Parsing with Tree-Adjoining Grammars

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High Level Overview

- 1st session
 - Specific motivations for Tree-Adjoining Grammars (TAGs)
 - Lexicalized TAG: definition, examples and extensions
 - Lexicalized TAGs from TreeBanks
 - Synchronous TAG

High Level Overview

- 2nd session
 - Statistical parsing: generative models for TAG
 - TAG-based shallow parsing: SuperTagging and Stapling
 - Bootstrapping between CFG and LTAG parsers

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Preliminaries

Formal Languages and NLP

Formal Language Theory	NLP
Language (possibly infinite)	Text Data, Corpus (finite)
Grammar	Grammar (usually inferred from data, produces infinite set)
Automata	Recognition/Generation algorithms

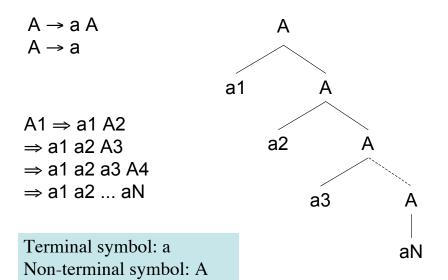
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Sentences as Strings

David	likes Verb		peanuts Noun	
Noun				
David	said	that	Mary	left
Noun	Verb	Comp	Noun	Verb

- Linear order: all important information is contained in the precedence information, e.g. useful "feature functions" are w-2, w-1, t-2, t-1, w0, w+1, w+2, t+2, t+1, etc.
- No hierarchical structure but every part-of-speech is lexicalized, e.g. Verb is lexicalized by likes
- Language (set of strings) generated by finite-state grammars

Finite State Grammars

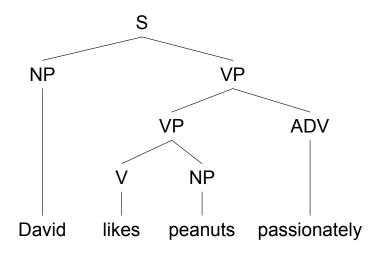


Context-Free Grammars

```
S → NP VP
VP → V NP | VP ADV
NP → David | peanuts
V → likes
ADV → passionately
```

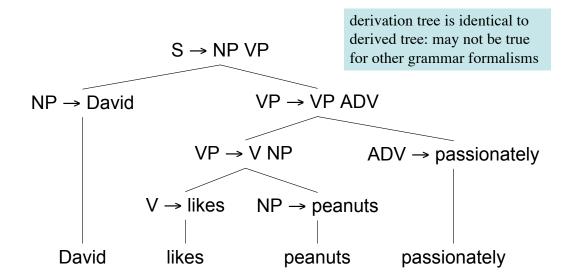
- CFGs generate strings, e.g. language of G above is the set:
 { David likes peanuts,
 David likes peanuts passionately,
 ... }
- Lexical sensitivity is lost
- CFGs also generate trees: hierarchical structure produced is non-trivial

CFG: Derived/Parse Tree



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CFG: Derivation Tree



Preliminaries

- Rules of the kind $\alpha \rightarrow \beta$ where α , β are strings of terminals and non-terminals
- Chomsky hierarchy: regular, context-free, context-sensitive, recursively enumerable
- Automata: finite-state, pushdown, LBA, Turing machines (analysis of complexity of parsing)
- A rule $\alpha \rightarrow \beta$ in a grammar is lexicalized if β contains a terminal symbol
- Lexicalization is a useful property, e.g. a rule like NP → NP creates infinite valid derivations

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Motivation #1

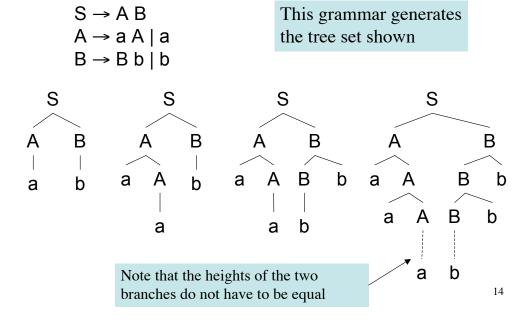
Context-sensitive predicates on trees bear less fruit than you think*

Strong vs. Weak Generative Capacity

- A property of a formal grammar, e.g. of a regular grammar or a CFG
- Weak Generative Capacity of a grammar is the set of strings or the language
- Strong Generative Capacity of a grammar is the set of structures (usually the set of trees) produced by the grammar
- The tree for an utterance/sentence is the source of semantics, so the set of trees is more relevant for CL/NLP

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Tree Sets



A Tree Set with no CFG

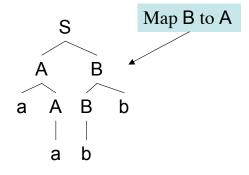
Claim: There is no CFG that can produce the tree set shown below: S S S S Α Α Α b b а b а b а b а а b а Note that the heights of the two 15 branches do not have to be equal

