

**Towards imaging flow at the base of the mantle with
seismic, mineral physics and geodynamic constraints**

Andy Nowacki¹ and Sanne Cottaar²

¹School of Earth and Environment, University of Leeds, UK

²Department of Earth Sciences, University of Cambridge, UK

6 **Abstract**

7 Perhaps the least ambiguous signal that the mantle is convecting comes from observa-
 8 tions of seismic anisotropy—the variation of wave speed with direction—which must arise
 9 due to the ordering of material as deformation occurs. Therefore significant effort has
 10 been made over many years to infer the direction and nature of mantle flow from these
 11 data. Observations have focussed on the boundary layers of the mantle, where deforma-
 12 tion is expected to be strongest and where anisotropy is usually present. While prospects
 13 for mapping flow seem good, the lack of knowledge of several key issues currently holds
 14 progress back. These include the cause of anisotropy in the lowermost mantle, the causative
 15 material’s response to shear, and the single-crystal or -phase seismic properties of the
 16 causative materials. In this chapter we review recent observations of lowermost mantle
 17 anisotropy, constraints on mineral elasticity and deformation mechanisms, and challenges
 18 in linking geodynamic modelling with seismic observations.

19 **1 Introduction**

20 Seismic anisotropy, i.e. the variation of seismic velocity with propagation direction
 21 and polarisation, is observed in a number of regions within the Earth. The strength of
 22 anisotropy is particularly strong in the crust, at the top and the bottom of the mantle,
 23 and in the inner core (Mainprice, 2007). In the upper mantle, observed seismic anisotropy
 24 has been used to map asthenospheric flows (Becker and Lebedev, this volume) and un-
 25 derstand slab dynamics (Huang and Zhao, this volume). In the lowermost mantle, un-
 26 derstanding anisotropy in terms of flow is more elusive, as seismic observations are sparse,
 27 and mineral physical constraints more uncertain. The dynamics of the lowermost man-
 28 tle are of particular interest, as they reflect the lower thermal and mechanical bound-
 29 ary layer of the convecting mantle. Mapping flow directions in this region would signif-
 30 icantly help our understanding of the role of this boundary in mantle dynamics, and more
 31 specifically the role of the large low-shear velocity provinces (‘LLSVPs’) (Rudolph et al.,
 32 this volume).

33 Albeit challenging, significant efforts have been made to use seismic anisotropy to
 34 understand the underlying crystal preferred orientations (CPO) and flow directions (e.g.,
 35 Karato, 1998). This is based on the assumption that flow, and the internal crystallographic
 36 deformation mechanisms that accommodate the flow, cause alignment of intrinsically anisotropic
 37 crystals. This chapter offers a condensed review of seismic observations and mineral phys-

38 ical and geodynamical constraints on seismic anisotropy, and for a more in-depth review
 39 we refer to Nowacki et al. (2011) and Romanowicz & Wenk (2017). Here, we focus on
 40 the endeavours, mainly over the last decade, to tie these disciplines together and map
 41 flow directions in the lowermost mantle, and the specific challenges posed when compar-
 42 ing these results to seismic observations.

43 2 Observational constraints on lowermost mantle flow

44 2.1 Global tomographic models

45 A number of tomographic modellers invert for seismic anisotropy in the lowermost
 46 mantle. Inverting the full anisotropic elastic tensor (i.e., all 21 parameters) is unfeasi-
 47 ble. The only component of anisotropy generally inverted for in the lowermost mantle
 48 is the velocity difference between horizontally polarised shear velocity, V_{SH} , and verti-
 49 cally polarised shear velocity, V_{SV} . This component of anisotropy is named radial anisotropy
 50 (or vertically transverse isotropy) and the degree of anisotropy can be expressed by the
 51 value $\xi = V_{SH}^2/V_{SV}^2 = C_{66}/C_{44}$, where C is the Voigt matrix representation of elas-
 52 ticity and the 3-axis is vertical.

53 For the upper mantle, radial anisotropy is well constrained due to the unique sen-
 54 sitivities of the two types of surface waves ([Becker and Lebedev, this volume](#)). For the
 55 lower mantle, one or both of normal modes and body waves must be used. Normal mode
 56 inversions for 1D radial models show no significant component of ξ (Beghein et al., 2006;
 57 de Wit & Trampert, 2015). 3D tomographic models show a mainly isotropic lower man-
 58 tle with lateral variations in ξ on the order of 0.97–1.03 in the lowermost mantle (e.g.,
 59 Moulik & Ekstrom, 2014; Auer et al., 2014; Chang et al., 2015; French & Romanowicz,
 60 2015). There are strong differences between these models, some of which can be attributed
 61 to their treatment of the crust in the inversion, which is shown to affect the radial anisotropic
 62 signature of the lowermost mantle (Ferreira et al., 2010; Panning et al., 2010). In gen-
 63 eral, a geographical trend emerges where $\xi > 1$ (equivalently, $V_{SH} > V_{SV}$) in regions
 64 with fast shear wave velocity interpreted to be slab graveyards, and opposite signature
 65 of $\xi < 1$ is seen in regions of slow shear wave velocity, i.e. the LLSVPs. In Figure 1 this
 66 relationship is illustrated with histograms of ξ values for the fast and slow regions as in-
 67 terpreted by Cottaar & Lekić (2016), as well as a vote map of ξ values, which at each
 68 point at 2800 km depth shows the count of all tomography models which have a value

of ξ above or below 1. While all models show a significant shift in their histograms for the fast and slow region, the shifts between their mean values is small, with the largest shift of 1.1% in SEMUCBwm1, and the smallest shift of 0.38% in SAVANI. The vote map also suggests a relationship between dV_S and ξ . Interpreting this general trend should be done with caution as any relationship between dV_S and ξ could be an artefact of the inversion, specifically the negative ξ values appear prone to be leakage of the slow isotropic velocities (Chang et al., 2015). One thing that is interesting to note from the vote map is the smaller slow shear region beneath the Ural mountains, dubbed the Perm anomaly (Lekić et al., 2012), does not correlate directly with a signal of $\xi < 1$, but a small anomaly showing $\xi < 1$ appears offset to the south.

Studies are even more limited in constraining P wave radial anisotropy ($\phi = V_{PV}^2/V_{PH}^2 = C_{33}/C_{11}$). Global studies constraining 1D radial P wave anisotropy show no agreement in the likely signature (Beghein et al., 2006; de Wit & Trampert, 2015). Global 3D studies have often applied an assumed scaling between the S and P wave anisotropy as a starting model. When they do include P wave radial anisotropy independently (Soldati et al., 2003; Tesoniero et al., 2016), they judge their results not to be robust. Inversions using body waves are heavily under-constrained (Boschi & Dziewoński, 2000). The synthetic study of P. J. Koelemeijer et al. (2012) shows general sensitivity of normal modes to P wave anisotropy, although it also predicts it is sensitive to trade-offs.

A potential way forward for global studies lies in the understanding of a third anisotropic parameter, $\eta = C_{13}/(C_{11} - 2C_{44})$, which is related to the S and P velocities at intermediate incidence angles. de Wit & Trampert (2015) show that this parameter has a robust 1D signature of $\eta < 1$ across the lower 1000 km of the mantle. Kawakatsu (2015) suggests a rewrite of η for a more physical relationship with wave incidence angle, and shows that constraining this parameter, η_κ , can help resolve whether horizontally isotropic layers could cause the observed anisotropy.

104 2.2 Regional body wave observations

Locally, deep mantle seismic anisotropy can be observed through shear wave splitting of body waves. One of the main challenges is to determine the relative contribution to splitting from the uppermost and lowermost mantle, and whilst often assuming the rest of the lower mantle is isotropic. A general approach is to use two seismic phases with

comparable ray paths across the upper mantle, while one reference phase has a different or no ray path across the lowermost mantle. Ideally the reference phase shows no or minimal splitting and all splitting in the other phase can be attributed to the lowermost mantle. Otherwise corrections for splitting from the upper mantle need to be applied to attribute splitting to the lower mantle (e.g., Wookey et al., 2005).

One potential set consists of the ScS and S phases (Figure 2). For the distance range of 60–85°, the S phase turns above the lowermost mantle, while the ScS phase samples the lowermost mantle (e.g., Lay & Young, 1991; Wookey & Kendall, 2008). A second set is the SKS and SKKS phases (at epicentral distances 108–122°), for which the ray paths exit the core at different locations and converge across the mantle (e.g., Niu & Perez, 2004; Wang & Wen, 2007; M. Long, 2009). SKS–SKKS pairs have the additional advantages over S–ScS that in an isotropic or radially-anisotropic mantle they exit the core purely polarised along the SV component, and any anisotropy along the down-going leg of the path can be ignored. Their disadvantage is that both phases can accrue splitting in the lowermost mantle and in the upper mantle. At times it is difficult to retrieve splitting parameters and these phases are usually only used to highlight discrepant phase pairs (e.g., Deng et al., 2017).

Lastly, S_{diff} phases (at 100–130° distance) are compared either to S/ScS at shorter distances, or to SKKS (or SKS) at longer distances (e.g., Kendall & Silver, 1996; Vinnik et al., 1998). The SV component of the diffracted wave attenuates much faster than the SH along the core-mantle boundary, which means S_{diff} at large distances ($>\sim 120^\circ$) becomes a purely SH polarised wave, and any splitting can be attributed to the upgoing leg of the ray path (Cottaar & Romanowicz, 2013).

In all cases, caution is required in interpreting body-wave observations if modelled using approximate methods such as ray theory, since shear waves at the base of the mantle have a large region of finite-frequency sensitivity. For S_{diff} , travel time differences between SH_{diff} and SV_{diff} can arise for purely isotropic models, especially with strong isotropic velocity gradients as one might expect due to the thermal boundary layer, due to different finite-frequency sensitivity of the two components along the boundary (Maupin, 1994; Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi et al., 2018). ScS suffers to a lesser extent from finite-frequency effects in 1D models, but ray theoretical interpre-

tations can badly misrepresent the strength and orientation of anisotropy when lateral variations in anisotropy may exist (Nowacki & Wookey, 2016).

The different phases have different sensitivity to the anisotropic tensor due to their propagation angle and the length of their propagating path across the lowermost mantle (Figure 2). S_{diff} has long horizontal propagation paths in the mantle, and therefore good sensitivity to radial anisotropy. SKS propagates at sub-vertical angles (18°–33°) across the lowermost mantle, so splitting is caused by the component of azimuthal anisotropy, i.e. variation of wave speed in the horizontal plane. SKKS (40°–50°) and ScS (62°–78°) propagate at intermediate angles, and are sensitive to tilted anisotropy. While early studies focused mainly on constraining the radial anisotropic component (e.g., Young & Lay, 1990; Matzel et al., 1996; Garnero & Lay, 1997), recent studies interpret their observations as tilted anisotropy, the main component constrained when accounting for the incidence angles in the lowermost mantle (e.g., Thomas et al., 2007; Wookey & Kendall, 2008; Nowacki et al., 2010).

One additional, unique type of observation worth mentioning are polarity observations of phases bouncing off of the so-called D'' discontinuities in the lowermost mantle (Thomas et al., 2011; Cobden & Thomas, 2013; Creasy et al., 2019; Pisconti et al., 2019). Azimuthal variations in the polarity measurements suggest these are sensitive to underlying anisotropy. As observations can be applied to S and P reflections ('SdS', and 'PdP'), they are to our knowledge the only body wave studies that have resolved a component of both S and P wave anisotropy for a single location.

Most observational studies focus on a single observational method, as well as a single azimuthal direction. To sufficiently constrain anisotropy in a single location to uniquely interpret flow direction, multiple techniques need to be combined (Creasy et al., 2019). Efforts have been made to target a single region from multiple angles using ScS (Nowacki et al., 2010; Wookey & Kendall, 2008) and polarisation measurements (Thomas et al., 2011), as well as combining multiple angles with multiple body wave phases (Ford & Long, 2015; Creasy et al., 2019; Wolf et al., 2019).

2.3 Observed regional anisotropy

This is not an exhaustive overview of body wave studies and for a full table of studies we refer to Romanowicz & Wenk (2017). Here we highlight consistencies across these

studies, mainly focusing on more recent studies which benefit from increased coverage by seismic arrays. Regional body wave studies largely agree with tomographic models on geographical trends in radial anisotropy, i.e. $\xi > 1$ where isotropic velocities are fast, and $\xi < 1$ where isotropic velocities are slow (e.g., Wookey & Kendall, 2007; Kawai & Geller, 2010). Models interpreting tilted anisotropy have overwhelmingly sampled isotropically fast areas and many find a sub-horizontal fast axis and thus a component of $\xi > 1$ (e.g., Thomas et al., 2007; Garnero et al., 2004; Wookey & Dobson, 2008; Nowacki et al., 2010), while several studies find a fast axis which is tilted from the horizontal by around 45° (Wookey et al., 2005; Cottaar & Romanowicz, 2013), which is not compatible with radial anisotropy. Particularly, regions just outside of LLSVPs appear to have strong and variable anisotropy, as is observed along the boundaries of the African LLSVP (Wang & Wen, 2007; Cottaar & Romanowicz, 2013; Lynner & Long, 2014; Grund & Ritter, 2019; Romanowicz & Wenk, 2017; Reiss et al., 2019), the Pacific LLSVP (Deng et al., 2017), and the Perm Anomaly (M. D. Long & Lynner, 2015). These observations show stronger anisotropy outside of the LLSVP and little to no anisotropy within the LLSVP, both in terms of tilted anisotropy (Cottaar & Romanowicz, 2013) and in terms of azimuthal anisotropy (e.g., Lynner & Long, 2014; Grund & Ritter, 2019). A change in sign from $\xi > 1$ to $\xi < 1$ is also observed towards the base of the Icelandic plume (Wolf et al., 2019).

While some consistency emerges on the types of anisotropy, and correlations with isotropic velocities, uncertainty lies in the strength of anisotropy observed. Tomographic models contain radial anisotropy on the order of several %, and amplitudes vary between models (see Figure 1). Local observations interpret tilted anisotropy of 0.8–1.5% across a layer of 250 km beneath North America (Nowacki et al., 2010) and up to 8% across 150 km beneath the Antarctic Ocean (Cottaar & Romanowicz, 2013). Such variations could represent true geographical observations, but biases could also occur as propagation angles used might not be optimal to observe the strongest splitting or assumed layer thicknesses. In these two example studies, interpreted amplitudes might also differ as one is interpreted ray-theoretically (Nowacki et al., 2010) and one by forward modelling (Cottaar & Romanowicz, 2013). Potentially, consistently constrained relative amplitudes in splitting might help map lateral variations in flow strength or direction.

210 **3 Forward modelling**

211 To provide synthetic tests for the hypothesis that anisotropy is caused by crystal
 212 preferred orientation (CPO), multi-disciplinary models are built that span many spa-
 213 tial scales (see flow chart in Figure 3). Geodynamic models provide maps of strain across
 214 10s to 1000s of km. The strain observed is accommodated on the micro scale by defor-
 215 mation mechanisms in a set of crystals, assuming a degree is accommodated by dislo-
 216 cation glide to create preferential orientation. The individual elastic constants of each
 217 of the deformed set of crystals are averaged using their orientations, giving the fully anisotropic
 218 tensor for a single location. This process needs to be repeated for many locations, to pro-
 219 vide an anisotropic model with signatures that can be observed over 10s or 100s of km
 220 by seismic waves. Here we explain the main choices and assumptions made in these mod-
 221 els.

222 While we focus on the hypothesis that CPO is the cause of seismic anisotropy in
 223 the lowermost mantle, studies have forward modelled the potential of shape preferred
 224 orientation (SPO) as well. SPO anisotropy is caused by layering or inclusions of strongly
 225 heterogeneous (but potentially intrinsically isotropic) material (Kendall & Silver, 1998;
 226 Hall et al., 2004; Creasy et al., 2019; Reiss et al., 2019). In the case of inclusions, anisotropy
 227 can be observed in the effective medium to which the waves are sensitive if a degree of
 228 alignment or preferred orientation persists over a broad area. This alignment of inclu-
 229 sions would result from local deformation, and thus also contain information about man-
 230 tle flow. However, studies observing high frequency scatterers in the lowermost mantle
 231 observe very weak velocity contrasts (<0.1%: Mancinelli & Shearer, 2013). Extremely
 232 strong isotropic velocity anomalies (10–30%) are only observed in thin patches of sev-
 233 eral 10s of km on top of the core–mantle boundary, the so-called ultra-low velocity zones
 234 (e.g., Garnero et al., 1998; Yu & Garnero, 2018).

