

## CMPT 379 Compilers

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## Attribute Grammars

- Syntax-directed translation uses a grammar to produce code (or any other “semantics”)
- Consider this technique to be a generalization of a CFG definition
- Each grammar symbol is associated with an attribute
- An attribute can be anything: a string, a number, a tree, any kind of record or object

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## Syntax directed Translation

- Models for translation from parse trees into assembly/machine code
- Representation of translations
  - Attribute Grammars (semantic actions for CFGs)
  - Tree Matching Code Generators
  - Tree Parsing Code Generators

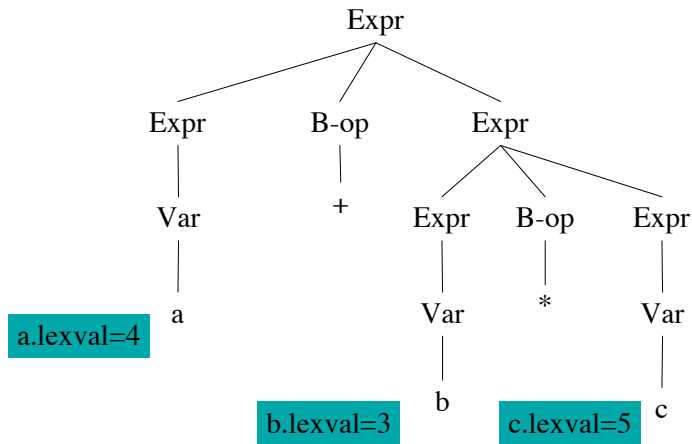
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## Attribute Grammars

- A CFG can be viewed as a (finite) representation of a function that relates strings to parse trees
- Similarly, an attribute grammar is a way of relating strings with “meanings”
- Since this relation is syntax-directed, we associate each CFG rule with a semantics (rules to build an abstract syntax tree)
- In other words, attribute grammars are a method to *decorate* or *annotate* the parse tree

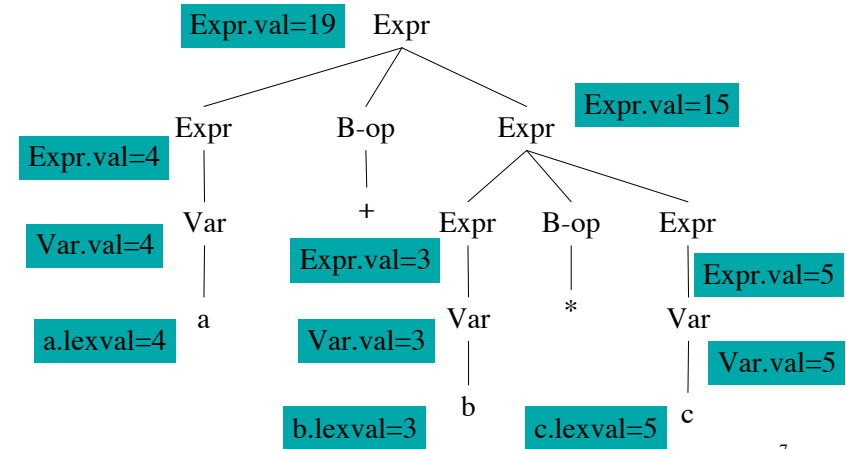
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## Example



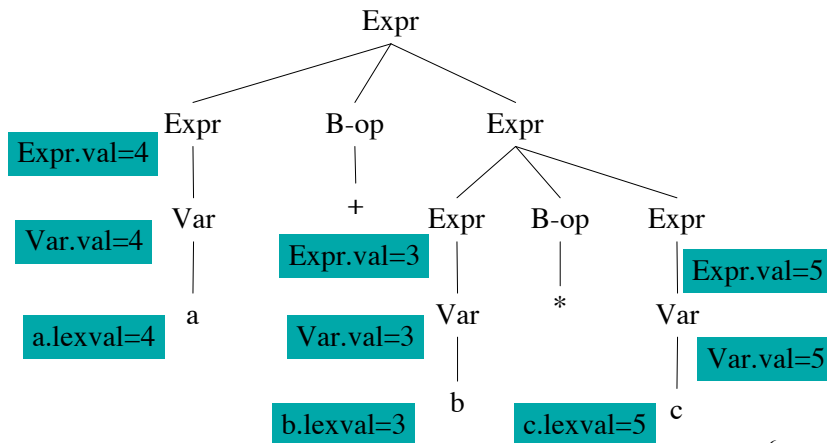
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## Example



