

NAME – ANSH GOEL

REG NO. – 20BCE1798

COURSE NAME – FOUNDATION OF DATA ANALYTICS (FDA)

COURSE CODE: 3505

DATE – 6TH OCTOBER, 2022

LAB-9

Q. Take a dataset and choose two attributes. Make a sample of 20 from them. Calculate the correlation using R and verify it using manual calculations.

```
> data(mtcars)
> head(mtcars)

  mpg cyl disp hp drat    wt  qsec vs am gear carb
Mazda RX4     21.0   6 160 110 3.90 2.620 16.46  0  1    4    4
Mazda RX4 Wag 21.0   6 160 110 3.90 2.875 17.02  0  1    4    4
Datsun 710    22.8   4 108  93 3.85 2.320 18.61  1  1    4    1
Hornet 4 Drive 21.4   6 258 110 3.08 3.215 19.44  1  0    3    1
Hornet Sportabout 18.7   8 360 175 3.15 3.440 17.02  0  0    3    2
Valiant      18.1   6 225 105 2.76 3.460 20.22  1  0    3    1
> mtcars

  mpg cyl disp hp drat    wt  qsec vs am gear carb
Mazda RX4     21.0   6 160.0 110 3.90 2.620 16.46  0  1    4    4
Mazda RX4 Wag 21.0   6 160.0 110 3.90 2.875 17.02  0  1    4    4
Datsun 710    22.8   4 108.0  93 3.85 2.320 18.61  1  1    4    1
Hornet 4 Drive 21.4   6 258.0 110 3.08 3.215 19.44  1  0    3    1
Hornet Sportabout 18.7   8 360.0 175 3.15 3.440 17.02  0  0    3    2
Valiant      18.1   6 225.0 105 2.76 3.460 20.22  1  0    3    1
Duster 360    14.3   8 360.0 245 3.21 3.570 15.84  0  0    3    4
Merc 240D     24.4   4 146.7  62 3.69 3.190 20.00  1  0    4    2
Merc 230      22.8   4 140.8  95 3.92 3.150 22.90  1  0    4    2
Merc 280      19.2   6 167.6 123 3.92 3.440 18.30  1  0    4    4
Merc 280C     17.8   6 167.6 123 3.92 3.440 18.90  1  0    4    4
Merc 450SE     16.4   8 275.8 180 3.07 4.070 17.40  0  0    3    3
Merc 450SL     17.3   8 275.8 180 3.07 3.730 17.60  0  0    3    3
Merc 450SLC    15.2   8 275.8 180 3.07 3.780 18.00  0  0    3    3
Cadillac Fleetwood 10.4   8 472.0 205 2.93 5.250 17.98  0  0    3    4
Lincoln Continental 10.4   8 460.0 215 3.00 5.424 17.82  0  0    3    4
Chrysler Imperial 14.7   8 440.0 230 3.23 5.345 17.42  0  0    3    4
Fiat 128       32.4   4  78.7  66 4.08 2.200 19.47  1  1    4    1
Honda Civic    30.4   4  75.7  52 4.93 1.615 18.52  1  1    4    2
Toyota Corolla 33.9   4  71.1  65 4.22 1.835 19.90  1  1    4    1
Toyota Corona   21.5   4 120.1  97 3.70 2.465 20.01  1  0    3    1
Dodge Challenger 15.5   8 318.0 150 2.76 3.520 16.87  0  0    3    2
```

```

> df<-data.frame(mtcars)
> df
      mpg cyl disp hp drat    wt  qsec vs am gear carb
Mazda RX4     21.0   6 160.0 110 3.90 2.620 16.46  0  1    4    4
Mazda RX4 Wag 21.0   6 160.0 110 3.90 2.875 17.02  0  1    4    4
Datsun 710    22.8   4 108.0  93 3.85 2.320 18.61  1  1    4    1
Hornet 4 Drive 21.4   6 258.0 110 3.08 3.215 19.44  1  0    3    1
Hornet Sportabout 18.7   8 360.0 175 3.15 3.440 17.02  0  0    3    2
Valiant     18.1   6 225.0 105 2.76 3.460 20.22  1  0    3    1
Duster 360    14.3   8 360.0 245 3.21 3.570 15.84  0  0    3    4
Merc 240D     24.4   4 146.7  62 3.69 3.190 20.00  1  0    4    2
Merc 230      22.8   4 140.8  95 3.92 3.150 22.90  1  0    4    2
Merc 280      19.2   6 167.6 123 3.92 3.440 18.30  1  0    4    4
Merc 280C     17.8   6 167.6 123 3.92 3.440 18.90  1  0    4    4
Merc 450SE     16.4   8 275.8 180 3.07 4.070 17.40  0  0    3    3
Merc 450SL     17.3   8 275.8 180 3.07 3.730 17.60  0  0    3    3
Merc 450SLC    15.2   8 275.8 180 3.07 3.780 18.00  0  0    3    3
Cadillac Fleetwood 10.4   8 472.0 205 2.93 5.250 17.98  0  0    3    4
Lincoln Continental 10.4   8 460.0 215 3.00 5.424 17.82  0  0    3    4
Chrysler Imperial 14.7   8 440.0 230 3.23 5.345 17.42  0  0    3    4
Fiat 128       32.4   4  78.7  66 4.08 2.200 19.47  1  1    4    1
Honda Civic    30.4   4  75.7  52 4.93 1.615 18.52  1  1    4    2
Toyota Corolla 33.9   4  71.1  65 4.22 1.835 19.90  1  1    4    1
Toyota Corona   21.5   4 120.1  97 3.70 2.465 20.01  1  0    3    1
Dodge Challenger 15.5   8 318.0 150 2.76 3.520 16.87  0  0    3    2
AMC Javelin    15.2   8 304.0 150 3.15 3.435 17.30  0  0    3    2
Camaro Z28     13.3   8 350.0 245 3.73 3.840 15.41  0  0    3    4
Pontiac Firebird 19.2   8 400.0 175 3.08 3.845 17.05  0  0    3    2
Fiat X1-9       27.3   4  79.0  66 4.08 1.935 18.90  1  1    4    1
Porsche 914-2   26.0   4 120.3  91 4.43 2.140 16.70  0  1    5    2
Lotus Europa    30.4   4  95.1 113 3.77 1.513 16.90  1  1    5    2
Ford Pantera L  15.8   8 351.0 264 4.22 3.170 14.50  0  1    5    4
Ferrari Dino    19.7   6 145.0 175 3.62 2.770 15.50  0  1    5    6
Maserati Bora   15.0   8 301.0 335 3.54 3.570 14.60  0  1    5    8

