Tiburon: A Weighted Tree Automata Toolkit

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Abstract. The availability of weighted finite-state string automata toolkits made possible great advances in natural language processing. However, recent advances in syntax-based NLP model design are unsuitable for these toolkits. To combat this problem, we introduce a weighted finite-state *tree* automata toolkit, which incorporates recent developments in weighted tree automata theory and is useful for natural language applications such as machine translation, sentence compression, question answering, and many more.

1 Introduction

The development of well-founded models of natural language processing applications has been greatly accelerated by the development of toolkits for finite-state automata. The influential observation of Kaplan & Kay, that cascades of phonological rewrite rules could be expressed as regular relations (equivalent to finite-state transducers) [1], was exploited by Koskenniemi in his development of the two-level morphology and accompanying system for its representation [2]. This system, which was a general program for analysis and generation of languages, pioneered the field of finite-state toolkits [3].

Successive versions of the two-level compiler, such as that written by Karttunen and others at Xerox [4], were used for large-scale analysis applications in many languages [3]. Continued advances, such as work by Karttunen in intersecting composition [5] and replacement [6, 7], eventually led to the development of the Xerox finite-state toolkit, which superseded the functionality and use of the two-level tools [3].

Meanwhile, interest in adding uncertainty to finite-state models grew alongside increased availability of large datasets and increased computational power. Ad-hoc methods and individual implementations were developed for integrating uncertainty into finite-state representations [8, 9], but the need for a general-purpose weighted finite-state toolkit was clear [10]. Researchers at AT&T led the way with their FSM Library [11] which represented weighted finite-state automata by incorporating the theory of semirings over rational power series cleanly into the existing

automata theory. Other toolkits, such as van Noord's FSA utilities [12], the RWTH toolkit [13], and the USC/ISI Carmel toolkit [14], provided additional interfaces and utilities for working with weighted finite-state automata. As in the unweighted case, the availability of this software led to many research projects that took advantage of pre-existing implementations [15–17] and the development of the software led to the invention of new algorithms and theory [18, 19].

While these toolkits are very robust and capable of development of a wide array of useful applications in NLP and beyond, they all suffer from the limitation that they can only operate on string-based regular languages. In the 1990s, this was begrudgingly accepted as sufficient — the power of computers and the relatively limited availability of data prevented any serious consideration of weighted automata of greater complexity, even though more complex automata models that better captured the syntactic nature of language had long been proposed [20]. As NLP research progressed and computing power and available data increased, researchers started creating serious probabilistic tree-based models for such natural language tasks as translation [21–23], summarization [24], paraphrasing [25], language modeling [26], and others. And once again, software implementations of these models were individual, one-off efforts that took entire theses worth of work to create [27]. An extension of the AT&T toolkit that uses approximation theory to represent higher-complexity structure such as context-free grammars in the weighted finite-state string automata framework was useful for handling certain representations [28], but a tree automata framework is required to truly capture tree models.

Knight and Graehl [29] put forward the case for the top-down tree automata theory of Rounds [20] and Thatcher [30] as a logical sequel to weighted string automata for NLP. All of the previously mentioned tree-based models fit nicely into this theory. Additionally, as Knight and Graehl mention [29], most of the desired general operations in a general weighted finite-state toolkit are applicable to top-down tree automata.

We thus propose and present a toolkit designed in the spirit of its predecessors but with the tree, not the string, as its basic data structure. Tiburon is a toolkit for manipulation of weighted top-down tree automata. It is designed to be easy to construct automata and work with them — after reading this article even a linguist with no computer

science background or a computer scientist with only the vaguest notions of tree automata should be able to write basic acceptors and transducers and understand how to make them more complex. To achieve these goals we have maintained simplicity in data format design, such that acceptors and transducers are very close to the way they appear in tree automata literature. We also provide a small set of generic but powerful operations that allow robust manipulation of data structures with simple commands that anyone can learn. In subsequent sections we present an introduction to the formats and operations in the Tiburon toolkit and demonstrate the powerful applications that can be easily built.

2 Related Work

The rich history of finite-state string automata toolkits was described in the previous section. Tree automata theory is extensively covered in [31]. Another treatment can be found in [32]. Timbuk [33] is a toolkit for unweighted finite state tree automata that has been used for cryptographic analysis. It is based on ELAN [34], a term rewriting computational system. MONA [35] is an unweighted tree automata tool aimed at the logic community. Probabilistic tree automata are originally due to [36].

