

**NAME – ANSH GOEL**

**REG NO. – 20BCE1798**

**COURSE NAME – FOUNDATION OF DATA ANALYTICS (FDA)**

**COURSE CODE: 3505**

**DATE – 6<sup>TH</sup> OCTOBER, 2022**

## **LAB-9**

**Q. Take a dataset and choose two attributes. Make a sample of 20 from them. Calculate the correlation using R and verify it using manual calculations.**

```
> data(mtcars)
> head(mtcars)
```

	mpg	cyl	dis	hp	drat	wt	qsec	vs	am	gear	carb
Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1

```
> mtcars
```

	mpg	cyl	dis	hp	drat	wt	qsec	vs	am	gear	carb
Mazda RX4	21.0	6	160.0	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160.0	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225.0	105	2.76	3.460	20.22	1	0	3	1
Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
Merc 230	22.8	4	140.8	95	3.92	3.150	22.90	1	0	4	2
Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
Merc 450SE	16.4	8	275.8	180	3.07	4.070	17.40	0	0	3	3
Merc 450SL	17.3	8	275.8	180	3.07	3.730	17.60	0	0	3	3
Merc 450SLC	15.2	8	275.8	180	3.07	3.780	18.00	0	0	3	3
Cadillac Fleetwood	10.4	8	472.0	205	2.93	5.250	17.98	0	0	3	4
Lincoln Continental	10.4	8	460.0	215	3.00	5.424	17.82	0	0	3	4
Chrysler Imperial	14.7	8	440.0	230	3.23	5.345	17.42	0	0	3	4
Fiat 128	32.4	4	78.7	66	4.08	2.200	19.47	1	1	4	1
Honda Civic	30.4	4	75.7	52	4.93	1.615	18.52	1	1	4	2
Toyota Corolla	33.9	4	71.1	65	4.22	1.835	19.90	1	1	4	1
Toyota Corona	21.5	4	120.1	97	3.70	2.465	20.01	1	0	3	1
Dodge Challenger	15.5	8	318.0	150	2.76	3.520	16.87	0	0	3	2

```
> df<-data.frame(mtcars)
> df
```

	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
Mazda RX4	21.0	6	160.0	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 wag	21.0	6	160.0	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225.0	105	2.76	3.460	20.22	1	0	3	1
Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
Merc 230	22.8	4	140.8	95	3.92	3.150	22.90	1	0	4	2
Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
Merc 450SE	16.4	8	275.8	180	3.07	4.070	17.40	0	0	3	3
Merc 450SL	17.3	8	275.8	180	3.07	3.730	17.60	0	0	3	3
Merc 450SLC	15.2	8	275.8	180	3.07	3.780	18.00	0	0	3	3
Cadillac Fleetwood	10.4	8	472.0	205	2.93	5.250	17.98	0	0	3	4
Lincoln Continental	10.4	8	460.0	215	3.00	5.424	17.82	0	0	3	4
Chrysler Imperial	14.7	8	440.0	230	3.23	5.345	17.42	0	0	3	4
Fiat 128	32.4	4	78.7	66	4.08	2.200	19.47	1	1	4	1
Honda Civic	30.4	4	75.7	52	4.93	1.615	18.52	1	1	4	2
Toyota Corolla	33.9	4	71.1	65	4.22	1.835	19.90	1	1	4	1
Toyota Corona	21.5	4	120.1	97	3.70	2.465	20.01	1	0	3	1
Dodge Challenger	15.5	8	318.0	150	2.76	3.520	16.87	0	0	3	2
AMC Javelin	15.2	8	304.0	150	3.15	3.435	17.30	0	0	3	2
Camaro Z28	13.3	8	350.0	245	3.73	3.840	15.41	0	0	3	4
Pontiac Firebird	19.2	8	400.0	175	3.08	3.845	17.05	0	0	3	2
Fiat X1-9	27.3	4	79.0	66	4.08	1.935	18.90	1	1	4	1
Porsche 914-2	26.0	4	120.3	91	4.43	2.140	16.70	0	1	5	2
Lotus Europa	30.4	4	95.1	113	3.77	1.513	16.90	1	1	5	2
Ford Pantera L	15.8	8	351.0	264	4.22	3.170	14.50	0	1	5	4
Ferrari Dino	19.7	6	145.0	175	3.62	2.770	15.50	0	1	5	6
Maserati Bora	15.0	8	301.0	335	3.54	3.570	14.60	0	1	5	8

```
> df_20<-df[sample(nrow(df),size=20),]
> df_20
```