```

```

> df_20<-df[sample(nrow(df),size=20),]
> df_20
      mpg cyl disp hp drat    wt  qsec vs am gear carb
Merc 450SLC    15.2   8 275.8 180 3.07 3.780 18.00  0  0    3    3
Hornet Sportabout 18.7   8 360.0 175 3.15 3.440 17.02  0  0    3    2
Chrysler Imperial 14.7   8 440.0 230 3.23 5.345 17.42  0  0    3    4
Fiat X1-9       27.3   4  79.0  66 4.08 1.935 18.90  1  1    4    1
Merc 280       19.2   6 167.6 123 3.92 3.440 18.30  1  0    4    4
Duster 360     14.3   8 360.0 245 3.21 3.570 15.84  0  0    3    4
Toyota Corolla 33.9   4  71.1  65 4.22 1.835 19.90  1  1    4    1
Datsun 710     22.8   4 108.0  93 3.85 2.320 18.61  1  1    4    1
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Hornet 4 Drive  21.4   6 258.0 110 3.08 3.215 19.44  1  0    3    1
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Dodge Challenger 15.5   8 318.0 150 2.76 3.520 16.87  0  0    3    2
Cadillac Fleetwood 10.4   8 472.0 205 2.93 5.250 17.98  0  0    3    4
Fiat 128       32.4   4  78.7  66 4.08 2.200 19.47  1  1    4    1
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Merc 280C     17.8   6 167.6 123 3.92 3.440 18.90  1  0    4    4
Lincoln Continental 10.4   8 460.0 215 3.00 5.424 17.82  0  0    3    4
> x<-df_20$mpg
> y<-df_20$cyl