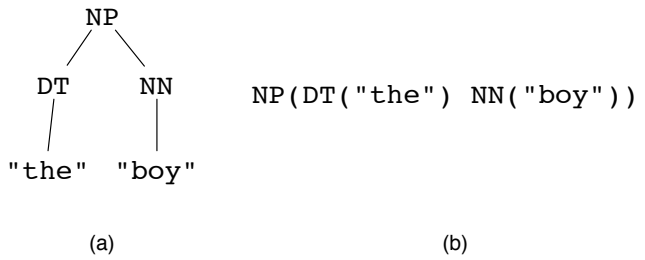

Fig. 1. (a) A typical syntax tree, and (b), its Tiburon representation

3 Trees

Tree automata represent sets of trees and tree relations. Formally, a tree is constructed from a ranked alphabet Σ. Each member of the alphabet is assigned one or more non-negative integers *rank* m, and Σ_m refers to all $x \in \Sigma$ with rank m. A tree over Σ is thus defined as:

– x, where $x \in \Sigma_0$, or

– $x(t_1, ...t_m)$, where $x \in \Sigma_m$ and $t_1, ..., t_m$ are trees over Σ.

Figure 1 shows a typical tree and its representation in Tiburon.

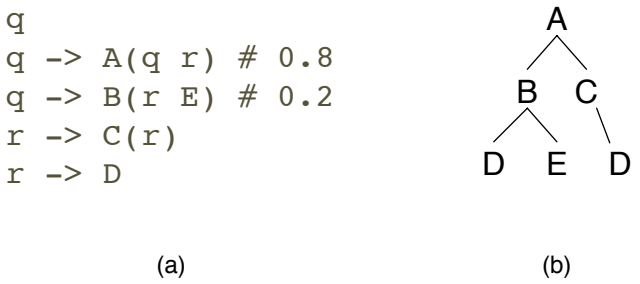

Fig. 2. (a) A regular tree grammar, and (b), a tree in the grammar's language

4 Regular Tree Grammars

As finite-state string acceptors recognize the same family of string languages as regular string grammars, so do finite-state tree acceptors recognize the same family of tree languages as regular tree grammars (RTG) [37]. For simplicity we favor the grammar representation, as tree acceptors must be written as hypergraphs, and this can be confusing. RTGs look very similar to context-free grammars (CFG) (in fact, a CFG is a special case of an RTG) and thus tend to be a very comfortable formalism. Analogous to their string counterpart, a weighted regular tree grammar (wRTG) recognizes a weighted, possibly infinite set of trees. Formally, a wRTG over Σ and under semiring $(\mathbb{K}, \oplus, \otimes, \bar{0}, \bar{1})$ consists of a finite set N of *nonterminal symbols* disjoint from Σ, a start symbol $s \in N$, and a set P of *productions* of the form $a \rightarrow r, \delta$, where $a \in N$, r is a tree over $\Sigma \cup N$, and $\delta \in \mathbb{K}$ is an associated weight. Informally, a wRTG "works" similar to a CFG in that from the start symbol, a sequence of rewrites is performed, replacing nonterminals with trees as specified by the productions, until the generated/recognized tree has no nonterminals remaining. To calculate the weight w of the resulting tree, start with $w = \bar{1}$ and for each production $p = a \rightarrow r, \delta$ used, let $w = w \otimes \delta$. Figure 2(a) shows a typical wRTG in Tiburon format. When weights are omitted on productions, a weight of $\bar{1}$ is assumed. Figure

2(b) shows one of the trees that this grammar recognizes. If we use the probability semiring, the tree has an associated weight of 0.16

```
qe
qe -> A(qe qo) # .1
qe -> A(qo qe) # .8
qe -> B(qo) # .1
qo -> A(qo qo) # .6
qo -> A(qe qe) # .2
qo -> B(qe) # .1
qo -> C # .1
```

(a)

```
B(C): 0.0100
A(C B(C)): 0.0008
B(A(C C)): 0.0006
A(B(C) C): 0.0001
B(B(B(C))): 0.0001
```

(b)