Generating Tree Sets

- A simple trick: start with a CFG that almost works
- Then re-label the node labels, map B to A to get the desired tree set
- But how can we directly generate the tree sets?
- We need a **generative device** that generates *trees*, not *strings*
- (Thatcher, 1967) and (Rounds, 1970) provided such a generative device

$$S \rightarrow A B$$

 $A \rightarrow a A \mid a$
 $B \rightarrow B b \mid b$

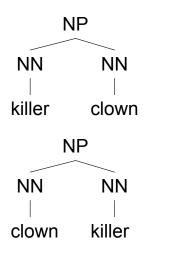


Some definitions

- A local set is defined as the set of the set of trees generated by each CFG
- A **recognizable set** is the set of trees generated by each CFGs plus a re-labeling homomorphism
- The recognizable sets strictly contain the local sets
- Recognizable sets provide surprising connections between automata theory, decidability and logic
- They also provide insights into NLP tasks like parsing and syntax-based MT

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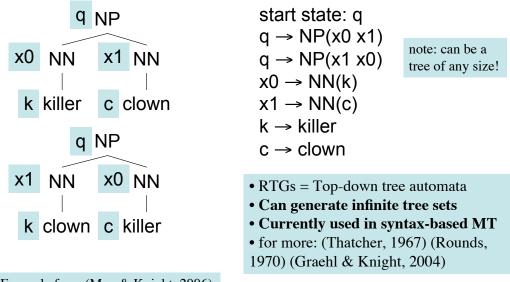
Regular Tree Grammars



Example from (May & Knight, 2006)

- Consider a simple tree set with two trees for the strings { *killer clown*, *clown killer* }
- No CFG can recognize this simple tree set without also recognizing trees for *clown clown* and *killer killer*
- A Regular Tree Grammar recognizes this tree set (analogy with regular grammars on strings)

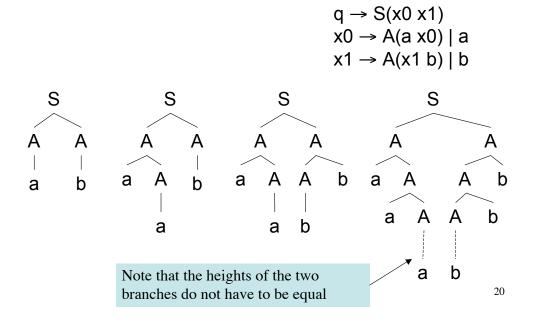
Regular Tree Grammars



Example from (May & Knight, 2006)

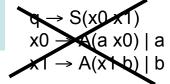
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Another RTG Example

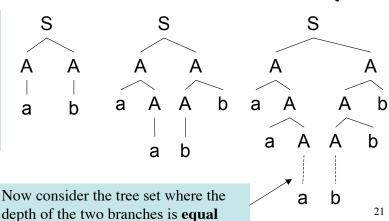


A Tree Set with no RTG

Claim: There is no RTG that can produce the tree set shown below:



RTG is like a regular grammar, the state cannot count how many times it was reached



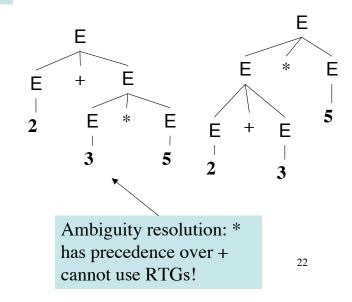
Tree Sets: Another Example

A more practical example

$$E \rightarrow E + E$$

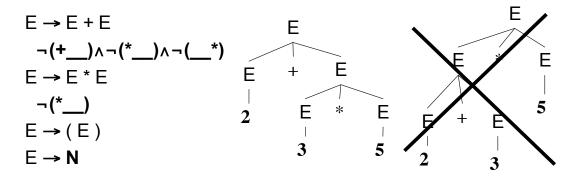
 $E \rightarrow E * E$
 $E \rightarrow (E)$
 $E \rightarrow N$

2+3*5 is ambiguous either 17 or 25



Tree Sets: Context-sensitivity

Eliminating ambiguity



similar to contextsensitive grammars!

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Context-sensitive Grammars

- Rules of the form $\alpha A\beta \rightarrow \alpha\gamma\beta$ where γ cannot be the empty string, also written as $A \rightarrow \gamma / \alpha _ \beta$
- CSGs are very powerful: they can generate languages like $\{a^{2^{i}}: i > 0\}$
- This kind of computational power is unlikely to be useful to describe natural languages
- Like other grammar formalisms in the Chomsky hierarchy CSGs generate string sets
- What if they are used to **recognize** tree sets?

Context-sensitive predicates

- Consider each CSG rule A → γ / α_β to be a predicate (i.e. either true or false)
- Apply all the rules in a CSG as predicates on an input tree
- If all predicates are true then accept the tree, else reject the tree
- Can be easily extended to a set of trees
- So a CSG can be used to accept a tree set
- Can we precisely describe this set of tree languages?

