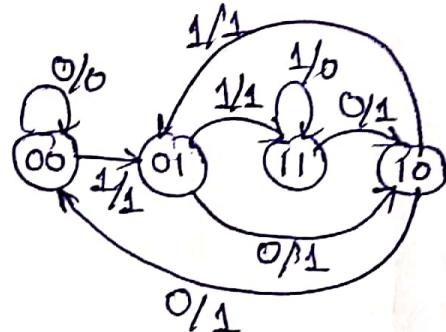


9.1.

State table

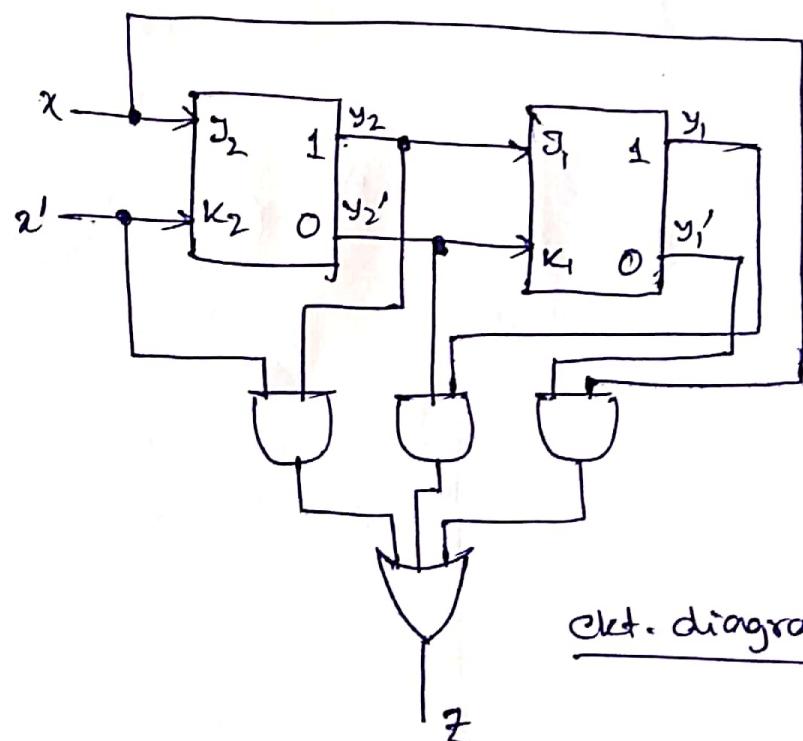
PS	NS		Z	
	x=0	x=1	x=0	x=1
00	0 0 0 1		0 0	1
01	1 0 1 1		1	1
11	1 0 1 1		1	0
10	0 0 0 1		1	1

State Diagram

$$Z = x'y_2 + y_1y_2' + xy_1'$$
 output function

$$\begin{array}{l|l} J_1 = y_2 & J_2 = x \\ K_1 = y_2' & K_2 = x' \end{array}$$

excitation function

ckt. diagram.

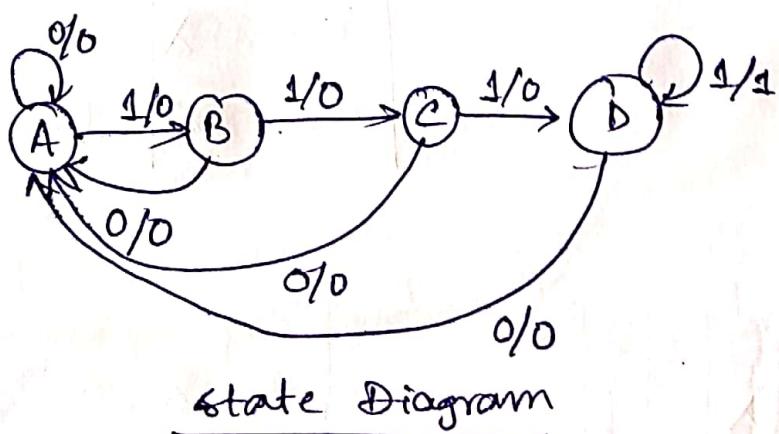
Excitation table.

y_1, y_2	$x=0$		$x=1$		z	
	J_1, K_1	J_2, K_2	J_1, K_1	J_2, K_2	$x=0$	$x=1$
00	01	01	01	10	0	1
01	10	10	10	10	1	1
11	10	01	10	10	1	0
10	10	01	01	10	1	1

ex-table for J-K

	J	K
0 → 0	0	x
0 → 1	1	x
1 → 0	x	1
1 → 1	x	0

* The circuit produces 0 output only if xy, y_2 is 000 or 111. J-K flip-flops are acting as D- flip-flops; so whatever input its taking, producing the same output after one clock pulse.

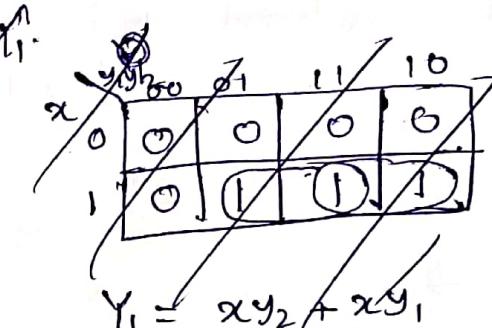
Q-2.State Assignment-

- A → 00
- B → 01
- C → 10
- D → 11

Excitation table

State table.

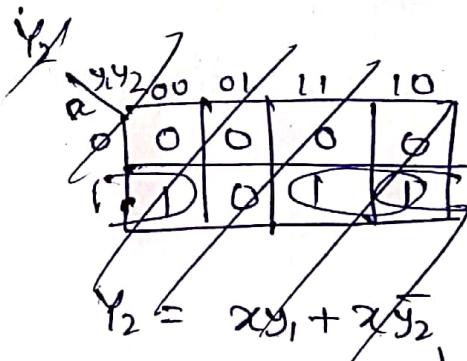
		output	
		$x=0$	$x=1$
		y_1, y_2	y_1, y_2
P	S	$x=0$	$x=1$
0	0	00	01
1	0	00	10
0	1	00	11
1	1	00	11



$$Z = xy_1, y_2$$

Excitation table.

		NS	
		$x=0$	$x=1$
		$S_1 R_1 \quad S_2 R_2$	$S_1 R_1 \quad S_2 R_2$
0	0	0X	0X
0	1	0X	01
1	0	01	10
1	1	01	01



$$Y_2 = xy_1 + x\bar{y}_2$$

	S	R
$0 \rightarrow 0$	0X	
$0 \rightarrow 1$	10	
$1 \rightarrow 0$	01	
$1 \rightarrow 1$	X0	

