

# Motion Estimation Algorithms

## General Figures

- Image Dimensions (max.): 112V x 112H
- Bit Depth: 14 bits (stored in uint16) → change to 8 !!
- Time for acquiring one whole image: 46ms ( $\approx$  max. 21 images/s)  
( @ CPU clock 24MHz with clock dividers 4 for ADC and Timers )  
(can not arbitrarily be reduced without loss in quality because of camera)
- Time for storing one image on FRAM: 287ms (measured)  
(can be reduced by factor  $\frac{1}{2}$  if changing bit depth to 8!)
- **Camera Specifications:**
  - focal length f: 4mm
  - difference between two pixels: 25 $\mu$ m
  - size of focal plane s: 112 \* 25 $\mu$ m = 2.8mm
  - field of view (FOV):  $2 * \arcsin(s/2f) \approx 41^\circ$
  - size of image plane in distance d:  $s/f * d = 1.26 \text{ m}$  for d = 1.8m
  - pixel size in distance d: 11.2mm for d = 1.8m
- **Example:**
  - @ 20 fps  $\Rightarrow$  1m/s  $\rightarrow$  50 mm = 4.5 pixels displacement per frame
  - @ 20 fps  $\Rightarrow$  1.4m/s  $\rightarrow$  70 mm = 6.25 pixels displ. per frame
  - $\Rightarrow$  We need to recover displacements of  $\pm 10$  pixels for normal walking speed!

## Differential Methods

- **Lucas-Kanade Algorithm**
  - Only for small motions, such that differential equation holds (often less than the pixel spacing)
    - pyramidal approach
      - small obstacles get lost
      - poor estimates propagate through all levels
  - can only recover displacements on edges / if enough brightness structure is available
  - MATLAB: performs well for very small displacements ( $\sim 1$  pixel)
  - high computational effort
- **Kanade–Lucas–Tomasi feature tracker**
  - same motion estimation as Lucas-Kanade-Method
  - only tracking features that are suitable for the tracking algorithm. The proposed features would be selected if both the eigenvalues of the gradient matrix were larger than some threshold.
  - same Problems as Lucas-Kanade algorithm

## Frequency-based Methods

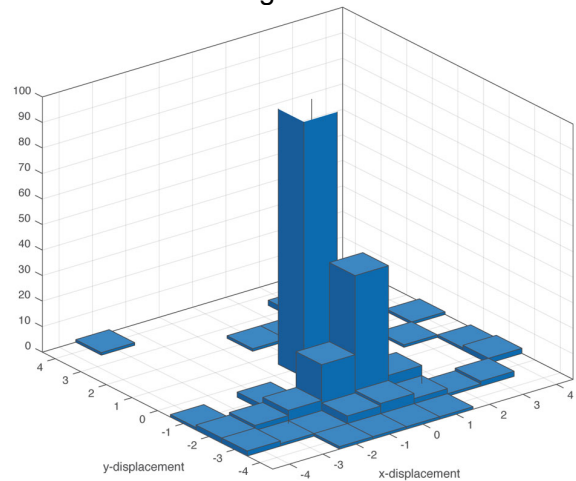
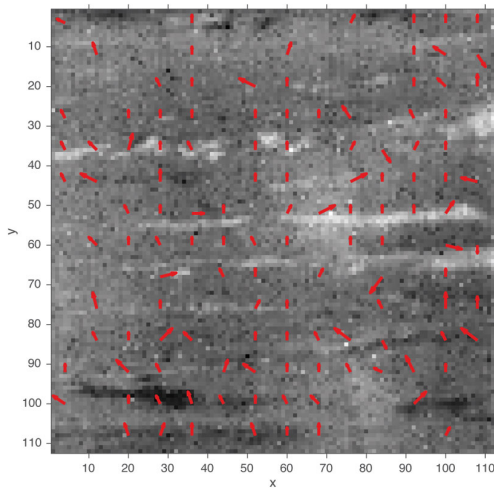
Idea: Transform image sequence from time-domain into frequency domain

- Only useful if „large“ sequence of images available
- high computational effort

## Correlation-based Methods

- **Block Correlation Algorithm (2D)**

- MATLAB: blocks of 8x8 pixels, +/- 4 pixels displacement search area
  - Number of Cost-Function evaluations:
    - $\text{numblocks\_x} * \text{numblocks\_y} * (2 * \text{searcharea\_x} + 1) * (2 * \text{searcharea\_y} + 1) * \text{blocksize\_x} * \text{blocksize\_y}$
    - $= \text{numpixels\_x} * \text{numpixels\_y} * (2 * \text{searcharea\_x} + 1) * (2 * \text{searcharea\_y} + 1)$
    - in this case: 1'016'064
  - performs well if enough brightness structure is available
  - estimates get arbitrary if too less structure
  - bias on (0, 0) displacement because of noise pattern from camera
  - relatively high computational effort (esp. for big search areas)
- TODO:
  - introduce quality figure for each estimate to detect poor estimates
  - how to deal with mask/noise pattern?
  - implement other than exhaustive search for big search areas