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Peters-Ritchie Theorem

- The Peters-Ritchie Theorem (Peters & Ritchie, 1967) states a surprising result about the generative power of CSG predicates
- Consider each tree set accepted by CSG predicates
- **Theorem**: The string language of this tree set is a context-free language
- Each CSG when applied as a set of predicates can be converted into a weakly equivalent CFG
- See also: (McCawley, 1967) (Joshi, Levy & Yueh, 1972) (Rogers, 1997)

Local Transformations

- This theorem was extended by (Joshi & Levy, 1977) to handle arbitrary boolean combinations and sub-tree / domination predicates
- Proof involves conversion of all CSG predicates into top-down tree automata that accept tree sets
- (Joshi & Levy, 1977) result shows that **local transformations** used in early linguistic formalisms can be all written down as weakly equivalent CFGs
- Important caveat: we assume some source generating trees which are then validated

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Locality of CSG predicates

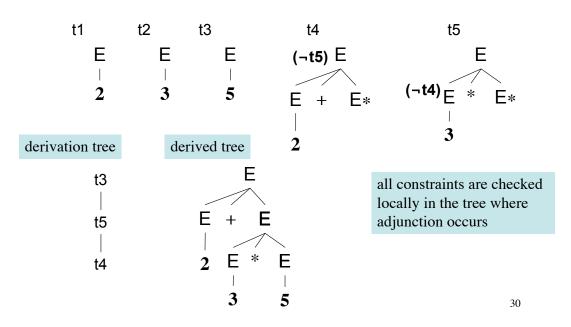
- An analysis of the kinds of CSG grammars used to define linguistic analyses in practice showed an interesting fact
- All the CSG predicates were very local
- They did not include in the context various parts of the tree that were arbitrarily far apart
- Long distance dependencies were expressed by chaining together many local CSG predicates
- This insight can be used to generate trees from an input string and validate them using CSG predicates

Tree-Adjoining Grammars

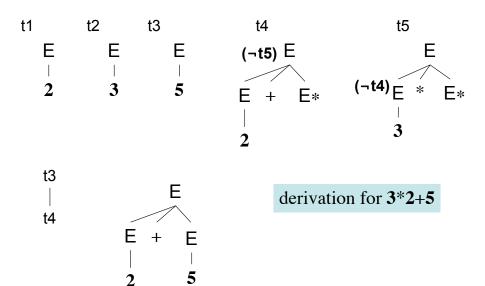
- Construct a tree set out of tree fragments
- Each fragment contains only the structure needed to express the locality of various CSG predicates
- Each tree fragment is called an elementary tree
- In general we need to expand even those nonterminals that are not leaf nodes: leads to the notion of adjunction

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Tree-Adjoining Grammars

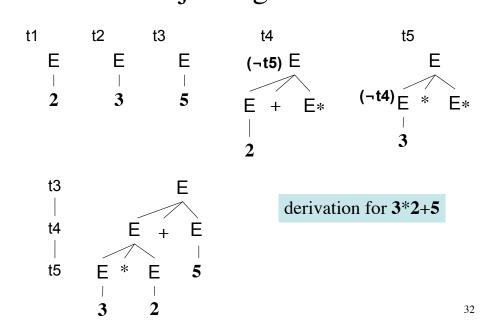


Tree-Adjoining Grammars



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Tree-Adjoining Grammars



Motivation #2

Lexicalization of Context-Free Grammars

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Lexicalization of Grammars

- We know that a CFG can be ambiguous: provide more than one parse tree for an input string
- A CFG can be infinitely ambiguous
- Structure can be introduced without influence from input string, e.g. the chain rule NP → NP has this effect
- Lexicalization of a grammar means that each rule or elementary object in the grammar is associated with some terminal symbol

Lexicalization of Grammars

- Lexicalization is an interesting idea for syntax, semantics (in linguistics) and sentence processing (in psycho-linguistics)
- What if each word brings with it the syntactic and semantic context that it requires?
- Let us consider lexicalization of Context-free Grammars (CFGs)

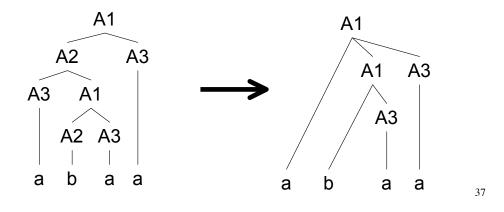
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Lexicalization of CFGs

- A **normal form** is a grammar transformation that does not change the language of the grammar
- Can we transform every CFG to a normal form where there is guaranteed to be a terminal symbol on the right hand side of each rule
- Answer: yes using Greibach Normal Form (GNF)
- GNF: every CFG can be transformed into the form $A \rightarrow a\alpha$ where A is a non-terminal, a is a terminal and α is a string of terminals and non-terminals

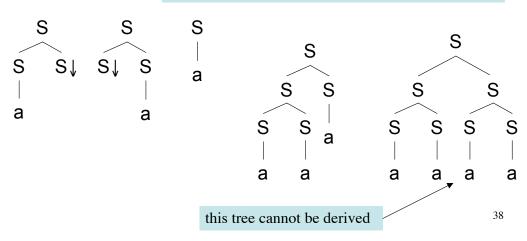
$T(G) \neq T(GNF(G))$

 $A1 \rightarrow A2 A3$ $A2 \rightarrow A3 A1 \mid b$ $A3 \rightarrow A1 A2 \mid a$ Greibach Normal Form does not provide a strongly equivalent lexicalized grammar: the original tree set is not preserved