Fig. 3. (a) `even.rtg`, and (b) its top 5 dervations

4.1 Generation

One fundamental operation on a wRTG is the generation of trees that are in the grammar's language. Naturally, one might want to know the tree of highest weight in a grammar. Knuth's extension [38] of Dijkstra's classic best-path algorithm [39] to the hypergraph case efficiently finds the best path in the tree recognizer equivalent of a wRTG. However, in many cases it is desirable to obtain a *list* of trees, ordered by weight. A machine translation application may output a wRTG encoding billions of partial translations, and we may want to list the top scoring 25,000 trees in a subsequent reranking operation. The `-k` operation in Tiburon adapts the k-best paths algorithm of Huang and Chiang [40] to wRTGs. For example, given the grammar `even.rtg` depicted in Figure 3(a), we issue this command:

```
java -jar tiburon.jar -k 5 even.rtg
```

The five derivations with highest probability in the grammar are returned, as depicted in Figure 3(b).

Another operation, `-g`, stochastically generates trees from a grammar, probabilistically choosing states to expand until a tree is obtained or a threshold of expansion is reached. This operation is useful for diagnosis — designers of

```
q
q -> S(np vp)
np -> NP(dt nn)
np -> NP(dt jj nn)
dt -> the
dt -> a
jj -> funny
jj -> blue
jj -> strange
nn -> fish
nn -> carrot
vp -> VP(v np)
v -> ate
v -> created
```

(a)

```
S(NP(the carrot) VP(ate NP(a fish))): 1.0000
S(NP(the fish) VP(created NP(a carrot))): 1.0000
S(NP(a carrot) VP(created NP(the funny fish))): 1.0000
S(NP(the fish) VP(created NP(a carrot))): 1.0000
S(NP(a fish) VP(created NP(a fish))): 1.0000
```

(b)

Fig. 4. (a) `vic.rtg`, and (b) five random dervations

wRTGs may wish to verify that their wRTGs generate trees according to the distribution they have in mind. Given the grammar `vic.rtg`, depicted in Figure 4(a), we issue this command:

```
java -jar tiburon.jar -g 5 vic.rtg
```

Five random derivations are returned, as seen in Figure 4(b).

```
q3
q3 -> A(q1 q1) # .25
q3 -> A(q3 q2) # .25
q3 -> A(q2 q3) # .25
q3 -> B(q2)    # .25
q2 -> A(q2 q2) # .25
q2 -> A(q1 q3) # .25
q2 -> A(q3 q1) # .25
q2 -> B(q1)    # .25
q1 -> A(q3 q3) # .025
q1 -> A(q1 q2) # .025
q1 -> A(q2 q1) # .025
q1 -> B(q3)    # .025
q1 -> C        # .9
```

(a)

```
qe_q3
qe_q3 -> A(qo_q1 qe_q1) # 0.2000
qe_q3 -> A(qo_q3 qe_q2) # 0.2000
qe_q3 -> A(qo_q2 qe_q3) # 0.2000
qe_q3 -> B(qo_q2) # 0.0250
qe_q3 -> A(qe_q1 qo_q1) # 0.0250
qe_q3 -> A(qe_q3 qo_q2) # 0.0250
qe_q3 -> A(qe_q2 qo_q3) # 0.0250
qe_q2 -> A(qe_q3 qo_q1) # 0.0250
qe_q2 -> A(qe_q1 qo_q3) # 0.0250
qe_q2 -> A(qe_q2 qo_q2) # 0.0250
qe_q2 -> A(qo_q3 qe_q1) # 0.2000
qe_q2 -> A(qo_q1 qe_q3) # 0.2000
qe_q2 -> A(qo_q2 qe_q2) # 0.2000
qe_q2 -> B(qo_q1) # 0.0250
```

(b)

Fig. 5. (a) `three.rtg`, and (b) a portion of the intersection of `two.rtg` and `three.rtg`. The complete grammar has 43 productions.