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## Example



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## Syntax directed definition

$\text{Var} \rightarrow \text{IntConstant}$   
 $\{ \$0.\text{val} = \$1.\text{lexval}; \}$   
 $\text{Expr} \rightarrow \text{Var}$   
 $\{ \$0.\text{val} = \$1.\text{val}; \}$   
 $\text{Expr} \rightarrow \text{Expr B-op Expr}$   
 $\{ \$0.\text{val} = \$2.\text{val} (\$1.\text{val}, \$3.\text{val}); \}$   
 $\text{B-op} \rightarrow +$   
 $\{ \$0.\text{val} = \text{PLUS}; \}$   
 $\text{B-op} \rightarrow *$   
 $\{ \$0.\text{val} = \text{TIMES}; \}$

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## Flow of Attributes in *Expr*

- Consider the flow of the attributes in the *Expr* syntax-directed defn
- The lhs attribute is computed using the rhs attributes
- Purely bottom-up: compute attribute values of all children (rhs) in the parse tree
- And then use them to compute the attribute value of the parent (lhs)

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## Inherited Attributes

- Synthesized attributes may not be sufficient for all cases that might arise for semantic checking and code generation
- Consider the (sub)grammar:  
Var-decl  $\rightarrow$  Type Id-comma-list ;  
Type  $\rightarrow$  **int** | **bool**  
Id-comma-list  $\rightarrow$  **ID**  
Id-comma-list  $\rightarrow$  **ID** , Id-comma-list

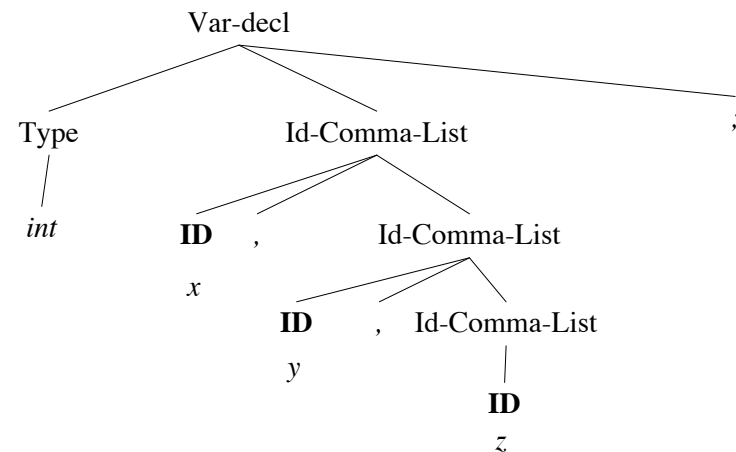
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## Synthesized Attributes

- **Synthesized attributes** are attributes that are computed purely bottom-up
- A grammar with semantic actions (or syntax-directed definition) can choose to use *only* synthesized attributes
- Such a grammar plus semantic actions is called an **S-attributed definition**

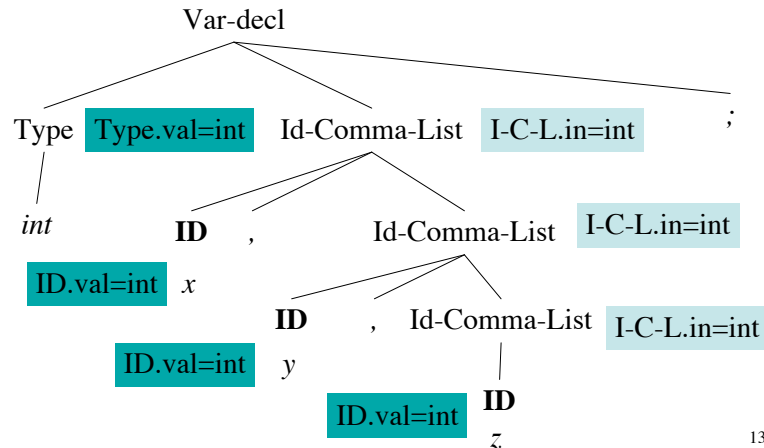
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## Example: *int x, y, z ;*



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Example: *int x, y, z ;*



## Flow of Attributes in *Var-decl*

- How do the attributes flow in the *Var-decl* grammar
- **ID** takes its attribute value from its parent node
- *Id-Comma-List* takes its attribute value from its left sibling *Type*
- Computing attributes purely bottom-up is not sufficient in this case
- Do we need synthesized attributes in this grammar?