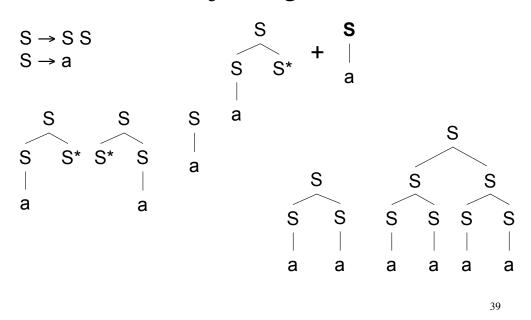


Tree Substitution Grammar

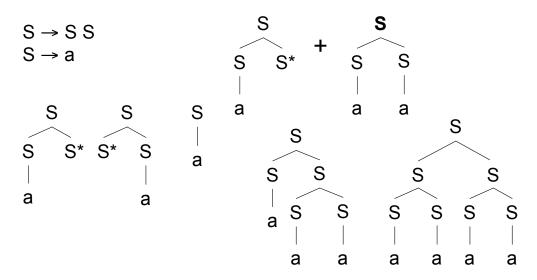
 $S \rightarrow S S$ $S \rightarrow a$ Consider a simple expansion of each context-free rule into a tree fragment where each fragment is lexicalized



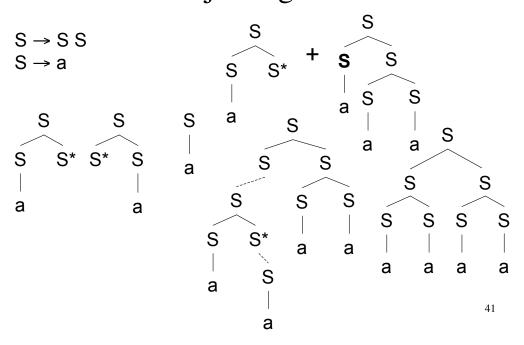
Tree Adjoining Grammar



Tree Adjoining Grammar



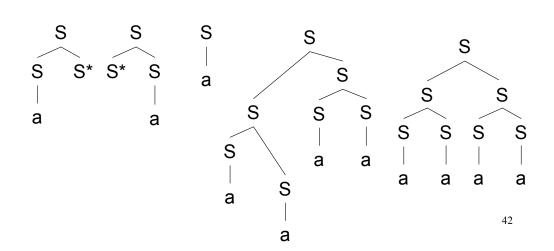
Tree Adjoining Grammar



Tree Adjoining Grammar

$$S \rightarrow S S$$

 $S \rightarrow a$

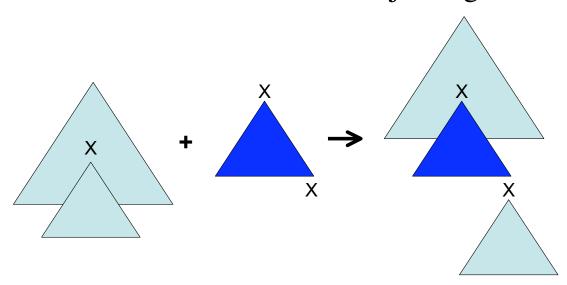


Lexicalization Through TAG

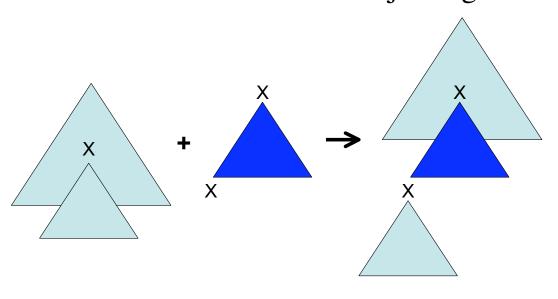
- This was an instructive example of how adjoining can be used to lexicalize CFGs while preserving the tree sets (strong generative capacity)
- (Joshi & Schabes, 1997) explain how every CFG can be strongly lexicalized by TAG
- (Joshi & Schabes, 1997) show that Tree-Adjoining Languages are closed under lexicalization: every TAL has a lexicalized TAG grammar

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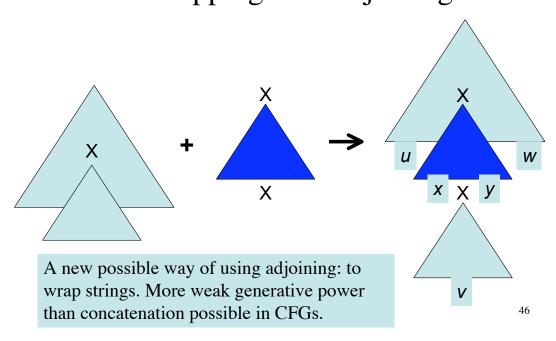
Tree-Insertion with adjoining



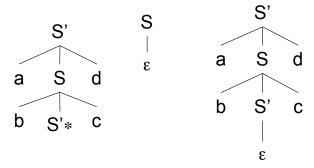
Tree-Insertion with adjoining



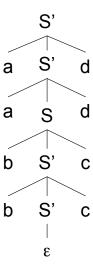
Wrapping with adjoining



Wrapping with Adjoining



This TAG can generate the language $L = \{ a^n b^n c^n d^n : n \ge 0 \}$ L is a context-sensitive language



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Motivation #3

Is Human Language Regular, Context-free or Beyond?