		y_1, y_2	00	01	11	10
		x	0	0	0	0
0	0	0	0	0	0	0
1	0	1	0	1	0	0

$$S_1 = \cancel{x} \cancel{y_1} \cancel{y_2}, xy_2$$

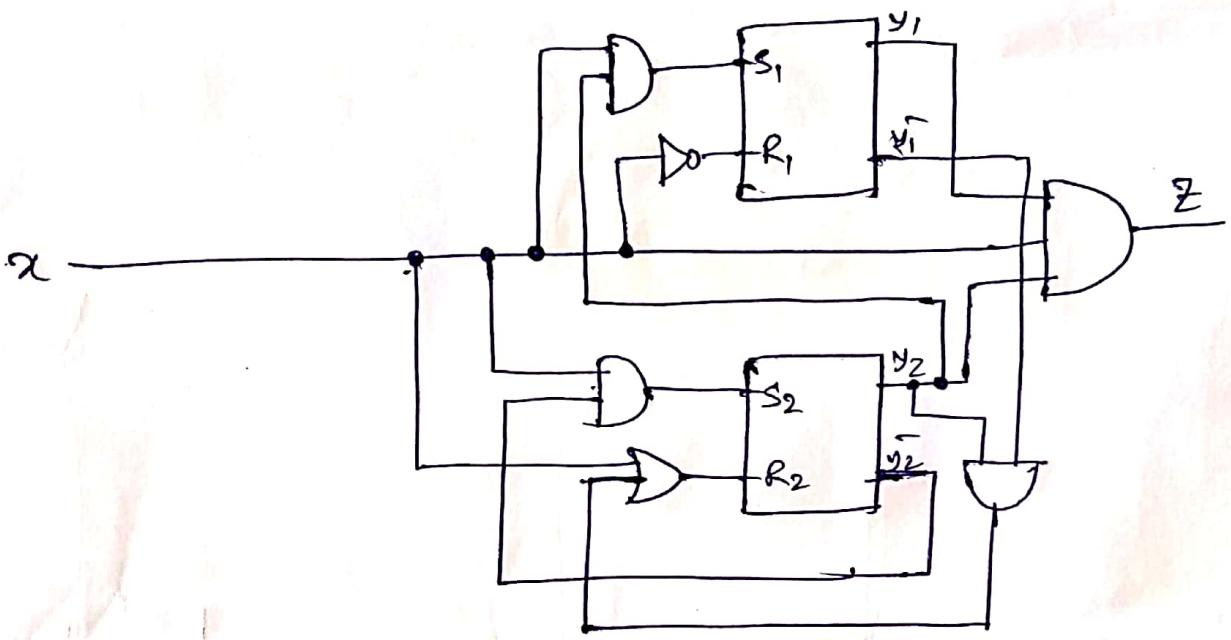
		y_1, y_2	00	01	11	10
		x	0	1	1	x
0	0	0	0	0	0	0
1	0	1	0	1	0	0

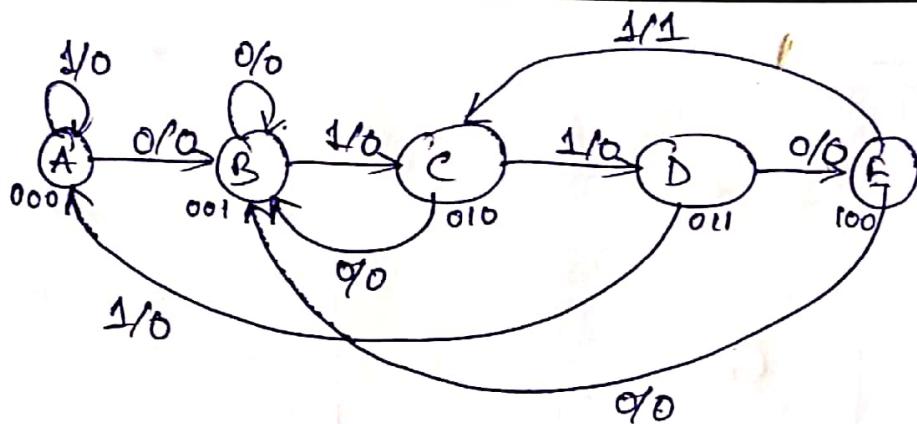
$$S_2 = x\bar{y}_2$$

		y_1, y_2	00	01	11	10
		x	0	x	1	D
0	0	0	0	0	0	0
1	x	0	0	0	0	0

$$R_1 = \bar{x}$$

$$R_2 = \bar{x} + \bar{y}_1 y_2$$



Q.3-State assignment-

$$\begin{aligned} A &\rightarrow 000 \\ B &\rightarrow 001 \\ C &\rightarrow 010 \\ D &\rightarrow 011 \\ E &\rightarrow 100 \end{aligned}$$

State table

PS $y_1y_2y_3$	NS		Z	
	$x=0$ y_1, y_2, y_3	$x=1$ y_1, y_2, y_3	$x=0$	$x=1$
000	001	000	0	0
001	000	010	0	0
010	001	011	0	0
011	100	000	0	0
100	001	010	0	1

$$T_1 = y_1 + \bar{x}y_2y_3$$

$y_1y_2y_3$	00	01	11	10
00	0	0	1	0
01	1	X	X	X
11	1	X	X	X
10	0	0	0	0

$$Z = xy_1y_2'y_3'$$

Excitation table.

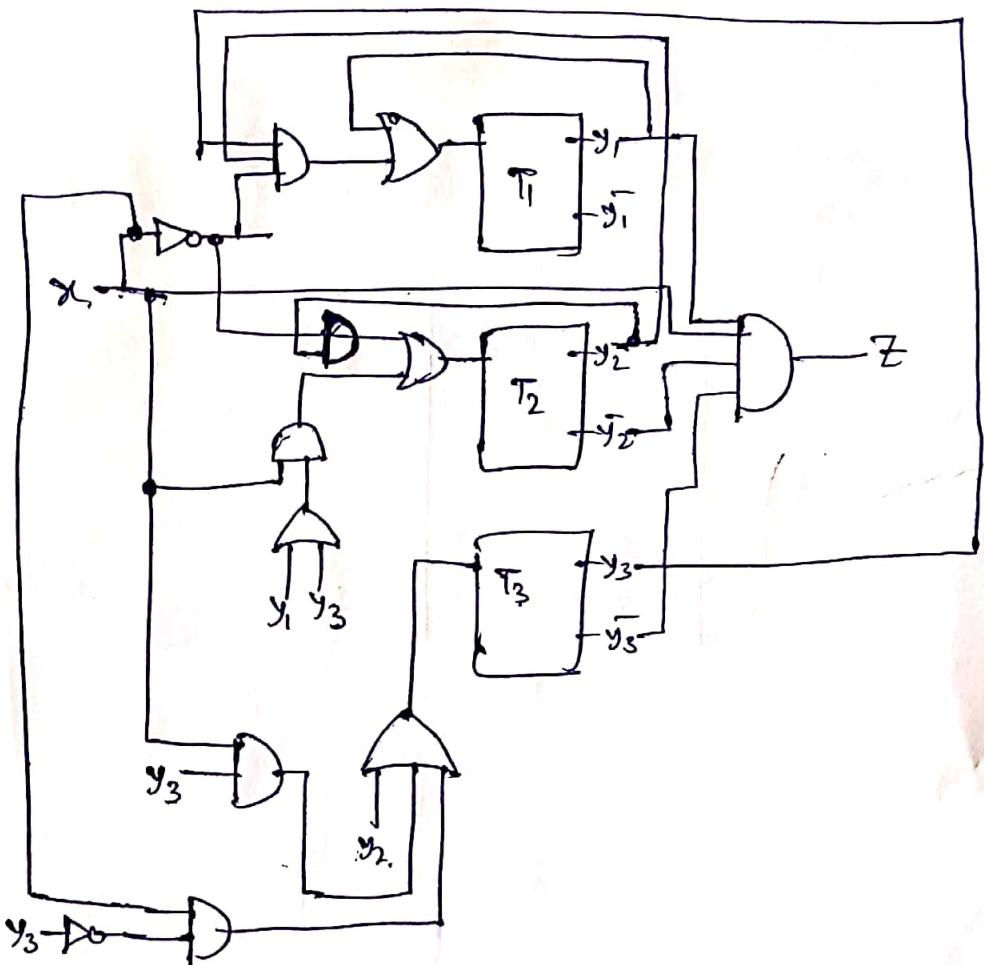
PS $y_1y_2y_3$	NS			
	$x=0$ $T_1 T_2 T_3$	$x=1$ $T_1 T_2 T_3$		
000	001	000		
001	000	011		
010	011	001		
011	111	011		
100	101	110		

