Introduction to MATLAB Programming

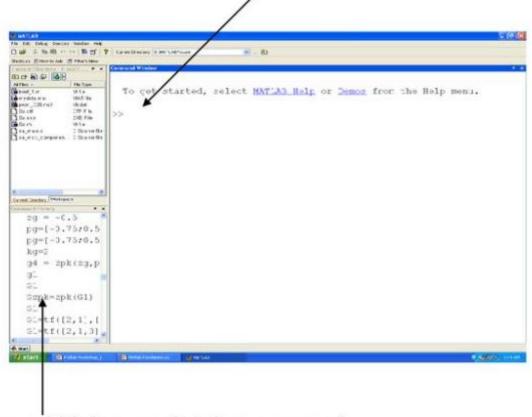
Outline

- MATLAB Environment
 - MATLAB layout
 - Data types
- MATLAB as a Calculator
- Variables
 - Built-in variables
 - Logical variables
 - String
- Matrices
 - Creating
 - Operation
 - Indexing
 - Matrices operation
- Build-in function
- Script file

MATLAB Desktop

On starting MATLAB:

* Matlab Command Prompt



The Command history maintains a record of Matlab functions you ran

Matlab Desktop

- The desktop provides different ways of interacting with Matlab
- Entering commands in the command window
- ✓ Viewing values stored in variables
- d Editing statements in Matlab functions and scripts
- □ Creating and annotating plots

Data types supported by MATLAB

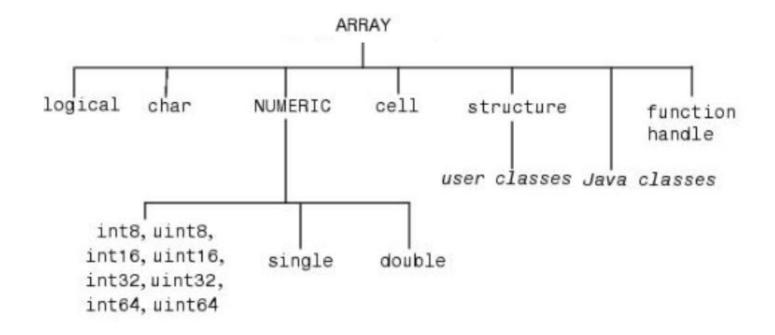
Name Description

• ------

- double double precision, floating point numbers (8 bytes per element)
- uint8 -unsigned 8-bit integers in the range [0-255] (1 byte per element)
- uint16 unsigned 16-bit integers in the range [0,65535]
- uint32 unsigned 32-bit integers in the range [0,4294967295]
- int8 singed 8-bit integers in the range [-128,127]
- int16 singed 16-bit integers in the range [-32768,32767]
- int32 singed 32-bit integers in the range [-2147483648,2147483647]
- single- single precision floating-point numbers (4 bytes per element)
- char characters (2 bytes per element using Unicode rep.)
- logical values are 0 or 1 (1 byte per element)
- All numeric computations (first 8 entries in the above table) in MATLAB are done using double quantities.
- uint8 is the frequently used 8-bit image.

Data Types

• There are 14 fundamental data types in MATLAB



Variables in MATLAB

- MATLAB stores all variables as matrices/arrays
 - A single value is just a 1 x 1 matrix
- You can store numerical values, characters, and strings into variables
- Meaningful variable names will help you make a good program (detailed naming rules are covered later)
 - Variable names are case sensitive be careful
 - -Variable, VARIABLE, variable, and vaRIAble are all different
- The data stored in a variable is stored in the memory assigned for MATLAB in your computer and when you exit MATLAB the data is erased
- Variables created are shown in the workspace window
- clear all will erase all variables (and other stuff) from the workspace

General Purpose Commands

who lists all variables in the current workspace

whos lists all variables in the workspace

including array sizes

clear clears all variables and functions from

memory

clc to clear the Command Window

Variables in MATLAB

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Built-in MATLAB Variables

Name	Meaning
ans	value of an expression when that expression is not assigned to a variable
eps	floating point precision
pi	π , (3.141492)
realmax	largest positive floating point number
realmin	smallest positive floating point number
Inf	∞ , a number larger than realmax, the result of evaluating $1/0$.
NaN	not a number, the result of evaluating $0/0$

Exception: i and j are preassigned to $\sqrt{-1}$. One or both of i or j are often reassigned as loop indices. More on this later.