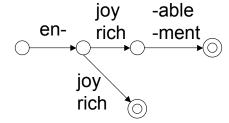
Natural Language & Complexity

- One notion of computational complexity: the complexity of various recognition and generation algorithms
- Another notion: the complexity of the description of human languages
- What is the lowest upper bound on the description of all human languages? regular, context-free or beyond?
- Describes a class of languages, including closure properties such as union, intersection, etc.
- Automata theory provides recognition algorithms, determinization, and other algorithms

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Grammar Size

- Consider the set of strings that includes *enjoy*, *enrich*, *enjoyable*, *enrichment* but not **joyable*, **richment*
- The CFG is clearly more compact
- Argument from learning:
 if you already know
 enjoyment then learning
 rich means you can
 generate enrichment as
 well



 $V \rightarrow X$

 $A \rightarrow X$ -able | X -ment

 $X \rightarrow en-NA$

 $NA \rightarrow joy \mid rich$

Regular grammars can be exponentially larger than equivalent CFGs

Sufficient Generative Capacity

- Does a formal grammar have sufficient generative capacity?
- Two cases: weak and strong generative capacity
- For strong GC: does the grammar permit the right kind of dependencies, e.g. nested dependencies
- For weak GC: usually requires some kind of homomorphism into a formal language whose weak GC can be determined (the formal language class should be closed under homomorphisms)

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Is NL regular: strong GC

- Regular grammars cannot derive nested dependencies
- Nested dependencies in English:
 - the shares that the broker recommended were bought N1 N2 V2 V1
 - the moment when the shares that the broker recommended were bought has passed
 N1 N2 N3 V3 V2 V1
- Can you provide an example with 4 verbs?
- Set of strings has to be infinite: competence vs. performance

Is NL regular: strong GC

- Assume that in principle we could process infinitely nested dependencies:
 competence assumption
- The reason we cannot is because of lack of memory in pushdown automata: performance can be explained
- CFGs can easily obtain nested dependencies

$$S \rightarrow a S b$$

 $S \rightarrow \varepsilon$

```
S1 ⇒ a1 S2 b1

⇒ a1 a2 S3 b2 b1

⇒ a1 a2 ... aN S bN ... b2 b1

⇒ a1 a2 ... aN bN ... b2 b1
```

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Is NL regular: Weak GC

- Consider the following set of strings (sentences):
 - -S = if S then S
 - -S = either S or S
 - -S = the man who said S is arriving today
- Map *if*, then to a and either, or to b
- Map everything else to the empty string
- This results in strings like *abba*, *abaaba*, or *abbaabba*

Is NL regular: Weak GC

- The language is the set of strings
 - L = { ww' : w from (a|b)* and w' is reversal of w }
- L can be shown to be non-regular using the pumping lemma for regular languages
- L is context-free

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Is NL context-free: Strong GC

- CFGs cannot handle crossing dependencies
- Dependencies like aN... a2 a1 bN... b2 b1 are not possible using CFGs
- But some widely spoken languages have clear cases of crossing dependencies
 - Dutch (Bresnan et al., 1982)
 - Swiss German (Shieber, 1984)
 - Tagalog (Rambow & MacLachlan, 2002)
- Therefore, in terms of strong GC, NL is not context-free

Is NL context-free: Weak GC

- Weak GC of NL being greater than context-free was harder to show, cf. (Pullum, 1982)
- (Huybregts, 1984) and (Shieber, 1985) showed that weak GC of NL was beyond context-free using examples with explicity case-marking from Swiss-German

```
mer d' chind em Hans es huus lönd hälfed aastriiche we children-acc Hans-dat house-acc let-acc help-dat paint-acc [ ( { ] ) }

this language is not context-free
```

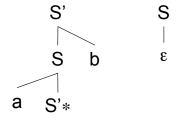
Generating Crossing Dependencies

```
1: S \rightarrow S B C
                              S1 \Rightarrow S2 B1 C1 (1)
2: S \rightarrow a C
                              ⇒ S3 B2 C2 B1 C1 (1)
3: a B \rightarrow a a
                              \Rightarrow a3 C3 B2 C2 B1 C1 (2)
4: C B \rightarrow B C
                              \Rightarrow a3 B2 C3 C2 B1 C1 (4)
5: B a \rightarrow a a
                              \Rightarrow a3 a2 C3 C2 B1 C1 (3)
                              \Rightarrow a3 a2 C3 B1 C2 C1 (4)
6: C \rightarrow b
                              \Rightarrow a3 a2 B1 C3 C2 C1 (4)
                              \Rightarrow a3 a2 a1 C3 C2 C1 (3)
                              \Rightarrow a3 a2 a1 b3 C2 C1 (6)
                              \Rightarrow a3 a2 a1 b3 b2 C1 (6)
                              \Rightarrow a3 a2 a1 b3 b2 b1 (6)
```

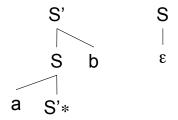
Simple Generation of Crossing Dependencies

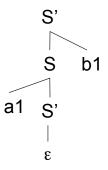
- Instead of using powerful swapping operations (corresponding to more powerful automata)
- We instead build local dependencies into elementary trees
- Strong GC: Crossing dependencies arise by simple composition of elementary trees
- The context-sensitive part is built into each elementary tree: the remaining composition is "context-free"
- Weak GC: Crossing dependencies = string wrapping