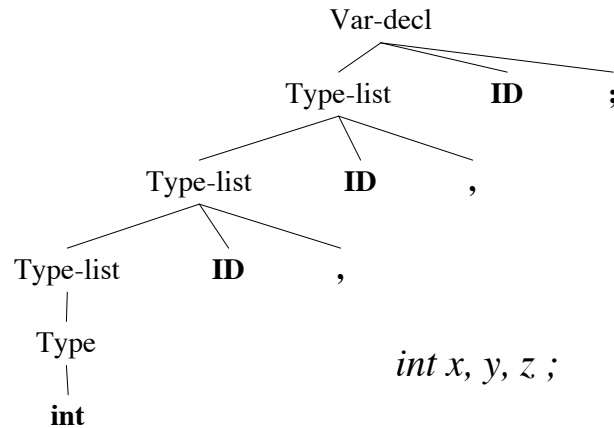
## Syntax-directed definition

$\text{Var-decl} \rightarrow \text{Type Id-comma-list ;}$   
 $\{ \$2.in = \$1.val; \}$   
 $\text{Type} \rightarrow \text{int} \mid \text{bool}$   
 $\{ \$0.val = \text{int}; \} \ \& \ \{ \$0.val = \text{bool}; \}$   
 $\text{Id-comma-list} \rightarrow \text{ID}$   
 $\{ \$1.val = \$0.in; \}$   
 $\text{Id-comma-list} \rightarrow \text{ID} , \text{Id-comma-list}$   
 $\{ \$1.val = \$0.in; \$3.in = \$0.in; \}$

## Inherited Attributes

- **Inherited attributes** are attributes that are computed at a node based on attributes from siblings or the parent
- Typically we combine synthesized attributes and inherited attributes
- It is possible to convert the grammar into a form that *only* uses synthesized attributes

## Removing Inherited Attributes



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## Removing inherited attributes

$\text{Var-decl} \rightarrow \text{Type-List ID ;}$

$\{ \$0.\text{val} = \$1.\text{val}; \}$

$\text{Type-list} \rightarrow \text{Type-list ID ,}$

$\{ \$0.\text{val} = \$1.\text{val}; \}$

$\text{Type-list} \rightarrow \text{Type}$

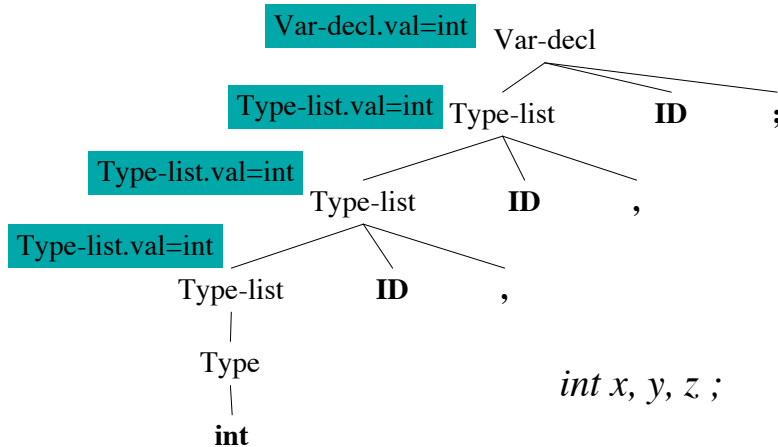
$\{ \$0.\text{val} = \$1.\text{val}; \}$

$\text{Type} \rightarrow \text{int} \mid \text{bool}$

$\{ \$0.\text{val} = \text{int}; \} \ \& \ \{ \$0.\text{val} = \text{bool}; \}$

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## Removing Inherited Attributes



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## Direction of inherited attributes

- Consider the syntax directed defs:

