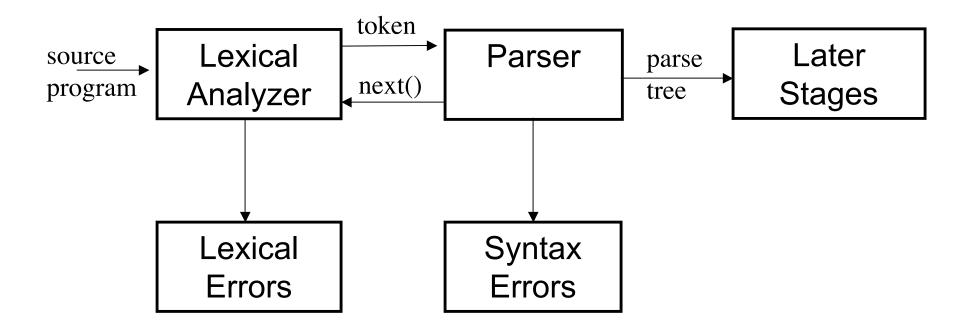
## CMPT 379 Compilers

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## Parsing



#### Context-free Grammars

- Set of rules by which valid sentences can be constructed.
- Example:

```
Sentence → Noun Verb Object
```

Noun → trees | compilers

Verb  $\rightarrow$  are | grow

Object → on Noun | Adjective

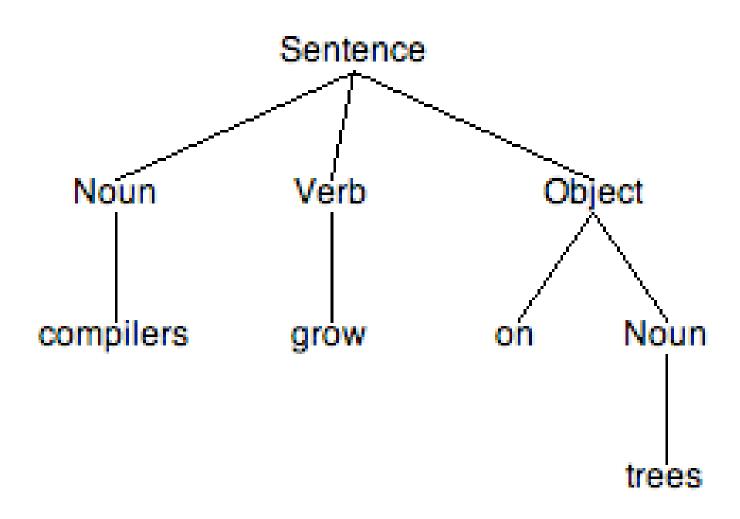
Adjective → *slowly* | *interesting* 

- What strings can Sentence derive?
- Syntax only no semantic checking

#### Derivations of a CFG

- compilers grow on trees
- compilers grow on Noun
- compilers grow Object
- compilers Verb Object
- Noun Verb Object
- Sentence

### Derivations and parse trees



#### Why use grammars for PL?

- Precise, yet easy-to-understand specification of language
- Construct parser automatically
  - Detect potential problems
- Structure and simplify remaining compiler phases
- Allow for evolution

#### **CFG** Notation

- A reference grammar is a concise description of a context-free grammar
- For example, a reference grammar can use regular expressions on the right hand sides of CFG rules
- Can even use ideas like comma-separated lists to simplify the reference language definition

#### Writing a CFG for a PL

- First write (or read) a reference grammar of what you want to be valid programs
- For now, we only worry about the structure, so the reference grammar might choose to over-generate in certain cases (e.g. bool x = 20;)
- Convert the reference grammar to a CFG
- Certain CFGs might be easier to work with than others (this is the **essence** of the study of CFGs and their parsing algorithms for compilers)

#### **CFG** Notation

Normal CFG notation

$$E \rightarrow E * E$$

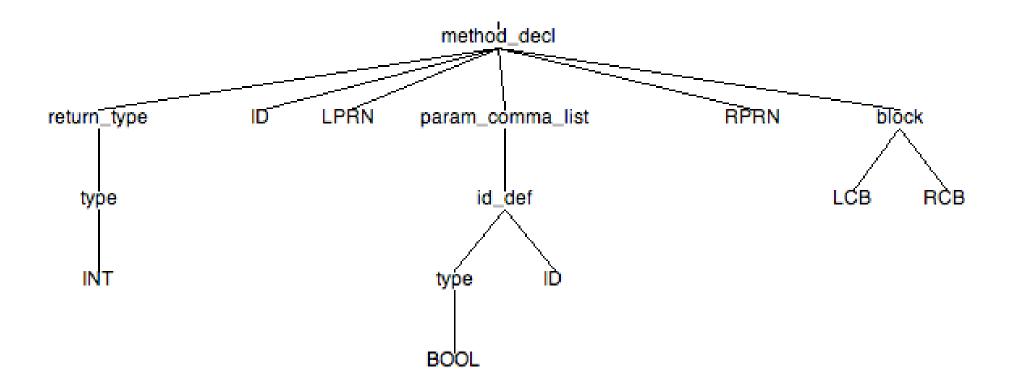
$$E \rightarrow E + E$$

Backus Naur notation

$$E := E * E | E + E$$

(an or-list of right hand sides)