Crossing Dependencies with Adjoining



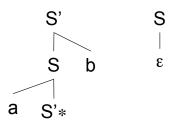
Crossing Dependencies with Adjoining

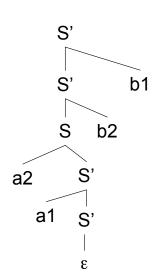




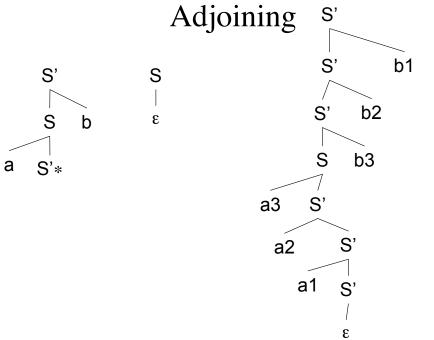
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Crossing Dependencies with Adjoining



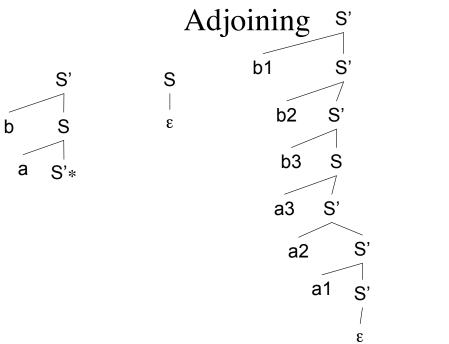


Crossing Dependencies with



Nested Dependencies with

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Tractable Descriptions

- Why not use context-sensitive grammars?
- For G, given a string x what is the complexity of an algorithm for the question: is x in L(G)?
 - Unrestricted Grammars/Turing machines: undecidable
 - Context-sensitive: NSPACE[n] linear non-deterministic space
 - Indexed Grammars: NP-complete
 - Tree-Adjoining Grammars: O(n⁶)
 - Context-free: O(n³)
 - Regular: O(n)

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Tractable Descriptions

- Another route to lexicalization of CFGs: categorial grammars (CG is not strongly equivalent to CFGs but can lexicalize them)
- Several different mathematically precise formal grammars were proposed to deal with the motivations presented here
- Some examples: head grammars (HG does string wrapping); combinatory categorial grammars (CCG; extends CG); linear indexed grammars (LIG; less powerful than indexed grammars)
- Using formal methods introduced with TAG, (Vijay-Shanker, 1987) and (Weir, 1988) showed that HG, CCG, LIG and TAG are all *weakly equivalent*!

Tree-Adjoining Grammars: Definition and Application to NL

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Tree-Adjoining Grammars

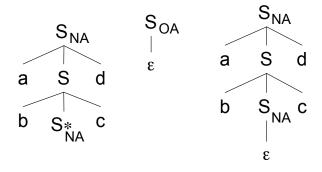
- A TAG G = (N, T, I, A, S) where
 - N is the set of non-terminal symbols
 - T is the set of terminal symbols
 - I is the set of initial or non-recursive trees built from N,
 T and domination predicates
 - A is the set of recursive trees: one leaf node is a nonterminal with same label as the root node
 - S is set of start trees (has to be initial)
 - I and A together are called *elementary trees*

Adjunction Constraints

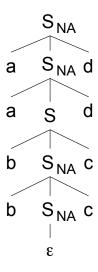
- Adjunction is the rewriting of a non-terminal in a tree with an auxiliary tree
- We can think of this operation as being "context-free"
- Constraints are essential to control adjunction: both in practice for NLP and for formal closure properties
- Three types of constraints:
 - null adjunction (NA): no adjunction allowed at a node
 - obligatory adjunction (OA): adjunction must occur at a node
 - selective adjunction (SA): adjunction of a pre-specified set of trees can occur at a node

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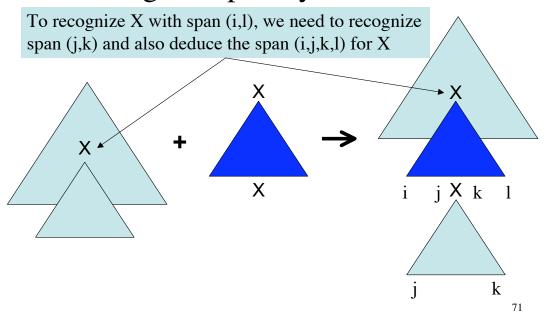
Adjunction Constraints



This TAG can generate the language $L = \{ a^n b^n c^n d^n : n \ge 1 \}$ Note that the OA & NA constraints are crucial to obtain the correct language



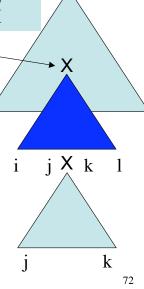
Parsing Complexity: CKY for TAG



Parsing Complexity: CKY for TAG

To recognize X with span (i,l), we need to recognize span (j,k) and also deduce the span (i,j,k,l) for X

- Each substring (i,l) can be a constituent, there are $O(n^2)$ substrings,
- \bullet For each of them we need to check for each non-terminal if it dominates an adjunction span (i,j,k,l)
- There are O(n⁴) such spans
- Hence we have complexity of recognizing membership of a string in a TAG to be O(n⁶)