```

```

> x
[1] 15.2 18.7 14.7 27.3 19.2 14.3 33.9 22.8 17.3 30.4 19.7 21.4 15.8 30.4 15.5 10.4 32.4 24.4 17.8 10.4
> y
[1] 8 8 8 4 6 8 4 4 8 4 6 6 8 4 8 8 4 4 6 8
```
> cor(x, y, method = c("pearson"))
[1] -0.8977234
> cor(x, y, method = c("kendall"))
[1] -0.8089641
> cor(x, y, method = c("spearman"))
[1] -0.917594
>

```

## Manual Calculations:

| Manual calculations |   |                  |                     |        | Page No.             | Date : / / |
|---------------------|---|------------------|---------------------|--------|----------------------|------------|
| x                   | y | (x - $\bar{x}$ ) | (y - $\bar{y}$ )    | $dxdy$ |                      |            |
| 15.2                | 8 | -5.4             | 1.8                 | -9.72  |                      |            |
| 18.7                | 8 | -1.9             | 1.8                 | -3.42  |                      |            |
| 14.7                | 8 | 5.9              | 1.8                 | 10.62  |                      |            |
| 27.3                | 4 | 6.7              | -2.2                | 14.74  |                      |            |
| 19.2                | 6 | -1.4             | -0.2                | 0.28   | $\bar{x} = 20.6$     |            |
| 14.3                | 8 | -6.3             | 1.8                 | -11.34 |                      |            |
| 33.9                | 4 | 13.3             | -2.2                | -29.26 | $\bar{y} = 6.2$      |            |
| 22.8                | 4 | 2.2              | <del>1.8</del> -2.2 | -4.84  | $\sum dx^2 = 958.92$ |            |
| 17.3                | 8 | -3.3             | 1.8                 | -5.94  | $\sum dy^2 = 63.2$   |            |
| 30.4                | 4 | 9.8              | -2.2                | -21.56 |                      |            |
| 19.7                | 6 | -0.9             | 0.2                 | 0.18   | $\sum dxdy = -221$   |            |
| 21.4                | 6 | 0.8              | -0.2                | -0.16  |                      |            |
| 15.8                | 8 | -4.8             | 1.8                 | 8.64   |                      |            |
| 30.4                | 4 | 9.8              | -2.2                | -21.56 |                      |            |
| 15.5                | 8 | -5.1             | 1.8                 | 9.18   |                      |            |
| 10.4                | 8 | -10.2            | 1.8                 | 18.36  |                      |            |
| 32.4                | 4 | 11.8             | -2.2                | -25.96 |                      |            |
| 24.4                | 4 | 3.8              | -2.2                | -8.36  |                      |            |
| 17.8                | 6 | -2.8             | -0.2                | 0.56   |                      |            |
| 10.4                | 8 | -10.2            | 1.8                 | -18.36 |                      |            |

| Asc order |        |       |             |             |        |        |
|-----------|--------|-------|-------------|-------------|--------|--------|
| $x$       | $d^2$  | $d$   | Rank of $y$ | Rank of $x$ | $dy^2$ | $dx^2$ |
| 1.5       | 121    | -11   | 16          | 5           | 3.24   | 24.16  |
| 1.5       | 36     | -6    | 16          | 10          | 3.24   | 3.61   |
| 3         | 144    | -12   | 16          | 4           | 3.24   | 34.81  |
| 4         | 144    | -12   | 4           | 16          | 4.84   | 44.84  |
| 5         | 225    | 15    | 9.5         | 11          | 0.04   | 1.96   |
| 6         | 169    | -13   | 16          | 3           | 3.24   | 39.69  |
| 7         | 256    | 16    | 4           | 20          | 4.84   | 176.84 |
| 8         | 100    | 10    | 4           | 14          | 4.84   | 4.48   |
| 9         | 64     | -8    | 4           | 12.5        | 3.24   | 10.89  |
| 10        | 182.25 | 13.5  | 9.5         | 11          | 0.04   | 96.04  |
| 11        | 6.25   | 2.5   | 9.5         | 13          | 3.24   | 0.64   |
| 12        | 12.25  | 3.5   | 16          | 7           | 4.84   | 23.04  |
| 13        | 81     | 2.5   | 4           | 17.5        | 3.24   | 96.04  |
| 14        | 182.25 | 13.5  | 16          | 6           | 2.24   | 26.01  |
| 15        | 100    | -10   | 2.5         | 15          | 3.24   | 121.21 |
| 16        | 210.25 | -14.5 | 16          |             | 4.84   | 144    |
| 17.5      | 225    | 15    | 4           | 19          | 4.84   | 7.84   |
| 17.5      | 121    | 11    | 4           | 15          | 0.04   | 104.04 |
| 19        | 0.25   | -0.5  | 9.5         | 9           | 3.24   |        |
| 20        | 210.25 | -14.5 | 16          | 1.5         |        |        |

$$\sum d^2 = 2367$$

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Correlation using Pearson's method

$$r = \frac{\sum dxy}{\sqrt{\sum d^2} \sqrt{\sum y^2}}$$

$$= \frac{-221}{\sqrt{2367} \sqrt{63.2}} = -0.8477234012$$

Correlation using Spearman's method.

$$r_s = 1 - \frac{6 \left[ \sum d_i^2 + \frac{1}{12} (m_1^3 - m_1) + \frac{1}{12} (m_2^3 - m_2) + \frac{1}{12} (m_3^3 - m_3) \right]}{n^3 - n}$$

$$2367 = \sum d^2$$

$$r_s = 1 - \frac{6 \left[ 2367 + \frac{1}{12} (7^3 - 7) + \frac{1}{12} (9^3 - 9) + \frac{1}{12} (4^3 - 4) + \frac{1}{12} (2^3 - 2) \right]}{20(349)}$$

Rank  $\rightarrow n$  Kendall's Method.

$$\gamma = \frac{\sum C - \sum D}{\sum C + \sum D} \Rightarrow -0.809$$

**Result:**

The manual calculations and R answers match each other.