## Parse Trees for programs



#### Arithmetic Expressions

• 
$$E \rightarrow E + E$$

- $E \rightarrow E * E$
- $E \rightarrow (E)$
- E → E
- E → id

# Leftmost derivations for id + id \* id

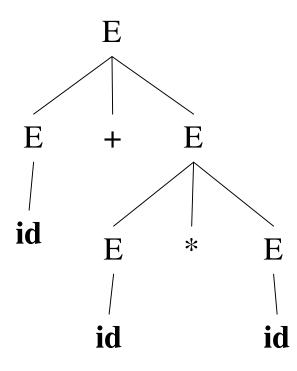
• 
$$E \Rightarrow E + E$$

$$\Rightarrow$$
 id + E

$$\Rightarrow$$
 id + E \* E

$$\Rightarrow$$
 id + id \* E

$$\Rightarrow$$
 id + id \* id



# Leftmost derivations for id + id \* id

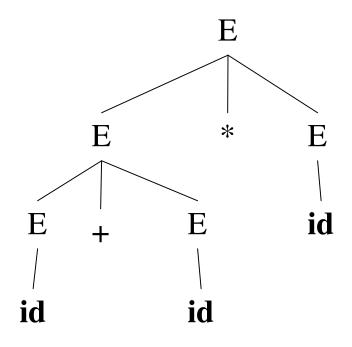
• 
$$E \Rightarrow E * E$$

$$\Rightarrow$$
 E + E \* E

$$\Rightarrow$$
 id + E \* E

$$\Rightarrow$$
 id + id \* E

$$\Rightarrow$$
 id + id \* id



#### Ambiguity

- Grammar is ambiguous if more than one parse tree is possible for some sentences
- Examples in English:
  - Two sisters reunited after 18 years in checkout counter
- Ambiguity is not acceptable in PL
  - Unfortunately, it's undecidable whether a grammar is ambiguous

## Ambiguity

- Alternatives
  - Massage grammar to make it unambiguous
  - Rely on "default" parser behavior
  - Augment parser
- Consider the original ambiguous grammar:

$$E \rightarrow E + E$$
  $E \rightarrow E * E$   
 $E \rightarrow (E)$   $E \rightarrow -E$   
 $E \rightarrow id$ 

 How can we change the grammar to get only one tree for the input id + id \* id

#### Dangling else ambiguity

• Original Grammar (ambiguous)

```
Stmt → if Expr then Stmt else Stmt
```

Stmt → if Expr then Stmt

Stmt → Other

• Unambiguous grammar

Stmt → MatchedStmt

Stmt → UnmatchedStmt

MatchedStmt → if Expr then MatchedStmt else MatchedStmt

MatchedStmt → Other

UnmatchedStmt → if Expr then Stmt

UnmatchedStmt → if Expr then MatchedStmt else UnmatchedStmt

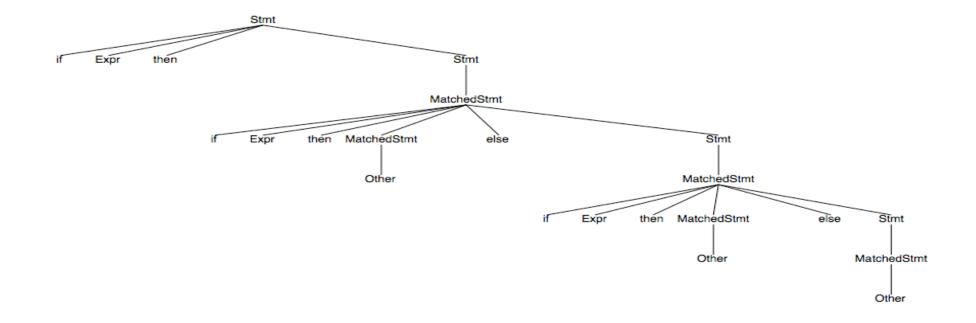
### Dangling else ambiguity

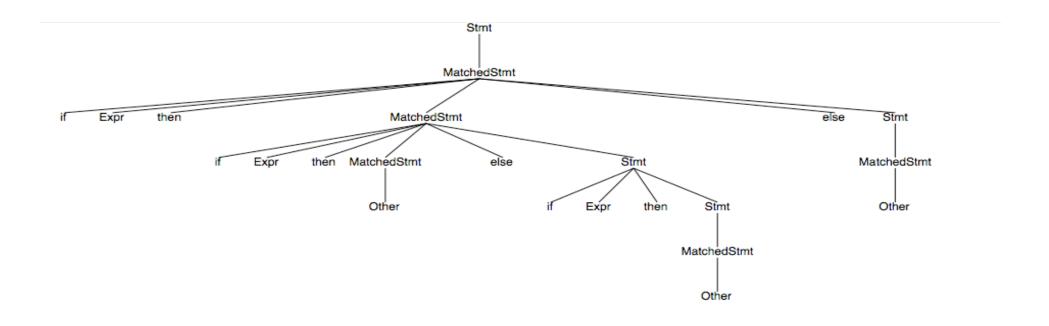
• Original Grammar (ambiguous)

```
Stmt → if Expr then Stmt else Stmt
Stmt → if Expr then Stmt
Stmt → Other
```

