

AVL

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Tree



Introduction

AVL Tree is also a Binary Search Tree but it is balanced tree.

Here balanced means the difference between height of right

subtree and left subtree is less than or equal to 1.

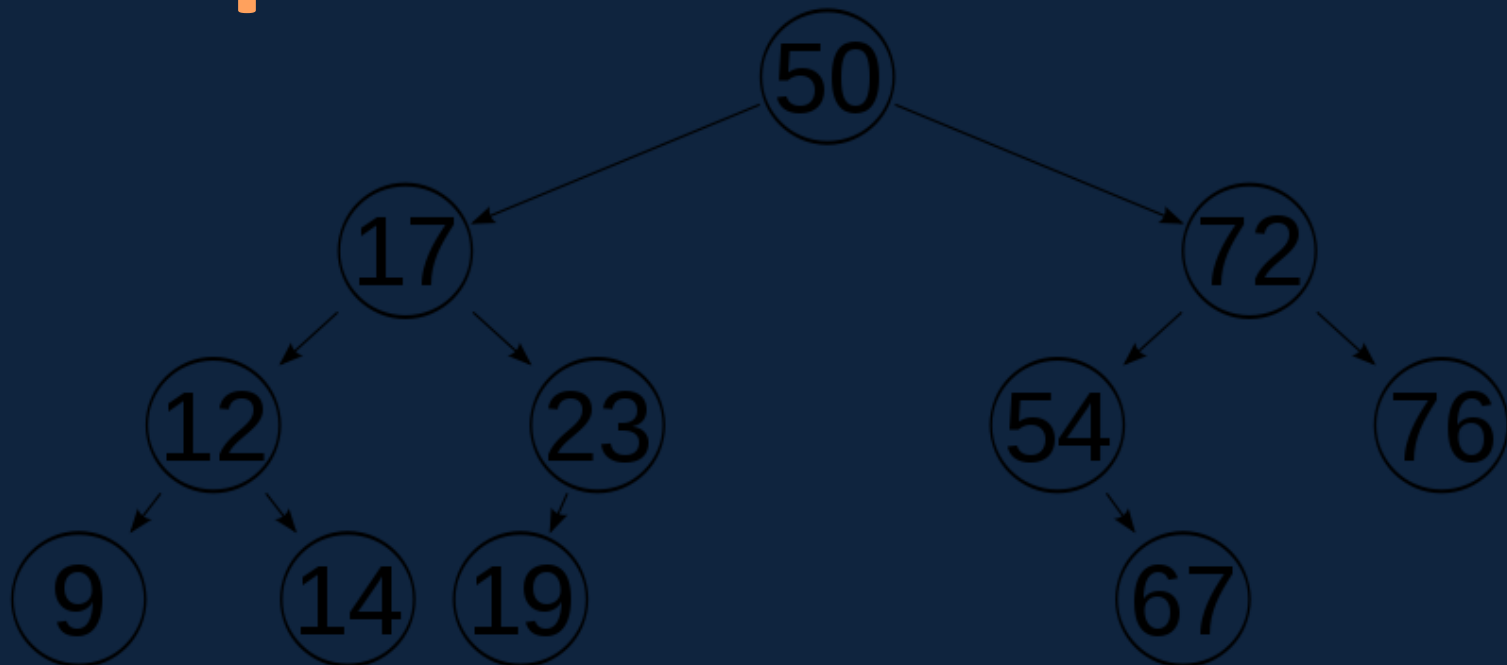
In AVL Tree every node will have one extra information

known as **BALANCE FACTOR**.

$$\text{BalanceFactor} = \text{HeightOfRightSubtree} - \text{HeightOfLeftSubtree}$$

The AVL tree is named after its two inventors, G.M. Adelson-Velsky and E.M. Landis, who published it in their 1962.