4.2 Intersection

Weighted intersection of wRTGs is useful for subdividing large problems into smaller ones. As noted in [31], RTGs (and by extension wRTGs) are closed under intersection. Thus, a wRTG representing machine translation candidate

sentences can be intersected with another wRTG representing an English syntax language model to produce reweighted translations. As a simpler example, consider the grammar `even.rtg` described above, which produces trees with an even number of labels. The grammar `three.rtg` depicted in Figure 5(a) produces trees with a number of labels divisible by three. We obtain a grammar which produces trees with a number of labels divisible by six. by using the following command. A portion of that grammar is shown in Figure 5(b).

```
java -jar tiburon.jar even.rtg three.rtg
```

```
t
t -> D(q r) # 0.2
t -> D(q s) # 0.3
q -> A # 0.3
r -> B # 0.2
s -> B # 0.6
s -> C # 0.4
```

(a)

```
D(A B): 0.0540
D(A C): 0.0360
D(A B): 0.0120
```

(b)

```
Warning: returning fewer
trees than requested
D(A B): 0.0660
D(A C): 0.0360
```

(c)

Fig. 6. (a) Undeterminized grammar `undet.rtg`, (b) k-best list without determinization, and (c) k-best list with determinization

4.3 Weighted Determinization

wRTGs produced by automated systems such as those used to perform machine translation [41] or parsing [42] frequently contain multiple derivations for the same tree with different weight. This is due to the systems' representation of their result space in terms of weighted partial results of various sizes that may be assembled in multiple ways. This property is undesirable if we wish to know the total probability of a particular tree in a language. It is also frequently undesirable to have repeated results in a k-best list. The `-d` operation invokes May and Knight's weighted determinization algorithm for tree automata [43]. As an example, consider the grammar, `undet.rtg`, depicted in Figure 6(a). This grammar has two differently-weighted derivations of the tree `D(A B)`, as we see when the top three derivations are obtained, depicted in Figure 6(b). The following command determinizes the grammar and attempts to return the top three derivations in the resulting grammar:

```
java -jar tiburon.jar -d 5 -k 3 undet.rtg
```

Of course, since there are now only two derivations, only two trees are returned, as seen in Figure 6(c). The `-d 5` argument signifies the maximum time allowed for determinization, in minutes. Determinization is, in the worst case, an exponential-time operation, so it is helpful in practical matters to have the ability to abort lengthy operations.

4.4 Pruning

In real systems using large grammars to represent complex tree languages, memory and cpu time are very real issues. Even as computers increase in power, the added complexity of tree automata forces practitioners to combat computationally intensive processes. One way of avoiding long running times is to prune weighted automata before operating on them. One technique for pruning finite-state (string) automata is to use the forward-backward algorithm to calculate the highest-scoring path each arc in the automaton is involved in, and then prune the arcs that are only in relatively low-scoring paths [44].

We adapt this technique for tree automata by using an adaptation [45] of the inside-outside algorithm [46]. The `-p` option with argument x removes productions from a tree grammar that are involved in paths x times or more worse than the best path. We demonstrate pruning using the `-c` option to look at an overview of a grammar. The file `c1s4.determ.rtg` represents a language of possible translations of a chinese sentence. We inspect the grammar as follows:

```
java -jar tiburon.jar -m tropical -c c1s4.determ.rtg
Check info:
        113 states
        168 rules
        28 unique terminal symbols
        2340 derivations
```

Note that the `-m tropical` flag is used because this grammar is weighted in the tropical semiring. We prune the grammar and then inspect it as follows:

```
java -jar tiburon.jar -m tropical -p 8 -c c1s4.determ.rtg
Check info:
        111 states
        158 rules
        28 unique terminal symbols
        780 derivations
```

Since we are in the tropical semiring, this command means "Prune all productions that are involved in derivations scoring worse than the best derivation plus 8". This roughly corresponds to derivations with probability 2980 times worse than the best derivation. A quick check of the top derivations after the pruning (using `-k`) shows that the pruned and unpruned grammars do not differ in their sorted derivation lists until the 455th-highest derivation.