Modified Grammar (unambiguous?)

```
Stmt → if Expr then Stmt
Stmt → MatchedStmt
MatchedStmt → if Expr then MatchedStmt else Stmt
MatchedStmt → Other
```





#### Other Ambiguous Grammars

- Consider the grammar
  R→R'|'R|RR|R'\*'|'('R')'|a|b
- What does this grammar generate?
- What's the parse tree for  $a|b^*a$
- Is this grammar ambiguous?

#### Left Factoring

• Original Grammar (ambiguous)

```
Stmt → if Expr then Stmt else Stmt
Stmt → if Expr then Stmt
Stmt → Other
```

• Left-factored Grammar (still ambiguous):

```
Stmt \rightarrow if Expr then Stmt OptElse
Stmt \rightarrow Other
OptElse \rightarrow else Stmt | \epsilon
```

#### Left Factoring

• In general, for rules

$$A \to \alpha \beta_1 \mid \alpha \beta_2 \mid \ldots \mid \alpha \beta_n \mid \gamma$$

• Left factoring is achieved by the following grammar transformation:

$$A \to \alpha A' \mid \gamma$$

$$A' \to \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$$

#### Grammar Transformations

- Left Factoring
- Removing cycles:  $A \Rightarrow^+ A$
- Removing  $\varepsilon$ -rules of the form  $A \to \varepsilon$
- Eliminating left recursion
- Conversion to normal forms:
  - Chomsky Normal Form,  $A \rightarrow B C$  and  $A \rightarrow a$
  - Greibach Normal Form, A  $\rightarrow$  a  $\beta$

#### Eliminating Left Recursion

• Simple case, for left-recursive pair of rules:

$$A \rightarrow A\alpha \mid \beta$$

• Replace with the following rules:

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \epsilon$$

• Elimination of immediate left recursion

#### Eliminating Left Recursion

• Example:

$$E \rightarrow E + T, E \rightarrow T$$

• Without left recursion:

$$E \rightarrow T E_1, E_1 \rightarrow + T E_1, E_1 \rightarrow \varepsilon$$

• Simple algorithm doesn't work for 2-step recursion:

$$S \rightarrow A a, S \rightarrow b$$
  
 $A \rightarrow A c, A \rightarrow S d, A \rightarrow \epsilon$ 

#### Eliminating Left Recursion

• Problem CFG:

$$S \rightarrow A a, S \rightarrow b$$
  
 $A \rightarrow A c, A \rightarrow S d, A \rightarrow \varepsilon$ 

• Expand possibly left-recursive rules:

$$S \rightarrow A a$$
,  $S \rightarrow b$   
 $A \rightarrow A c$ ,  $A \rightarrow A a d$ ,  $A \rightarrow b d$ ,  $A \rightarrow \epsilon$ 

• Eliminate immediate left-recursion

$$S \rightarrow A \ a \ , S \rightarrow b$$
  
 $A \rightarrow b \ d \ A_1 \ , A \rightarrow A_1 \ , A_1 \rightarrow c \ A_1 \ , A_1 \rightarrow a \ d \ A_1 \ , A_1 \rightarrow \epsilon$ 

#### Non-CF Languages

- The pumping lemma for CFLs [Bar-Hillel] is similar to the pumping lemma for RLs
- For a string wuxvy in a CFL for  $u, v \neq \varepsilon$  and the string is long enough then  $wu^n xv^n y$  is also in the CFL for  $n \geq 0$
- Not strong enough to work for every non-CF language (cf. Ogden's Lemma)

#### Non-CF Languages

$$L_1 = \{wcw \mid w \in (a|b)*\}$$
 $L_2 = \{a^nb^mc^nd^m \mid n \ge 1, m \ge 1\}$ 
 $L_3 = \{a^nb^nc^n \mid n \ge 0\}$ 

#### CF Languages

$$L_4 = \{wcw^R \mid w \in (a|b)*\}$$
 $S \to aSa \mid bSb \mid c$ 
 $L_5 = \{a^nb^mc^md^n \mid n \ge 1, m \ge 1\}$ 
 $S \to aSd \mid aAd$ 
 $A \to bAc \mid bc$ 

#### Summary

- CFGs can be used describe PL
- Derivations correspond to parse trees
- Parse trees represent structure of programs
- Ambiguous CFGs exist
- Some forms of ambiguity can be fixed by changing the grammar
- Grammars can be simplified by left-factoring
- Left recursion in a CFG can be eliminated