$A \rightarrow L M$

$\{ \$1.\text{in} = \$0.\text{in}; \$2.\text{in} = \$1.\text{val}; \$0.\text{val} = \$2.\text{val}; \}$

$A \rightarrow Q R$

$\{ \$2.\text{in} = \$0.\text{in}; \$1.\text{in} = \$2.\text{val}; \$0.\text{val} = \$1.\text{val}; \}$

- Problematic definition:  $\$1.\text{in} = \$2.\text{val}$
- Difference between incremental processing vs. using the completed parse tree

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## Incremental Processing

- Incremental processing: constructing output as we are parsing
- Bottom-up or top-down parsing
- Both can be viewed as left-to-right and depth-first construction of the parse tree
- Some inherited attributes cannot be used in conjunction with incremental processing

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## Top-down translation

- Assume that we have a top-down predictive parser
- Typical strategy: take the CFG and eliminate left-recursion
- Suppose that we start with an attribute grammar
- Can we still eliminate left-recursion?

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## L-attributed Definitions

- A syntax-directed definition is **L-attributed** if for a CFG rule  
 $A \rightarrow X_1..X_{j-1}X_j..X_n$  two conditions hold:
  - Each inherited attribute of  $X_j$  depends on  $X_1..X_{j-1}$
  - Each inherited attribute of  $X_j$  depends on  $A$
- These two conditions ensure left to right and depth first parse tree construction
- Every S-attributed definition is L-attributed

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## Top-down translation

```
E → E + T
    { $0.val = $1.val + $3.val; }
E → E - T
    { $0.val = $1.val - $3.val; }
T → IntConstant
    { $0.val = $1.lexval; }
E → T
    { $0.val = $1.val; }
T → ( E )
    { $0.val = $1.val; }
```

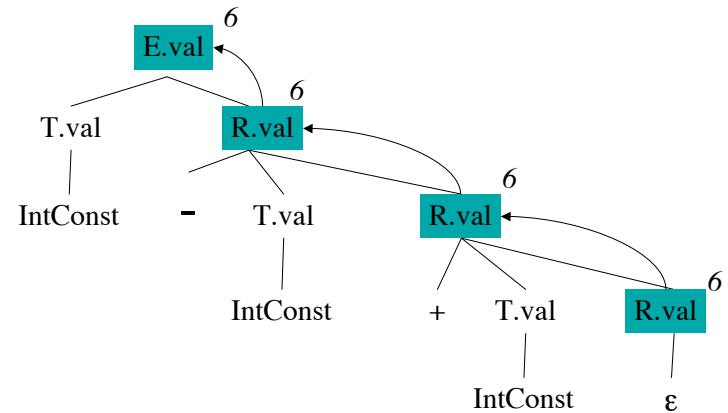
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## Top-down translation

$E \rightarrow T R$   
 $\{ \$2.in = \$1.val; \$0.val = \$2.val; \}$   
 $R \rightarrow + T R$   
 $\{ \$3.in = \$0.in + \$2.val; \$0.val = \$3.val; \}$   
 $R \rightarrow - T R$   
 $\{ \$3.in = \$0.in - \$2.val; \$0.val = \$3.val; \}$   
 $R \rightarrow \epsilon \{ \$0.val = \$0.in; \}$   
 $T \rightarrow ( E ) \{ \$0.val = \$1.val; \}$   
 $T \rightarrow \text{IntConstant} \{ \$0.val = \$1.lexval; \}$

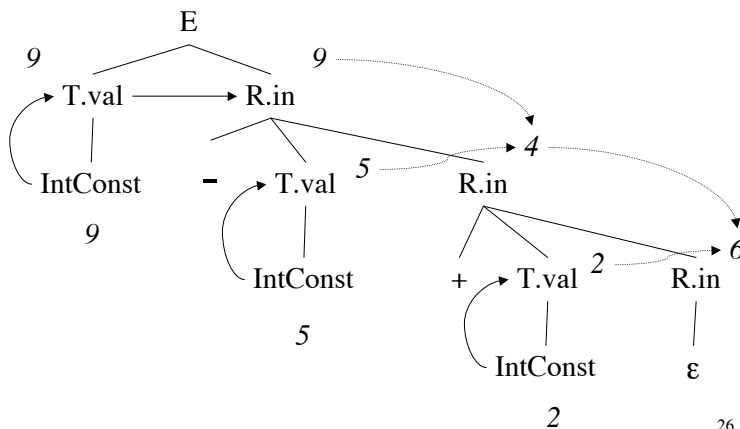
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## Example: 9 - 5 + 2