239 **3.1 Geodynamic models**

240 Assumptions on the flow occurring in the lowermost mantle have varying degrees
 241 of complexities. In the simplest of models, horizontal flow is assumed causing simple hor-
 242 izontal shear as one might expect in a iso-chemical thermal boundary layer (as used in
 243 Wookey & Kendall, 2007). Anisotropy observed, however, does not have to represent lo-
 244 cal deformation, but could represent fossilized anisotropy. Anisotropic material can be

245 formed elsewhere and be transported and rotated without overriding the preferred orientation.
246 Therefore it is important to track the history of deformation for material in
247 a given location. To represent change in flow direction in downwellings and upwellings
248 in the lowermost mantle, corner flow streamlines can be used (Tommasi et al., 2018).

249 A range of studies use fully numerical models, where a number of assumptions on
250 parameters for the lower mantle need to be made. The history of deformation is tracked
251 by passive tracers that are advected through the model and record the velocity gradient
252 at each step. The deformation history is generally used from the top of the lower mantle
253 (e.g., Cottaar et al., 2014), or from the bridgemanite to post-perovskite transition (e.g
254 Walker et al., 2011).

255 In one approach (Cottaar et al., 2014; Chandler et al., 2018), the CitcomS program
256 (Zhong et al., 2000) is used to solve for the conservation of mass, momentum and en-
257 ergy, in a system that is heated from below, and where a slab is forced down from the
258 top. Tracers are introduced at the top of the slab, and a large number of them eventu-
259 ally end up in the lowermost mantle, although the final distribution is irregular and shows
260 clumping of tracers.

261 In a different approach (Walker et al., 2011; Nowacki et al., 2013), the flow field
262 is the instantaneous flow predicted by isotropic wave velocities, the gravity field, a 1D
263 viscosity model, and other geophysical constraints (Simmons et al., 2009). Because the
264 inversion assumes that flow does not change with time, regularly-spaced tracers can be
265 back-propagated to the top of D'' across the flow field, after which they are forward prop-
266 agated to track the deformation along the path. The advantage of this method is that
267 one retrieves a regularly-sampled global anisotropic model that holds some potential re-
268 lationship to the isotropic velocities, and that can thus be compared to global or regional
269 seismic observations. Additionally, this method tests a prior assumed relationship be-
270 tween isotropic velocities and the flow field, testing models of thermal and/or thermo-
271 chemical heterogeneity in the lower mantle.

272 While these geodynamical models represent test cases to explain lowermost seis-
273 mic anisotropy, they are simplified in many ways. The geodynamical models have not
274 explicitly included the bridgemanite to post-perovskite transitions, which only has a small
275 density jump (Murakami et al., 2004; Oganov & Ono, 2004), but would cause significant
276 viscosity weakening (Hunt et al., 2009) and allow slab material to spread more easily (Nak-

277 agawa & Tackley, 2011). The viscosity model would be even more complex if the forma-
 278 tion of CPO could be fed back into the geodynamical model creating anisotropic viscos-
 279 ity. So far, models have not tested the hypothesis of LLSVPs representing a different com-
 280 position (e.g., Garnero et al., 2016), which appears important to understand the later-
 281 ally varying anisotropy around LLSVP boundaries.

282 **3.2 Mineralogical constraints**

283 In the upper mantle, the mineral olivine is abundant, and, with a highly anisotropic
 284 crystal, represents a straightforward candidate to explain CPO anisotropy ([Becker and](#)
 285 [Lebedev, this volume](#)). For the lowermost mantle the debate is still open as to which min-
 286 eral or polymineralic assemblage can explain the observed anisotropy. For a candidate
 287 mineral or assemblage, we need to know its single crystal elasticity, which depending on
 288 crystal symmetry can be described by three to 21 independent parameters. We mostly
 289 rely on first-principle or *ab initio* calculations which solve the electronic Schrödinger equa-
 290 tion to obtain the crystal structure and the elasticity at high pressures and temperatures
 291 ([Buchen, this volume](#)). Merely obtaining isotropic average elasticity information from
 292 experiments under these extreme conditions is very challenging, let alone measuring the
 293 independent anisotropic parameters (e.g., Marquardt et al., 2009; Finkelstein et al., 2018).

294 Additionally, we need to know how the candidate mineral or assemblage deforms
 295 ([Miyagi, this volume](#)). To create seismic anisotropy, a mineral must significantly deform
 296 by dislocation glide. In dislocation glide, dislocations within the crystal move along crys-
 297 tallographic planes. Preferred orientation results when crystals rotate to accommodate
 298 glide along its weakest glide planes. Other mechanisms like diffusion creep or disloca-
 299 tion climb are not usually thought to cause preferred orientation, though this is not al-
 300 ways the case (Wheeler, 2009, 2010; Dobson et al., 2019). If dislocation glide is the pre-
 301 fered mechanism, the next question that arises is what are the relative strengths of the
 302 different slip systems (i.e., glide plane and slip directions). Calculations explore the rel-
 303 ative strengths of different deformation mechanisms and glide systems by calculating lat-
 304 tice friction and forces required to slip a dislocation (Peierls stress) in atomistic mod-
 305 els (Walker et al., 2010; Cordier et al., 2012). Experimentally, slip system activities can-
 306 not usually be measured for single crystals of the phases of interest here. Instead, ma-
 307 terials are deformed under compressive or shear stress in a large-volume apparatus (usu-
 308 ally on analogue materials), or in a diamond-anvil cell (For further details ?Romanow-

icz & Wenk, 2017) The resulting deformation may be imaged by X-ray diffraction. Dominant slip systems may be estimated by inspection of the orientation distribution functions (ODFs) of the crystallographic planes of interest, or inverted for by comparing forward calculations of the experimental deformation with the results obtained.

To determine macroscopic anisotropy from these mineralogical constraints, the set of slip systems are combined with a deformation tensor to model a set of deformed crystals. Most often this is done using a homogenisation method such as the viscoplastic self-consistent method (VPSC; Lebensohn & Tomé, 1993).

Forming the majority of the lowermost mantle, and thus the likeliest candidates to be the anisotropy-causing phases, are bridgmanite, post-perovskite and ferropericlase.

3.2.1 Bridgmanite

Bridgmanite, $(\text{Mg}, \text{Fe})\text{SiO}_3$ -perovskite, is the most abundant mineral in the lower mantle (and in the Earth). Its pure Mg-endmember shows $\sim 11\%$ P wave and up to 15% S wave anisotropy (Oganov et al., 2001; Wentzcovitch et al., 2006; Stackhouse, Brodholt, Wookey, et al., 2005), and shows little (Li et al., 2005; Zhang et al., 2016) or variable (Fu et al., 2019) variation with the inclusion of iron.

There are mixed results on bridgmanite being a suitable candidate to explain anisotropy. Both experiments and calculations proposed a dominant glide plane of (001) (Wenk et al., 2004; Merkel et al., 2007; Ferré et al., 2007) which results in the opposite radial anisotropy to that observed (e.g., Wenk et al., 2011), while other experiments and calculations argue for a dominant (100) glide plane (Mainprice et al., 2008; Tsujino et al., 2016), which can create the observed $V_{SH} > V_{SV}$ in simple shear. Miyagi & Wenk (2016) report a change from (001)-dominated glide to (100) around 55 GPa.

Bridgmanite is also known to be a very strong mineral. Experiments deforming a multi-phase mixture of bridgmanite and a smaller fraction of the weaker phase ferropericlase (or analogs), show in some cases that the ferropericlase takes up the majority of the deformation (Girard et al., 2016; Kaercher et al., 2016; Miyagi & Wenk, 2016), while in others the strong bridgmanite phase still dominates deformation (Wang et al., 2013) in line with simulations in a finite element model (Madi et al., 2005). Recently atomistic calculations have shown that the resistance to dislocation glide is very high, and dis-

location climb should dominate (Boioli et al., 2017). Dislocation climb dominance could explain the general lack of anisotropy across most of the lower mantle, as well the high viscosity of the lower mantle (Reali et al., 2019). However, attempts to explain weak anisotropy around ponded subducted slabs in the uppermost lower mantle in terms of bridgmanite CPO (Tsujino et al., 2016; Walpole et al., 2017; Ferreira et al., 2019; Fu et al., 2019) would be therefore puzzling.

345 *3.2.2 Post-perovskite*

Post-perovskite is a high-pressure polymorph of bridgmanite, which could become stable in the lowermost mantle (Murakami et al., 2004; Oganov & Ono, 2004). Compared to bridgmanite, post-perovskite is (1) more anisotropic (Iitaka et al., 2004; Stackhouse, Brodholt, & Price, 2005; Wentzcovitch et al., 2006; Zhang et al., 2016), and (2) much weaker to deform (Hunt et al., 2009; Ammann et al., 2010; Goryaeva et al., 2016). Therefore it is an attractive candidate to explain anisotropy observed in the lowermost mantle. If, and to what degree, post-perovskite is actually stable at the pressures in the lowermost mantle is still up for debate (see overviews in Cobden et al. (2015) and Hirose et al. (2015)), but invoking the presence of post-perovskite helps explain S-to-P velocity ratios in the lowermost mantle (P. Koelemeijer et al., 2018). If present, the strongly positive Clapeyron slope of its phase transition from bridgmanite implies post-perovskite is stable in a thicker layer in cold regions than in hot regions (Oganov & Ono, 2004; Tsuchiya et al., 2004). Potentially post-perovskite becomes unstable again in the thermal boundary layer close to the core-mantle boundary, creating a lens of post-perovskite (Hernlund et al., 2005).

Testing post-perovskite as a candidate to explain anisotropy is difficult as the preferred slip system of post-perovskite is uncertain and diamond-anvil cell experimental results have varied widely over the past 15 years (For further details, see ?, in this volume.). The most recent results can be split in two categories. Experiments using MgSiO_3 post-perovskite, and MnGeO_3 or MgGeO_3 analogs, show a preferred slip plane of (001) (e.g., Miyagi et al., 2010; Hirose et al., 2010; Nisr et al., 2012; X. Wu et al., 2017). Experiments using CaIrO_3 postperovskite as an analog show a dominant slip system of [100](010) (where $[hkl]$ gives the Burgers vector; e.g., Yamazaki et al., 2006; Niwa et al., 2012; Hunt et al., 2016). Atomistic models confirm the results of the latter category, showing both slip systems [100](010) and [001](010) (Cordier et al., 2012; Goryaeva et al., 2015, 2017)

as well as the occurrence of twinning $1/2 < 110 > \{1\bar{1}0\}$ (Carrez et al., 2017). Additionally, it is suggested that post-perovskite could inherit preferred orientation or texture through the phase transition from bridgmanite (Dobson et al., 2013). Interpretation of the texture inheritance in deformation experiments has been specifically argued to explain part of the variation in interpreted preferred glide plane (e.g., Walte et al., 2009; Miyagi et al., 2011). This could only be the case if bridgmanite forms CPO texture due to dislocation glide, which is debatable (Boioli et al., 2017). A more feasible scenario is bridgmanite inheriting texture from post-perovskite in a reverse transition which could occur in the hotter regions (Dobson et al., 2013; Walker et al., 2018).

The importance of the incorporation of aluminium and iron into post-perovskite for our purposes depends on its effect on the stability field, deformation mechanisms, rheology and single-crystal anisotropy of the non-endmember phase. Iron- and aluminium-bearing post-perovskite is likely to be as anisotropic as the magnesian end-member at lowermost mantle conditions (??Zhang et al., 2016), but there is little evidence for its effect on plasticity. Recent work suggests that iron will strongly partition into ferropericlase in the lowermost mantle in any event (?), thus its importance may be limited.

3.2.3 Ferropericlase

Ferropericlase ($\text{Mg}, \text{Fe}\text{O}$) is present in the lower mantle with a molar abundance of 10–30% (e.g., McDonough & Sun, 1995). Before post-perovskite was discovered in 2004, ferropericlase was already considered a potential explanation of lowermost mantle anisotropy (Yamazaki & Karato, 2002). It is cubic, and its elasticity can thus be described by three independent parameters. These are constrained both through *ab initio* calculations (Karki et al., 2000; Z. Wu et al., 2013) and through experiments (e.g., Jackson et al., 2006). The results of these studies show significant single crystal anisotropy, as well as an increase of anisotropy with Fe content, related to changes in C_{12} and C_{44} with cell volume via pressure (Marquardt et al., 2009; Antonangeli et al., 2011; Finkelstein et al., 2018).

Ferropericlase is much weaker than bridgmanite (Cordier et al., 2012). Atomistic calculations of pure MgO endmember have shown dominating slip systems of $\langle 110 \rangle \{1\bar{1}0\}$ and $\langle 110 \rangle \{100\}$ (Carrez et al., 2009; Amodeo et al., 2011, 2016). Experiments on pure MgO (Merkel et al., 2002; Girard et al., 2012) and $(\text{Mg}, \text{Fe})\text{O}$ (Lin et al., 2009) show dominant slip on $\langle 110 \rangle \{1\bar{1}0\}$, while higher temperature experiments on $(\text{Mg}, \text{Fe})\text{O}$ also ac-

tivate $\langle 110 \rangle \{100\}$, consistent with the calculations. Whether ferropericlase can explain the observed anisotropy depends on the degree of single crystal anisotropy (related to the Fe content), its abundance in the lowermost mantle (i.e. whether ferropericlase grains become interconnected), and the general strength contrast between ferropericlase and bridgmanite or post-perovskite. However, it should be noted that even in the two-phase experiments discussed earlier, where ferropericlase takes up the bulk of the deformation, coherent CPO does not develop in the ferropericlase, potentially due to the polyphase geometry causing strain heterogeneity in the ferropericlase crystals (Kaercher et al., 2016; Miyagi & Wenk, 2016).

411 3.2.4 Other phases

Whilst post-perovskite, bridgmanite and ferropericlase are expected to dominate the lowermost mantle, it is possible that other phases play a role in causing anisotropy.

Though peridotite comprises ~5% of Ca-perovskite (CaMgSiO_3) in the lower mantle, basaltic compositions may hold up to 30% (McDonough & Sun, 1995), and hence Ca-pv may be important if subducted material can accumulate at the base of the mantle. Sample recovery issues mean that high-pressure and -temperature experiments are difficult and the phase boundary between cubic and tetragonal Ca-pv is still being determined (Thomson et al., 2019), but molecular dynamics simulations (Li et al., 2006) show maximum single-crystal shear wave anisotropy of 25%, similar to other phases mentioned here. Room-temperature diamond-anvil cell experiments (Miyagi et al., 2009) and Peierls–Nabarro modelling (Ferre et al., 2009) suggest Ca-pv might form a CPO in deformation by glide on the cubic slip system $\langle 1\bar{1}0 \rangle \{110\}$, and experiments on the analogue CaGeO_3 suggest Ca-perovskite may be weaker than MgO (Wang et al., 2013), but relatively few studies have yet examined this further.

Silica phases may also make up ~20% of a basaltic lower mantle. While it seems likely that stishovite is stable until about 1500 km depth, uncertainty remains as to when in the lower mantle silica transitions from the CaCl_2 structure to seifertite (e.g., Sun et al., 2019). This may be important since whilst seifertite appears to be only moderately anisotropic (?) and hence is likely not be a large contributor to lowermost mantle anisotropy, CaCl_2 -type silica may have much stronger shear wave anisotropy of about 30% (?). Un-

432 fortunately we do not currently have constraints on how silica phases may accommodate
 433 strain.

434 If hydrogen can be carried to the deep mantle, then hydrous phases such as alu-
 435 minous phase D or phase H might occur in D'' (e.g., ??), whilst aluminous phase δ -AlOOH
 436 is likely present in basaltic compositions (e.g., ?), and iron-rich regions could contain Fe-
 437 rich phases such as FeO₂ or FeOOH (e.g., ?). Some of these phases may be strongly anisotropic,
 438 however compared to the nominally anhydrous silicates like bridgmanite and post-perovskite,
 439 little work has been done to understand their deformation mechanisms.

440 4 Joint geodynamic–seismic modelling

441 4.1 Recent developments

442 Several endeavours—mainly over the last decade—have tried to tie together all the
 443 fields and constraints discussed so far, in order to interpret anisotropy in the lowermost
 444 mantle. The long-term, sometimes enigmatic, goal of these studies is to map flow direc-
 445 tions in the lowermost mantle to understand its role in the overall mantle convection (as
 446 the title of this chapter suggests). Most studies to this date, however, attempt to con-
 447 strain the underlying cause of anisotropy taking their best guess at the flow regime.

448 In terms of the cause of anisotropy, recent studies rely heavily on post-perovskite
 449 being stable in the lowermost mantle to explain the observed anisotropy, arguing that
 450 bridgmanite produces the wrong radial anisotropic signature, and ferropericlase is not
 451 abundant enough to dominate anisotropic signatures. Bridgmanite not playing a major
 452 role can also be argued in light of the recent results that bridgmanite is too strong to
 453 cause dislocation glide and develop preferred orientation (Boioli et al., 2017).

