## CMPT 413 Computational Linguistics

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## Minimum Cost Edit Distance

- String edit distance: what is the minimum number of changes (char insertions or deletions) to transform the string *intention* into *execution*?
- Assume cost of insertion is 1 and cost of deletion is 1

## Levenshtein Distance

- Cost is fixed across characters
  - Insertion cost is 1
  - Deletion cost is 1
- Two different costs for substitutions
  - Substitution cost is 1 (transformation)
  - Substitution cost is 2 (one deletion + one insertion)

#### **Edit Distance**

• Think of it as an alignment between target and source

$$t_1, t_2, \dots, t_n$$
 Find  $D(n,m)$  recursively  $s_1, s_2, \dots, s_m$ 

$$D(i,j) = min \begin{cases} D(i-1,j) & + \text{cost}(t_i,\emptyset) \text{ insertion into target} \\ D(i-1,j-1) + \text{cost}(t_i,s_j) \text{ substitution/identity} \\ D(i,j-1) & + \text{cost}(\emptyset,s_j) \text{ deletion from source} \end{cases}$$

$$D(0,0) = 0$$

$$D(i,0) = D(i-1,0) + \cot(t_i,\emptyset)$$

$$D(0,j) = D(0,j-1) + \cot(\emptyset,s_j)$$

```
Function MinEditDistance (target, source)
n = length(target)
m = length(source)
Create matrix D of size (n+1,m+1)
D[0,0] = 0
 for i = 1 to n
  D[i,0] = D[i-1,0] + insert-cost
 for j = 1 to m
  D[0,i] = D[0,i-1] + delete-cost
 for i = 1 to n
   for j = 1 to m
     D[i,j] = MIN(D[i-1,j] + insert-cost,
                  D[i-1,j-1] + subst/eq-cost,
                  D[i,j-1] + delete-cost)
 return D[n,m]
```

source

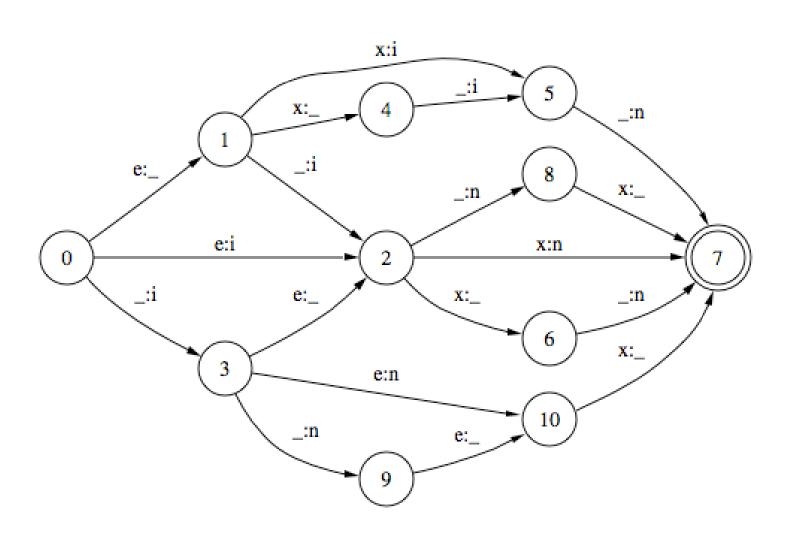
#### target

		g	a	m	b	1	e
	0	1	2	3	4	5	6
g	1	0	1	2	3	4	5
u	2	1	2,	3	4	5	6
m	3	2	3	$2_{e}$	3	4	5
b	4	3	4	3	$2_e$	3,	4
О	5	4	5	4	3	4	$5_s$

## Edit distance

- Useful in many NLP applications
- Comparing system output with human output, e.g. input: ibm output: IBM vs. Ibm
- Error correction
- Defined over character edits or word edits, e.g. MT evaluation:
  - Foreign investment in Jiangsu 's agriculture on the increase
  - Foreign investment in Jiangsu agricultural investment increased