$$T_2 = x'y_2 + xy_1 + x'y_3$$

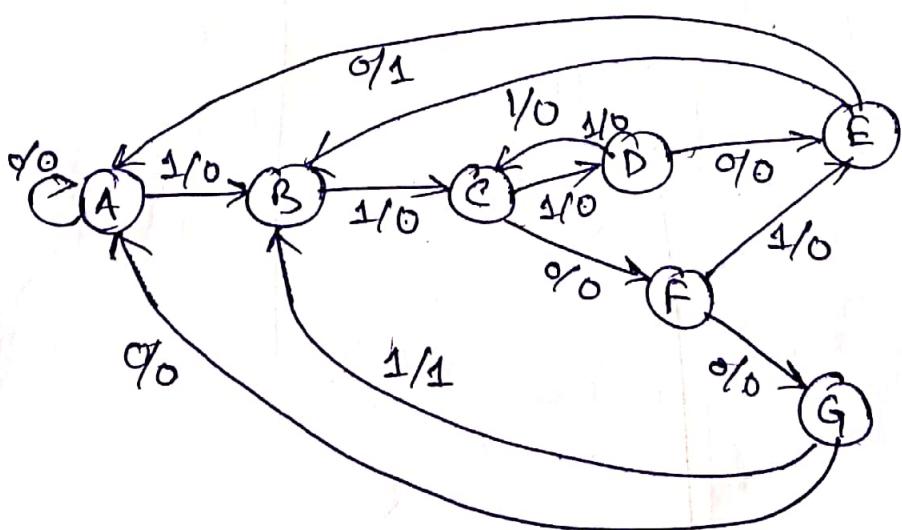
$y_1y_2y_3$	00	01	11	10
xy_1	0	0	1	0
00	0	X	X	X
01	0	X	X	X
11	1	X	X	X
10	0	1	1	0

$$T_3 = y_2 + \alpha y_3 + \alpha' y_3'$$

αy_1	00	01	11	10
00	1	0	1	1
01	1	x	x	x
11	0	x	x	x
10	0	1	1	1



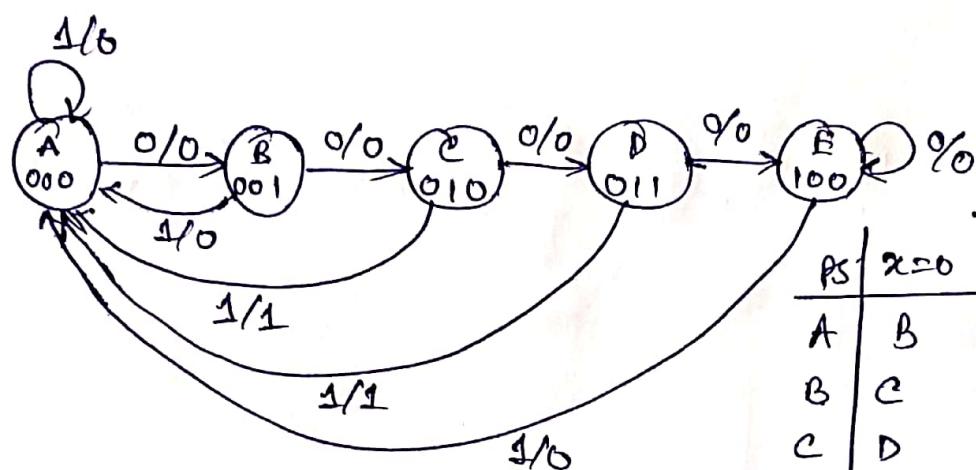
Q.4.



Possible in
7 states.

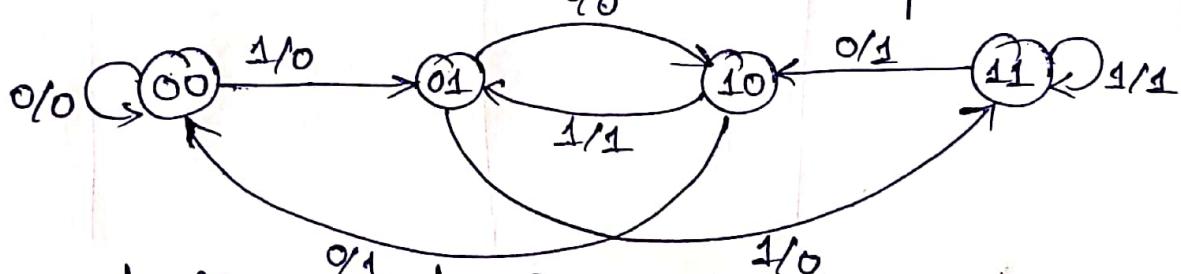
Q.T.

a)



PS	$x=0$	$x=1$	z
A	B	A	0 0
B	C	A	0 0
C	D	A	0 1
D	E	A	0 1
E	E	A	0 0

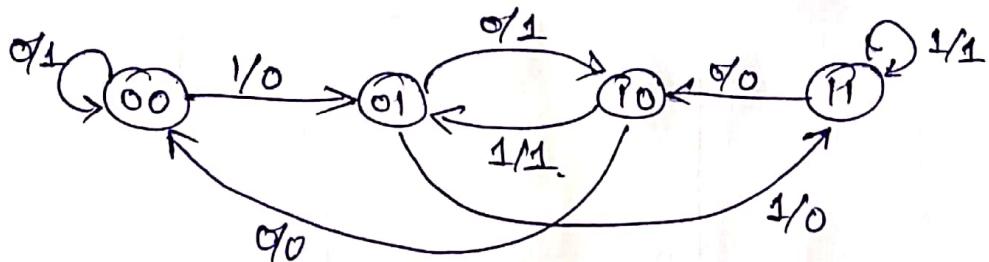
b)



PS	$x=0$	$x=1$	z
00	0	0	
01	0	0	
10	0	1	
11	1	1	

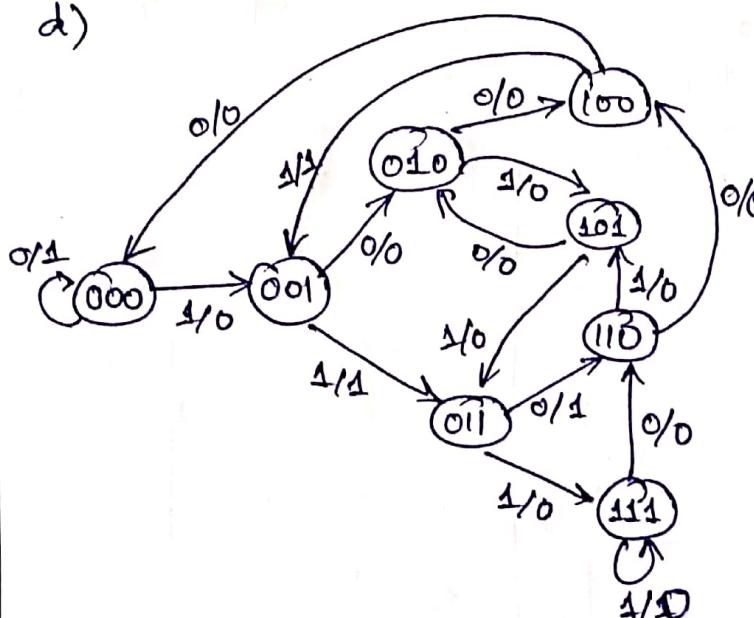
PS	$x=0$	$x=1$	z
00	0 0	0 1	0 0
01	1 0	1 1	0 0
10	0 0	0 1	1 1
11	1 0	1 1	1 1