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## Example: 9 - 5 + 2



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## Translation Scheme

- A *translation scheme* is a CFG where each rule is associated with a semantic attribute
  - A TS that maps infix expressions to postfix:
- $E \rightarrow T R$   
 $R \rightarrow + T \{ \text{print}( '+' ); \} R$   
 $R \rightarrow - T \{ \text{print}( '-' ); \} R$   
 $R \rightarrow \epsilon$   
 $T \rightarrow \text{id} \{ \text{print}( \text{id.lookup} ); \}$

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## LR parsing and inherited attributes

- As we just saw, inherited attributes are possible when doing top-down parsing
- How can we compute inherited attributes in a bottom-up shift-reduce parser
- Problem: doing it incrementally (while parsing)
- Note that LR parsing implies depth-first visit which matches L-attributed definitions

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## Example: Synthesized Attributes

```

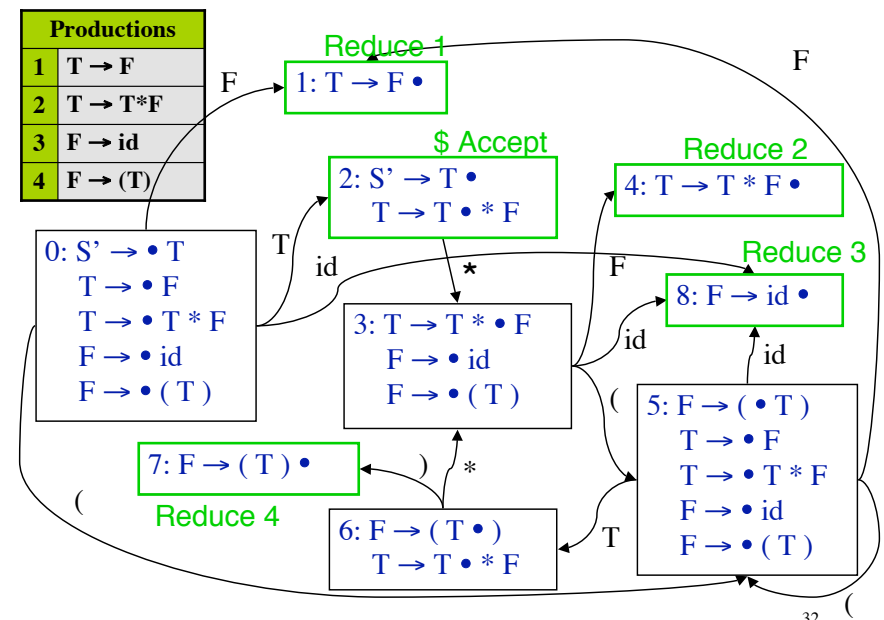
T → F    { $0.val = $1.val; }
T → T * F
          { $0.val = $1.val * $3.val; }
F → id
          { val := id.lookup();
            if (val) { $0.val = $1.val; }
            else { error; } }
F → ( T ) { $0.val = $1.val; }
    
```

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## LR parsing and inherited attributes

- Attributes can be stored on the stack used by the shift-reduce parsing
- For synthesized attributes: when a reduce action is invoked, store the value on the stack based on value popped from stack
- For inherited attributes: transmit the attribute value when executing the **goto** function

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## Trace “(id<sub>val=3</sub>)\*id<sub>val=2</sub>”

Stack	Input	Action	Attributes
0	( id ) * id \$	Shift 5	
0 5	id ) * id \$	Shift 8	
0 5 8	) * id \$	Reduce 3 F→id, pop 8, goto [5,F]=1	a.Push id.val=3; { \$0.val = \$1.val }
0 5 1	) * id \$	Reduce 1 T→F, pop 1, goto [5,T]=6	a.Pop; a.Push 3; { \$0.val = \$1.val }
0 5 6	) * id \$	Shift 7	a.Pop; a.Push 3;
0 5 6 7	* id \$	Reduce 4 F→(T), pop 7 6 5, goto [0,F]=1	{ \$0.val = \$2.val } 3 pops; a.Push 3