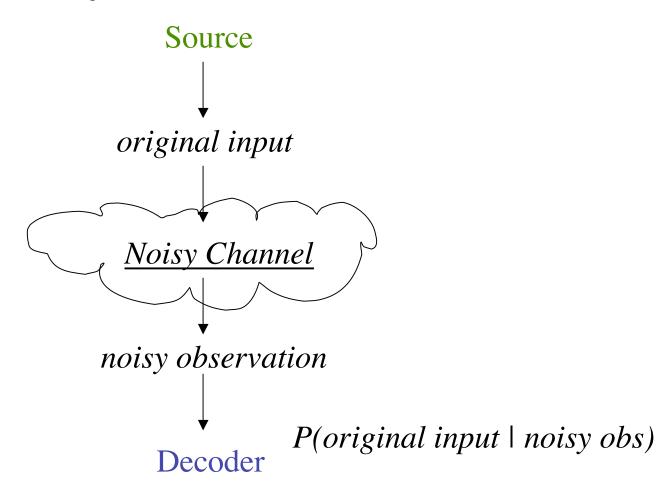
## Edit distance and FSTs



## Spelling Correction

- Types of spelling correction
  - non-word error detectione.g. *hte* for *the*
  - isolated word error detection
    - e.g. *acres* vs. *access* (cannot decide if it is the right word for the context)
  - context-dependent error detection (real world errors)
    - e.g. she is a talented acres vs. she is a talented actress

## Noisy Channel Model



## Bayes Rule: computing P(orig | noisy)

• let x = original input, y = noisy observation

$$p(x \mid y) = \frac{p(x,y)}{p(y)} \qquad p(y \mid x) = \frac{p(y,x)}{p(x)}$$

$$p(x,y) = p(y,x)$$

$$p(x \mid y) \times p(y) = p(y \mid x) \times p(x)$$

$$p(x \mid y) = \frac{p(y \mid x) \times p(x)}{p(y)} \qquad \underline{Bayes Rule}$$

## Chain Rule

$$p(a,b,c \mid d) = p(a \mid b,c,d) \times$$

$$p(b \mid c,d) \times$$

$$p(c \mid d)$$

Approximations: Bias vs. Variance

$$p(a \mid b, c, d) \approx p(a \mid b, c)$$
 less bias  $p(a \mid b)$   $p(a)$  more variance

## Single Error Spelling Correction

- Insertion (addition)
  - acress vs. cress
- Deletion
  - acress vs. actress
- Substitution
  - acress vs. access
- Transposition (reversal)
  - acress vs. caress

# Noisy Channel Model for Spelling Correction (Kernighan, Church and Gale, 1990)

• t is the typo and c is the correct word

$$P(c \mid t) = p(t \mid c) \times p(c)$$

Find the best candidate for the correct word

$$\hat{c} = \underset{c \in C}{\operatorname{arg max}} P(t \mid c) \times P(c)$$

$$P(t \mid c) = ?? P(c) = \frac{f(c)}{N}$$

Noisy Channel Model for Spelling Correction (Kernighan, Church and Gale, 1990) single error, condition on previous letter

$$P(t \mid c) = \begin{cases} \frac{del[c_{p-1}, c_p]}{chars[c_{p-1}, t_p]} & (xy)_c \text{ typed as } (x)_t \\ \frac{ins[c_{p-1}, t_p]}{chars[c_{p-1}]} & (x)_c \text{ typed as } (xy)_t \\ \frac{sub[t_p, c_p]}{chars[c_p]} & (y)_c \text{ typed as } (x)_t \\ \frac{rev[c_p, c_{p+1}]}{chars[c_p, c_{p+1}]} & (xy)_c \text{ typed as } (yx)_t \end{cases}$$

#### Noisy Channel model for Spelling Correction

- The del, ins, sub, rev matrix values need data in which contain known errors
   (training data)
- Accuracy on single errors on unseen data (test data)

#### Noisy Channel model for Spelling Correction

- Experiments: 87% accuracy for machine vs. 98% average human accuracy
- What are the limitations of this model?
  - ... was called a "stellar and versatile **acress** whose combination of sass and glamour has defined her ...

KCG model best guess is acres