Example



After every insertion / deletion we need to check the BALANCE FACTOR

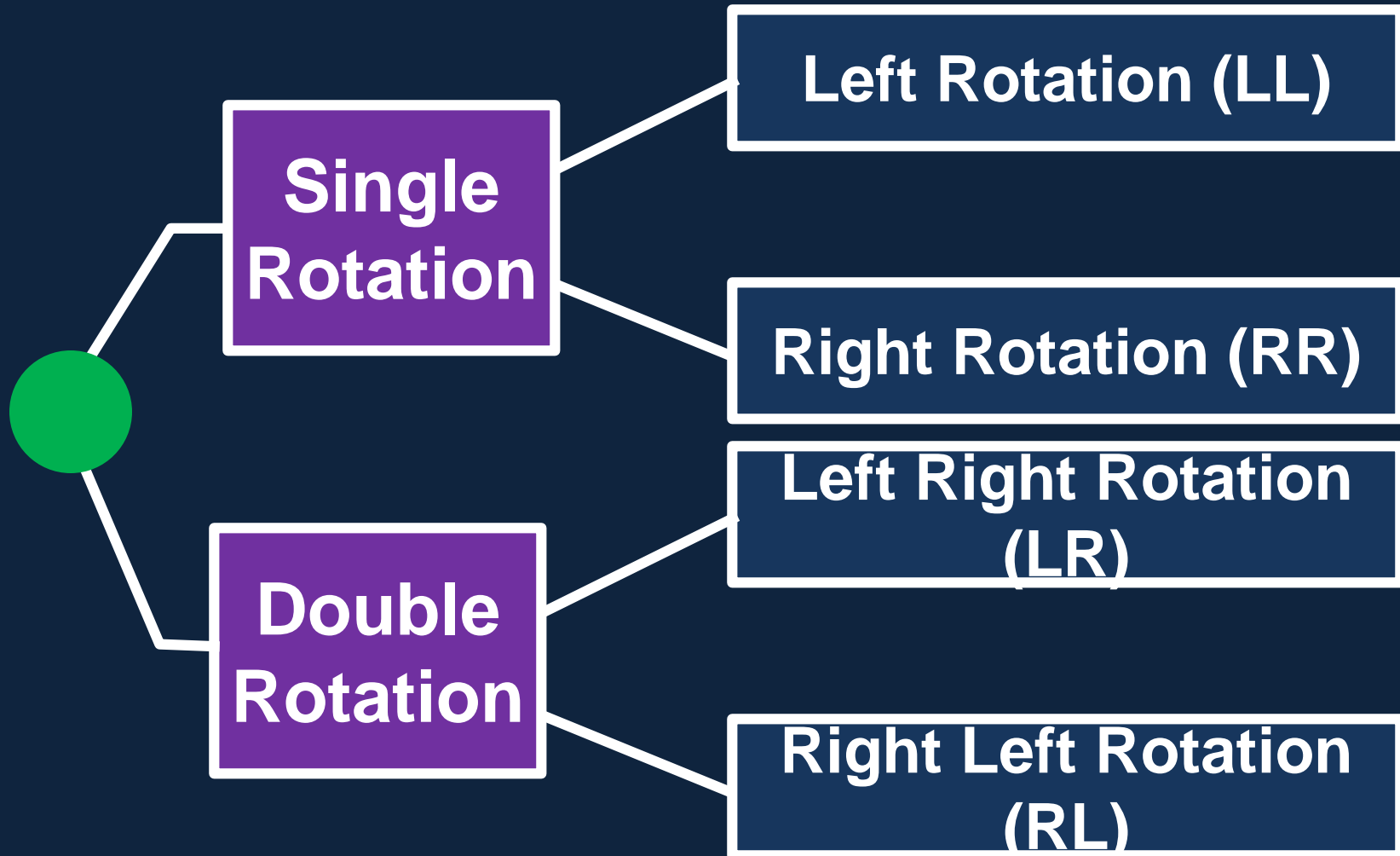
If it is other than -1 or 0 or +1 then we perform ROTATION to make the Tree Balance.

**Not
e**

➤ **All AVL Trees are Binary Search Trees but All Binary Search Trees need not be AVL Tree**

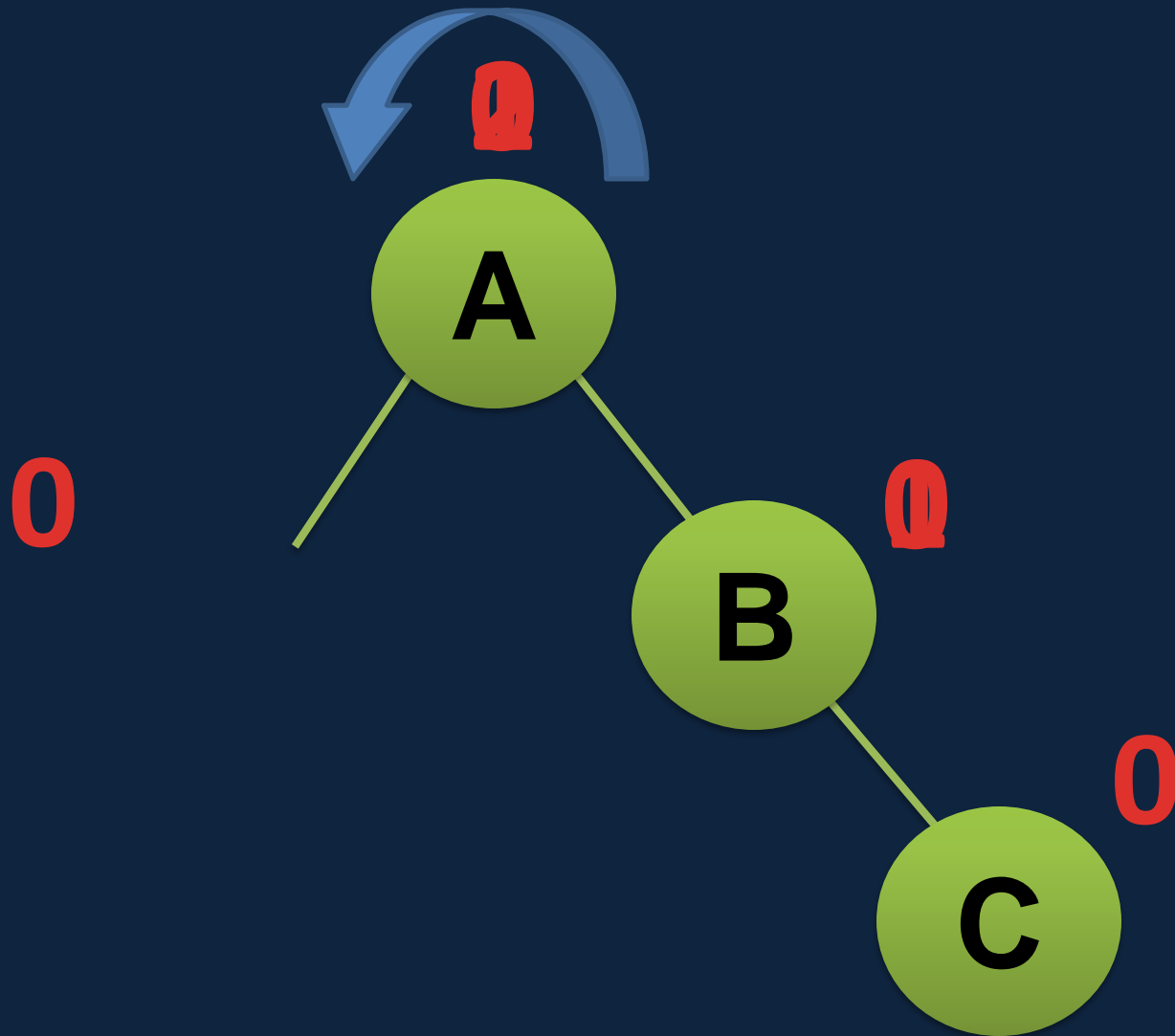
➤ **All Binary Search Trees are Binary Trees but All Binary Trees need not be Binary Search Tree**