(c)



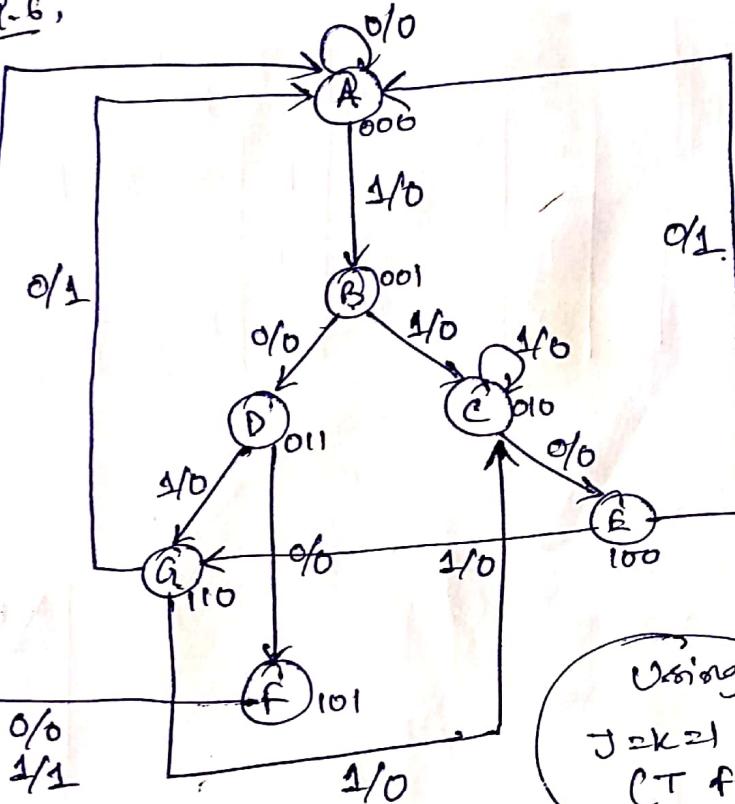
PS	NS		Z	
	$x=0$	$x=1$	$x=0$	$x=1$
00	00	01	1	0
01	10	11	1	0
10	00	01	0	1
11	10	11	0	1

(d)



PS	NS		Z	
	$x=0$	$x=1$	$x=0$	$x=1$
000	000	001	1	0
001	010	011	0	1
010	100	101	0	0
011	110	111	1	0
100	000	001	0	1
101	010	011	0	0
110	100	101	1	0
111	110	111	0	0

Q.6,



State diagram.

state Assignment

$A \rightarrow 000$
 $B \rightarrow 001$
 $C \rightarrow 010$
 $D \rightarrow 011$
 $E \rightarrow 100$
 $F \rightarrow 101$
 $G \rightarrow 110$

excitation table

PS	NS		Z		$\alpha = 0$ T_1, T_2, T_3	$\alpha = 1$ T_1, T_2, T_3
	$x=0$	$x=1$	$x=0$	$x=1$		
000	000	001	0	0	0 0 0	0 0 1
001	011	010	0	0	0 1 0	0 1 1
010	100	010	0	0	1 1 0	0 0 0
011	101	110	0	0	1 1 0	1 0 1
100	000	110	1	0	1 0 0	0 1 0
101	000	000	0	1	1 0 1	1 0 1
110	000	010	1	0	1 1 0	1 0 0

State table

$$T_1 = \bar{x}y_1 + y_2y_3 + xy_2$$

$$+ y_1y_3 + y_1y_2$$

y_3y_1	00	01	11	10
y_2y_1	00	0	(1)	(1)
01	1	1	x	1
11	0	1	x	1
10	0	0	1	0

$$T_2 = \bar{x}y_2 + y_1y_2y_3 + xy_1y_2y_3$$

$$+ y_1y_3 + y_1y_2$$

y_3y_1	00	01	11	10
y_2y_1	00	0	(1)	(1)
01	0	0	x	1
11	1	0	x	0
10	0	1	0	0

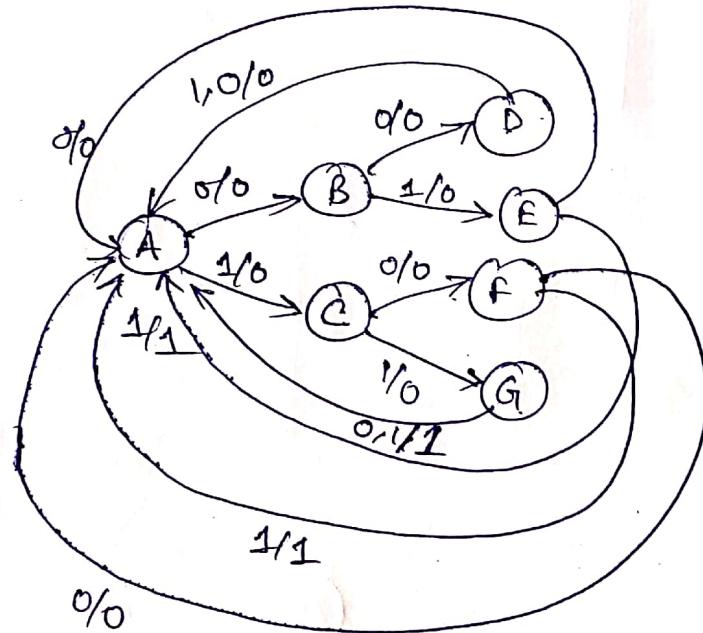
$$T_3 = x'y_3 + xy_1y_3 + xy_1y_2$$

$$+ xy_1y_2$$

y_3y_1	00	01	11	10
y_2y_1	00	0	0	0
01	0	1	x	0
11	0	1	x	0
10	1	1	1	0

Q.7

	S R
0 → 0	0 X
0 → 1	1 0
1 → 0	0 1
1 → 1	X 0



State Assignment.