454 The dominant glide plane in post-perovskite that is argued to explain anisotropy
 455 varies with studies arguing for dominant glide on (010) (Walker et al., 2011; Nowacki et
 456 al., 2013; Creasy et al., 2017; Tommasi et al., 2018; Ford et al., 2015) and (001) (Nowacki
 457 et al., 2010; Cottaar et al., 2014; Walker et al., 2018; X. Wu et al., 2017; Chandler et al.,
 458 2018). These studies range from finding a best fitting model from a qualitative compar-
 459 ison to previously published observations (i.e., Cottaar et al., 2014; Tommasi et al., 2018)
 460 to a quantitative misfit with local observations (Nowacki et al., 2010; Ford et al., 2015;
 461 Creasy et al., 2017) or with global anisotropic models (Walker et al., 2011, 2018). Of course,
 462 all of these studies have made different assumptions and choices, which may affect the

final conclusion. One example is the choice of elastic constants—for instance, a dominant glide system on the (010) plane results in $V_{SH} > V_{SV}$ when using elastic constants of Stackhouse, Brodholt, & Price (2005), and in $V_{SV} > V_{SH}$ when using those of Wentzcovitch et al. (2006) (Yamazaki & Karato, 2007; Wenk et al., 2011). Similarly, studies may choose to use constants derived at a single pressure and temperature—not necessarily those of the part of the mantle of interest—or attempt to include the variable anisotropic effects as P and T vary (Walker et al., 2011).

A number of recent studies are worth highlighting. Tommasi et al. (2018) explore the anisotropy resulting from deformation constraints from atomistic modelling instead of experimental results, arguing for a dominant glide plane of (010). Atomistic calculations, which will hopefully converge with experimental results in the future, offer a great step forward into constraining the deformation in the lowermost mantle. Their modelling finds weak radial anisotropy of $V_{SH} > V_{SV}$ and sub-horizontal fast polarization directions in simple corner flow.

Their modelled elastic tensors with post-perovskite and periclase in an upwelling tracer can also fit the recent observations of changing anisotropy beneath Iceland by Wolf et al. (2019). However, the paper also presents models of pure bridgmanite and periclase that can fit the observations for the assumed change in flow.

Walker et al. (2018) explore texture inheritance from (001) slip in post-perovskite to bridgmanite (Dobson et al., 2013) on a global scale. Such a model can explain the observed sharp changes in the signature of anisotropy from regions dominated by cold downwellings, to regions dominated by hot upwellings or LLSVPs. Comparable results for texture inheritance were shown by Chandler et al. (2018) using the tracking of single tracers from downwelling to upwelling.

Most of the studies mentioned have pre-assumed the flow pattern either locally or globally and the models of different compositions are tested against seismic observations. Only the studies of Ford et al. (2015) and Creasy et al. (2017) both fit the compositional model as well as the flow direction. For both cases, this is applied to one locality where anisotropy is constrained from different azimuthal directions. Ford et al. (2015) suggest mainly vertical flows occur just to the East of the African LLSVP, while Creasy et al. (2017) suggest horizontal flows in a region of fast isotropic velocities beneath New Zealand and Australia.

495 **4.2 Example case: comparing a model to seismic observations**

496 Many of the multi-disciplinary modelling studies discussed above compare their synthetic elasticity models to ray-theoretically derived local body wave observations. A number of studies explore the limitations of interpreting body waves observations in terms 497 of anisotropy by analysing synthetic observations; for example for 1D isotropic or radially 498 anisotropic models for S_{diff} waves (Maupin, 1994; Komatitsch et al., 2010; Borgeaud 499 et al., 2016; Parisi et al., 2018) and for ScS waves (Kawai & Geller, 2010). Nowacki & 500 Wookey (2016) extend the analysis for ScS waves to full synthetic anisotropic models with 501 small-scale variations from the model of Walker et al. (2011) (cf. Figure 3). They conclude 502 that ray-theoretical interpretations hold up for the simplest anisotropic models, 503 but break down for those with variable anisotropy. Additionally, the finite-frequency wave 504 senses less splitting than a ray-theoretical interpretation of an anisotropic model would 505 suggest, as the finite-frequency sensitivity will average over the strongly varying anisotropic 506 medium, sensing an effective medium.

509 Here we explore these limitations further by combining the forward modelling in
 510 a subducting slab of Cottaar et al. (2014) with the full-wave modelling of Nowacki & Wookey
 511 (2016) and analyse S_{diff}, ScS, SKS, and SKKS phases in a finite-frequency framework.

512 **4.2.1 Geodynamic and texture modelling**

513 We use the results of Cottaar et al. (2014). We refer the reader to the original work
 514 for a full description of parameters used, but note that in this type of modelling, uncer-
 515 tainty can be introduced via a number of parameters including: the chosen relative crit-
 516 ical resolved shear stresses on each slip system; the lack of a non-glide mechanism to ac-
 517 commodate strain and reset texture (such as diffusion creep); the phase boundary be-
 518 tween phases; the single-crystal elastic constants; and the stress-strain homogenisation
 519 scheme. In the following we give a short summary of the modelling details.

520 Deformation is tracked along tracer particles (Figure 4a) across the lowermost man-
 521 tle using CitcomS (Zhong et al., 2000), where 500 grains are modelled with the viscoplas-
 522 tic self-consistent method (VPSC; Lebensohn & Tomé, 1993) to accommodate the de-
 523 formation. 75% of these grains are post-perovskite ('ppv') or bridgmanite ('pv'), and 25%
 524 are periclase. For post-perovskite, a dominant glide plane of (100) ('ppv 100' model), (010)
 525 ('ppv 010'), or (001) ('ppv 001') is assumed. The assumed glide planes for periclase are

543 **Table 1.** Summary of synthetic paths used to investigate anisotropy in the geodynamic slab
 544 model.

Code	Description, phases ^a	Source longitude (°)	Source latitude (°)	Focal mechanism ^b
A	Across slab: SKS–SKKS	0	–90	090/0/–90
B	Along slab: SKS–SKKS, S _{diff}	–55	0	180/30/0
C	Along slab: ScS, S _{diff}	0	0	280/30/–90

^a Phases analysed from full-wavefield synthetics.

^b Given as strike/dip/rake of the fault plane in °.

All events at 650 km depth.

526 weaker, and this phase ends up accommodating 35–40% of the deformation. For the elas-
 527 tic constants, the values of Stackhouse, Brodholt, Wookey, et al. (2005) are used for post-
 528 perovskite and bridgmanite, and those of Karki et al. (2000) for periclase. Cottaar et
 529 al. (2014) note that model ppv 001 is in general agreement with the radial anisotropy
 530 observed at the bottom of slabs and fast directions of azimuthal anisotropy is parallel
 531 to flow directions. The radial anisotropy in model ppv 010 also has the right sign, but
 532 is very weak in nature.

533 4.2.2 Seismic modelling

534 We seek to compare the predicted seismic characteristics of our geodynamic slab
 535 model to regional observations of anisotropy, including splitting in S_{diff}, SKS–SKKS and
 536 S–ScS differential splitting, as well as observations of changes in splitting intensity (Chevrot,
 537 2000). In order to do this, we simulate the propagation of waves through the model in
 538 two directions—along the slab and across it—for a range of geometries. We use synthet-
 539 ics in the epicentral distance range $55^\circ \leq \Delta \leq 80^\circ$ for ScS, $100^\circ \leq \Delta \leq 130^\circ$ for
 540 SKS, $110^\circ \leq \Delta \leq 130^\circ$ for SKKS and $95^\circ \leq \Delta \leq 120^\circ$ for S_{diff}. Table 1 outlines the
 541 geometries used in this study and which phases are investigated for each, whilst Figure 4b
 542 shows the location of the events and receivers.

560 We calculate the seismic response of the slab using the spectral element method
 561 as implemented in the SPECFEM3D_GLOBE code (Komatitsch & Tromp, 2002). In or-

562 der to remove time in writing intermediate files, we use a version of the code where cre-
 563 ating the spectral element mesh and solving the equations of motion are performed in
 564 the same program (Komatitsch et al., 2003; Nowacki & Wookey, 2016). We use two chunks
 565 of the cubed sphere with 800 spectral elements along each side, giving seismograms ac-
 566 curate at frequencies below 0.2 Hz, similar to the dominant period of the waves at these
 567 distances.

568 The elasticity model is mapped to the seismic computational mesh by finding the
 569 nearest neighbouring tracer particle within a defined ‘slab’ region, which is below 400 km
 570 above the CMB and within 150 km from any given particle. Beyond this distance, the
 571 nearest particle’s elasticity grades smoothly to the background 1D velocity, given by AK135
 572 (Kennett et al., 1995), over a 100 km distance using Voigt averaging between the isotropic
 573 and full elastic tensor. This smoothing distance was chosen to avoid artificially extend-
 574 ing the region of the mantle influenced by the slab, whilst avoiding seismic artifacts from
 575 a spatially abrupt transition between isotropic and anisotropic mantle.

576 4.2.3 Synthetic analysis

577 We can process synthetics from our forward model in the same way as data and
 578 compare the two. For the purposes of this example, we show a selection of results for the
 579 three paths, for different combinations of seismic phases, analysing the shear wave split-
 580 ting in ScS, S_{diff}, and differential splitting between SKS and SKKS. In all cases, we anal-
 581 yse the shear wave splitting in a window around the arrival of interest using the minimum-
 582 eigenvalue method of Silver & Chan (1991), with errors as updated by Walsh et al. (2013).
 583 The fast axis here is defined as the angle ϕ' from the radial component (or the vertical
 584 at the bottoming point of the seismic ray, Figure 1c in Nowacki et al. (2010)). We also
 585 consider the splitting intensity (SI; Chevrot, 2000) for SKS and SKKS waves, where the
 586 polarisation is known to be radial, and S_{diff} waves, where almost all SV energy is lost
 587 along the diffracted path, rendering them horizontally polarised. For this reason, S_{diff}
 588 SI is calculated in the opposite sense to usual for SK(K)S waves, interchanging the ra-
 589 dial and transverse components in the calculation. Discrepant SKS–SKKS splitting pairs
 590 are identified where either one of the phases shows null splitting, whilst the other does
 591 within error, or the two phases’ 95% confidence region of the small-eigenvalue surface
 592 do not overlap. Additionally, for all splitting measurements we use the automatic clas-

593 sification method of Wuestefeld et al. (2010) to calculate Q , a measure of quality between
 594 –1 and 1. –1 indicates a null, 1 a good measurement, and 0 a likely poor measurement.

595 We consider first the splitting in ScS for path ‘C’ (Figure 5). This path is similar
 596 to observations of splitting along palaeosubduction zones such as beneath the Caribbean
 597 (Garnero et al., 2004; Maupin et al., 2005; Nowacki et al., 2010, e.g.,). In general, it seems
 598 that $\phi' \approx 90^\circ$ ($\xi > 1$) in many slab regions (Nowacki et al., 2011; Romanowicz & Wenk,
 599 2017); in the Caribbean in particular, Garnero et al. (2004) infer a systematic rotation
 600 in the fast angle across the palaeoslab region, giving a change in ϕ' from $\sim 105^\circ$ to \sim
 601 75° .

611 Returning to Figure 5, it is clear that plasticity models ppv 010 and ppv 100 are
 612 better candidates than the remaining models at reproducing the $V_{\text{SH}} > V_{\text{SV}}$ and vari-
 613 able ϕ' signals seen in data. Note that this is a different conclusion from Cottaar et al.
 614 (2014), which could be due to the added complexity in this study of investigating the
 615 non-horizontal orientation of the waves, which can cause rotations in ϕ' (see Figure 2).
 616 The models produce values of δt which are mostly comparable to those seen in nature,
 617 though larger at up to 6 s in the synthetics versus $\sim 2\text{--}3$ s as observed. The strength of
 618 anisotropy present in the models is up to $A^U = 0.1$, which is about one-third of the pre-
 619 dicted single crystal anisotropy of ppv in the lowermost mantle (Stackhouse, Brodholt,
 620 Wookey, et al., 2005).

621 We next show results for path ‘B’, which samples the slab similarly, but using S_{diff}
 622 and SKS–SKKS phases, in Figures 6 and 7. SI for S_{diff} should be large only when a sig-
 623 nificant non-radial anisotropy is present, which is generally the case within and at the
 624 edges of the slab.

637 It is notable in all cases that the pattern of ϕ' and δt is complex and variable across
 638 the slab, with large regions of null splitting even where strong anisotropy is present. Null
 639 splitting may occur when the polarisation of a shear wave travelling through an anisotropic
 640 medium is close to the fast or show shear wave orientations (which are perpendicular)
 641 in that direction, and this may be the cause here. Variability in ϕ' is expected because
 642 of the pattern of flow in the model, and we observe fairly smooth rotations of ϕ' from
 643 north to south in the ppv models, similarly to data. However, the pv case shows δt vari-
 644 ations do not correlate strongly to simple features in the elasticity model. This illustrates
 645 the sometime non-intuitive manner in which the seismic wave averages structure, and

646 cautions against the use of approximate methods like ray theory when calculating syn-
 647 synthetics in such models for data comparison.

648 SKS–SKKS pairs, in contrast, show relatively straightforward behaviour, with dis-
 649 crepant pairs concentrating near the edges of the high-anisotropy areas as expected. The
 650 ‘core’ of the deformed material does not show discrepant splitting, as both phases show
 651 similar behaviour. Notably, for ppv 001 there is a region in the northeast which does not
 652 show the expected behaviour. We see a similar non-intuitive behaviour in path A (Fig-
 653 ure 4b). Here, although some discrepant pairs straddle the edge of the slab for ppv 001,
 654 very few paths show this for any of the other models. Inferring the edges of anisotropic
 655 regions therefore must again be done with caution.

656 We also examine the raw difference in splitting intensity between SKS and SKKS
 657 at the same seismograms, $\Delta SI = SI_{SKS} - SI_{SKKS}$ (Figure 8). Measuring ΔSI is com-
 658 putationally simple, and hence holds the promise for automatic global mapping of D''
 659 anisotropy. Comparing with the differential splitting predictions (Figures 4c, 6 and 7),
 660 it appears that the along-slab path B (Figure 8b) shows straightforward behaviour, where
 661 ΔSI deviates significantly from 0 where the slab is significantly anisotropic, either pos-
 662 itively or negatively depending on the exact elastic structure in the model. This agrees
 663 well with the differential splitting interpretation. For path A, however (Figure 8a), a large
 664 negative ΔSI signal is present at the eastern end of most models, though this is not cor-
 665 related to significant differential splitting (Figure 4c). Most models also show large ΔSI
 666 in the central northern part, but again this is not reflected in differential splitting. This
 667 suggests that although there is significant difference between the elastic structure expe-
 668 rienced by the SKS and SKKS waves in these regions as they cross the edge of the anisotropic
 669 part of the slab, the shear wave splitting is not sufficiently coherent and clear to provide
 670 a strong signal. Nevertheless, these calculations suggest that a more global SKS–SKKS
 671 comparison holds promise for detecting regions where anisotropy changes rapidly.

676 5 Limitations, advances, and the way forward

677 5.1 The inverse problem

678 The final goal of observing anisotropy in the lowermost mantle is, as the title of
 679 this chapter suggests, to map flow directions. We have discussed the forward model and
 680 the large number of assumptions required to create an anisotropic model and compare

681 it to seismic observations. For most studies discussed in Section 4.1 the flow model was
 682 one of the prior assumptions and different potential compositions are explored; only the
 683 recent studies of Ford et al. (2015) and Creasy et al. (2017) locally interpret flow direc-
 684 tion.

685 Results for a suite of candidate deformation mechanisms, like those in Figure 5, im-
 686 mediately make tempting a potentially circular line of reasoning: given an assumed flow
 687 model and the data, can we infer the deformation mechanism responsible for anisotropy?
 688 And with that improved estimate of deformation mechanism, can we then infer the flow
 689 field? As discussed, uncertainty as to the very cause of anisotropy in the lowermost man-
 690 tle makes such reasoning perilous. It is also worth noting that if the rheology in geody-
 691 namic models is set in part based on observations of seismic anisotropy, and the assump-
 692 tion made of a particular deformation mechanism, then there is an added danger in the
 693 use of such dynamic models to then infer the mechanism of anisotropy.

694 Despite these problems, we can proceed with caution if we hold in mind that it is
 695 the *combination* of the flow model, deformation mechanism and mineral elasticity which
 696 is being tested against the data in each instance, not any one of these in isolation. In-
 697 tuitively, varying any one of these might lead to an equally well-fitting set of synthetic
 698 observations when varying another.