Rotations



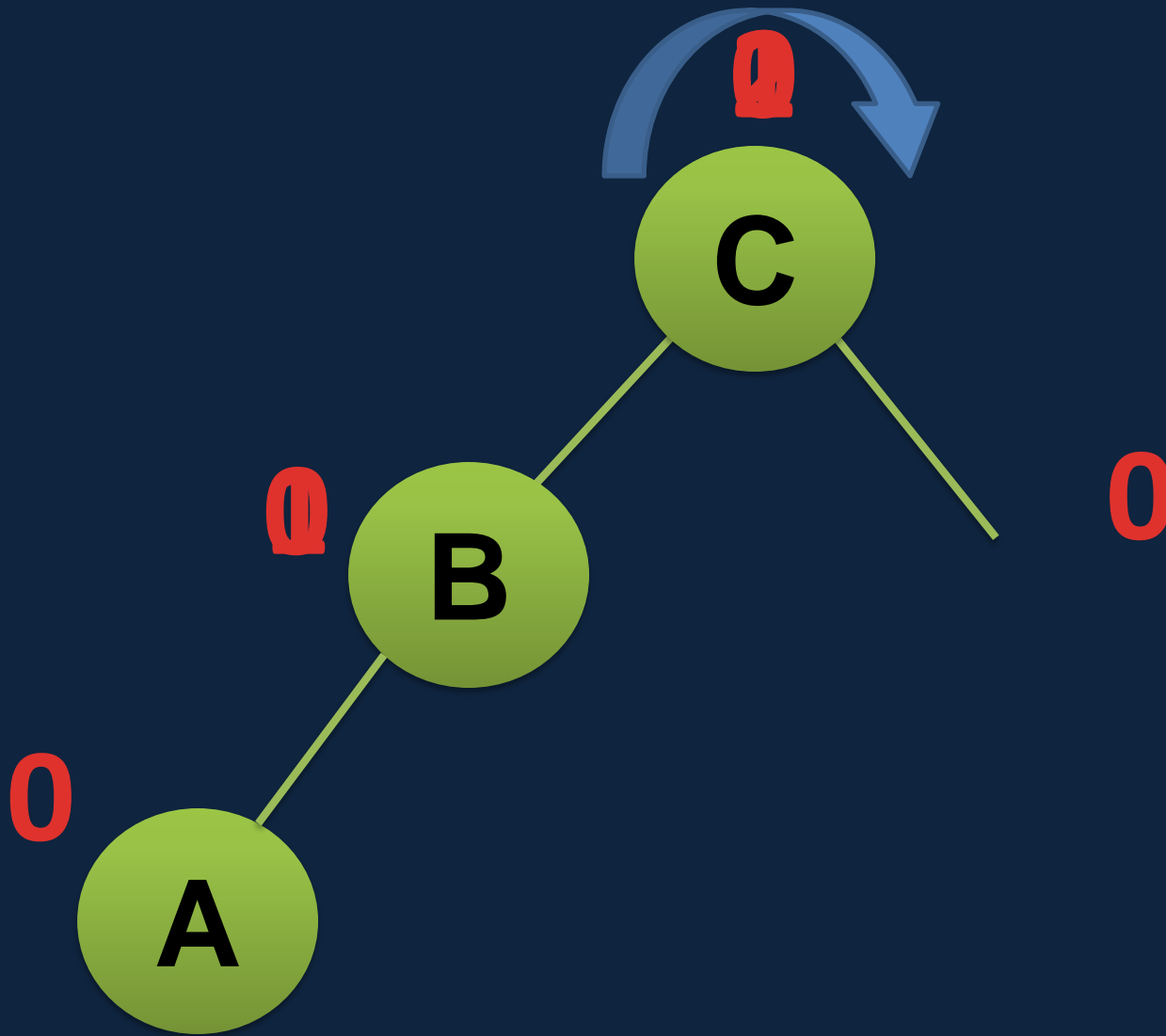
LL Rotation

Insert: A , B , C



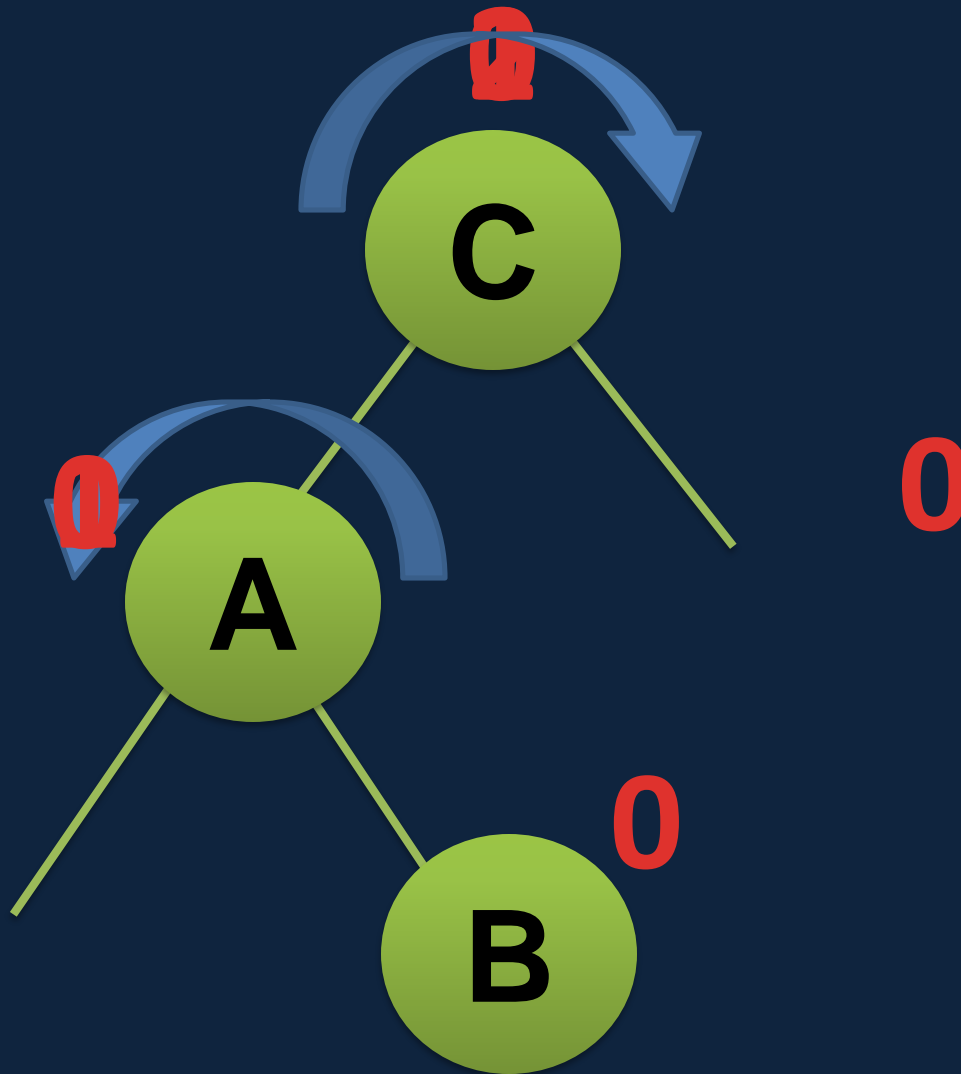
RR Rotation

Insert: C , B , A



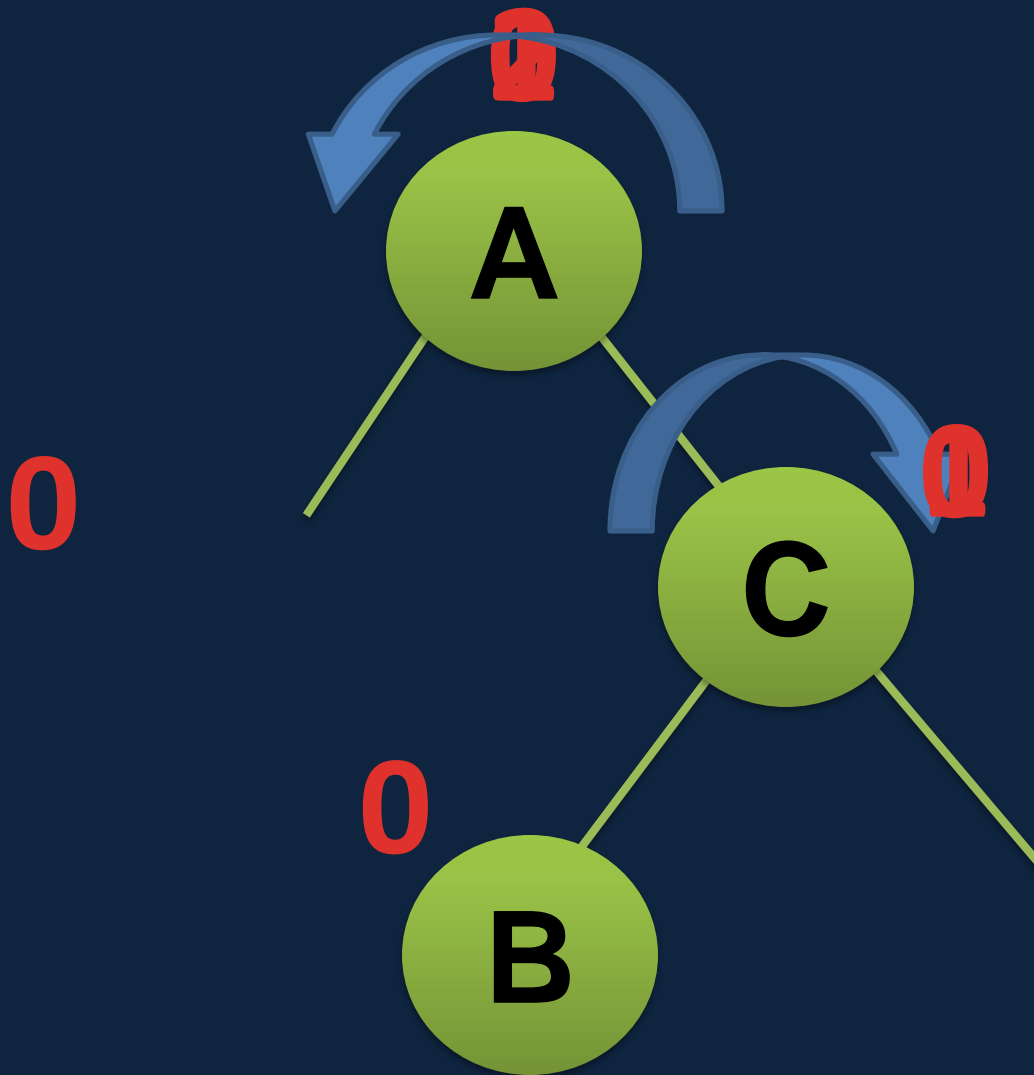
LR Rotation

Insert: C , A , B