- A → 000
- B → 001
- C → 010
- D → 011
- E → 100
- F → 101
- G → 110

NS (Excitation Table)

NS $y_1y_2y_3$	NS $x=0$		NS $x=1$		Z	$x=0$	$x=1$	$x=0$	$x=1$	
	$y_1y_2y_3$	$y_1y_2y_3$	$y_1y_2y_3$	$y_1y_2y_3$						
A 000	001	010	0	0		0X	0X	10	0X	10 0X
B 001	011	100	0	0		0X	10	X0	10	0X 01
C 010	101	110	0	0		10	01	10	10	X0 0X
D 011	000	000	0	0		0X	01	01	0X	01 01
E 100	000	000	0	1		01	0X	0X	01	0X 0X
F 101	000	000	0	1		01	0X	01	01	0X 01
G 110	000	000	1	1		01	01	0X	01	01 0X

$$S_1 = y_1'y_2y_3' + xy_1'y_2'y_3$$

$$R_1 = y_1,$$

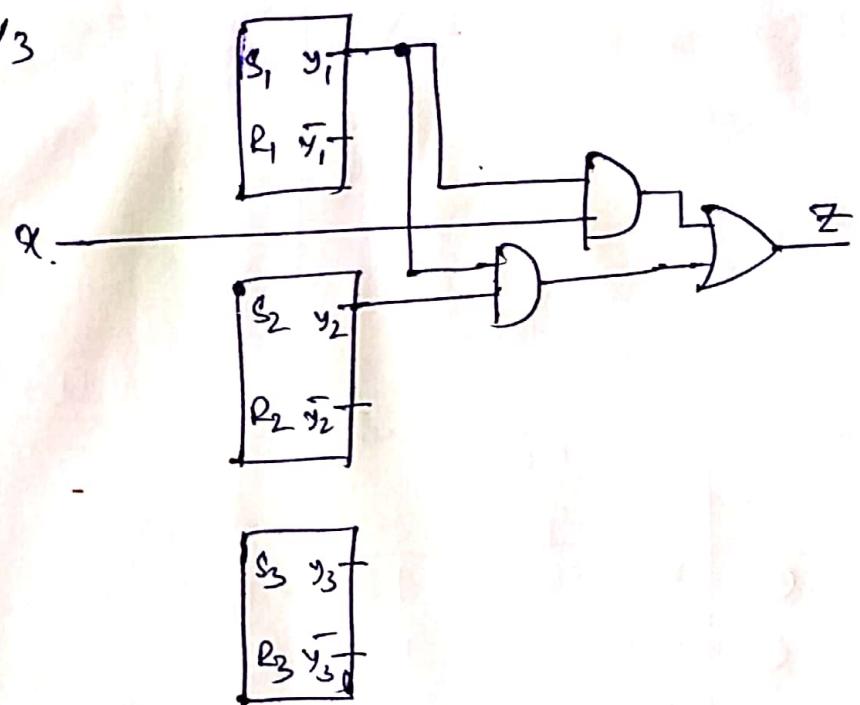
$$S_2 = xy_1'y_3' + x'y_1'y_2'y_3$$

$$R_2 = y_1 + x'y_3' + y_2y_3$$

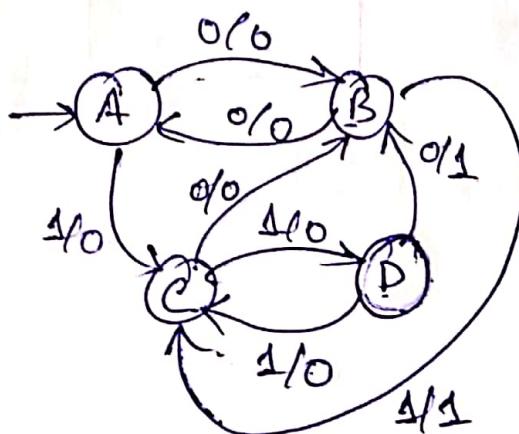
$$S_3 = x'y_1'y_3$$

$$R_3 = y_1 + x + y_2y_3$$

$$Z = y_1y_2 + xy_1$$



Q.10.



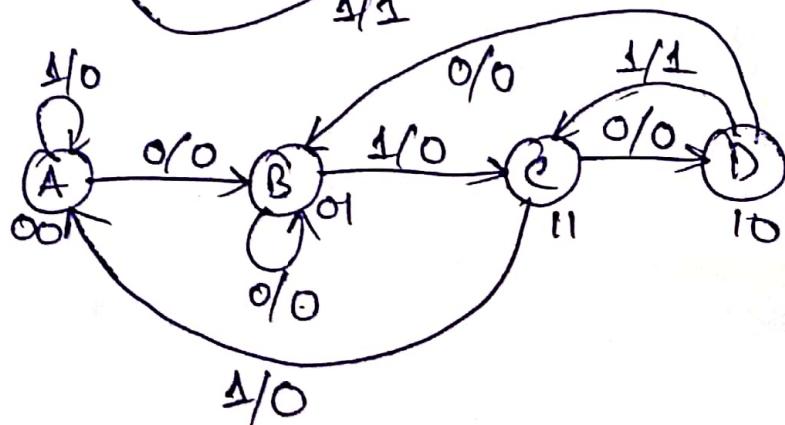
A: even no of 0's

B: odd no. of 0's

C: odd no. of 1's

D: even no. of 1's.

Q.11.



State table -

		NS		$\neg Z$	
		$x=0$	$x=1$	$x=0$	$x=1$
		$y_1 y_2$	$y_1' y_2'$	$y_1 y_2$	$y_1' y_2'$
state assignment	A 00	01	00	0	0
	B 01	01	11	0	0
	C 11	10	00	0	0
	D 10	01	11	0	1

Excitation table for U, V .

		NS			
		$x=0$	$x=1$		
		$U, V, U_1 V_2$	$U_1 V_2', U_2 V_2$		
$U=S, V=R \oplus S$					
	$U \quad V$				
$0 \rightarrow 0$	0 X	0 X 1	0 X 0 X	0 0	0 0
$0 \rightarrow 1$	1 1	0 X 1 1	1 1 1 1	0 0	0 0
$1 \rightarrow 0$	0 1	1 1 0 1	0 1 0 1	0 0	0 0
$1 \rightarrow 1$	0 0	0 1 1 1	1 1 1 1	0 0	1 1
	1 1 }				

		NS		Z	
		$x=0$	$x=1$	$x=0$	$x=1$
		$U_1 V_1, U_2 V_2$	$U_1 V_2', U_2 V_2$	$U_2 V_2$	$U_1 V_2$
$U=S, V=R \oplus S$					
	$U_1 \quad V_1$				
$0 \rightarrow 0$	0 X 1	0 X 0 X	0 X 1	0 0	0 0
$0 \rightarrow 1$	0 X 1 1	1 1 1 1	1 1 1 1	0 0	0 0
$1 \rightarrow 0$	1 1 0 1	0 1 0 1	0 1 0 1	0 0	0 0
$1 \rightarrow 1$	1 1 1 1	1 1 1 1	1 1 1 1	0 0	1 1
	1 1 }				

$$U_1 = x'y_1y_2 + xy'y_2' + xy_1y_2'$$

$$U_2 = y_1'y_2 + y_1y_2' + x'y_1'$$

$$V_2 = 1$$

Q.12.

@	PS	NS	excitation
	0	0	0
	0	1	1
	1	0	X
	1	1	Not possible

Given State table-

PS	<u>NS, Z</u>	
	$x=0$	$x=1$
A	B, 0	B, 0
B	C, 0	A, 1
C	B, 0	D, 0
D	C, 0	B, 1

* Assignment should be done in such a way that there's no $1 \rightarrow 1$ transition. One such possible assignment is—

$$\begin{aligned} A &\rightarrow 11 \\ B &\rightarrow 00 \\ C &\rightarrow 01 \\ D &\rightarrow 10 \end{aligned}$$

PS	<u>NS</u>	
	y_1, y_2	y_1, y_2, z
y_1, y_2	$x=0$	$x=1$
11	XX, 0	XX, 0
00	10, 0	11, 1
01	X0, 0	X1, 0
10	1X, 0	0X, 1

$$\begin{aligned} y_1 &= x' + y_2' \\ y_2 &= x \\ z &= xy_1' \end{aligned}$$

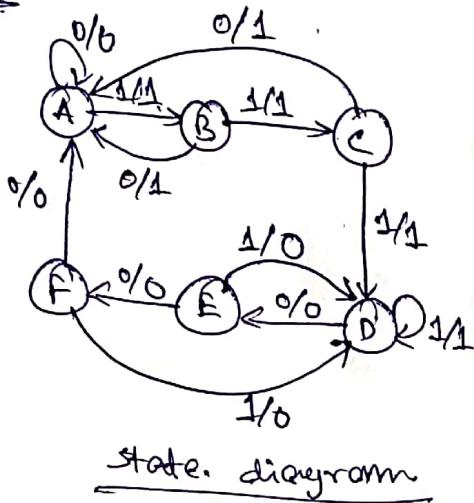
(B) The constraint that no memory element can have a transition $1 \rightarrow 1$ means not all state tables can be realized with $\log(n)$ no. of memory element where $n = \text{no. of states}$. An n -state table can be always realized by an ~~n-state~~ n memory elements in which each state is represented by a 'one of n ' coding. Such assignments are not necessarily the best, in general it would be difficult to realize by min. no. of state variables.