699 Is finding the dominant mineral (or multi-phase system) and deformation systems
 700 creating lowermost mantle anisotropy the biggest hurdle in the way to mapping flow?
 701 If we constrain the main source of anisotropy, could we create a map of flow across the
 702 mantle? To do that, we would be interested in making a number of inverse steps (shown
 703 in Figure 3 by the white dashed arrows), each of which is non-linear and under-determined:

- 704 1. *Using the seismic observations to find the constrained parts of the seismic anisotropic*
 705 *tensor.* Constraints on the anisotropic tensor will always be limited by the prop-
 706 agation direction of the seismic phases used (Figure 2) and the azimuthal cover-
 707 age, generally leaving large parts of the anisotropic tensor unconstrained, and re-
 708 verting studies to assume symmetries (i.e. radial or azimuthal anisotropy). Ad-
 709 ditionally, the resulting anisotropic tensor would always reflect the effective elas-
 710 tic tensor that the seismic waves observed at long wavelengths, and could result
 711 from an entire suite of small-scaled heterogeneously (an)isotropic media (e.g., Backus,
 712 1962; Capdeville & Cance, 2014; Fichtner et al., 2013). In this chapter we have

frequently made the major assumption that the anisotropy of the effective tensor is due to underlying intrinsic anisotropy (CPO), and not caused by small-scale isotropic heterogeneity (SPO).

- 713 2. *Mapping from the effective anisotropic tensor to a set of textured minerals or a*
 714 *specific mineral with preferred orientation.* Accounting for the null-space in the
 715 elastic tensor, there would be no unique fit here and many assumptions on the min-
 716 eral physics need to be made. One could not account for the entire suite of po-
 717 tential deformation mechanisms occurring, presence of other minerals and the re-
 718 lated multi-phase deformation effects. With the assumption of a single dominant
 719 mineral and glide mechanism, the main imaged fast polarisation direction in the
 720 elastic tensor would be preferentially fit. There is no value in mapping the strength
 721 of the anisotropy into a degree of preferentially aligned minerals, as the amplitudes
 722 of the effective elastic tensor will be underestimated (as shown by the synthetic
 723 results in Section 4.2).
- 724 3. *Mapping from textured minerals to potential deformation history and flow direc-*
 725 *tions.* A single textured mineral can result from various deformation histories as
 726 it can both reflect the deformation it is undergoing, or fossilised deformation, which
 727 could be displaced and rotated. To uniquely constrain the flow model, many ob-
 728 servations in different locations will have to be combined, as well as including other
 729 constraints, i.e. isotropic velocities, the gravity field, and past plate tectonic mod-
 730 els.

731 While we choose to highlight the true inverse steps of this problem, this poses mul-
 732 tiple layers of non-uniqueness, which makes a flow map for the lowermost mantle based
 733 on anisotropy appear unobtainable. For the foreseeable future, mapping mantle flow will
 734 have to rely on simplified relationships between fast polarisation directions and flow with
 735 understanding of the conditions under which these are valid. For the upper mantle, a
 736 simple relationship is posed as the fast axis of deformed olivine generally aligns with the
 737 flow direction, which has allowed interpretation of asthenospheric flow from anisotropy,
 738 although the validity of under volatile-rich conditions, e.g. in the mantle wedge above
 739 subduction zones, where observations also become more complex ([see Becker and Lebe-](#)
 740 [dev, this volume](#)). For the lowermost mantle, Cottaar et al. (2014) pose a similar rela-
 741 tionship between horizontal fast direction and horizontal flow direction specifically for
 742 post-perovskite with dominant (001)-glide for a simple case of a slab spreading out on
 743
 744
 745

746 the CMB. Such a relationship should be tested statistically under many flow conditions,
 747 rotations, and deformations, and using full-waveform modelling. Tommasi et al. (2018)
 748 present a relationship of sub-parallel fast polarisation directions to the flow direction for
 749 post-perovskite with dominant (010)-glide and twinning for simple horizontal flow. Their
 750 study tests, not statistically but very systematically, the limitations of this relationship
 751 in corner flows and the ability of different seismic phases to detect these polarisation di-
 752 rections.

753 Creasy et al. (2019) pose a different question: with our current level of non-uniqueness
 754 in the interpretation, how many independent seismic observations do we need in a sin-
 755 gle location to interpret composition and flow? They show statistically that roughly 10
 756 or more measurements of fast direction or reflection polarisations with various azimuths
 757 and incidence angles are needed to uniquely constrain the anisotropic tensor to make an
 758 interpretation with some confidence. It is challenging to find locations to which this can
 759 be applied due to available earthquake–station geometries.

760 Whilst it is unlikely that the mineralogical parameters we have discussed will be
 761 tightly constrained for some time, and similarly seismic data coverage will probably not
 762 improve vastly, it is conceivable that probabilistic approaches to inferring flow from anisotropy
 763 may enable progress by incorporating uncertainties in all the input parameters as in Fig-
 764 ure 3 and retrieving an ensemble of acceptable flow histories. Such a model suite would
 765 however likely be a vast undertaking, requiring many millions of forward iterations, in-
 766 cluding geodynamic and full waveform modelling. This is unfeasible with the current com-
 767 bination of forward numerical methods and computational resources, but the future may
 768 bring this within our grasp.

769 5.2 Outlook

770 While mapping flow clearly remains an ambitious goal, current studies of anisotropy
 771 do provide new insights into the deepest mantle. Specifically, the goal to find the source
 772 of anisotropy reveals the potential importance of post-perovskite to be stable in the man-
 773 tle, as bridgemanite might be too strong to cause texturing (Boioli et al., 2017) and fer-
 774 ropericlase, as the minor phase, might not deform coherently (Miyagi & Wenk, 2016).
 775 Observations of lateral changes in anisotropy could highlight where post-perovskite is
 776 present, which relates to the temperature field and thus the convective patterns. A ma-

777 jor step forward in understanding the role of post-perovskite would be to resolve its dom-
 778 inant deformation mechanisms. It remains to be seen if the latest theoretical calculations
 779 (e.g., Goryaeva et al., 2017) will converge with future experimental results.

780 Studies of anisotropy are also illuminating the nature of the LLSVP boundaries.
 781 From a seismological point of view, the claim that the radial anisotropy switches sign
 782 inside and outside the LLSVPs needs to be further tested for its robustness. Any rela-
 783 tionship between the isotropic and anisotropic velocities in tomographic models could
 784 be an artefact (e.g., Chang et al., 2015). Local observations of splitting, however, have
 785 confirmed strong changes in anisotropy around the edges of the LLSVPs (e.g., Cottaar
 786 & Romanowicz, 2013; Wang & Wen, 2007; Lynner & Long, 2014). The nature of the LLSVPs
 787 poses major unanswered questions, and understanding the changing signatures of anisotropy
 788 can help resolve to what degree their boundaries represent a purely thermal or a thermo-
 789 chemical gradient. In the thermal case, change in anisotropy could be explained by a phase
 790 transition from post-perovskite to perovskite (Dobson et al., 2013) or by a change in flow
 791 direction, likely from horizontal outside to vertical within the LLSVPs or plumes (e.g.
 792 Wolf et al., 2019). In the case where LLSVPs represent thermo-chemical piles, the bound-
 793 ary could also be mechanical with separate convection inside and outside the piles (e.g.,
 794 Garnero & McNamara, 2008). Currently, capturing all the variation in parameters which
 795 contribute to the development of anisotropy whilst correctly relating these to observa-
 796 tions is computationally constrained. However, while we are far from producing a global
 797 flow map based on anisotropic variations, anisotropic studies play a role in answering
 798 these fundamental questions on the nature of the lowermost mantle. With the answers
 799 to these questions, flow can be more easily interpreted on the basis of mapped isotropic
 800 velocity variations.

801 Acknowledgments

802 The authors thank Andrew Walker for discussion and improvement of the manuscript,
 803 and acknowledge two anonymous reviewers and editor Hauke Marquardt for helpful and
 804 constructive comments. AN is supported by the Natural Environment Research Coun-
 805 cil (NERC grant reference number NE/R001154/1). SC is supported by the European
 806 Research Council (ERC) under the European Union’s Horizon 2020 research and innov-
 807 ation programme (grant agreement No. 804071 - ZoomDeep) and the Natural Environ-

808 ment Research Council (NERC grant reference number NE/R010862/1). Computations
 809 were performed on ARCHER.

810 References

- 811 Ammann, M. W., Brodholt, J. P., Wookey, J., & Dobson, D. P. (2010). First-
 812 principles constraints on diffusion in lower-mantle minerals and a weak D'' layer.
 813 *Nature*, 465(7297), 462-465. doi: 10.1038/nature09052
- 814 Amodeo, J., Carrez, P., Devincre, B., & Cordier, P. (2011). Multiscale modelling of
 815 MgO plasticity. *Acta Materialia*, 59(6), 2291–2301.
- 816 Amodeo, J., Dancette, S., & Delannay, L. (2016). Atomistically-informed crystal
 817 plasticity in MgO polycrystals under pressure. *International Journal of Plasticity*,
 818 82, 177–191.
- 819 Antonangeli, D., Siebert, J., Aracne, C. M., Farber, D. L., Bosak, A., Hoesch, M.,
 820 ... Badro, J. (2011). Spin crossover in ferropericlase at high pressure: A seismo-
 821 logically transparent transition? *Science*, 331(6013), 64–67.
- 822 Auer, L., Boschi, L., Becker, T. W., Nissen-Meyer, T., & Giardini, D. (2014). Sa-
 823 vani: A variable resolution whole-mantle model of anisotropic shear velocity vari-
 824 ations based on multiple data sets. *Journal Of Geophysical Research-Solid Earth*,
 825 119(4), 3006-3034. doi: 10.1002/2013JB010773
- 826 Backus, G. (1962). Long-wave elastic anisotropy produced by horizontal lay-
 827 ering. *Journal Of Geophysical Research*, 67(11), 4427-4440. doi: 10.1029/
 828 JZ067i011p04427
- 829 Beghein, C., Trampert, J., & van Heijst, H. J. (2006). Radial anisotropy in seis-
 830 mic reference models of the mantle. *Journal Of Geophysical Research-Solid Earth*,
 831 111(B2), B02303. doi: 10.1029/2005JB003728
- 832 Boioli, F., Carrez, P., Cordier, P., Devincre, B., Gouriet, K., Hirel, P., ... Ritter-
 833 bex, S. (2017). Pure climb creep mechanism drives flow in Earth's lower mantle.
 834 *Science advances*, 3(3), e1601958.
- 835 Borgeaud, A. F., Konishi, K., Kawai, K., & Geller, R. J. (2016). Finite frequency
 836 effects on apparent S-wave splitting in the D'' layer: Comparison between ray the-
 837 ory and full-wave synthetics. *Geophysical Journal International*, 207(1), 12–28.
- 838 Boschi, L., & Dziewoński, A. (2000). Whole Earth tomography from delay times
 839 of P, P_cP, and PKP phases: Lateral heterogeneities in the outer core or radial

- 840 anisotropy in the mantle? *Journal Of Geophysical Research-Solid Earth*, 105(B6),
841 13675-13696.
- 842 Capdeville, Y., & Cance, P. (2014). Residual homogenization for elastic wave propa-
843 gation in complex media. *Geophysical Journal International*, 200(2), 986–999.
- 844 Carrez, P., Ferr e, D., & Cordier, P. (2009). Peierls-Nabarro modelling of dislo-
845 cations in MgO from ambient pressure to 100 GPa. *Modelling And Simulation In*
846 *Materials Science And Engineering*, 17(3), 035010. doi: 10.1088/0965-0393/17/3/
847 035010
- 848 Carrez, P., Goryaeva, A. M., & Cordier, P. (2017). Prediction of mechanical twin-
849 ning in magnesium silicate post-perovskite. *Scientific reports*, 7(1), 17640.
- 850 Chandler, B., Yuan, K., Li, M., Cottaar, S., Romanowicz, B., Tomé, C., & Wenk, H.
851 (2018). A refined approach to model anisotropy in the lowermost mantle. In *Iop*
852 *conference series: Materials science and engineering* (Vol. 375, p. 012002).
- 853 Chang, S.-J., Ferreira, A. M. G., Ritsema, J., van Heijst, H. J., & Woodhouse, J. H.
854 (2015). Joint inversion for global isotropic and radially anisotropic mantle struc-
855 ture including crustal thickness perturbations. *Journal of Geophysical Research:*
856 *Solid Earth*, 120(6), 4278-4300. doi: 10.1002/2014JB011824
- 857 Chevrot, S. (2000). Multichannel analysis of shear wave splitting. *Journal Of Geo-
858 physical Research-Solid Earth*, 105(B9), 21579-21590.
- 859 Cobden, L., & Thomas, C. (2013). The origin of D'' reflections: A systematic study
860 of seismic array data sets. *Geophysical Journal International*, 194(2), 1091–1118.
- 861 Cobden, L., Thomas, C., & Trampert, J. (2015). Seismic detection of post-
862 perovskite inside the Earth. In *The earth's heterogeneous mantle* (pp. 391–440).
863 Springer.
- 864 Cordier, P., Amodeo, J., & Carrez, P. (2012). Modelling the rheology of MgO un-
865 der Earth's mantle pressure, temperature and strain rates. *Nature*, 481(7380),
866 177-180. doi: 10.1038/nature10687
- 867 Cottaar, S., & Lekić, V. (2016, nov). Morphology of seismically slow lower-mantle
868 structures. *Geophys. J. Int.*, 207(2), 1122–1136. doi: 10.1093/gji/ggw324
- 869 Cottaar, S., Li, M., McNamara, A. K., Romanowicz, B., & Wenk, H.-R. (2014, Au-
870 gust). Synthetic seismic anisotropy models within a slab impinging on the core-
871 mantle boundary. *Geophysical Journal International*, 199(1), 164-177. doi: 10
872 .1093/gji/ggu244

- 873 Cottaar, S., & Romanowicz, B. (2013). Observations of changing anisotropy across
874 the southern margin of the African LLSVP. *Geophysical Journal International*,
875 195(2), 1184-1195. doi: 10.1093/gji/ggt285
- 876 Creasy, N., Long, M. D., & Ford, H. A. (2017). Deformation in the low-
877 ermost mantle beneath Australia from observations and models of seismic
878 anisotropy. *Journal of Geophysical Research: Solid Earth*, 122(7), 5243-5267.
879 doi: 10.1002/2016JB013901
- 880 Creasy, N., Pisconti, A., Long, M. D., Thomas, C., & Wookey, J. (2019). Constraining
881 lowermost mantle anisotropy with body waves: a synthetic modelling study.
882 *Geophysical Journal International*, 217(2), 766-783.
- 883 de Wit, R., & Trampert, J. (2015, November). Robust constraints on average radial
884 lower mantle anisotropy and consequences for composition and texture. *Earth and*
885 *Planetary Science Letters*, 429, 101-109. doi: 10.1016/j.epsl.2015.07.057
- 886 Deng, J., Long, M. D., Creasy, N., Wagner, L., Beck, S., Zandt, G., ... Minaya, E.
887 (2017). Lowermost mantle anisotropy near the eastern edge of the Pacific LLSVP:
888 constraints from SKS-SKKS splitting intensity measurements. *Geophysical Journal*
889 *International*, 210(2), 774-786.
- 890 Dobson, D. P., Lindsay-Scott, A., Hunt, S., Bailey, E., Wood, I., Brodholt, J. P., ...
891 Wheeler, J. (2019). Anisotropic diffusion creep in postperovskite provides a new
892 model for deformation at the core-mantle boundary. *Proceedings of the National*
893 *Academic of Sciences*, 116(52), 26389-26393.
- 894 Dobson, D. P., Miyajima, N., Nestola, F., Alvaro, M., Casati, N., Liebske, C.,
895 ... Walker, A. M. (2013). Strong inheritance of texture between perovskite
896 and post-perovskite in the D'' layer. *Nature Geoscience*, 6(7), 575-578. doi:
897 10.1038/ngeo1844
- 898 Ferré, D., Carrez, P., & Cordier, P. (2007). First principles determination of dislo-
899 cations properties of MgSiO₃ perovskite at 30 GPa based on the Peierls-Nabarro
900 model. *Physics of the Earth and Planetary Interiors*, 163(1-4), 283-291.
- 901 Ferre, D., Cordier, P., & Carrez, P. (2009, January). Dislocation modeling in cal-
902 cium silicate perovskite based on the Peierls-Nabarro model. *American Mineralo-*
903 *gist*, 94(1), 135-142. doi: 10.2138/am.2009.3003
- 904 Ferreira, A. M. G., Faccenda, M., Sturgeon, W., Chang, S.-J., & Schardong, L.
905 (2019, April). Ubiquitous lower-mantle anisotropy beneath subduction zones.