	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
Merc 450SLC	15.2	8	275.8	180	3.07	3.780	18.00	0	0	3	3
Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
Chrysler Imperial	14.7	8	440.0	230	3.23	5.345	17.42	0	0	3	4
Fiat X1-9	27.3	4	79.0	66	4.08	1.935	18.90	1	1	4	1
Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
Toyota Corolla	33.9	4	71.1	65	4.22	1.835	19.90	1	1	4	1
Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
Merc 450SL	17.3	8	275.8	180	3.07	3.730	17.60	0	0	3	3
Honda Civic	30.4	4	75.7	52	4.93	1.615	18.52	1	1	4	2
Ferrari Dino	19.7	6	145.0	175	3.62	2.770	15.50	0	1	5	6
Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
Ford Pantera L	15.8	8	351.0	264	4.22	3.170	14.50	0	1	5	4
Lotus Europa	30.4	4	95.1	113	3.77	1.513	16.90	1	1	5	2
Dodge Challenger	15.5	8	318.0	150	2.76	3.520	16.87	0	0	3	2
Cadillac Fleetwood	10.4	8	472.0	205	2.93	5.250	17.98	0	0	3	4
Fiat 128	32.4	4	78.7	66	4.08	2.200	19.47	1	1	4	1
Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
Lincoln Continental	10.4	8	460.0	215	3.00	5.424	17.82	0	0	3	4

```
> x<-df_20$mpg
> y<-df_20$cyl
```

```

> x
[1] 15.2 18.7 14.7 27.3 19.2 14.3 33.9 22.8 17.3 30.4 19.7 21.4 15.8 30.4 15.5 10.4 32.4 24.4 17.8 10.4
> y
[1] 8 8 8 4 6 8 4 4 8 4 6 6 8 4 8 8 4 4 6 8
>
> cor(x, y, method = c("pearson"))
[1] -0.8977234
> cor(x, y, method = c("kendall"))
[1] -0.8089641
> cor(x, y, method = c("spearman"))
[1] -0.917594
>

```

## Manual Calculations:

Manual calculations					Page No. <span style="border: 1px solid black; padding: 2px;">  </span>
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$x$	$y$	$\frac{dx}{(x - \bar{x})}$	$\frac{dy}{(y - \bar{y})}$	$dxdy$	
15.2	8	-5.4	1.8	-9.72	
18.7	8	-1.9	1.8	-3.42	
14.7	8	5.9	1.8	10.62	
27.3	4	6.7	-2.2	14.74	
19.2	6	-1.4	-0.2	0.28	
14.3	8	-6.3	1.8	-11.34	
33.9	4	13.3	-2.2	-29.26	
22.8	4	2.2	-2.2	-4.84	
17.3	8	-3.3	1.8	-5.94	
30.4	4	9.8	-2.2	-21.56	
19.7	6	-0.9	-0.2	0.18	
21.4	6	0.8	-0.2	-0.16	
15.8	8	-4.8	1.8	8.64	
30.4	4	9.8	-2.2	-21.56	
15.5	8	-5.1	1.8	-9.18	
10.4	8	-10.2	1.8	-18.36	
32.4	4	11.8	-2.2	-25.96	
24.4	4	3.8	-2.2	-8.36	
17.8	6	-2.8	-0.2	0.56	
10.4	8	-10.2	1.8	-18.36	
					$\bar{x} = 20.6$ $\bar{y} = 6.2$ $\sum dx^2 = 958.92$ $\sum dy^2 = 63.2$ $\sum dxdy = -221$

Asc order

$x$	$d^2$	$d$	Rank of $y$	Rank of $x$	$dy^2$	$dx^2$
1.5	121	-11	16	5	3.24	24.16
1.5	36	-6	16	10	3.24	3.61
3	144	-12	16	4	3.24	34.81
4	144	12	4	16	4.84	44.89
5	225	15	9.5	11	0.04	1.96
6	169	-13	16	3	3.24	34.69
7	256	16	4	20	4.84	176.84
8	100	10	4	14	4.84	44.8
9	64	-8	16	8	3.24	10.89
9	64	-8	4	12.5	4.84	96.04
10	182.25	13.5	9.5	11	0.04	0.81
11	6.25	2.5	9.5	13	0.04	0.64
12	12.25	3.5	16	7	3.24	23.04
13	81	25.9	4	17.5	4.84	96.04
14	182.25	13.5	16	6	2.24	26.01
15	100	-10	16	1.5	3.24	104.00
16	210.25	-14.5	16		4.84	129.24
17.5	225	15	4	19	4.84	144
17.5	121	11	4	15	4.84	784
19	0.25	-0.5	9.5	9	0.04	104.04
20	210.25	-14.5	16	1.5	3.24	



$$\sum d^2 = 2367$$

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Correlation using Pearson's method

$$r = \frac{\sum dxdy}{\sqrt{\sum x^2} \sqrt{\sum y^2}} = \frac{-221}{\sqrt{458.92} \sqrt{69.2}} = -0.8477234012$$

Correlation using Spearman's method.

$$r_s = 1 - 6 \left[ \frac{\sum D_i^2}{n^3 - n} + \frac{1}{12} (m_1^3 - m_1) + \frac{1}{12} (m_2^3 - m_2) + \frac{1}{12} (m_3^3 - m_3) \right]$$

$$r_s = 1 - 6 \left[ \frac{2367}{20(39)} + \frac{1}{12} (7^3 - 7) + \frac{1}{12} (9^3 - 9) + \frac{1}{12} (4^3 - 4) + \frac{1}{12} (2^3 - 2) \right]$$

$$= -0.87$$

Rank  $\rightarrow$  Kendall's Method.

$$\tau = \frac{\sum C - \sum D}{\sum C + \sum D} \Rightarrow -0.809$$

**Result:**

The manual calculations and R answers match each other.