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Q.13.

State table

PS	NS, z	
	$x=0$	$x=1$
A	A, 0	B, 1
B	A, 1	C, 1
C	A, 1	D, 1
D	E, 0	D, 1
E	F, 0	D, 0
F	A, 0	D, 0

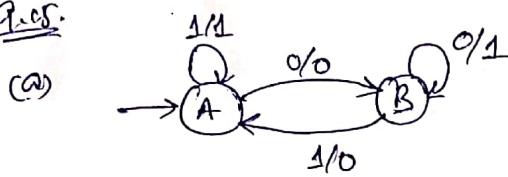
Q.14.

x_1	x_2	x_3	x_4	Z
1	1	0	0	1
1	0	0	1	0
0	0	1	0	1
0	1	0	1	0
1	0	1	0	0
0	1	0	0	0
1	0	0	0	1
0	0	0	1	1
0	0	1	1	0
0	1	1	0	0

Solving K-map & Considering other inputs to be don't care, we get,

$$\begin{aligned}
 f(x_1, x_2, x_3, x_4) &= x_1 x_3' x_4' + x_1' x_2' x_3' \\
 &\quad + x_1' x_2' x_4'
 \end{aligned}$$

Q.15.



(b) An output of 0 from $N \oplus N$ identifies the final state as B, while an o/p of 1 identifies the final state as A. Once the state of N is known, it's straightforward to determine the i/p to N and state to which N goes by observing its o/p. Consequently except for the first bit, each of subsequent bits can be decoded.

Q.16.

NS, write, shift

PS	I.-#	0	1	2	3
A	B, #, R	A, 0, R	A, 1, R	A, 0, R	A, 1, R
B		C, 2, R	D, 3, R	I, 2, L	I, 3, L
C	E, #, L	C, 0, R	C, 1, R	B, 2, L	B, 3, L
D	F, #, L	D, 0, R	D, 1, R	F, 2, L	F, 3, L
E		G, 2, L	H, 1, L	F, 2, L	
F		H, 0, L	G, 3, L		I, 3, L
G		G, 0, L	G, 1, L	B, 2, R	B, 3, R
H	A, #, R	H, 0, L	H, 1, L	H, 2, L	H, 3, L
I	J, #, R	J, 0, L	I, 1, L	I, 2, L	I, 3, L
II	Halt	J, 0, R	J, 1, R	J, 0, R	J, 1, R
III	Halt	Halt	Halt		

State A: Starting state,

the m/c restores the original symbols of the present block and moves ~~to~~ to test the next block.

State B:

Col. (0,1): The head checks ~~for~~ the leftmost original symbol of the block.

Col(2,3): A palindrome detected.

State C & D:

(#H1,2,3): The head searches for the rightmost original symbol of the block. State C is for the case that the leftmost symbol is a 0 and D for the case that it is a 1.

State E & F: (0,1) : The head checks the rightmost symbol and compares it with the leftmost symbol. (E is for 0 and F for 1)

(2,3) : At this point, the m/e knows that the current symbol is the middle of an odd-length palindrome.

State G: The symbols that were checked so far can be members of a palindrome.

(0,1,2,3) : The head searches for the leftmost original symbol of the block.

State H: At this point, the m/e knows that the block is not a palindrome.

(0,1,2,3) : The head goes to the beginning of the block, so that it will be ready to restore the original symbols (as indicated in state A)

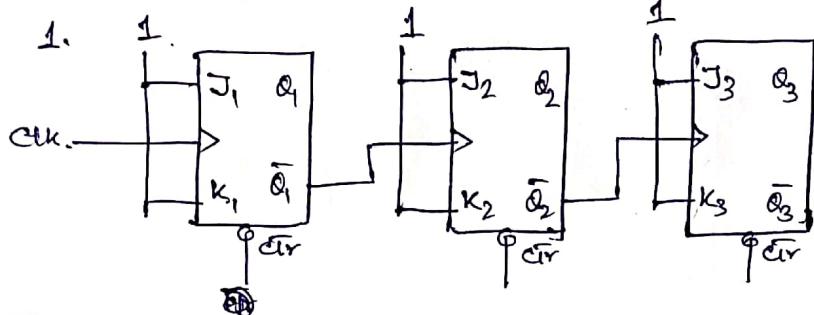
State I:

The m/e now knows that the block is a palindrome. Therefore the head goes to the beginning of the block, so that it will be ready to restore the original symbols (as indicated in state J)

States J and Halt:

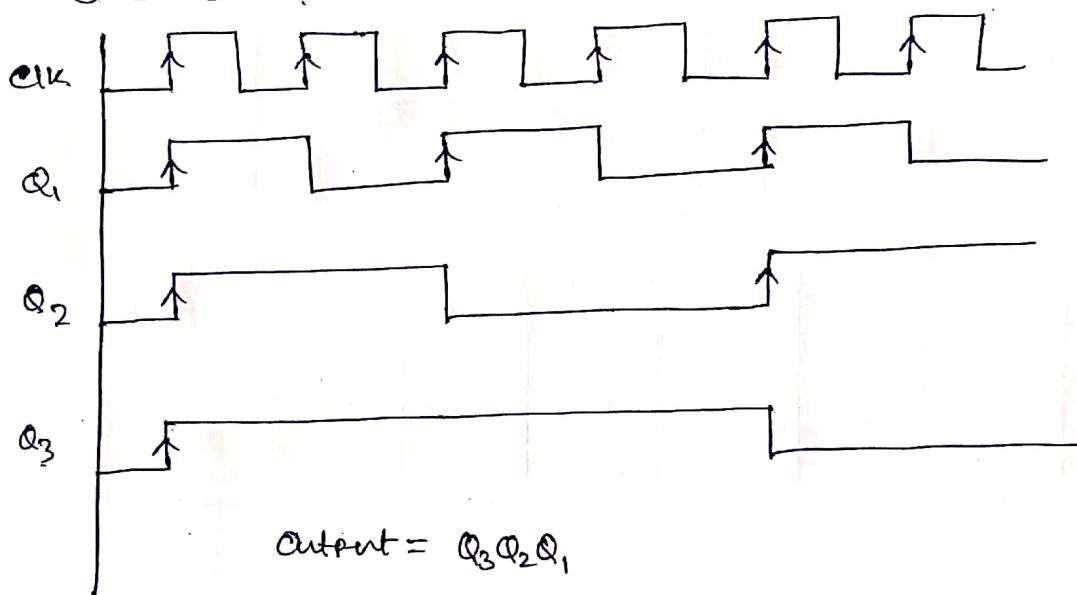
The original symbols are restored and the m/e stops at the first # to the right of the block.