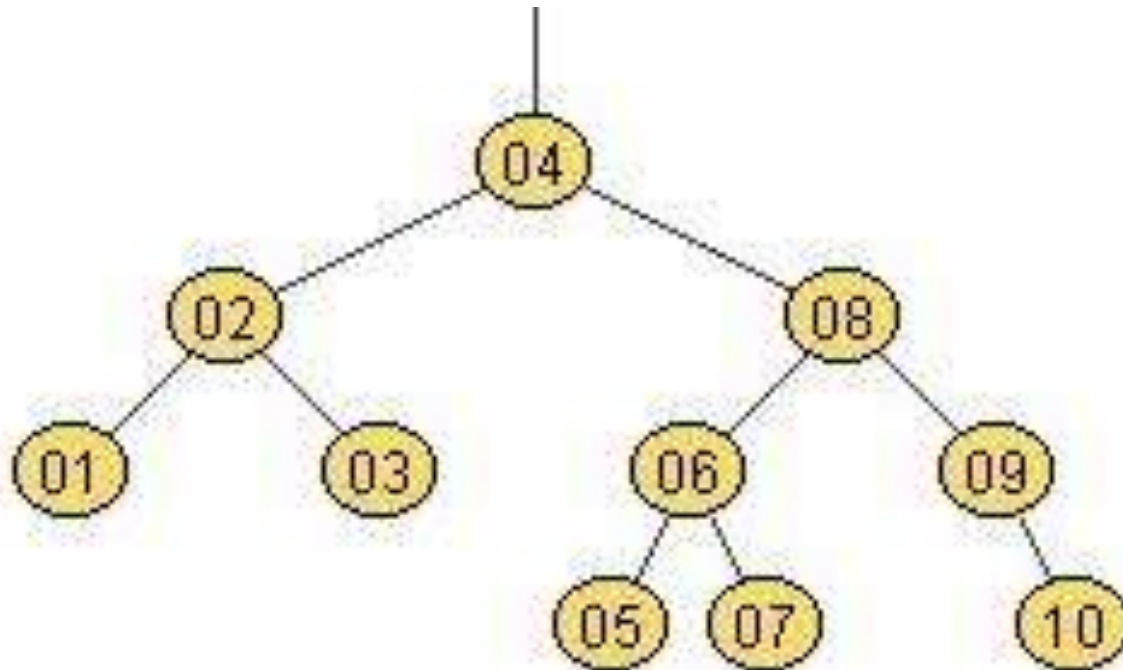
RL Rotation

Insert: A , C , B



Example

Construct AVL Tree by inserting 1 to 10



Deletion

Deletion in AVL Tree have 3

cases

1. Deleting node without any child
2. Deleting node with one child
3. Deleting node with two children

1. Deleting node without any child

Step – 1:

Find given node in AVL Tree by performing search operation

Step – 2:

Remove given node in AVL Tree by using 'delete' operator

Step – 3:

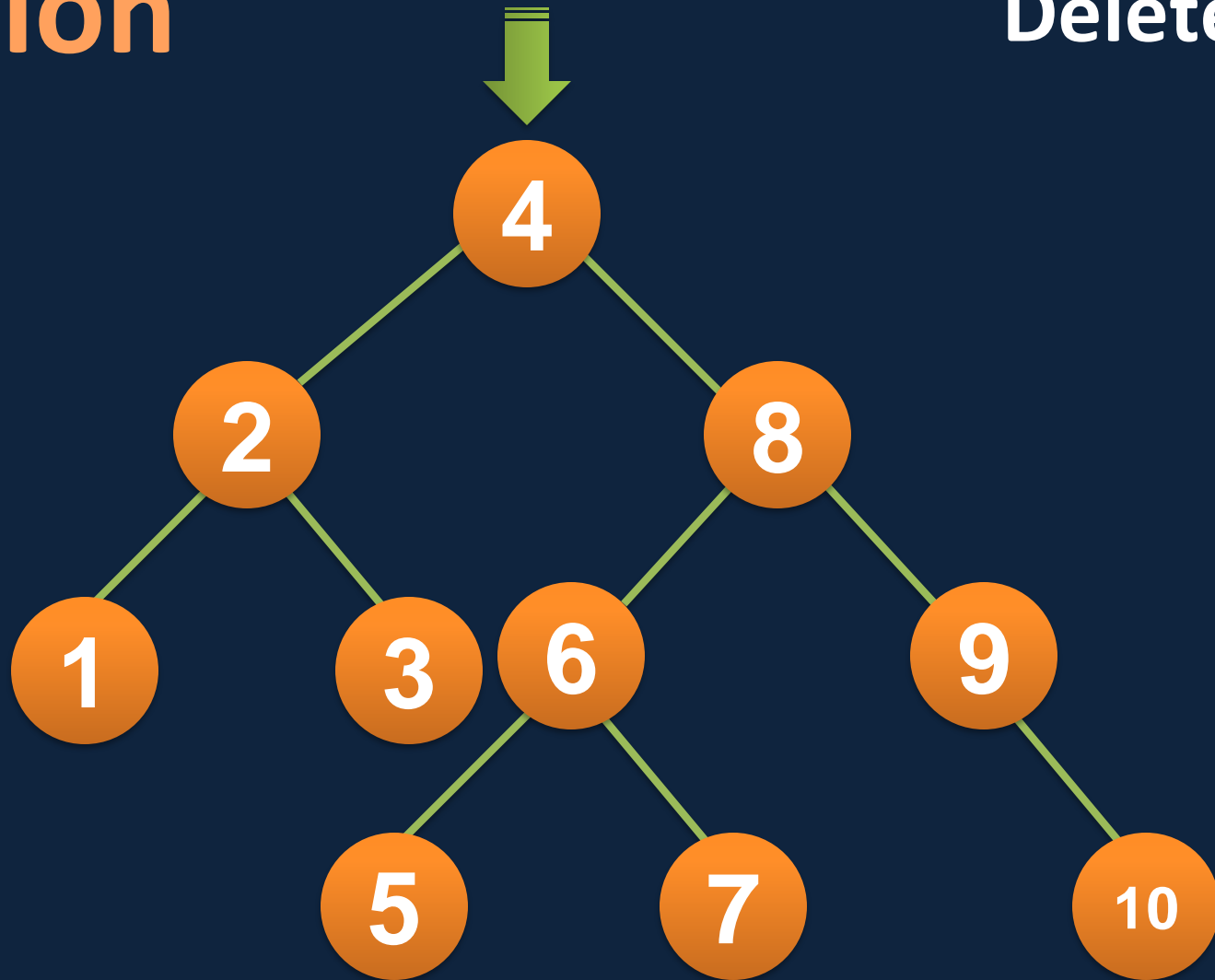
Check balance factor of each node in AVL tree

Step – 4:

If tree is not balanced perform suitable Rotation operation to make tree balanced

Deletion

Delete: 5



2. Deleting node with one child

Step – 1:

Find given node in AVL Tree by performing search operation

Step – 2:

Make a link between its Parent and its Child

Step – 3:

Remove given node in AVL Tree by using 'delete' operator

Step – 4:

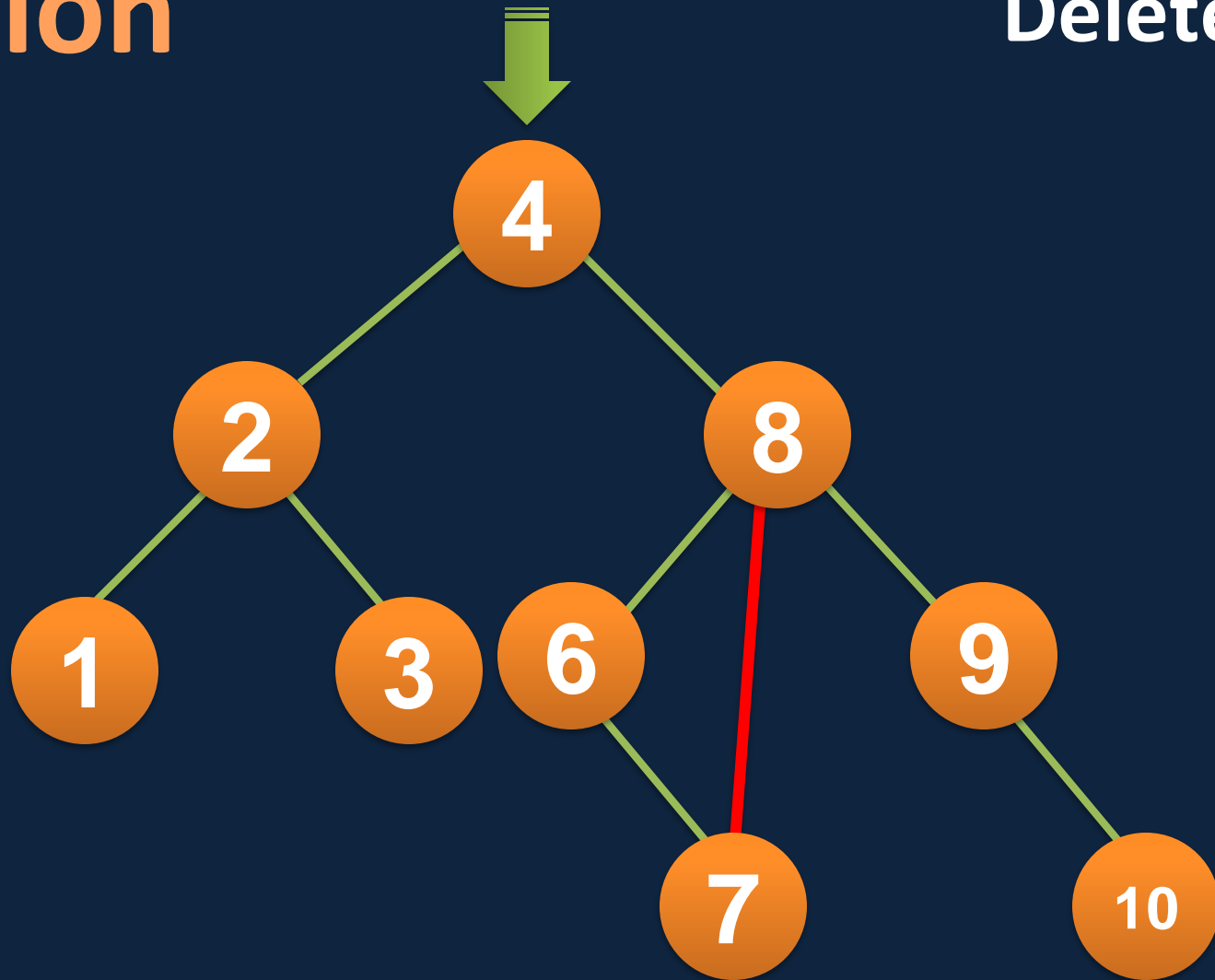
Check balance factor of each node in AVL tree

Step – 5:

If tree is not balanced perform suitable Rotation operation to make tree balanced

