



# CMPT-413: Computational Linguistics

## HMM3: Parsing with Hidden Markov Models

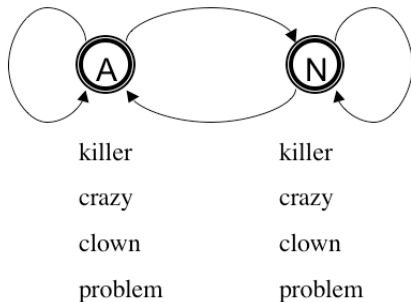
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# Hidden Markov Model

$$\text{Model } \theta = \begin{cases} \pi_i & \text{probability of starting at state } i \\ a_{i,j} & \text{probability of transition from state } i \text{ to state } j \\ b_i(o) & \text{probability of output } o \text{ at state } i \end{cases}$$



# Hidden Markov Model Algorithms

- ▶ HMM as parser: compute the best sequence of states for a given observation sequence.
- ▶ HMM as language model: compute probability of given observation sequence.
- ▶ HMM as learner: given a corpus of observation sequences, learn its distribution, i.e. learn the parameters of the HMM from the corpus.
  - ▶ Learning from a set of observations with the sequence of states provided (states are not hidden) [\[Supervised Learning\]](#)
  - ▶ Learning from a set of observations without any state information. [\[Unsupervised Learning\]](#)

# HMM as Parser


$$\pi =$$

A	0.25
N	0.75

$$a =$$

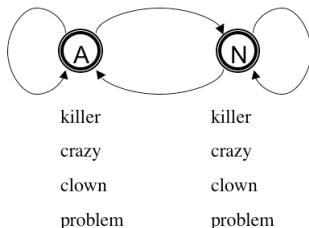
$a_{ij}$	A	N
A	0.0	1.0
N	0.5	0.5

$$b =$$

$b_i(o)$	clown	killer	problem	crazy
A	0	0	0	1
N	0.4	0.3	0.3	0

*The task: for a given observation sequence find the most likely state sequence.*

# HMM as Parser



- ▶ Find most likely sequence of states for *killer clown*
- ▶ Score every possible sequence of states: AA, AN, NN, NA
  - ▶  $P(\text{killer clown, AA}) = \pi_A \cdot b_A(\text{killer}) \cdot a_{A,A} \cdot b_A(\text{clown}) = 0.0$
  - ▶  $P(\text{killer clown, AN}) = \pi_A \cdot b_A(\text{killer}) \cdot a_{A,N} \cdot b_N(\text{clown}) = 0.0$
  - ▶  $P(\text{killer clown, NN}) = \pi_N \cdot b_N(\text{killer}) \cdot a_{N,N} \cdot b_N(\text{clown}) = 0.75 \cdot 0.3 \cdot 0.5 \cdot 0.4 = 0.045$
  - ▶  $P(\text{killer clown, NA}) = \pi_N \cdot b_N(\text{killer}) \cdot a_{N,A} \cdot b_A(\text{clown}) = 0.0$
- ▶ Pick the state sequence with highest probability (NN=0.045).

# HMM as Parser

- ▶ As we have seen, for input of length 2, and a HMM with 2 states there are  $2^2$  possible state sequences.
- ▶ In general, if we have  $q$  states and input of length  $T$  there are  $q^T$  possible state sequences.
- ▶ Using our example HMM, for input *killer crazy clown problem* we will have  $2^4$  possible state sequences to score.
- ▶ Our naive algorithm takes exponential time to find the best state sequence for a given input.
- ▶ The **Viterbi algorithm** uses dynamic programming to provide the best state sequence with a time complexity of  $q^2 \cdot T$