(B)



clk is
the edge
triggered.

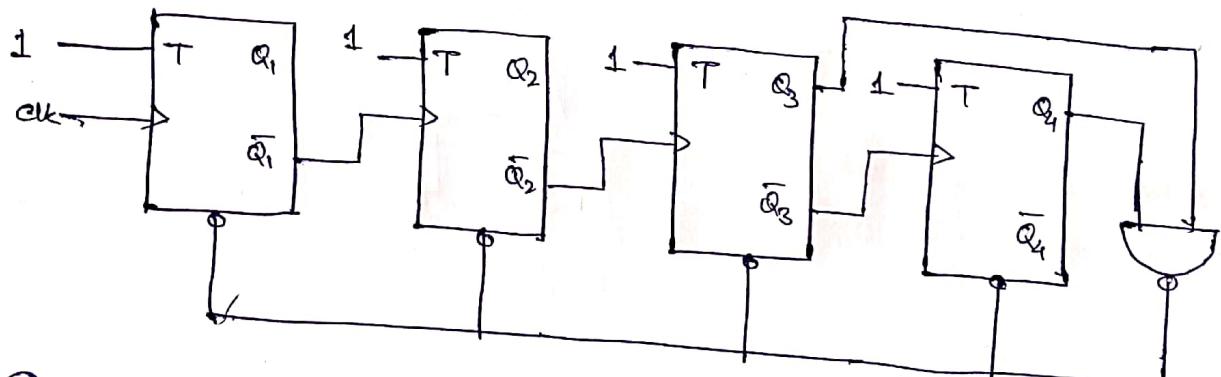
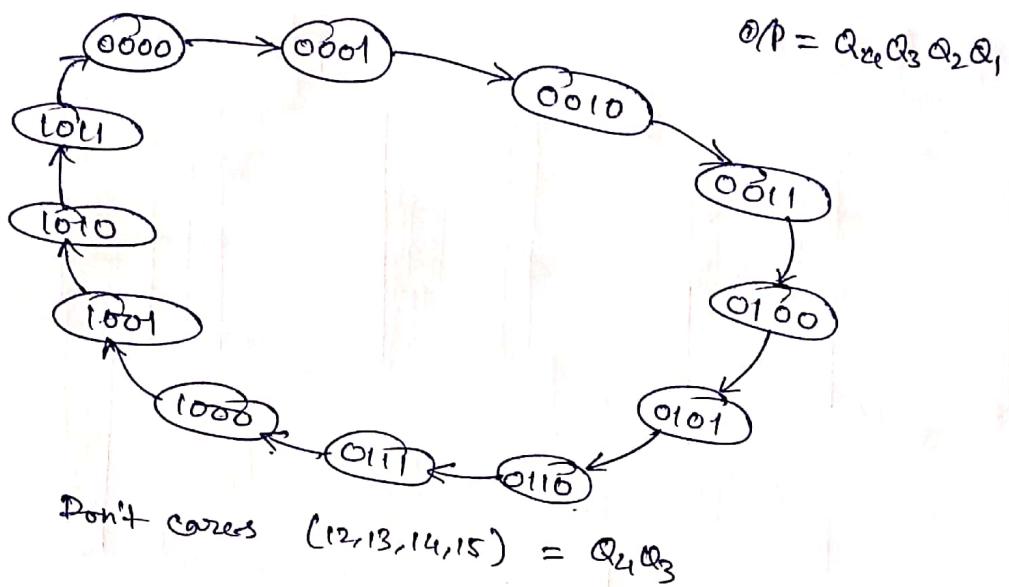
Timing Diagram.



$$\text{Output} = Q_3 Q_2 Q_1$$

$$\text{Input freq} = 2^3 \times \text{O/p freq.}$$

②



③

Don't cares $(10, 11, 12, 13, 14, 15) = Q_4 Q_2 + Q_4 Q_3$

$O/P \rightarrow Q_4 Q_3 Q_2 Q_1$

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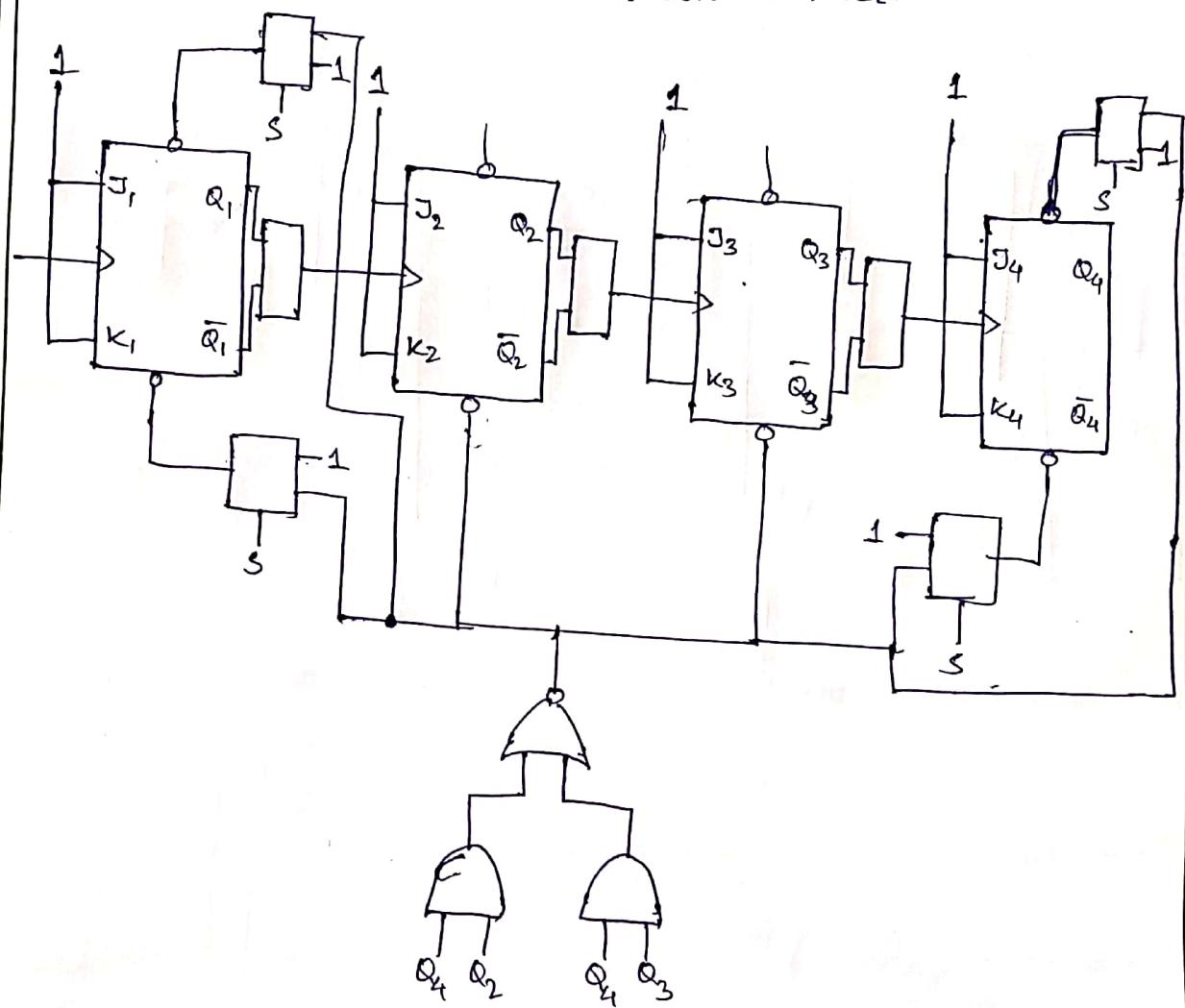
DATE