- 906 *Nature Geoscience*, 12(4), 301. doi: 10.1038/s41561-019-0325-7
- 907 Ferreira, A. M. G., Woodhouse, J. H., Visser, K., & Trampert, J. (2010). On the ro-
908 bustness of global radially anisotropic surface wave tomography. *Journal Of Geo-*
909 *physical Research-Solid Earth*, 115, B04313. doi: 10.1029/2009JB006716
- 910 Fichtner, A., Kennett, B. L., & Trampert, J. (2013). Separating intrinsic and appar-
911 ent anisotropy. *Physics of the Earth and Planetary Interiors*, 219, 11–20.
- 912 Finkelstein, G. J., Jackson, J. M., Said, A., Alatas, A., Leu, B. M., Sturhahn, W.,
913 & Toellner, T. S. (2018). Strongly anisotropic magnesiowüstite in Earth's lower
914 mantle. *Journal of Geophysical Research: Solid Earth*, 123(6), 4740–4750.
- 915 Ford, H. A., & Long, M. D. (2015, August). A regional test of global models for
916 flow, rheology, and seismic anisotropy at the base of the mantle. *Physics of the*
917 *Earth and Planetary Interiors*, 245, 71-75. doi: 10.1016/j.pepi.2015.05.004
- 918 Ford, H. A., Long, M. D., He, X., & Lynner, C. (2015, June). Lowermost mantle
919 flow at the eastern edge of the African Large Low Shear Velocity Province. *Earth*
920 *and Planetary Science Letters*, 420, 12-22. doi: 10.1016/j.epsl.2015.03.029
- 921 French, S. W., & Romanowicz, B. (2015, September). Broad plumes rooted at the
922 base of the Earth's mantle beneath major hotspots. *Nature*, 525(7567), 95-99. doi:
923 10.1038/nature14876
- 924 Fu, S., Yang, J., Tsujino, N., Okuchi, T., Purevjav, N., & Lin, J.-F. (2019). Single-
925 crystal elasticity of (Al, Fe)-bearing bridgmanite and seismic shear wave radial
926 anisotropy at the topmost lower mantle. *Earth and Planetary Science Letters*,
927 518, 116–126.
- 928 Garnero, E. J., & Lay, T. (1997). Lateral variations in lowermost mantle shear
929 wave anisotropy beneath the north Pacific and Alaska. *Journal Of Geophysical*
930 *Research-Solid Earth*, 102(B4), 8121-8135. doi: 10.1029/96JB03830
- 931 Garnero, E. J., Maupin, V., Lay, T., & Fouch, M. J. (2004). Variable azimuthal
932 anisotropy in Earth's lowermost mantle. *Science*, 306(5694), 259-261. doi: 10
933 .1126/science.1103411
- 934 Garnero, E. J., & McNamara, A. K. (2008). Structure and dynamics of Earth's
935 lower mantle. *Science*, 320(5876), 626-628. doi: 10.1126/science.1148028
- 936 Garnero, E. J., McNamara, A. K., & Shim, S.-H. (2016, June). Continent-sized
937 anomalous zones with low seismic velocity at the base of Earth's mantle. *Nature*
938 *Geoscience*, 9(7), 481-489. doi: 10.1038/ngeo2733

- 939 Garnero, E. J., Revenaugh, J., Williams, Q., Lay, T., & Kellogg, L. (1998). Ultralow velocity zone at the core–mantle boundary. In M. Gurnis, M. E. Wysession,
 940 E. Knittle, & B. A. Buffett (Eds.), *The Core–Mantle Boundary Region* (pp. 319–
 941 334). Washington, D.C., USA: American Geophysical Union.
- 943 Girard, J., Amulele, G., Farla, R., Mohiuddin, A., & Karato, S.-i. (2016, January). Shear deformation of bridgmanite and magnesiowustite aggregates at lower mantle
 944 conditions. *Science*, 351(6269), 144–147. doi: 10.1126/science.aad3113
- 946 Girard, J., Chen, J., & Raterron, P. (2012). Deformation of periclase single crystals at high pressure and temperature: Quantification of the effect of pressure on
 947 slip-system activities. *Journal of Applied Physics*, 111(11), 112607.
- 949 Goryaeva, A. M., Carrez, P., & Cordier, P. (2015). Modeling defects and plasticity in MgSiO₃ post-perovskite: Part 2—Screw and edge [100] dislocations. *Physics
 950 and chemistry of minerals*, 42(10), 793–803.
- 952 Goryaeva, A. M., Carrez, P., & Cordier, P. (2016). Low viscosity and high attenuation in MgSiO₃ post-perovskite inferred from atomic-scale calculations. *Scientific
 953 reports*, 6, 34771.
- 955 Goryaeva, A. M., Carrez, P., & Cordier, P. (2017). Modeling defects and plasticity in MgSiO₃ post-perovskite: Part 3—Screw and edge [001] dislocations. *Physics
 956 and Chemistry of Minerals*, 44(7), 521–533.
- 958 Grund, M., & Ritter, J. R. (2019). Widespread seismic anisotropy in Earth’s lower-
 959 most mantle beneath the Atlantic and Siberia. *Geology*, 47(2), 123–126.
- 960 Hall, S. A., Kendall, J.-M., & Van der Baan, M. (2004). Some comments on the effects of lower-mantle anisotropy on SKS and SKKS phases. *Physics of The Earth
 961 and Planetary Interiors*, 146(3-4), 469–481. doi: 10.1016/j.pepi.2004.05.002
- 963 Hernlund, J., Thomas, C., & Tackley, P. J. (2005). A doubling of the post-
 964 perovskite phase boundary and structure of the Earth’s lowermost mantle. *Nature*, 434(7035), 882–886. doi: 10.1038/nature03472
- 966 Hirose, K., Nagaya, Y., Merkel, S., & Ohishi, Y. (2010). Deformation of MnGeO₃
 967 post-perovskite at lower mantle pressure and temperature. *Geophysical Research
 968 Letters*, 37(L20302), 1–5. doi: 10.1029/2010GL044977
- 969 Hirose, K., Wentzcovitch, R., Yuen, D., & Lay, T. (2015). Mineralogy of the deep
 970 mantle - The post-perovskite phase and its geophysical significance. *Treatise on
 971 Geophysics*, 85–115.

- 972 Hunt, S. A., Walker, A. M., & Mariani, E. (2016, May). In-situ measurement of tex-
973 ture development rate in CaIrO₃ post-perovskite. *Physics of the Earth and Plane-*
974 *tary Interiors*. doi: 10.1016/j.pepi.2016.05.007
- 975 Hunt, S. A., Weidner, D. J., Li, L., Wang, L., Walte, N. P., Brodholt, J. P., &
976 Dobson, D. P. (2009). Weakening of calcium iridate during its transformation
977 from perovskite to post-perovskite. *Nature Geoscience*, 2(11), 794-797. doi:
978 10.1038/NGEO663
- 979 Iitaka, T., Hirose, K., Kawamura, K., & Murakami, M. (2004). The elasticity of
980 the MgSiO₃ post-perovskite phase in the Earth's lowermost mantle. *Nature*,
981 430(6998), 442-445. doi: 10.1038/nature02702
- 982 Jackson, J. M., Sinogeikin, S. V., Jacobsen, S. D., Reichmann, H. J., Mackwell,
983 S. J., & Bass, J. D. (2006). Single-crystal elasticity and sound velocities of
984 (Mg_{0.94}Fe_{0.06})O ferropericlase to 20 GPa. *Journal of Geophysical Research: Solid*
985 *Earth*, 111(B9).
- 986 Kaercher, P., Miyagi, L., Kanitpanyacharoen, W., Zepeda-Alarcon, E., Wang, Y.,
987 Parkinson, D., ... Wenk, H. (2016, December). Two-phase deformation of lower
988 mantle mineral analogs. *Earth and Planetary Science Letters*, 456, 134-145. doi:
989 10.1016/j.epsl.2016.09.030
- 990 Karato, S.-i. (1998). Some remarks on the origin of seismic anisotropy in the D''
991 layer. *Earth Planets Space*, 50, 1019-1028.
- 992 Karki, B., Wentzcovitch, R., de Gironcoli, S., & Baroni, S. (2000). High-pressure lat-
993 tice dynamics and thermoelasticity of MgO. *Physical Review B*, 61(13), 8793.
- 994 Kawai, K., & Geller, R. J. (2010). The vertical flow in the lowermost man-
995 tle beneath the Pacific from inversion of seismic waveforms for anisotropic
996 structure. *Earth and Planetary Science Letters*, 297(1-2), 190-198. doi:
997 10.1016/j.epsl.2010.05.037
- 998 Kawakatsu, H. (2015). A new fifth parameter for transverse isotropy. *Geophysical*
999 *Journal International*, 204(1), 682-685.
- 1000 Kendall, J.-M., & Silver, P. G. (1996). Constraints from seismic anisotropy on
1001 the nature of the lowermost mantle. *Nature*, 381(6581), 409-412. doi: 10.1038/
1002 381409a0
- 1003 Kendall, J.-M., & Silver, P. G. (1998). Investigating causes of D'' anisotropy. In *The*
1004 *core-mantle boundary region* (p. 97-118). American Geophysical Union.

- 1005 Kennett, B. L. N., Engdahl, E., & Buland, R. (1995). Constraints on seismic ve-
 1006 locities in the Earth from travel-times. *Geophysical Journal International*, 122(1),
 1007 108-124. doi: 10.1111/j.1365-246X.1995.tb03540.x
- 1008 Koelemeijer, P., Schuberth, B., Davies, D., Deuss, A., & Ritsema, J. (2018, July).
 1009 Constraints on the presence of post-perovskite in Earth's lowermost mantle from
 1010 tomographic-geodynamic model comparisons. *Earth and Planetary Science Let-
 1011 ters*, 494, 226-238. doi: 10.1016/j.epsl.2018.04.056
- 1012 Koelemeijer, P. J., Deuss, A., & Trampert, J. (2012). Normal mode sensitiv-
 1013 ity to earth's D'' layer and topography on the core-mantle boundary: what we
 1014 can and cannot see. *Geophysical Journal International*, 190(1), 553-568. doi:
 1015 10.1111/j.1365-246X.2012.05499.x
- 1016 Komatitsch, D., & Tromp, J. (2002). Spectral-element simulations of global seismic
 1017 wave propagation - I. Validation. *Geophysical Journal International*, 149(2), 390-
 1018 412.
- 1019 Komatitsch, D., Tsuboi, S., Ji, C., & Tromp, J. (2003). A 14.6 billion degrees
 1020 of freedom, 5 teraflops, 2.5 terabyte earthquake simulation on the Earth Sim-
 1021 ulator. *Proceedings of the ACM/IEEE SC2003 Conference (SC'03)*, 1-8. doi:
 1022 10.1145/1048935.1050155
- 1023 Komatitsch, D., Vinnik, L. P., & Chevrot, S. (2010). SHdiff-SVdiff splitting in an
 1024 isotropic Earth. *Journal Of Geophysical Research-Solid Earth*, 115, B07312. doi:
 1025 10.1029/2009JB006795
- 1026 Krischer, L., Megies, T., Barsch, R., Beyreuther, M., Lecocq, T., Caudron, C., &
 1027 Wassermann, J. (2015). Obspy: A bridge for seismology into the scientific Python
 1028 ecosystem. *Computational Science & Discovery*, 8(1), 014003.
- 1029 Lay, T., & Young, C. (1991). Analysis of seismic SV waves in the core's penumbra.
 1030 *Geophysical Research Letters*, 18(8), 1373-1376. doi: 10.1029/91GL01691
- 1031 Lebensohn, R., & Tomé, C. (1993). A self-consistent anisotropic approach for
 1032 the simulation of plastic-deformation and texture development of polycrystals—
 1033 application to zirconium alloys. *Acta Metallurgica Et Materialia*, 41(9), 2611–
 1034 2624. doi: 10.1016/0956-7151(93)90130-K
- 1035 Lekić, V., Cottaar, S., Dziewoński, A., & Romanowicz, B. (2012, December). Cluster
 1036 analysis of global lower mantle tomography: A new class of structure and implica-
 1037 tions for chemical heterogeneity. *Earth and Planetary Science Letters*, 357-358,

- 1038 68-77. doi: 10.1016/j.epsl.2012.09.014
- 1039 Li, L., Brodholt, J. P., Stackhouse, S., Weidner, D. J., Alfredsson, M., & Price,
1040 G. D. (2005). Elasticity of (Mg, Fe)(Si, Al)O₃-perovskite at high pressure. *Earth
1041 and Planetary Science Letters*, 240(2), 529–536.
- 1042 Li, L., Weidner, D. J., Brodholt, J. P., Alf  , D., Price, G. D., Caracas, R., & Wentz-
1043 covitch, R. M. (2006). Elasticity of {CaSiO}\$_{3}\$ perovskite at high pressure
1044 and high temperature. *Physics of The Earth and Planetary Interiors*, 155(3-4),
1045 249-259. doi: 10.1016/j.pepi.2005.12.006
- 1046 Lin, J.-F., Wenk, H.-R., Voltolini, M., Speziale, S., Shu, J., & Duffy, T. S. (2009).
1047 Deformation of lower-mantle ferropericlase (Mg, Fe)O across the electronic spin
1048 transition. *Physics and Chemistry of Minerals*, 36(10), 585.
- 1049 Long, M. (2009). Complex anisotropy in D'' beneath the eastern pacific from SKS-
1050 SKKS splitting discrepancies. *Earth and Planetary Science Letters*, 283(1-4), 181-
1051 189. doi: 10.1016/j.epsl.2009.04.019
- 1052 Long, M. D., & Lynner, C. (2015, September). Seismic anisotropy in the lowermost
1053 mantle near the Perm Anomaly. *Geophysical Research Letters*, 42(17), 7073-7080.
1054 doi: 10.1002/2015GL065506
- 1055 Lynner, C., & Long, M. D. (2014, May). Lowermost mantle anisotropy and defor-
1056 mation along the boundary of the African LLSVP. *Geophysical Research Letters*,
1057 41(10), 3447-3454. doi: 10.1002/2014GL059875
- 1058 Madi, K., Forest, S., Cordier, P., & Boussuge, M. (2005). Numerical study of creep
1059 in two-phase aggregates with a large rheology contrast: Implications for the lower
1060 mantle. *Earth and Planetary Science Letters*, 237(1-2), 223–238.
- 1061 Mainprice, D. (2007). Seismic anisotropy of the eep Earth from a mineral and rock
1062 physics perspective. In *Treatise on Geophysics* (p. 437-491). Elsevier. doi: 10
1063 .1016/B978-044452748-6.00045-6
- 1064 Mainprice, D., Tommasi, A., Ferr e, D., Carrez, P., & Cordier, P. (2008). Pre-
1065 dicted glide systems and crystal preferred orientations of polycrystalline silicate
1066 Mg-Perovskite at high pressure: Implications for the seismic anisotropy in the
1067 lower mantle. *Earth and Planetary Science Letters*, 271(1-4), 135-144. doi:
1068 10.1016/j.epsl.2008.03.058
- 1069 Mancinelli, N. J., & Shearer, P. M. (2013). Reconciling discrepancies among esti-
1070 mates of small-scale mantle heterogeneity from PKP precursors. *Geophysical Jour-*

- 1071 *nal International*, 195(3), 1721–1729.

