

Integer programming

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Given

```
Weekday_vs_workers= matrix(data=c("SUNDAY", "MONDAY", "TUESDAY", "WEDNESDAY", "THURSDAY", "FRIDAY", "SATUARDAY"),  
Dayoff_vs_wage= matrix(data=c("Sunday and Monday", "Monday and Tuesday", "Tuesday and Wednesday", "Wednesday and Thursday", "Thursday and Friday", "Friday and Saturday", "Saturday and Sunday"),  
Dayoff_vs_wage
```

```
##      [,1]      [,2]  
## [1,] "Sunday and Monday"      "775"  
## [2,] "Monday and Tuesday"      "800"  
## [3,] "Tuesday and Wednesday"   "800"  
## [4,] "Wednesday and Thursday"  "800"  
## [5,] "Thursday and Friday"      "800"  
## [6,] "Friday and Saturday"      "775"  
## [7,] "Saturday and Sunday"      "750"
```

```
Weekday_vs_workers
```

```
##      [,1]      [,2]  
## [1,] "SUNDAY"      "18"  
## [2,] "MONDAY"      "27"  
## [3,] "TUESDAY"      "22"  
## [4,] "WEDNESDAY"    "26"  
## [5,] "THURSDAY"     "25"  
## [6,] "FRIDAY"       "21"  
## [7,] "SATUARDAY"    "19"
```

Let Number of Workers in a shift are $x_1, x_2, x_3, x_4, x_5, x_6, x_7$

Hence Objective Function is to minimize the number off workers in the week. There-Fore $\text{Min: } 775x_1 + 800x_2 + 800x_3 + 800x_4 + 800x_5 + 775x_6 + 750x_7$

Constraints are $x_2 + x_3 + x_4 + x_5 + x_6 \geq 18$; $x_3 + x_4 + x_5 + x_6 + x_7 \geq 27$; $x_1 + x_4 + x_5 + x_6 + x_7 \geq 22$; $x_1 + x_2 + x_5 + x_6 + x_7 \geq 26$; $x_1 + x_2 + x_3 + x_6 + x_7 \geq 25$; $x_1 + x_2 + x_3 + x_4 + x_7 \geq 21$; $x_1 + x_2 + x_3 + x_4 + x_5 \geq 19$;

```
library(lpSolveAPI)  
  
Sol <- read.lp("Integer_programming.lp")  
  
solve(Sol)
```

```
## [1] 0
```

```
get.objective(Sol)
```

```
## [1] 25675
```

```
get.variables(Sol)
```

```
## [1] 2 4 5 0 8 1 13
```

The minimum cost is 25,675 dollars

Number of workers available on Sunday is 19,

Monday is 27,

Tuesday is 24,

Wednesday is 28,

Thursday is 25,

Friday is 24,

Saturday is 20.