Matrices and Vectors

All Matlab variables are matrices

- A vector is a matrix with one row or one column.
- A scalar is a matrix with one row and one column.
- A character string is a row of column vector of characters.

Consequences:

- Rules of linear algebra apply to addition, subtraction and multiplication.
- Elements in the vectors and matrices are addressed with Fortran-like subscript notation, e.g., x(2), A(4,5). Usually this notation is clear from context, but it can be confused with a function call,

```
y = sqrt(5) sqrt is a built-in function z = f(3) ls f a function or variable?
```

Creating MATLAB Variables

MATLAB variables are created with an assignment statement

```
>> x = expression
```

where expression is a legal combinations of numerical values, mathematical operators, variables, and function calls.

The expression can involve:

- Manual entry
- · Built-in functions that return matrices
- Custom (user-written) functions that return matrices
- Loading matrices from text files or "mat" files

Element-by-Element Creation of Matrices and Vectors

A matrix, a column vector, and a row vector:

$$A = \begin{bmatrix} 3 & 2 \\ 3 & 1 \\ 1 & 4 \end{bmatrix}$$

$$x = \begin{bmatrix} 5 \\ 7 \\ 9 \\ 2 \end{bmatrix}$$
$$v = \begin{bmatrix} 9 & -3 & 4 & 1 \end{bmatrix}$$

```
As MATLAB variables:
  >> A = [3 2; 3 1; 1 4]
  >> x = [5; 7; 9; 2]
```

Element-by-Element Creation of Matrices and Vectors

For manual entry, the elements in a vector are enclosed in square brackets. When creating a row vector, separate elements with a space.

Separate columns with a semicolon

```
>> w = [2; 6; 1]
w =
2
6
1
```

Element-by-Element Creation of Matrices and Vectors

When assigning elements to matrix, row elements are separated by spaces, and columns are separated by semicolons

Transpose Operator

Once it is created, a variable can be transformed with other operators. The transpose operator converts a row vector to a column vector (and vice versa), and it changes the rows of a matrix to columns.

```
>> v = [2 4 1 7]

v =

2 4 1 7

>> w = v'

w =

2

4

1

7
```

Transpose Operator(2)

Overwriting Variables

Once a variable has been created, it can be reassigned

```
>> x = 2;
>> x = x + 2
x =
y = [1 2 3 4]
>> y = y'
```

Using Functions to Create Matrices and Vectors

Create vectors with built-in functions:

linspace and logspace

Create matrices with built-in functions:

```
ones, zeros, eye, diag, ...
```

Note that ones and zeros can also be used to create vectors.

Creating vectors with linspace (1)

The linspace function creates vectors with elements having uniform linear spacing.

Syntax:

```
x = linspace(startValue, endValue)
x = linspace(startValue, endValue, nelements)
```

Examples:

```
>> u = linspace(0.0,0.25,5)

u =

0 0.0625 0.1250 0.1875 0.2500

>> u = linspace(0.0,0.25);
```

Remember: Ending a statement with semicolon suppresses the output.

Creating vectors with linspace (2)

Column vectors are created by appending the transpose operator to linspace

```
>> v = linspace(0,9,4)'
v =

0
3
6
9
```

Example: A Table of Trig Functions

```
>> x = linspace(0,2*pi,6)'; (note transpose)
>> y = sin(x);
>> z = cos(x);
>> [x y z]
ans =

0 0 1.0000
1.2566 0.9511 0.3090
2.5133 0.5878 -0.8090
3.7699 -0.5878 -0.8090
5.0265 -0.9511 0.3090
6.2832 0 1.0000
```

The expressions y = sin(x) and z = cos(x) take advantage of vectorization. If the input to a vectorized function is a vector or matrix, the output is often a vector or matrix having the same shape. More on this later.

Creating vectors with logspace

The logspace function creates vectors with elements having uniform logarithmic spacing.