1072 Marquardt, H., Speziale, S., Reichmann, H. J., Frost, D. J., & Schilling, F. R.
 1073 (2009). Single-crystal elasticity of $(\text{Mg}_{0.9}\text{Fe}_{0.1})\text{O}$ to 81 GPa. *Earth and Planetary Science Letters*, 287(3-4), 345-352. doi: 10.1016/j.epsl.2009.08.017

1075 Matzel, E., Sen, M., & Grand, S. (1996). Evidence for anisotropy in the deep mantle
 1076 beneath Alaska. *Geophysical Research Letters*, 23(18), 2417-2420. doi: 10.1029/
 1077 96GL02186

1078 Maupin, V. (1994). On the possibility of anisotropy in the D'' layer as inferred from
 1079 the polarization of diffracted S waves. *Physics of The Earth and Planetary Interiors*,
 1080 87(1-2), 1-32. doi: 10.1016/0031-9201(94)90019-1

1081 Maupin, V., Garnero, E. J., Lay, T., & Fouch, M. J. (2005). Azimuthal anisotropy
 1082 in the D'' layer beneath the Caribbean. *Journal Of Geophysical Research-Solid*
 1083 *Earth*, 110(B8), B08301. doi: 10.1029/2004JB003506

1084 McDonough, W., & Sun, S. (1995). The composition of the Earth. *Chemical Geology*,
 1085 120(3-4), 223-253.

1086 Merkel, S., McNamara, A. K., Kubo, A., Speziale, S., Miyagi, L., Meng, Y., ...
 1087 Wenk, H.-R. (2007). Deformation of $(\text{Mg},\text{Fe})\text{SiO}_3$ post-perovskite and D''
 1088 anisotropy. *Science*, 316(5832), 1729-1732. doi: 10.1126/science.1140609

1089 Merkel, S., Wenk, H.-R., Shu, J., Shen, G., Gillet, P., Mao, H., & Hemley, R. (2002).
 1090 Deformation of polycrystalline MgO at pressures of the lower mantle. *Journal Of*
 1091 *Geophysical Research-Solid Earth*, 107(B11), 2271. doi: 10.1029/2001JB000920

1092 Miyagi, L., Kanitpanyacharoen, W., Kaercher, P., Lee, K. K. M., & Wenk, H.-R.
 1093 (2010). Slip systems in MgSiO_3 post-perovskite: Implications for D'' anisotropy.
 1094 *Science*, 329(5999), 1639-1641. doi: 10.1126/science.1192465

1095 Miyagi, L., Kanitpanyacharoen, W., Stackhouse, S., Militzer, B., & Wenk, H.-R.
 1096 (2011). The enigma of post-perovskite anisotropy: Deformation versus trans-
 1097 formation textures. *Physics And Chemistry Of Minerals*, 38(9), 665-678. doi:
 1098 10.1007/s00269-011-0439-y

1099 Miyagi, L., Merkel, S., Yagi, T., Sata, N., Ohishi, Y., & Wenk, H.-R. (2009,
 1100 May). Diamond anvil cell deformation of CaSiO_3 perovskite up to 49 GPa.
 1101 *Physics of the Earth and Planetary Interiors*, 174(1-4), 159–164. doi: 10.1016/
 1102 j.pepi.2008.05.018

1103 Miyagi, L., & Wenk, H.-R. (2016). Texture development and slip systems in bridg-

- 1104 manite and bridgmanite + ferropericlase aggregates. *Physics and Chemistry of*
1105 *Minerals*, 43(8), 597–613.
- 1106 Moulik, P., & Ekstrom, G. (2014, oct). An anisotropic shear velocity model of the
1107 Earth's mantle using normal modes, body waves, surface waves and long-period
1108 waveforms. *Geophys. J. Int.*, 199(3), 1713–1738. doi: 10.1093/gji/ggu356
- 1109 Murakami, M., Hirose, K., Kawamura, K., Sata, N., & Ohishi, Y. (2004). Post-
1110 perovskite phase transition in MgSiO₃. *Science*, 304(5672), 855-858. doi: 10.1126/
1111 science.1095932
- 1112 Nakagawa, T., & Tackley, P. J. (2011). Effects of low-viscosity post-perovskite on
1113 thermo-chemical mantle convection in a 3-D spherical shell. *Geophysical research*
1114 *letters*, 38(4).
- 1115 Nisr, C., Ribárik, G., Ungar, T., Vaughan, G. B. M., Cordier, P., & Merkel, S.
1116 (2012). High resolution three-dimensional X-ray diffraction study of dislocations in
1117 grains of MgGeO₃ post-perovskite at 90 GPa. *Journal Of Geophysical Research*,
1118 117(B3), B03201. doi: 10.1029/2011JB008401
- 1119 Niu, F., & Perez, A. (2004). Seismic anisotropy in the lower mantle: A comparison
1120 of waveform splitting of SKS and SKKS. *Geophysical Research Letters*, 31(24),
1121 L24612. doi: 10.1029/2004GL021196
- 1122 Niwa, K., Miyajima, N., Seto, Y., Ohgushi, K., Gotou, H., & Yagi, T. (2012). In situ
1123 observation of shear stress-induced perovskite to post-perovskite phase transition
1124 in CaIrO₃ and the development of its deformation texture in a diamond-anvil cell
1125 up to 30 GPa. *Physics of The Earth and Planetary Interiors*, 194-195(C), 10-17.
1126 doi: 10.1016/j.pepi.2012.01.007
- 1127 Nowacki, A., Walker, A. M., Wookey, J., & Kendall, J.-M. (2013). Evaluating post-
1128 perovskite as a cause of D'' anisotropy in regions of palaeosubduction. *Geophysical*
1129 *Journal International*, 192(3), 1085-1090. doi: 10.1093/gji/ggs068
- 1130 Nowacki, A., & Wookey, J. (2016, September). The limits of ray theory when mea-
1131 suring shear wave splitting in the lowermost mantle with ScS waves. *Geophysical*
1132 *Journal International*, 207, 1573-1583. doi: 10.1093/gji/ggw358
- 1133 Nowacki, A., Wookey, J., & Kendall, J.-M. (2010). Deformation of the lowermost
1134 mantle from seismic anisotropy. *Nature*, 467(7319), 1091-1095. doi: 10.1038/
1135 nature09507
- 1136 Nowacki, A., Wookey, J., & Kendall, J.-M. (2011). New advances in using seis-

- mic anisotropy, mineral physics and geodynamics to understand deformation
in the lowermost mantle. *Journal of Geodynamics*, 52(3-4), 205-228. doi:
10.1016/j.jog.2011.04.003
- Oganov, A., Brodholt, J. P., & Price, G. D. (2001). The elastic constants of
MgSiO₃ perovskite at pressures and temperatures of the Earth's mantle. *Nature*,
411(6840), 934-937. doi: 10.1038/35082048
- Oganov, A., & Ono, S. (2004). Theoretical and experimental evidence for a post-
perovskite phase of MgSiO₃ in Earth's D'' layer. *Nature*, 430(6998), 445-448. doi:
10.1038/nature02701
- Panning, M., Lekić, V., & Romanowicz, B. (2010). Importance of crustal correc-
tions in the development of a new global model of radial anisotropy. *Journal Of
Geophysical Research-Solid Earth*, 115, B12325. doi: 10.1029/2010JB007520
- Parisi, L., Ferreira, A. M. G., & Ritsema, J. (2018, May). Apparent splitting of S
waves propagating through an isotropic lowermost mantle. *Journal of Geophysical
Research: Solid Earth*, 123(5), 3909-3922. doi: 10.1002/2017JB014394
- Pisconti, A., Thomas, C., & Wookey, J. (2019, May). Discriminating between causes
of D'' anisotropy using reflections and splitting measurements for a single path.
Journal of Geophysical Research: Solid Earth. doi: 10.1029/2018JB016993
- Ranganathan, S. I., & Ostoja-Starzewski, M. (2008). Universal elastic anisotropy
index. *Physical Review Letters*, 101(5), 055504. doi: 10.1103/PhysRevLett.101
.055504
- Reali, R., Van Orman, J. A., Pigott, J. S., Jackson, J. M., Boioli, F., Carrez, P., &
Cordier, P. (2019). The role of diffusion-driven pure climb creep on the rheology
of bridgemanite under lower mantle conditions. *Scientific reports*, 9(1), 2053.
- Reiss, M., Long, M., & Creasy, N. (2019). Lowermost mantle anisotropy beneath
Africa from differential SKS-SKKS shear-wave splitting. *Journal of Geophysical
Research: Solid Earth*. doi: 10.1029/2018JB017160
- Romanowicz, B., & Wenk, H.-R. (2017, August). Anisotropy in the deep Earth.
Physics of the Earth and Planetary Interiors, 269, 58-90. doi: 10.1016/j.pepi.2017
.05.005
- Silver, P. G., & Chan, W. W. (1991). Shear-wave splitting and subcontinental
mantle deformation. *Journal Of Geophysical Research-Solid Earth*, 96(B10),
16429-16454. doi: 10.1029/91JB00899

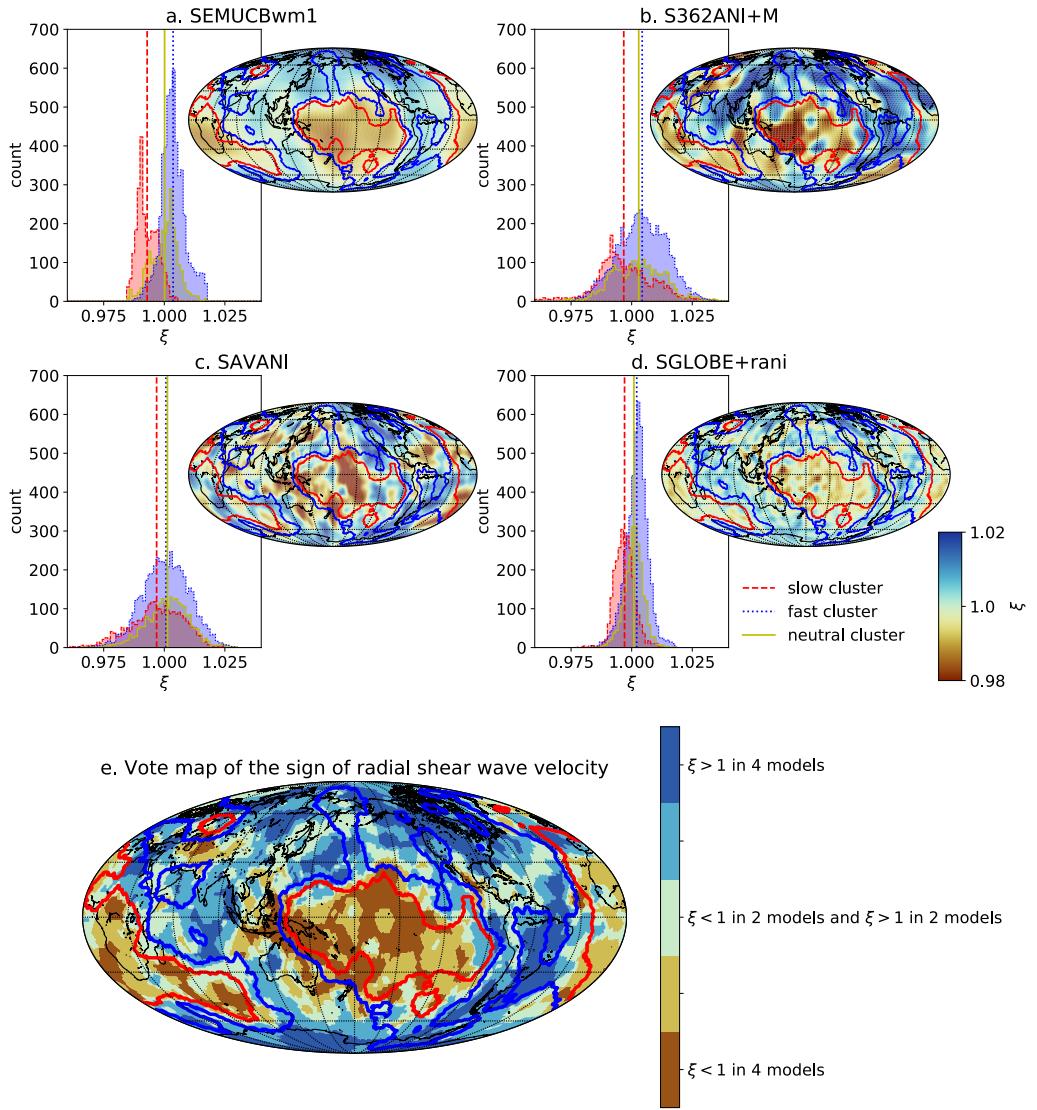
- 1170 Simmons, N. A., Forte, A. M., & Grand, S. (2009). Joint seismic, geodynamic
1171 and mineral physical constraints on three-dimensional mantle heterogeneity:
1172 Implications for the relative importance of thermal versus compositional
1173 heterogeneity. *Geophysical Journal International*, 177(3), 1284-1304. doi:
1174 10.1111/j.1365-246X.2009.04133.x
- 1175 Soldati, G., Boschi, L., & Piersanti, A. (2003). Outer core density heterogeneity and
1176 the discrepancy between PKP and PcP travel time observations. *Geophysical Re-*
1177 *search Letters*, 30(4), 1190. doi: 10.1029/2002GL016647
- 1178 Stackhouse, S., Brodholt, J. P., & Price, G. D. (2005). High temperature elastic
1179 anisotropy of the perovskite and post-perovskite Al_2O_3 . *Geophysical Research Let-*
1180 *ters*, 32(13), L13305. doi: 10.1029/2005GL023163
- 1181 Stackhouse, S., Brodholt, J. P., Wookey, J., Kendall, J.-M., & Price, G. D. (2005).
1182 The effect of temperature on the seismic anisotropy of the perovskite and post-
1183 perovskite polymorphs of MgSiO_3 . *Earth and Planetary Science Letters*, 230(1-2),
1184 1-10. doi: 10.1016/j.epsl.2004.11.021
- 1185 Sun, N., Shi, W., Mao, Z., Zhou, C., & Prakapenka, V. B. (2019, December). High
1186 pressure-temperature study on the thermal equations of state of seifertite and
1187 CaCl_2 -type SiO_2 . *Journal of Geophysical Research: Solid Earth*, 124(12), 12620–
1188 12630. doi: 10.1029/2019JB017853
- 1189 Tesoniero, A., Cammarano, F., & Boschi, L. (2016, July). S-to-P heterogeneity ratio
1190 in the lower mantle and thermo-chemical implications. *Geochemistry, Geophysics,*
1191 *Geosystems*, 17(7), 2522-2538. doi: 10.1002/2016GC006293
- 1192 Thomas, C., Wookey, J., Brodholt, J. P., & Fieseler, T. (2011). Anisotropy as
1193 cause for polarity reversals of D'' reflections. *Earth and Planetary Science Letters*,
1194 307(3-4), 369-376. doi: 10.1016/j.epsl.2011.05.011
- 1195 Thomas, C., Wookey, J., & Simpson, M. (2007). D'' anisotropy beneath Southeast
1196 Asia. *Geophysical Research Letters*, 34(4), L04301. doi: 10.1029/2006GL028965
- 1197 Thomson, A. R., Crichton, W. A., Brodholt, J. P., Wood, I. G., Siersch, N. C., Muir,
1198 J. M. R., ... Hunt, S. A. (2019, August). Seismic velocities of CaSiO_3 perovskite
1199 can explain LLSVPs in Earth's lower mantle. *Nature*, 572(7771), 643–647. doi:
1200 10.1038/s41586-019-1483-x
- 1201 Tommasi, A., Goryaeva, A., Carrez, P., Cordier, P., & Mainprice, D. (2018,
1202 June). Deformation, crystal preferred orientations, and seismic anisotropy in

- 1203 the Earth's D'' layer. *Earth and Planetary Science Letters*, 492, 35-46. doi:
 1204 10.1016/j.epsl.2018.03.032
- 1205 Tsuchiya, T., Tsuchiya, J., Umemoto, K., & Wentzcovitch, R. M. (2004). Phase
 1206 transition in MgSiO₃ perovskite in the earth's lower mantle. *Earth and Planetary
 1207 Science Letters*, 224(3-4), 241-248. doi: 10.1016/j.epsl.2004.05.017
- 1208 Tsujino, N., Nishihara, Y., Yamazaki, D., Seto, Y., Higo, Y., & Takahashi, E. (2016,
 1209 October). Mantle dynamics inferred from the crystallographic preferred orientation
 1210 of bridgemanite. *Nature*, 539(7627), 81-84. doi: 10.1038/nature19777
- 1211 Vinnik, L. P., Breger, L., & Romanowicz, B. (1998). Anisotropic structures at the
 1212 base of the Earth's mantle. *Nature*, 393(6685), 564-567. doi: 10.1038/31208
- 1213 Walker, A. M., Carrez, P., & Cordier, P. (2010). Atomic-scale models of disloca-
 1214 tion cores in minerals: Progress and prospects. *Mineralogical Magazine*, 74(3),
 1215 381-413. doi: 10.1180/minmag.2010.074.3.381
- 1216 Walker, A. M., Dobson, D. P., Wookey, J., Nowacki, A., & Forte, A. M. (2018). The
 1217 anisotropic signal of topotaxy during phase transitions in D''. *Physics of the Earth
 1218 and Planetary Interiors*, 276, 159-171. doi: 10.1016/j.pepi.2017.05.013
- 1219 Walker, A. M., Forte, A. M., Wookey, J., Nowacki, A., & Kendall, J.-M. (2011).
 1220 Elastic anisotropy of D'' predicted from global models of mantle flow. *Geochem-
 1221 istry Geophysics Geosystems*, 12(10), Q10006. doi: 10.1029/2011GC003732
- 1222 Walker, A. M., & Wookey, J. (2012). MSAT—A new toolkit for the analysis of elas-
 1223 tic and seismic anisotropy. *Computers & Geosciences*, 49, 81–90. doi: 10.1016/j
 1224 .cageo.2012.05.031
- 1225 Walpole, J., Wookey, J., Kendall, J.-M., & Masters, T.-G. (2017). Seismic anisotropy
 1226 and mantle flow below subducting slabs. *Earth and Planetary Science Letters*,
 1227 465, 155–167.
- 1228 Walsh, E., Arnold, R., & Savage, M. K. (2013, October). Silver and Chan revisited.
 1229 *Journal of Geophysical Research: Solid Earth*, 118(10), 5500-5515. doi: 10.1002/
 1230 jgrb.50386
- 1231 Walte, N. P., Heidelbach, F., Miyajima, N., Frost, D. J., Rubie, D. C., & Dobson,
 1232 D. P. (2009). Transformation textures in post-perovskite: Understanding mantle
 1233 flow in the D'' layer of the Earth. *Geophysical Research Letters*, 36, L04302. doi:
 1234 10.1029/2008GL036840
- 1235 Wang, Y., Hilairet, N., Nishiyama, N., Yahata, N., Tsuchiya, T., Morard, G., &