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## Example: Inherited Attributes

$E \rightarrow T R$

{ \$2.in = \$1.val; \$0.val = \$2.val; }

$R \rightarrow + T R$

{ \$3.in = \$0.in + \$2.val; \$0.val = \$3.val; }

$R \rightarrow \epsilon$  { \$0.val = \$0.in; }

$T \rightarrow ( E )$  { \$0.val = \$1.val; }

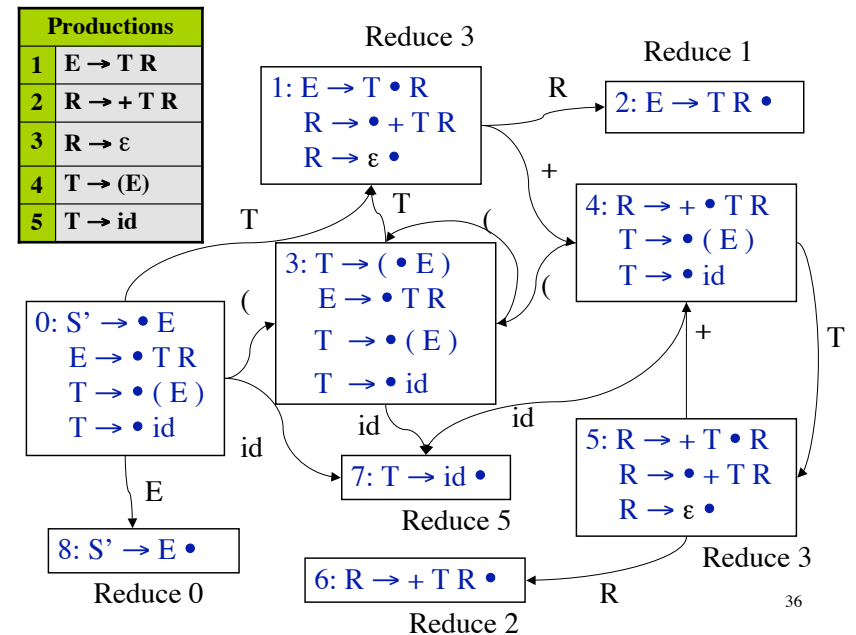
$T \rightarrow id$  { \$0.val = id.lookup; }

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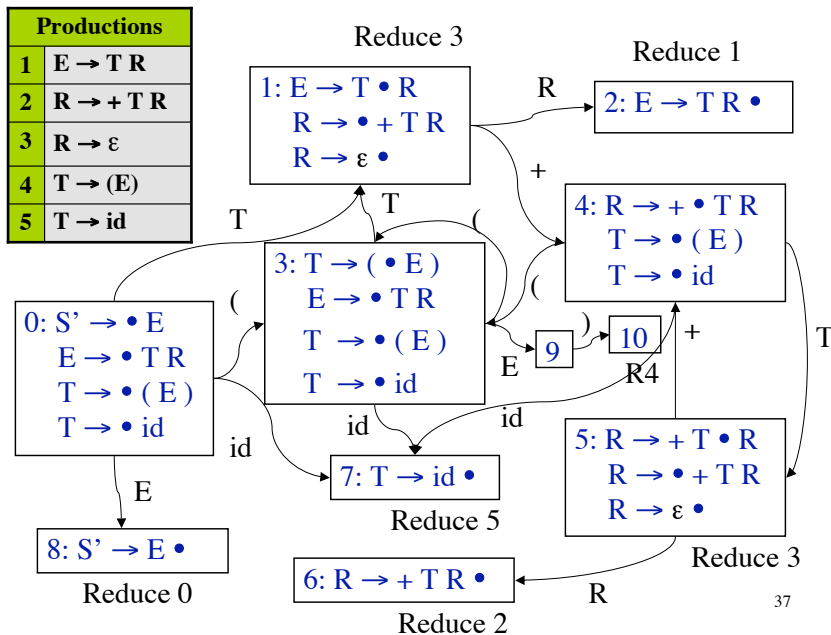
## Trace “(id<sub>val=3</sub>)\*id<sub>val=2</sub>”