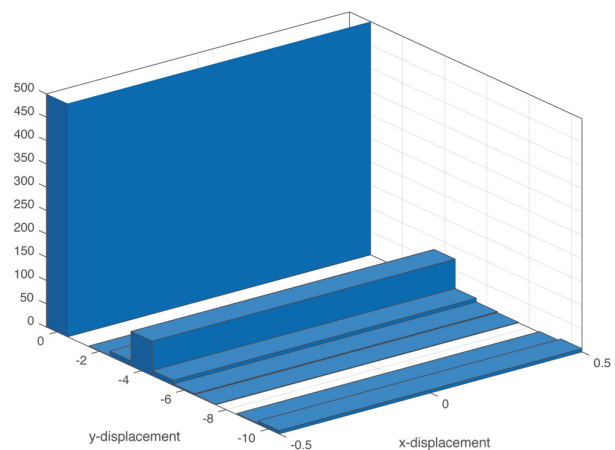
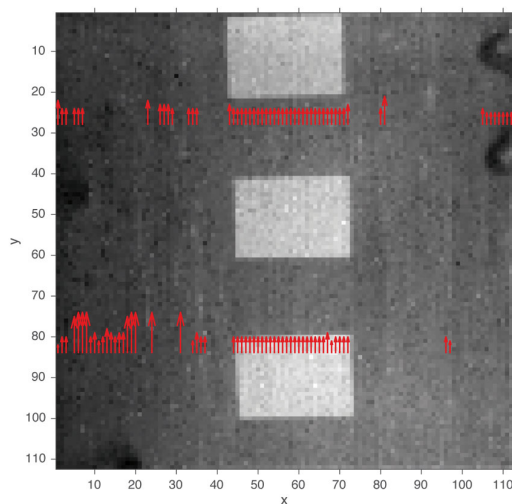


- **Simplified Block Correlation Algorithm, evaluating only certain points**

- Idea: same as block correlation algorithm, but the cost function is only evaluated at some predefined points within the block
- MATLAB:
  - Number of cost-function evaluations:
    - $\text{numblocks\_x} * \text{numblocks\_y} * (2 * \text{searcharea\_x} + 1) * (2 * \text{searcharea\_y} + 1) * (\text{blocksize\_x} + \text{blocksize\_y})$
    - in this case: 254'016
  - Performance is significantly worse than normal Block Correlation Algorithm
  - less computational effort

- **1D Correlation Algorithm**

- MATLAB: block size: 1x56 pixels, +- 10 pixel search area (in y-direction)
  - Number of cost-function evaluations:
    - $\text{numblocks\_x} * \text{numblocks\_y} * (2 * \text{searcharea\_x} + 1) * (2 * \text{searcharea\_y} + 1) * \text{blocksize\_x} * \text{blocksize\_y}$
    - $= \text{numpixels\_x} * \text{numpixels\_y} * (2 * \text{searcharea\_x} + 1) * (2 * \text{searcharea\_y} + 1)$
    - in this case: 263'424
  - computational effort is not too big, and can even be reduced if one considers only single columns
  - performs well, also for big displacements up to 10 pixels
  - estimates get arbitrary if too less structure
  - bias on (0, 0) displacement because of noise pattern from camera
  - If displacement is not exactly along the y-axis, the estimates may get arbitrarily bad (depending on the brightness structure)
- TODO:
  - introduce quality figure for each estimate to detect poor estimates
  - how to deal with mask/noise pattern?
  - implement other than exhaustive search for big search areas



- **2x1D Correlation Algorithms using only certain rows/columns**

- Idea: Only evaluate certain rows and columns and estimate the optical flow at the intersection points by evaluating horizontal and vertical 1D-displacement separately.
- MATLAB: block size 8x8, search area +- 4 pixels
  - Number of cost-function evaluations:
    - $\text{numblocks\_x} * \text{numblocks\_y} * \{ (2 * \text{searcharea\_x} + 1) * \text{blocksize\_x} + (2 * \text{searcharea\_y} + 1) * \text{blocksize\_y} \}$
    - in this case: 28'224
  - use less memory (not whole image has to be acquired/stored)
  - if displacements are not purely horizontal or vertical, small objects can easily be lost and estimate can get very bad!