TAG Formal Properties

(Vijay-Shanker, 1987)

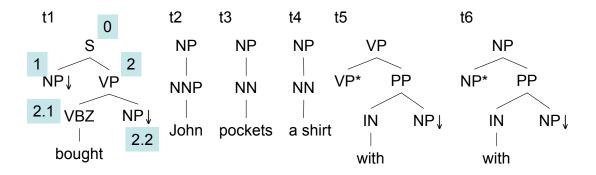
- Membership is in P: O(n⁶)
- Tree-Adjoining Languages (TALs) are closed under *union*, *concatenation*, *Kleene closure* (*), *h*, *h*-¹, *intersection with regular languages*, and *regular substitution*
- There is also a pumping lemma for TALs
- TALs are a full abstract family of languages (AFL)
- TALs are not closed under intersection, intersection with CFLs, and complementation

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Lexicalized TAG

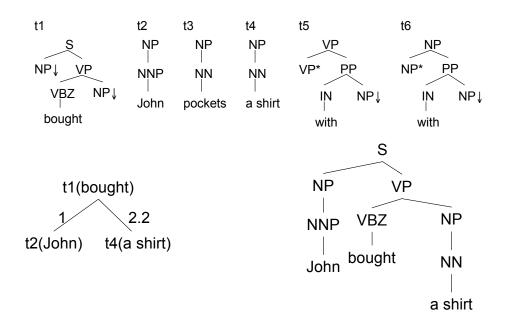
- A Lexicalized TAG (LTAG) is a TAG where each elementary tree has at least one terminal symbol as a leaf node
- A non-lexicalized TAG can always be converted to a lexicalized TAG (Joshi & Schabes, 1997)
- Lexicalization has some useful effects:
 - finite ambiguity: corresponds to our intuition about NL ambiguities,
 - statistical dependencies between words can be captured which can improve parsing accuracy

Lexicalized TAG: example



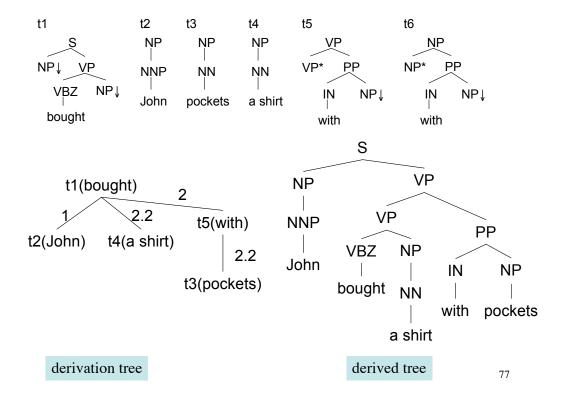
Gorn tree address: an index for each node in the tree

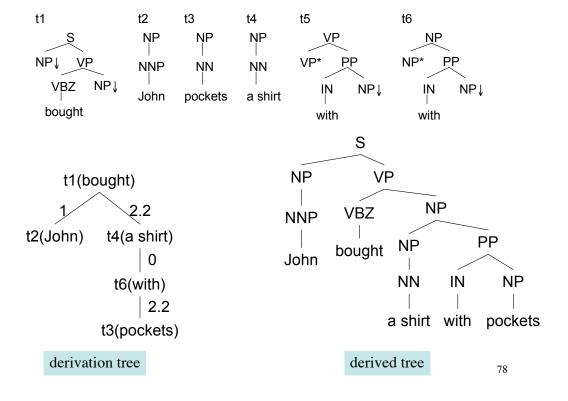
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derivation tree

derived tree





Comparison with Dependency Grammar

- Compare the derivation tree with the usual notion of a dependency tree
- Note that a TAG derivation tree is a formal representation of the derivation
- In a Lexicalized TAG, it can be interpreted as a particular kind of dependency tree
- Different dependencies can be created by changing the elementary trees
- LTAG derivations relate dependencies between words to detailed phrase types and constituency

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Localization of Dependencies

- Syntactic
 - agreement: person, number, gender
 - subcategorization: sleeps (null), eats (NP), gives (NP NP)
 - filler-gap: who_i did John ask Bill to invite t_i
 - word order: within and across clauses as in scrambling, clitic movement, etc.

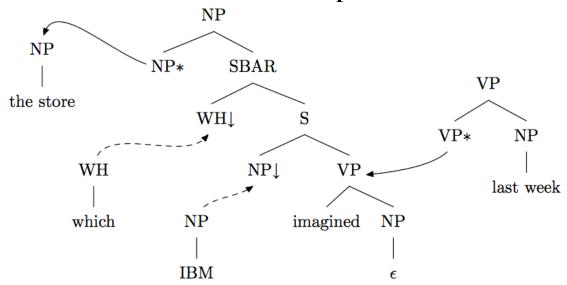
Localization of Dependencies

• Semantic

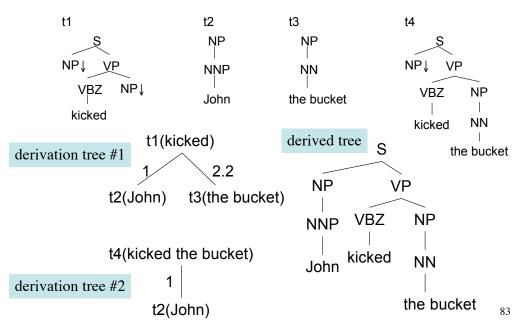
- function-argument: all arguments of the word that lexicalizes the elementary tree (also called the *anchor* or *functor*) are localized
- word clusters (word idioms): noncompositional meaning, e.g. give a cold shoulder to, take a walk
- word co-occurences, lexical semantic aspects of word meaning