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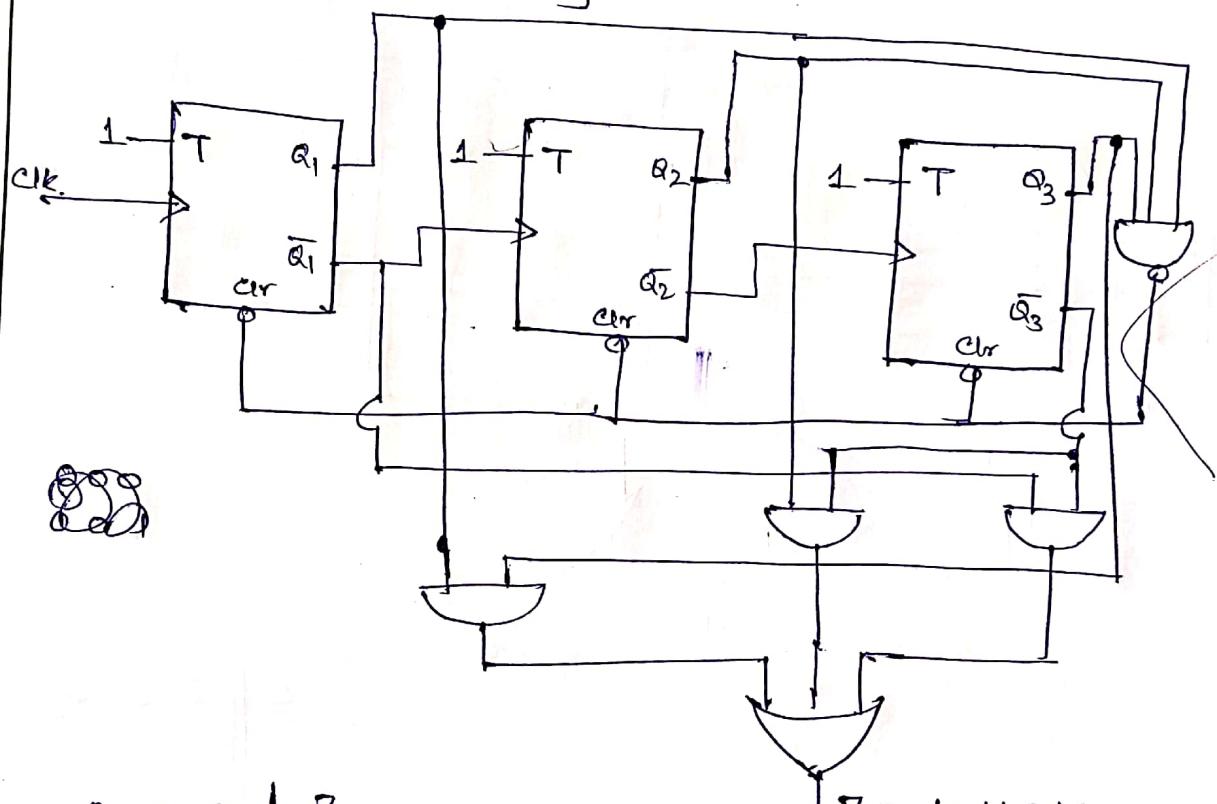
6

$S = 1$: up counter.

$S = 0$: Down counter.



5 Sequence generator to generate the sequence 1011010 [using T flip-flops and the edge triggered clock]



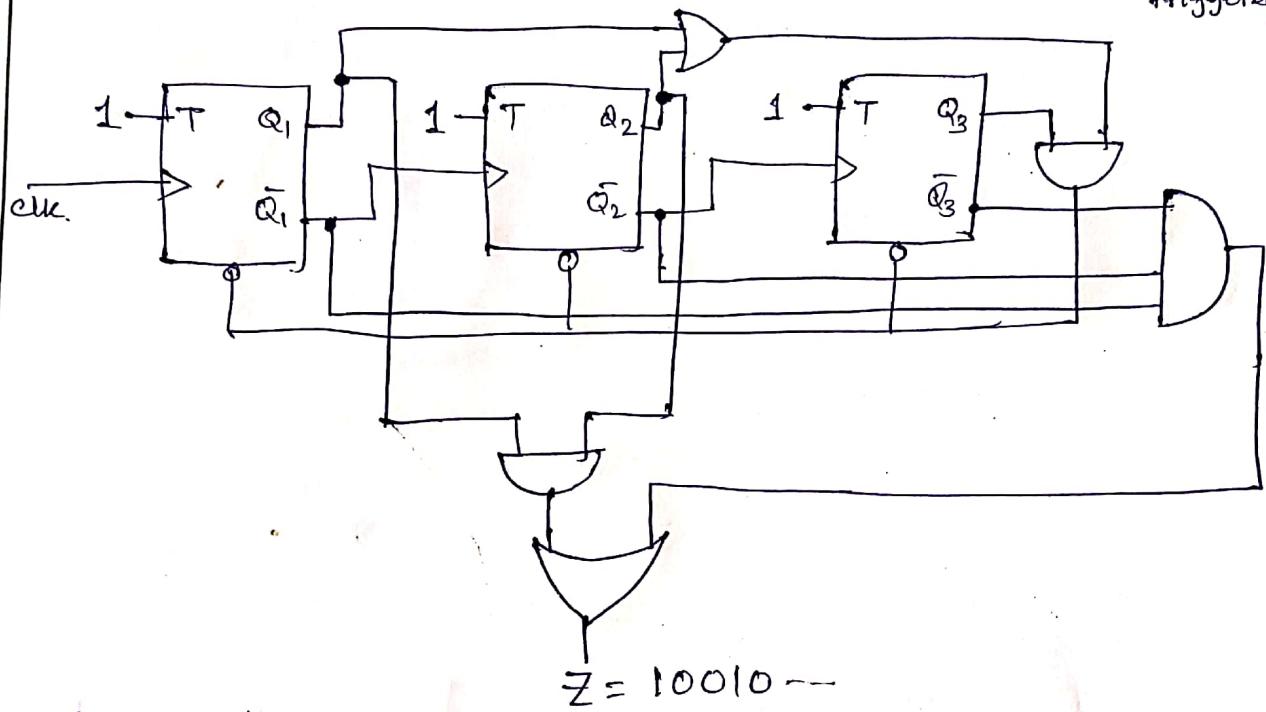
$Q_3\ Q_2\ Q_1$	Z
0 0 0	1
0 0 1	0
0 1 0	1
0 1 1	1
1 0 0	0
1 0 1	1
1 1 0	0

$$Z = \bar{Q}_1 \bar{Q}_3 + Q_3 Q_1 + \bar{Q}_3 Q_2$$

DATE

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(b) pulse train generator of 10010 [T f/f & clk
two edge triggered]



<u>$Q_3\ Q_2\ Q_1$</u>	<u>Z</u>
0 0 0	1
0 0 1	0
0 1 0	0
0 1 1	1
1 0 0	0
+ 0 1	
+ 1 0	

$$Z = Q_1 Q_2 + \bar{Q}_1 \bar{Q}_2 \bar{Q}_3$$

$$\text{clr} = Q_3(Q_1 + Q_2)$$