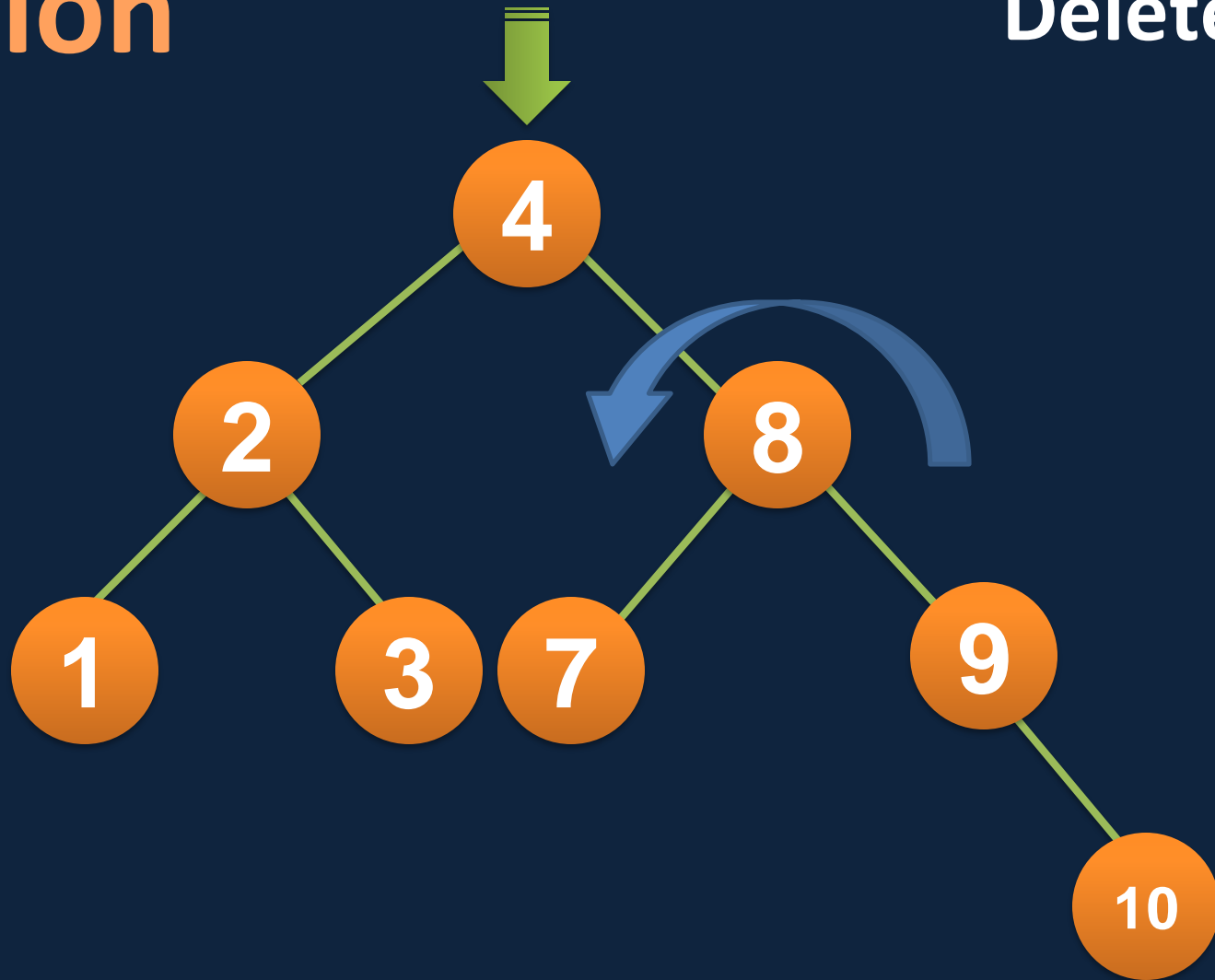
Deletion

Delete: 6



Deletion

Delete: 7



3. Deleting node with two children

Step – 1:

Find given node in AVL Tree by performing search operation

Step – 2:

Find the Smallest node in its Right Subtree

Step – 3:

Swap both given node and the Smallest node in its right subtree

Step – 4:

Remove given node in AVL Tree by using 'delete' operator

Step – 5:

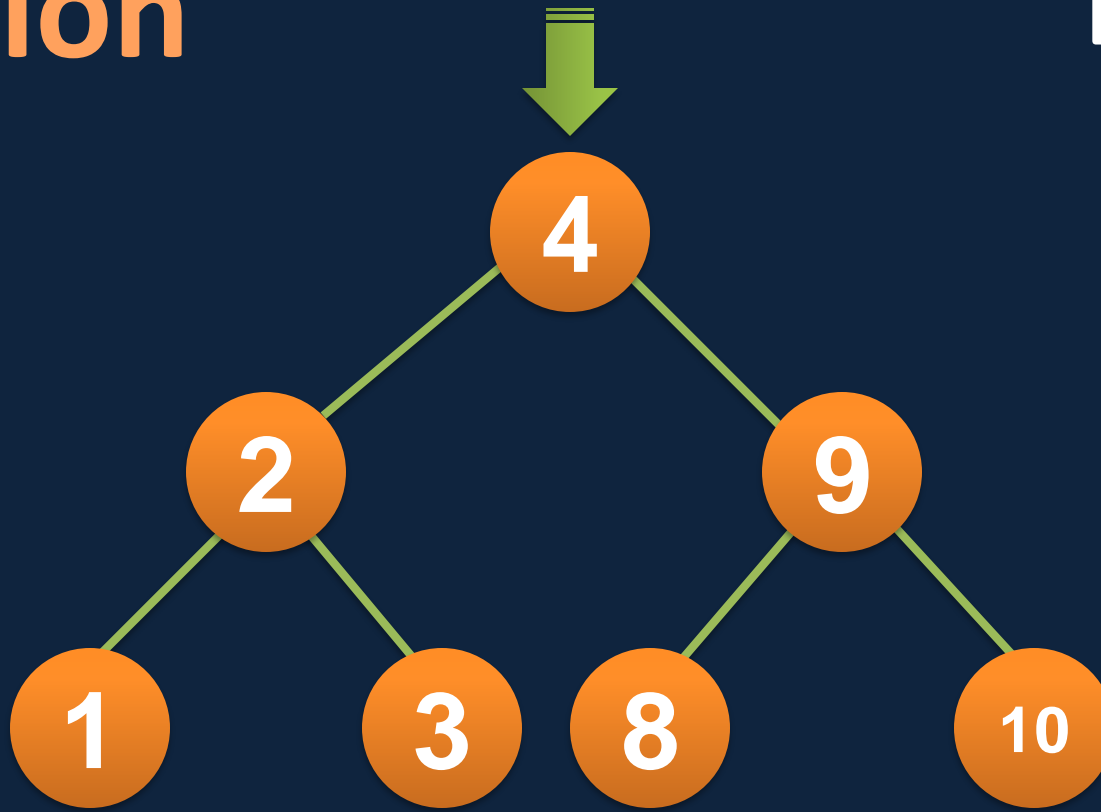
Check balance factor of each node in AVL tree

Step – 6:

If tree is not balanced perform suitable Rotation operation to make tree balanced

Deletion

Delete: 4



Assignment

Construct AVL Tree by inserting 10 to 1

Write applications of AVL
Trees

Explain Deletion in AVL Tree in
detail