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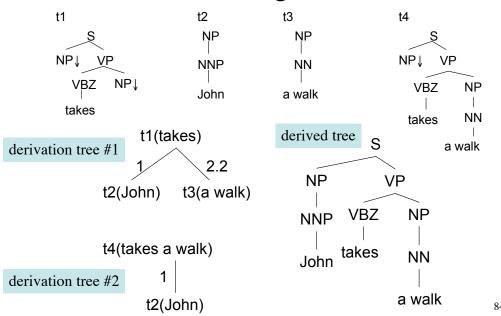
Localization of Dependencies



Idioms



Phrasal/Light Verbs



TAG and Generation

- TAG has some useful properties with respect to the problem of NL generation
- Adjunction allows a generation planning system to add useful lexical information to existing constituents
- Makes planning for generation output more flexible
 - e.g. if the system has a constituent *the book*, it can choose to add new information to it: *the red book*, if there is a distractor for that entity for the hearer
- cf. Matthew Stone's SPUD system

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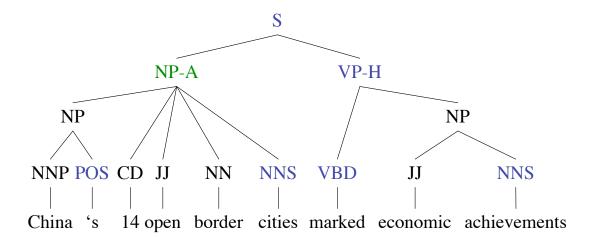
Mapping a TreeBank into Lexicalized TAG derivations

LTAG Derivations from TreeBanks

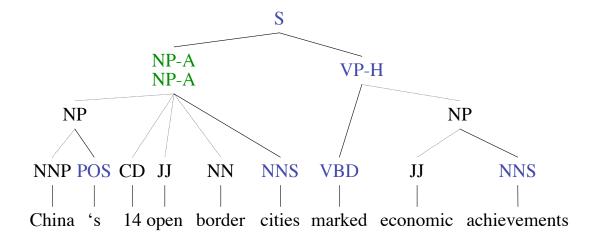
- TreeBanks contain phrase structure trees or dependency trees
- Converting dependency trees into LTAG is trivial
- For phrase structure trees: exploit head percolation rules (Magerman, 1994) and argument-adjunct heuristic rules
- First mark TreeBank tree with head and argument information
- Then use this information to convert the TreeBank tree into an LTAG derivation
- More sophisticated approaches have been tried in (Xia, 1999) (Chiang, 2000) and (Chen, 2000)

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LTAG derivations from TreeBanks

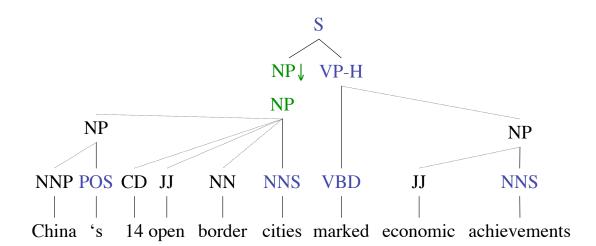


LTAG derivations from TreeBanks

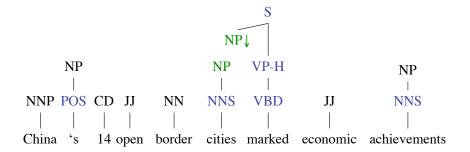


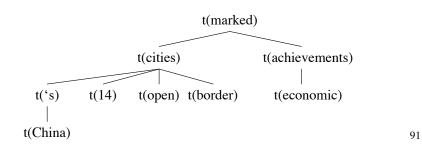
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LTAG derivations from TreeBanks



LTAG derivations from TreeBanks





Synchronous TAG

Synchronous TAG

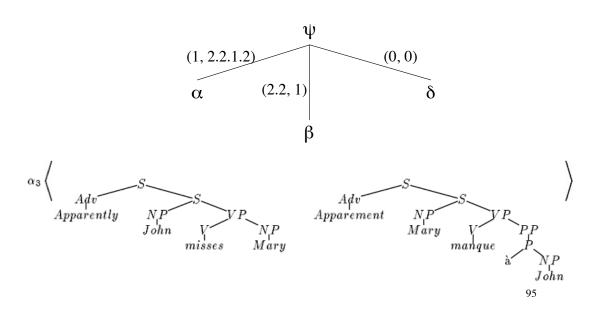
(Shieber, 1994)

- Just like TAG we have derivation trees
- Except each node in the derivation is not a single elementary tree but rather a pair of trees
- The derivation tree now can be used to build a pair of derived trees
- Synchronous TAG can be used to generate a pair of derived trees or map a source input string to target output string
- Applications: NL semantics (scope ambiguity, etc.) and syntax-based machine translation

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Synchronous TAG



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