Stack	Input	Action	Attributes
0 1	* id \$	Reduce 1 T→F, pop 1, goto [0,T]=2	{ \$0.val = \$1.val } a.Pop; a.Push 3
0 2	* id \$	Shift 3	a.Push mul
0 2 3	id \$	Shift 8	a.Push id.val=2
0 2 3 8	\$	Reduce 3 F→id, pop 8, goto [3,F]=4	a.Pop a.Push 2
0 2 3 4	\$	Reduce 2 T→T * F pop 4 3 2, goto [0,T]=2	{ \$0.val = \$1.val * \$2.val; }
0 2	\$	Accept	3 pops; a.Push 3*2=6

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Trace “ $id_{val=3} + id_{val=2}$ ”

Stack	Input	Action	Attributes
0 1 4 5 6	\$	Reduce 2 $R \rightarrow + T R$ Pop 4 5 6, goto [1,R]=2	{ $\$0.val = \$3.val$ pop; attr.Push(5); }
0 1 2	\$	Reduce 1 $E \rightarrow T R$ Pop 1 2, goto [0,E]=8	{ $\$0.val = \$3.val$ pop; attr.Push(5); }
0 8	\$	Accept	{ $\$0.val = 5$ attr.top = 5; }

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Trace “ $id_{val=3} + id_{val=2}$ ”

Stack	Input	Action	Attributes
0	id + id \$	Shift 7	
0 7	+ id \$	Reduce 5 $T \rightarrow id$ pop 7, goto [0,T]=1	{ $\$0.val = id.val$ pop; attr.Push(3)
0 1	+ id \$	Shift 4	{ $\$2.in = \$1.val$ $R.in := (1).attr$ }
0 1 4	id \$	Shift 7	
0 1 4 7	\$	Reduce 5 $T \rightarrow id$ pop 7, goto [4,T]=5	{ $\$0.val = id.val$ pop; attr.Push(2); }
0 1 4 5	\$	Reduce 3 $R \rightarrow \epsilon$ goto [5,R]=6	{ $\$3.in = \$0.in + \$1.val$ $(5).attr = (1).attr + 2$ $\$0.val = \$0.in$ $\$0.val = (5).attr \neq 5$ }

Marker Non-terminals

$E \rightarrow T R$   
 $R \rightarrow + T \{ \text{print( '+' ); } \} R$   
 $R \rightarrow - T \{ \text{print( '-' ); } \} R$   
 $R \rightarrow \epsilon$   
 $T \rightarrow id \{ \text{print( id.lookup ); } \}$

Actions that should be done after recognizing T but before predicting R

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## Marker Non-terminals

$E \rightarrow T R$   
 $R \rightarrow + T M R$   
 $R \rightarrow - T N R$   
 $R \rightarrow \epsilon$   
 $T \rightarrow \mathbf{id} \{ \text{print}(\mathbf{id.lookup}); \}$   
 $M \rightarrow \epsilon \{ \text{print}(' '); \}$   
 $N \rightarrow \epsilon \{ \text{print}('- '); \}$

Equivalent SDT using  
marker non-terminals

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## Tree Matching Code Generators

- To provide a unique output, we assign costs to the use of each tree pattern
- E.g. assigning uniform costs leads to smaller code or instruction costs can be used for optimizing code generation
- Three algorithms: Maximal Munch (§9.12), Dynamic Programming (§9.11), Tree Grammars

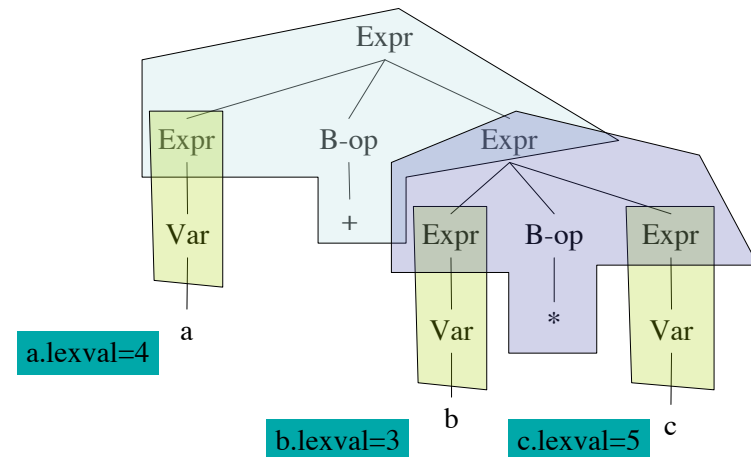
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## Tree Matching Code Generators