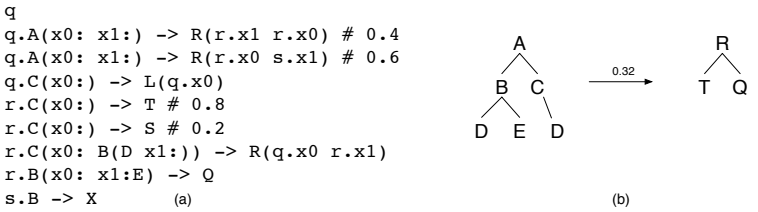

Fig. 7. (a) A tree-to-tree transducer, and (b), a weighted transduction licensed by the transducer

5 Tree Transducers

Top-down tree transducers in Tiburon come in two varieties: *tree-to-tree* [20, 30] and *tree-to-string* [47]. They represent the weighted transformation of a tree language into either a tree language or a string language, respectively. One can also think of transducers as representing a language of weighted tree/tree or tree/string pairs [48, 49]. We omit a formal definition of top-down tree transducers here; we refer the reader to [31] for a thorough treatment.

Figure 7(a) shows a sample tree-to-tree transducer in Tiburon format. Like a tree grammar, it has a start symbol and a set of optionally weighted productions. A transduction operation walks down an input tree, transforming it and recursively processing its branches. For example, the first production in Figure 7(a) means: "When in state q, facing an input subtree with root symbol A and two children about which we know nothing, replace it with an output subtree rooted at R with two children. To compute the output subtree's left child, recursively process the input subtree's right child with state r. To compute the output subtree's right child, recursively process the input subtree's left child with state r." Figure 7(b) shows one transduction licensed by this transducer. The format for tree-to-string transducers in Tiburon is similar to that for tree-to-tree transducers; the sole differences are the right side of productions are strings, not trees, and the special symbol `*e*` representing the empty string may be used.

Knight and Graehl [29] describe a wide hierarchy of transducer classes. Transducers in Tiburon are specifically *top-down transducers with extended left-hand sides*, also known as **xR** (or **xRs** for top-down extended left-hand side tree-to string transducers) in Knight and Graehl's hierarchy. top-down, or "root-to-frontier" (often abbreviated "R") transducers. This means the left side of productions can be trees of arbitrary depth. The sixth and seventh productions in Figure 7(a) show an example of extended left-hand side productions. There are no restrictions on copying or deleting of variable children; the seventh production shows an example of a deleted child. The xR and xRs class of transducers were specifically selected for Tiburon because of their good fit with natural language applications [20, 29].

5.1 Forward and Backward Application

Application is the operation of passing a tree or grammar onto a transducer and obtaining the resultant image. Tiburon supports forward application of a tree onto a tree-to-tree or tree-to-string transducer with the `-l` operation (for "left-side" transduction). If the transducer in Figure 7(a) is in a file `xr1.trans` the transduction performed in Figure 7(b) can be accomplished as follows:

```
echo "A(B(D E) C(D))" | java -jar tiburon.jar -l -s xr1.trans
q2
```

```
q2 -> R(q0 q1) # 0.4000

q1 -> Q # 1.0000

q0 -> S # 0.2000

q0 -> T # 0.8000
```

The `-s` flag tells Tiburon to expect the input tree from *stdin* instead of a file. As seen above, the image of a tree onto a tree-to-tree transducer is a wRTG. The image of a tree onto a tree-to-string transducer is a wCFG, currently represented in Tiburon as a one-state wRTG. The image of a wRTG onto the transducers supported in Tiburon is not a wRTG [31] and as such is currently not supported. However, limited versions of the transducers supported, such as transducers that do not copy their variables, do produce wRTG images [31]. We will soon release the next version of Tiburon, which will support the `-r` operation for backward application (the inverse image of a tree or wRTG onto a transducer is a wRTG, but this has not yet been implemented) and forward application of wRTGs onto limited classes of transducers.

5.2 Composition

We often want to build a cascade of several small transducers and then programmatically combine them into one. Unlike string transducers, general top-down tree transducers are not closed under composition, that is, a transduction carried out by a sequence of two transducers may not be possible with a single transducer. Engelfriet showed that top-down tree transducers that do not allow deletion or copying of variables (known as RLN transducers; the L signifies "linear" and the "N" signifies "non-deleting") are closed under composition [50]. Tiburon, however, allows composition of tree-to-tree transducers without checking if the transducers to be composed are composable. For example, consider the transducer below, which is in a file `xr2.trans`:

```
q

q.R(x0: x1:) -> R(R q.x1 R q.x0)

q.T -> B # 0.6
```

```
q.T -> D # 0.4

q.Q -> C

q.S -> E

q.X -> A
```

The following command composes `xr1.trans` with `xr2.trans` and passes a tree through them, returning the top three output derivations:

```
echo "A(B(D E) C(D))" | java -jar tiburon.jar -ls -k 3 \
    xr1.trans xr2.trans
R(R C R B): 0.1920
R(R C R D): 0.1280
R(R C R E): 0.0800
```

`xr1.trans` is not RLN, it is xRL (i.e. it has an extended left side and deletes variables but does not copy), but in this case the two transducers are composable. We believe that many of the xR transducers used in natural language applications will not suffer from the general noncomposability of their class.