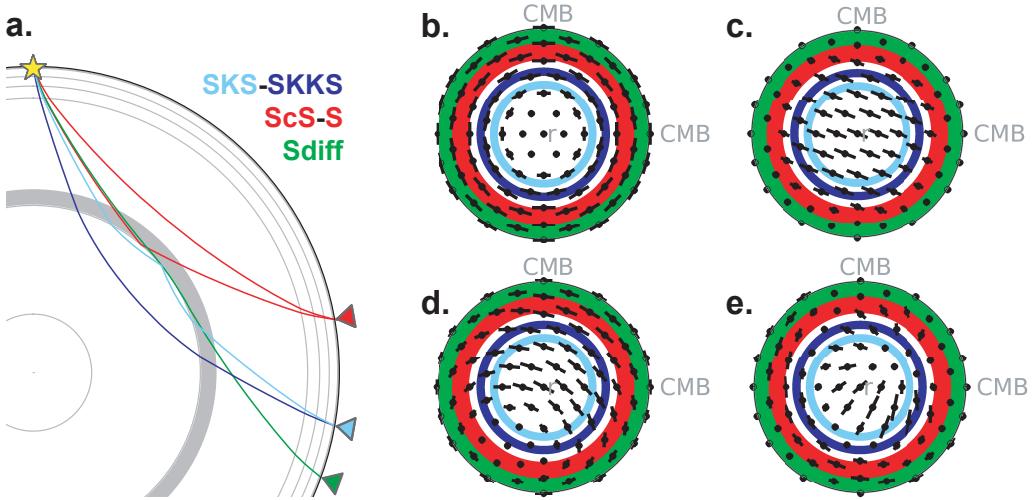
- 1236 Fiquet, G. (2013). High-pressure, high-temperature deformation of CaGeO₃
1237 (perovskite)±MgO aggregates: Implications for multiphase rheology of the lower
1238 mantle. *Geochemistry, Geophysics, Geosystems*, 14(9), 3389–3408.
- 1239 Wang, Y., & Wen, L. (2007). Complex seismic anisotropy at the border of a very
1240 low velocity province at the base of the Earth's mantle. *Journal Of Geophysical*
1241 *Research-Solid Earth*, 112(B9), B09305. doi: 10.1029/2006JB004719
- 1242 Wenk, H.-R., Cottaar, S., Tomé, C. N., McNamara, A. K., & Romanowicz, B.
1243 (2011). Deformation in the lowermost mantle: From polycrystal plasticity to
1244 seismic anisotropy. *Earth and Planetary Science Letters*, 306(1-2), 33-45. doi:
1245 10.1016/j.epsl.2011.03.021
- 1246 Wenk, H.-R., Lonardeli, I., Pehl, J., Devine, J., Prakapenka, V., Shen, G., & Mao,
1247 H.-K. (2004). In situ observation of texture development in olivine, ringwoodite,
1248 magnesiowüstite and silicate perovskite at high pressure. *Earth and Planetary*
1249 *Science Letters*, 226(3), 507-519. doi: 10.1016/j.epsl.2004.07.033
- 1250 Wentzcovitch, R. M., Tsuchiya, T., & Tsuchiya, J. (2006). MgSiO₃ postperovskite at
1251 D'' conditions. *Proceedings Of The National Academy Of Sciences Of The United*
1252 *States Of America*, 103(3), 543-546. doi: 10.1073/pnas.0506879103
- 1253 Wheeler, J. (2009, September). The preservation of seismic anisotropy in the Earth's
1254 mantle during diffusion creep. *Geophysical Journal International*, 178(3), 1723-
1255 1732. doi: 10.1111/j.1365-246X.2009.04241.x
- 1256 Wheeler, J. (2010, July). Anisotropic rheology during grain boundary diffusion
1257 creep and its relation to grain rotation, grain boundary sliding and superplasticity.
1258 *Philosophical Magazine*, 90(21), 2841-2864. doi: 10.1080/14786431003636097
- 1259 Wolf, J., Creasy, N., Pisconti, A., Long, M. D., & Thomas, C. (2019). An investi-
1260 gation of seismic anisotropy in the lowermost mantle beneath iceland. *Geophysical*
1261 *Journal International*. doi: 10.1093/gji/ggz312
- 1262 Wookey, J., & Dobson, D. P. (2008). Between a rock and a hot place: The core-
1263 mantle boundary. *Philosophical Transactions Of The Royal Society Of London*
1264 *Series A-Mathematical Physical And Engineering Sciences*, 366(1885), 4543-4557.
1265 doi: 10.1098/rsta.2008.0184
- 1266 Wookey, J., & Kendall, J.-M. (2007). Seismic anisotropy of post-perovskite and the
1267 lowermost mantle. In K. Hirose, J. Brodholt, T. Lay, & D. A. Yuen (Eds.), *Post-*
1268 *perovksite: The last mantle phase transition* (pp. 171–189). Washington, D.C.,

- 1269 USA: American Geophysical Union Geophysical Monograph 174.
- 1270 Wookey, J., & Kendall, J.-M. (2008). Constraints on lowermost mantle mineralogy
1271 and fabric beneath Siberia from seismic anisotropy. *Earth and Planetary Science
1272 Letters*, 275(1-2), 32-42. doi: 10.1016/j.epsl.2008.07.049
- 1273 Wookey, J., Kendall, J.-M., & Rümpker, G. (2005). Lowermost mantle anisotropy
1274 beneath the north Pacific from differential S–ScS splitting. *Geophysical Journal
1275 International*, 161(3), 829-838. doi: 10.1111/j.1365-246X.2005.02623.x
- 1276 Wu, X., Lin, J.-F., Kærcher, P., Mao, Z., Liu, J., Wenk, H.-R., & Prakapenka, V. B.
1277 (2017). Seismic anisotropy of the D'' layer induced by (001) deformation of post-
1278 perovskite. *Nature Communications*, 8, 14669.
- 1279 Wu, Z., Justo, J. F., & Wentzcovitch, R. M. (2013). Elastic anomalies in a spin-
1280 crossover system: Ferropericlase at lower mantle conditions. *Physical review let-
1281 ters*, 110(22), 228501.
- 1282 Wuestefeld, A., Al-Harrasi, O., Verdon, J. P., Wookey, J., & Kendall, J.-M. (2010).
1283 A strategy for automated analysis of passive microseismic data to image seismic
1284 anisotropy and fracture characteristics. *Geophysical Prospecting*, 58(5), 753-771.
1285 doi: 10.1111/j.1365-2478.2010.00891.x
- 1286 Yamazaki, D., & Karato, S. (2007). Lattice-preferred orientation of lower man-
1287 tle materials and seismic anisotropy in the D'' layer. In *Post-perovskite: The last
1288 mantle phase transition* (pp. 69–78). Washington, D.C., USA: American Geophys-
1289 ical Union.
- 1290 Yamazaki, D., & Karato, S.-i. (2002). Fabric development in (Mg,Fe)O during large
1291 strain, shear deformation: implications for seismic anisotropy in Earth's lower
1292 mantle. *Physics of The Earth and Planetary Interiors*, 131(3-4), 251-267. doi:
1293 10.1016/S0031-9201(02)00037-7
- 1294 Yamazaki, D., Yoshino, T., Ohfuchi, H., Ando, J.-i., & Yoneda, A. (2006). Origin of
1295 seismic anisotropy in the D'' layer inferred from shear deformation experiments on
1296 post-perovskite phase. *Earth and Planetary Science Letters*, 252(3-4), 372-378.
1297 doi: 10.1016/j.epsl.2006.10.004
- 1298 Young, C. J., & Lay, T. (1990). Multiple phase analysis of the shear velocity struc-
1299 ture in the D'' region beneath Alaska. *Journal of Geophysical Research: Solid
1300 Earth*, 95(B11), 17385–17402.
- 1301 Yu, S., & Garnero, E. J. (2018). Ultra-low velocity zone locations: A global assess-

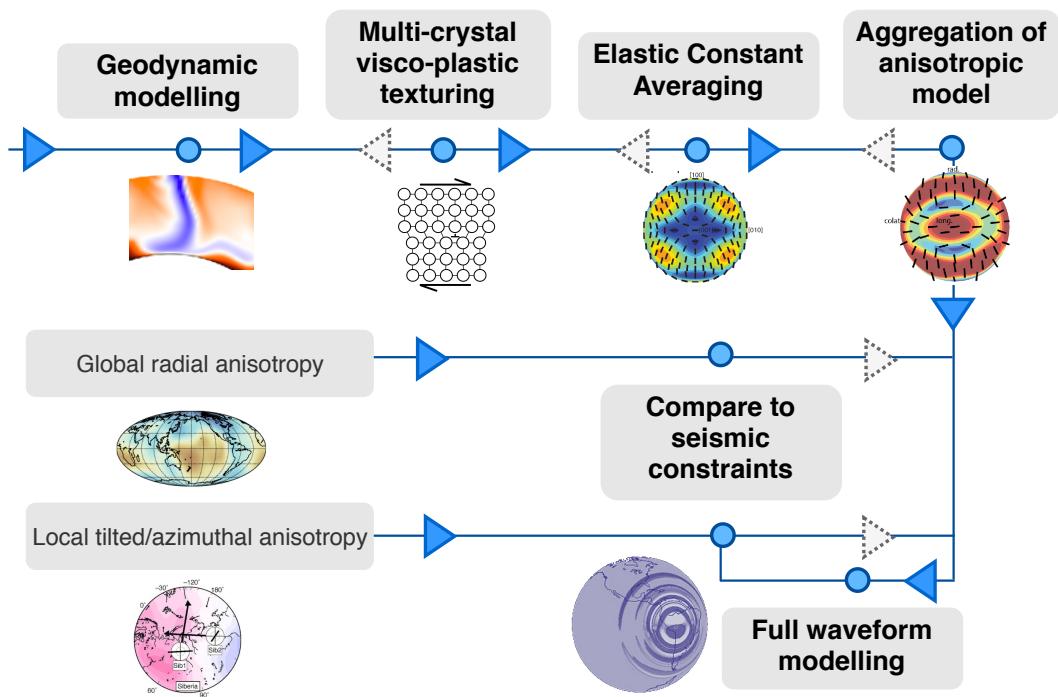
- 1302 ment. *Geochemistry, Geophysics, Geosystems*, 19(2), 396–414.
- 1303 Zhang, S., Cottaar, S., Liu, T., Stackhouse, S., & Militzer, B. (2016). High-pressure,
- 1304 temperature elasticity of Fe-and Al-bearing MgSiO₃: Implications for the Earth's
- 1305 lower mantle. *Earth and Planetary Science Letters*, 434, 264–273.
- 1306 Zhong, S., Zuber, M. T., Moresi, L., & Gurnis, M. (2000). Role of temperature-
- 1307 dependent viscosity and surface plates in spherical shell models of mantle convec-
- 1308 tion. *Journal of Geophysical Research: Solid Earth*, 105(B5), 11063–11082.



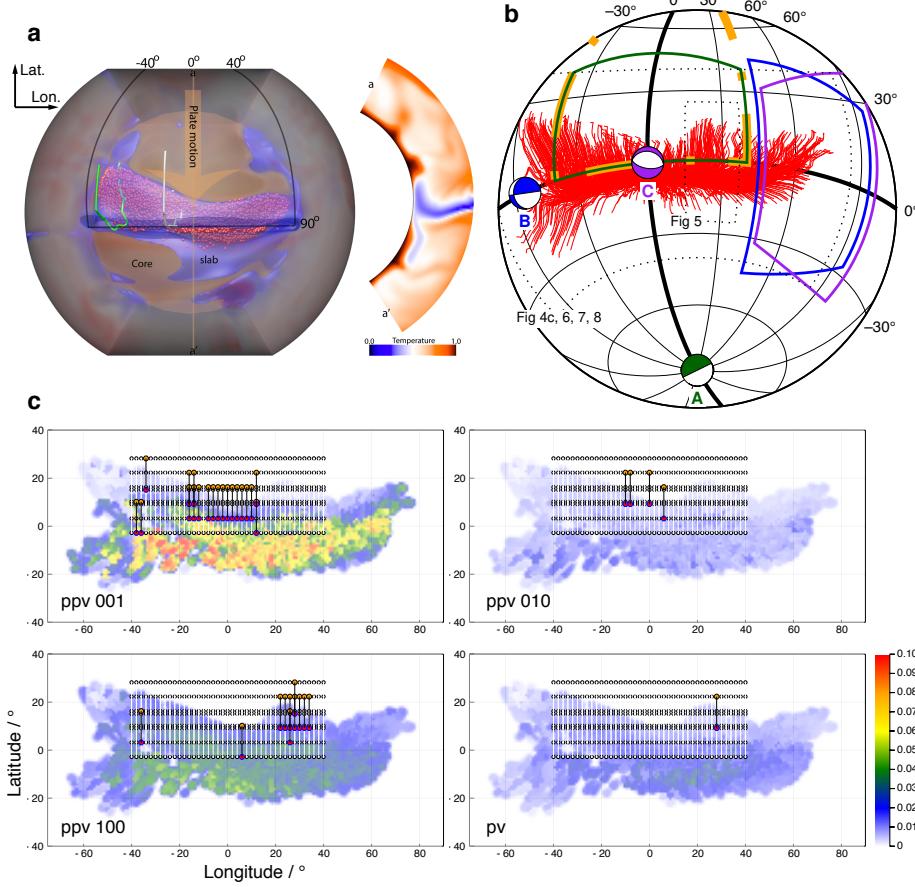
95 **Figure 1.** a. -d. Maps show shear wave radial anisotropic parameter ξ at 2800 km depth
96 for SEMUCBwm1 (French and Romanowicz, 2014), S362ANI+M (Moulik and Ekstrom 2014),
97 SAVANI (Auer et al. 2014), SGLOBE-rani (Chang et al., 2015). Red and blue contours show
98 bounds at three votes for the isotropic slow and fast cluster based on votes across five isotropic
99 models (Cottaar & Lekić, 2016). Histograms show distribution and mean values of ξ in the differ-
100 ent cluster vote areas, red-'slow', blue-'fast', yellow-'neutral' (boundaries for 'neutral' cluster are
101 not shown on the maps). e. Vote map showing where models agree on $\xi > 1$ or $\xi < 1$ (V_{SH} or
102 V_{SV} being faster, respectively). All models agree that $\xi > 1$ for 18% of the map, while for $\xi < 1$
103 the area is 13%.