- Write tree patterns that match portions of the parse tree
- Each tree pattern can be associated with an action (just like attribute grammars)
- There can be multiple combinations of tree patterns that match the input parse tree

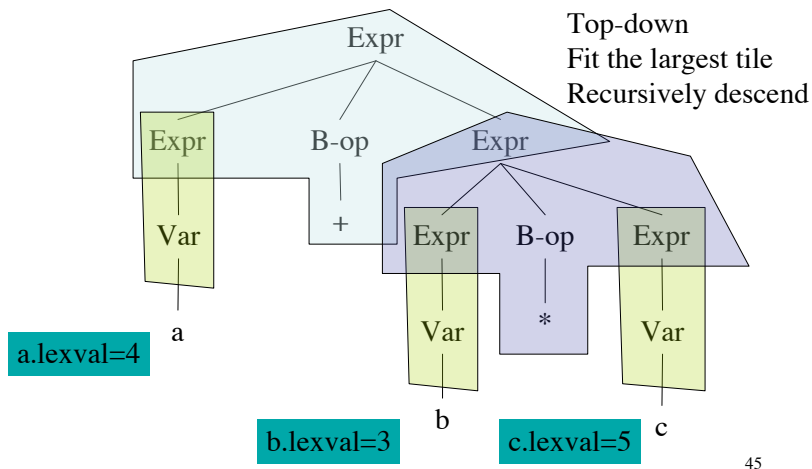
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## Maximal Munch: Example 1



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## Maximal Munch: Example 2

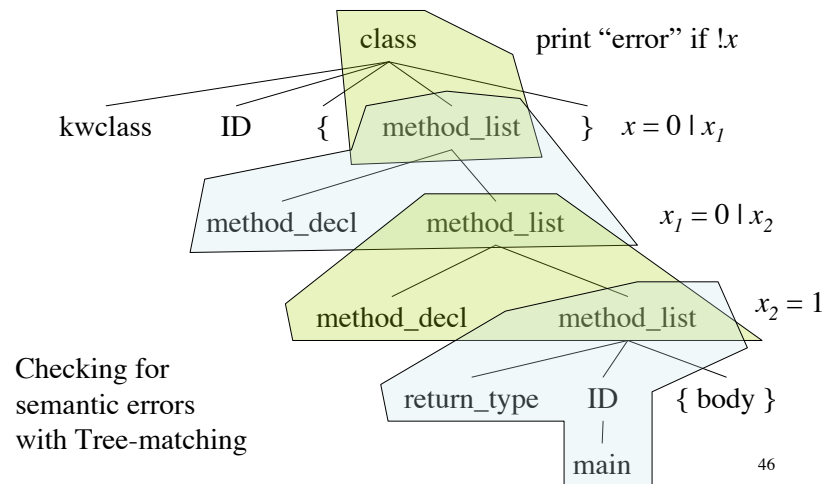


## Tree Parsing Code Generators

- Take the prefix representation of the syntax tree
  - E.g.  $(+ (* c1 r1) (+ ma c2))$  in prefix representation uses an inorder traversal to get  $+ * c1 r1 + ma c2$
- Write CFG rules that match substrings of the above representation and non-terminals are registers or memory locations
- Each matching rule produces some predefined output
- Example 9.18 (Dragon book)

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## Maximal Munch: Example 2



## Code-generation Generators

- A CGG is like a compiler-compiler: write down a description and generate code for it
- Code generation by:
  - Adding semantic actions to the original CFG and each action is executed while parsing, e.g. yacc
  - Tree Rewriting: match a tree and commit an action, e.g. lcc
  - Tree Parsing: use a grammar that generates trees (not strings), e.g. twig, burs, iburg

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# Summary

- The parser produces concrete syntax trees
- Abstract syntax trees: define semantic checks or a syntax-directed translation to the desired output
- Attribute grammars: static definition of syntax-directed translation
  - Synthesized and Inherited attributes
  - S-attribute grammars
  - L-attributed grammars
- Complex inherited attributes can be defined if the full parse tree is available