(\mathbf{Z}_d)$	$\langle 3_s \rangle$	$4_s$	$5_{s}$	$6_s$	$7_s$
3	t	$3_d$	$\widecheck{4_{s}}$	$\sqrt{5_s}$	$6_s$	$7_s$	$8_s$
4	е	$4_d$	$3_e$	$\widecheck{4_i}$	(5 <sub>e</sub> )	$-(6_i)$	$7_i$
5	n	$5_d$	$4_d$	$5_{s}$	$\overset{\smile}{6_{\mathcal{S}}}$	$7_s$	8s

Levenshtein distance between *execu* and *inten* = 8

	$i \rightarrow$	0	1	2	3	4	5	6	7	8	9
j			0	V	0	•		+	i	0	n
<u></u>			е	Х	е	С	u	L	l	0	n
0		$ 0_e\rangle$	$1_i$	$2_i$	$3_i$	$4_i$	$5_{i}$	$6_i$	${\sf 7}_i$	$8_i$	$9_i$
1	i	$ (1_d)\langle$	$2_s$	$3_s$	$4_{S}$	$5_{s}$	$6_s$	$7_s$	6e	$7_i$	$8_i$
2	n	$\widetilde{2_d}$	$\langle 3_s \rangle$	$4_{s}$	$5_{s}$	$6_{s}$	$7_s$	$8_s$	$7_d$	$8_s$	$7_e$
3	t	$3_d$	$\widecheck{4_{s}}$	$\sqrt{5_s}$	$6_s$	$7_s$	$8_s$	$7_e$	$8_i$	$9_s$	$8_d$
4	е	$4_d$	$3_e$	$\widecheck{f 4}_i$	$\sqrt{5_e}$	$-(6_i)$	$7_i$	$8_i$	$9_s$	$10_s$	$9_d$
5	n	$5_d$	$4_d$	$5_{s}$	$\overset{\smile}{6_{s}}$	$7_s$	8s	$9_s$	$10_s$	<b>11</b> <sub>s</sub>	10 <sub>e</sub>
6	t	$6_d$	$5_d$	$6_s$	$7_s$	$8_s$	$\overset{\smile}{9_s}$	8e	$9_i$	$10_i$	$11_i$
7	i	$7_d$	$6_d$	$7_s$	$8_s$	$9_s$	$10_s$	$\widecheck{\mathtt{9}_d}$	8e	$9_i$	$10_i$
8	0	$8_d$	$7_d$	$8_s$	$9_s$	$10_s$	$11_s$	$10_d$	$\widecheck{\mathtt{9}_d}$	8e	$9_i$
9	n	$9_d$	$8_d$	$9_s$	$10_s$	$11_s$	<b>12</b> <sub>s</sub>	$11_d$	$10_d$	$\widecheck{\mathtt{9}_d}$	8e

Levenshtein distance between *execution* and *intention* = 8