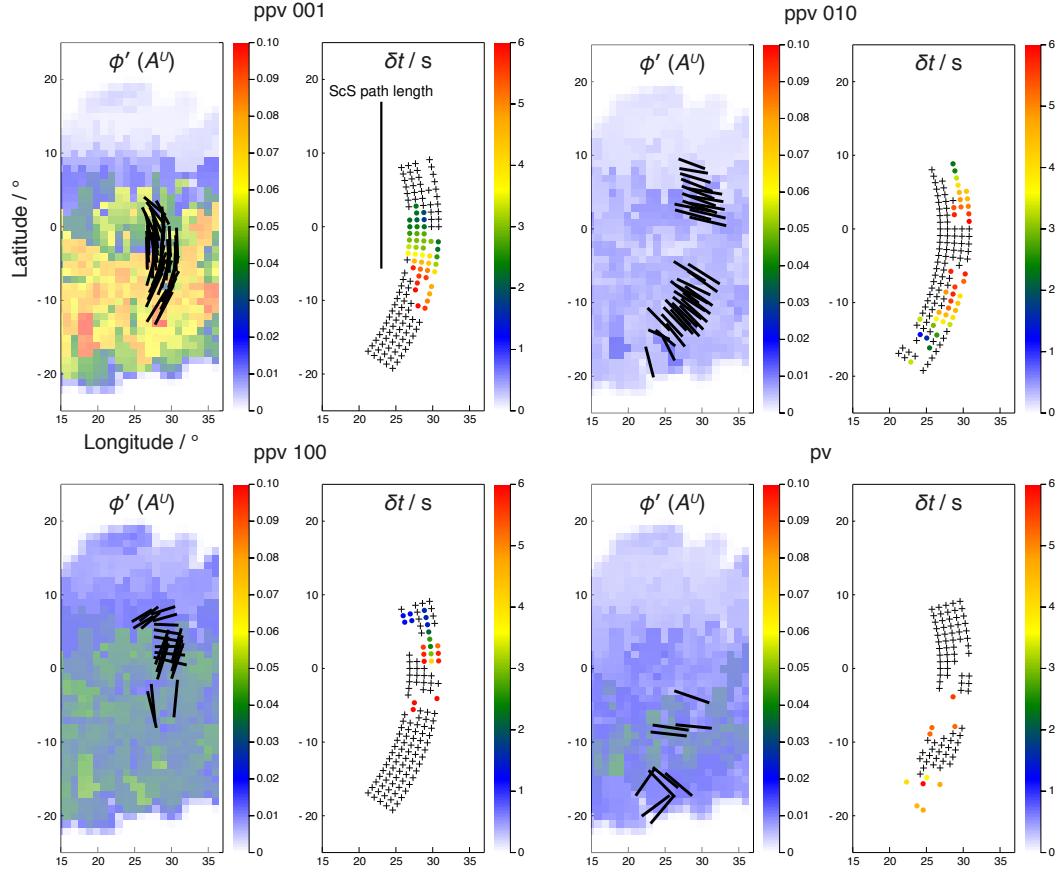
201 **Figure 2.** a. Ray paths for general body wave (pairs) used to constrain lowermost mantle
 202 anisotropy: SKS-SKKS (blue), ScS-S (red), S_{diff} (green) (made with Obspy; Krischer et al.,
 203 2015). b.-e. Hemisphere projections of various assumed anisotropic symmetries viewed from
 204 above (made with MSAT; Walker & Wookey, 2012). Bars show splitting direction and bar
 205 lengths show splitting strength as a function of shear wave propagation direction. Coloured shad-
 206 ing shows general sensitivity of body waves (see a.) although there is some overlap. b. Radial
 207 anisotropy with $\xi = 1.03$ c. 3% azimuthal anisotropy with a fast axis direction of 112° . d. Tilted
 208 anisotropy, i.e. anisotropy in c. tilted by 40° . e. Full anisotropic tensor for 75% post-perovskite
 209 and 25% periclase in a downgoing slab (see Section 4.2).



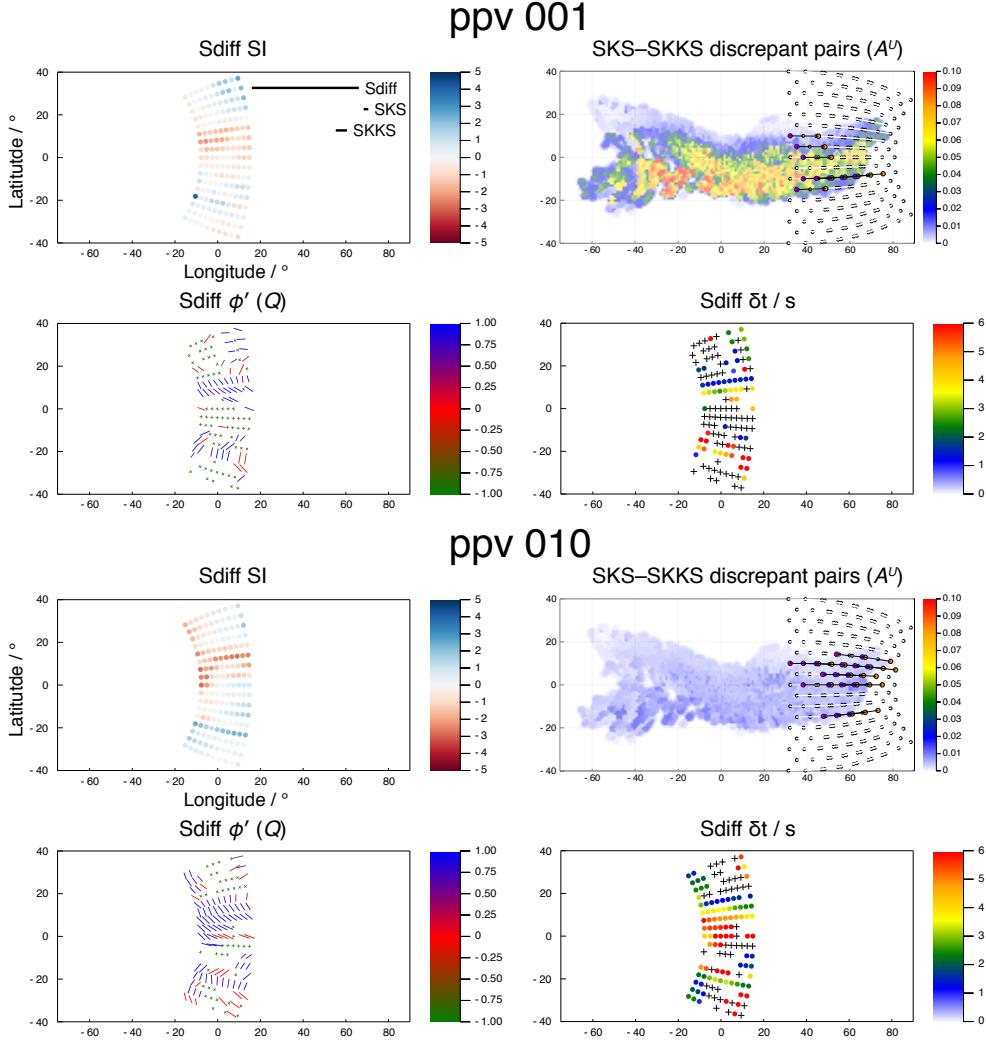
235 **Figure 3.** Showing the general steps in forward modelling from a flow model to interpreting
 236 seismic observations following the filled blue arrows as discussed in Section 3 . Dashed arrows
 237 indicate the inverse steps to go from seismic observations to flow directions, for which challenges
 238 and limitations are discussed in Section 5



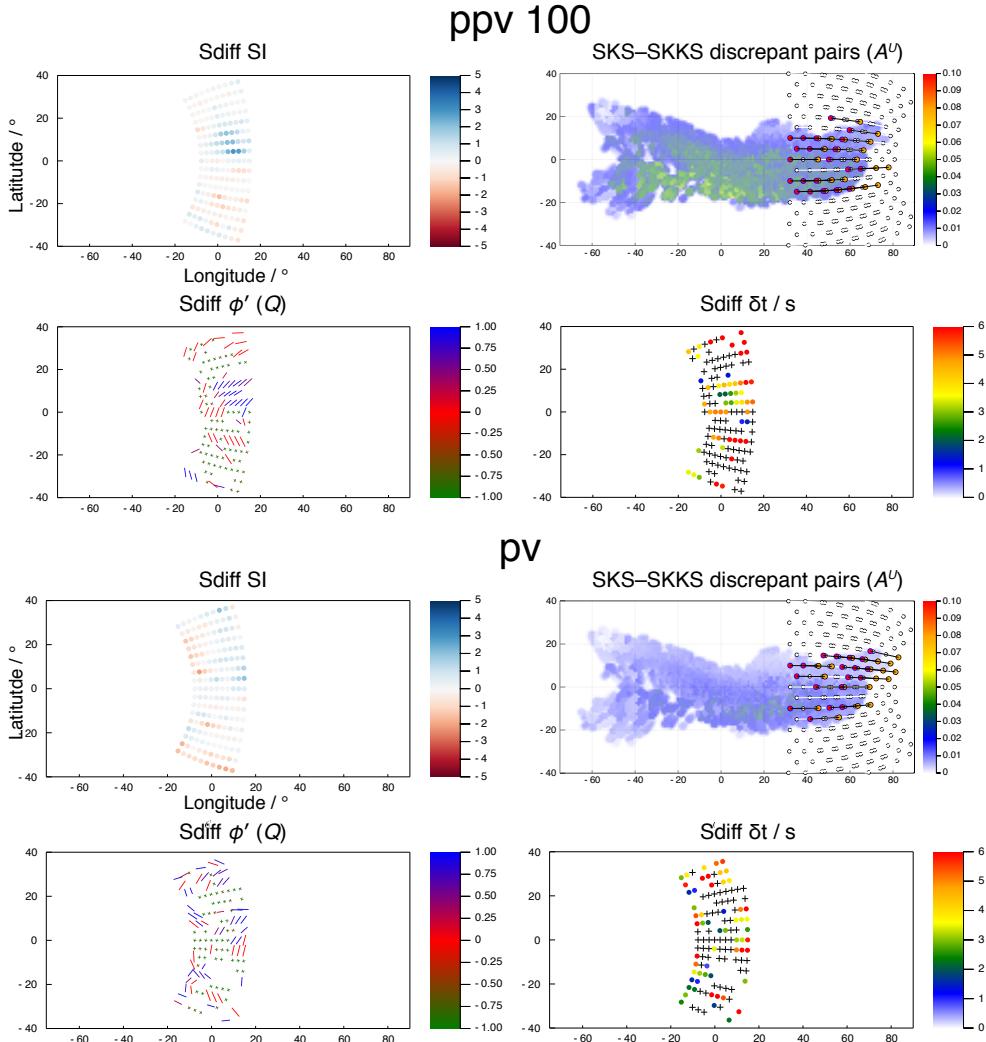
545 **Figure 4.** (a) Geodynamical setup of forward calculation, taken from Figure 1 of Cottaar et
 546 al. (2014). A slab is imposed, moving from north to south, which subducts along the equator.
 547 Tracer particles are shown by orange dots, with the path for two highlighted as green and white
 548 lines. Section a–a' along longitude 0° to the right shows non-dimensional temperature. (b) Ge-
 549 ometry of synthetic seismic sources and receivers in relation to the slab model. Sources are shown
 550 by colour-coded lower-hemisphere focal mechanisms (annotated with the code in Table 1), match-
 551 ing the receiver locations, shown by open areas with solid boundaries. Red lines show the paths
 552 of tracer particles, and orange dash-dotted lines show the slab edges in panel (a). Areas shown
 553 by other figures are indicated by dotted black lines and labelled. (c) Discrepant SKS-SKKS split-
 554 ting for path ‘A’ (Table 1) for each plasticity model. Red and orange circles respectively show
 555 the core piercing points for SKKS and SKS waves for pairs which are discrepant, whilst white
 556 circles denote the piercing points of pairs which are not. Underlying colour shows the strength of
 557 anisotropy at the bottom of the slab texture model, using the universal elastic anisotropy index,
 558 A^U (Ranganathan & Ostoja-Starzewski, 2008) according to the colour scale on the bottom right.
 559 (For approximate path lengths of SKS and SKKS in the lowermost mantle, see Figure 6.)



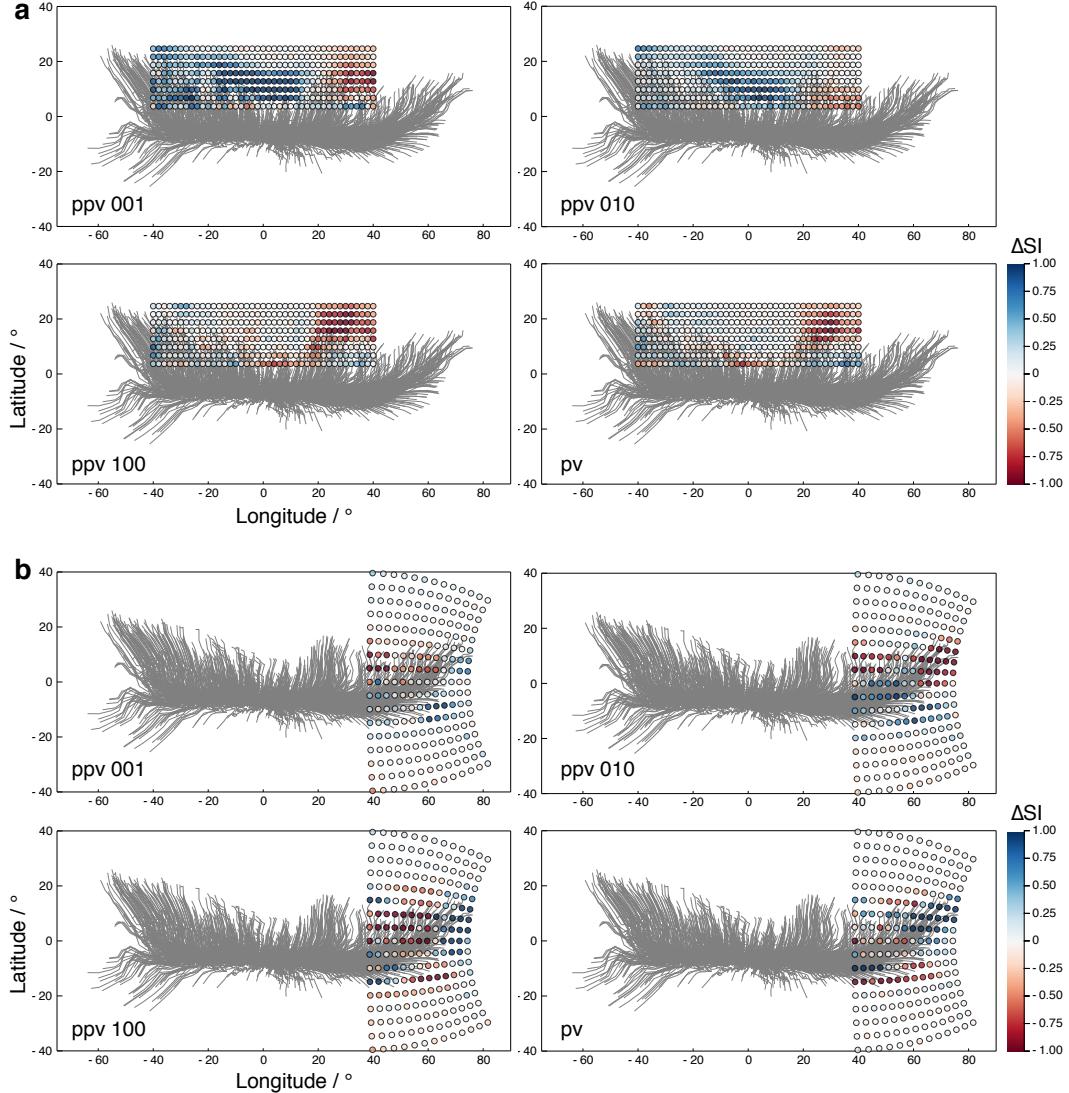
602 **Figure 5.** Shear-wave splitting results for the ScS phase for path ‘C’ (Table 1), for each
 603 slab texture. Each panel shows on the left the fast shear wave orientation in the ray frame (see
 604 Nowacki et al., 2010, Figure 1c), ϕ' , as a black bar located at the ScS core bounce point. Bars
 605 oriented left-right ($\phi' = 90^\circ$) correspond to radial anisotropy with $\xi > 1$, and vertical bars mean
 606 $\xi < 1$ ($\phi' = 0^\circ$), with non-radial anisotropy otherwise (when $0^\circ \neq \phi' \neq 90^\circ$). Colour beneath the
 607 bars is as in Figure 4c. On the right we show the amount of splitting, δt at each bounce point,
 608 coloured by the second scale bar. Crosses signify null measurements. The length of the ray path
 609 of ScS in the lowermost 250 km of the mantle is shown in the right hand panel for the ppv 001
 610 case.



625 **Figure 6.** Shear-wave splitting results for the path ‘B’ (Table 1) and models ppv001 and
 626 ppv010. For each plasticity model, four panels show: (top left) the splitting intensity (Chevrot,
 627 2000) of S_{diff} as colour; (bottom left) the ray-frame fast shear wave orientation of S_{diff} , coloured
 628 by the splitting quality measure Q (Wuestefeld et al., 2010); (bottom right) slow shear-wave
 629 delay time δt , coloured as per the scale bar; and (top right) pairs of discrepant SKS–SKKS
 630 splitting, where the red and orange circles show the core piercing point of SKKS and SKS, re-
 631 spectively, and white circles indicate no discrepant splitting; background colour shows strength
 632 of anisotropy as in Figure 4c. S_{diff} points are plotted at the end of the core-diffracted part of
 633 the path. The lengths of the ray paths of S_{diff} , SKS and SKKS in the lowermost 250 km of the
 634 mantle are shown in the SI panel for the ppv 001 case.



635 **Figure 7.** Shear-wave splitting results for the path ‘B’ (Table 1) and models ppv100 and pv.
 636 Features as for Figure 6.



672 **Figure 8.** Difference in splitting intensity between SKS and SKKS, ΔSI , for (a) path A and
 673 (b) path B (Table 1). ΔSI is shown by colour according to the scale, lower right, at the midpoint
 674 between SKS and SKKS core–mantle boundary piercing points. Grey lines in the background
 675 show the path of tracers particles in the geodynamic model.