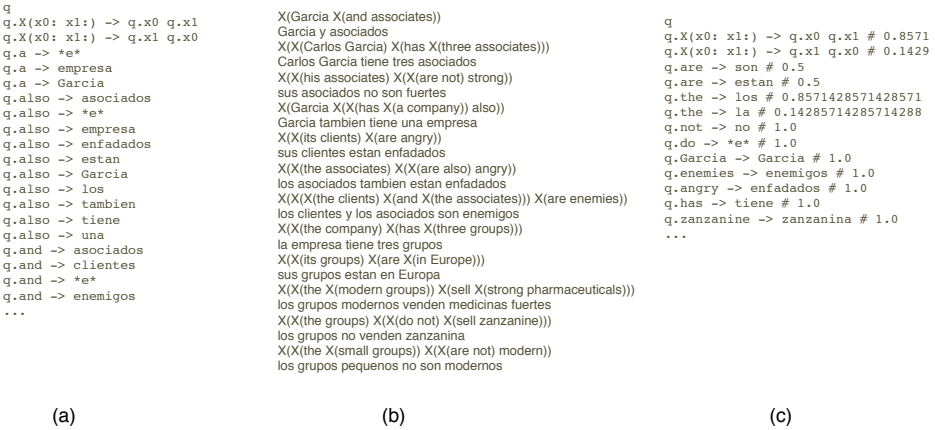

Fig. 8. (a) Portion of a 261-production unweighted tree-to-string transducer. (b) 15 (tree, string) training pairs. (c) Portion of the 31-production weighted tree-to-string transducer produced after 20 iterations of EM training (the remaining productions had probability 0).

5.3 Training

A common task in building tree transducer models is the assignment of appropriate weights to productions. We can use Expectation-Maximization training [51] to set the weights of an unweighted tree transducer such that they maximize the likelihood of a training corpus of tree/tree or tree/string pairs. Tiburon provides the `-t` operation, which implements the techinque decribed by Graehl and Knight for training tree transducers using EM [52].

As an example, consider training a machine translation model using bilingual input/output pairs. Given the 261-production unweighted tree-to-string transducer depicted in Figure 8(a) in file `y1.ts`, and the 15 tree/string pairs in Figure 8(b) in file `y1.train`, we run the command:

```
java -jar tiburon.jar -t 20 y1.train y1.trans
```

This produces the weighted tree-to-string transducer in Figure 8(c).

6 Applications Using Tiburon

We will next breifly describe two natural language applications that we have built using Tiburon.

6.1 The Yamada Translation Model

The translation model of Yamada and Knight [22] is a specialized model for predicting a Japanese string given an English tree. The custom implementation of this model, built by Yamada as part of his PhD thesis [27], took more than one year to complete. Graehl and Knight [52] showed how this model could be represented as a four-state tree-to-string transducer. We built an untrained transducer from Yamada's model and trained it on the same data used by Yamada and Knight to produce their alignment sentence pairs [22]. The complete process took only 2 days. For complete results we refer the reader to [53].

6.2 Japanese Transliteration

Knight and Graehl [54] describe a cascade of finite-state string transducers that perform English-Japanese transliteration. Of course, a weighted string transducer toolkit such as Carmel is well suited for this task, but Tiburon is suited for

the job as well. By converting string transducers into monadic (non-branching) tree transducers, we obtain equivalent results. We have used simple scripts to transform the string transliteration transducers into these monadic trees, and have been able to reproduce the transliteration operations. Thus, we see how Tiburon may be used for string-based applications as well as tree-based applications.

7 Conclusion

We have described Tiburon, a general weighted finite-state tree automata toolkit, and described some of its functions and their use in constructing natural language applications.

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