Syntax:

```
x = logspace(startValue, endValue)
x = logspace(startValue, endValue, nelements)
```

creates nelements elements between $10^{\text{startValue}}$ and 10^{endValue} . The default value of nelements is 100.

Example:

```
>> w = logspace(1,4,4)
w =
10 100 1000 10000
```

Functions to Create Matrices (1)

Name	Operation(s) Performed
diag	create a matrix with a specified diagonal entries, or extract diagonal entries of a matrix
eye	create an identity matrix
ones	create a matrix filled with ones
rand	create a matrix filled with random numbers
zeros	create a matrix filled with zeros
linspace	create a row vector of linearly spaced elements
logspace	create a row vector of logarithmically spaced elements

Functions to Create Matrices (2)

ones and zeros are also used to create vectors. To do so, set either nrows or ncols to 1.

Functions to Create Matrices (3)

The eye function creates identity matrices of a specified size. It can also create non-square matrices with ones on the main diagonal.

Syntax:

```
A = eye(n)
A = eye(nrows, ncols)
```

Examples:

Functions to Create Matrices (4)

The optional second input argument to eye allows non-square matrices to be created.

where $D_{i,j} = 1$ whenever i = j.

Functions to Create Matrices (5)

The diag function can either create a matrix with specified diagonal elements, or extract the diagonal elements from a matrix

Syntax:

```
A = diag(v)

v = diag(A)
```

Example: Use diag to create a matrix

```
>> v = [1 2 3];

>> A = diag(v)

A =

1 0 0

0 2 0

0 0 3
```

Functions to Create Matrices (6)

Example: Use diag to extract the diagonal of a matrix

Indexing Matrices (1)

If A is a matrix, A(i,j) selects the element in the ith row and jth column. Subscript notation can be used on the right hand side of an expression to refer to a matrix element.

```
>> A = [1 2 3; 4 5 6; 7 8 9];

>> b = A(3,2)

b =

8

>> c = A(1,1)

c =
```

Indexing Matrices (2)

Subscript notation is also used to assign matrix elements

```
>> A(1,1) = c/b
A =
0.2500 2.0000 3.0000
4.0000 5.0000 6.0000
7.0000 8.0000 9.0000
```

Referring to elements beyond the dimensions the matrix results in an error

```
>> A = [1 2 3; 4 5 6; 7 8 9];
>> A(1,4)
??? Index exceeds matrix dimensions.
```

Indexing Matrices (3)

Assigning an element that is beyond the existing dimensions of the matrix causes the matrix to be resized!

In other words, MATLAB automatically resizes matrices on the fly.

Colon notation

Colon notation is very powerful and very important in the effective use of MATLAB. The colon is used as both an operator and as a wildcard.

Use colon notation to:

- create vectors
- refer to or extract ranges of matrix elements

Colon Notation

Syntax:

startValue:endValue

startValue:increment:endValue

Note: startValue, increment, and endValue do not need to be

integers

Colon Notation

Creating row vectors:

```
>> s = 1:4

s =

1 2 3 4

>> t = 0:0.1:0.4

t =

0 0.1000 0.2000 0.3000 0.4000
```

Colon Notation

Creating column vectors:

```
>> u = (1:5)'
u =

1
2
3
4
5

>> v = 1:5'
v =

1 2 3 4
```

v is a row vector because 1:5' creates a vector between 1 and the transpose of 5.

Use colon as a wildcard to refer to an entire column or row

Or use colon notation to refer to subsets of columns or rows

Colon notation is often used in compact expressions to obtain results that would otherwise require several steps.

Example:

```
>> A = ones(8,8);
>> A(3:6,3:6) = zeros(4,4)
A =

1     1     1     1     1     1     1
1     1     1     1     1     1
1     1     1     1     1     1
1     1     0     0     0     0
1     1     1     0     0
1     1     1     1
1     1     0     0     0     0
1     1     1
1     1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
1     1     1     1
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1     1     1
1     1     1
1     1     1
1     1     1
1     1     1
1     1     1
1     1
1     1     1
1     1
1     1
```

Finally, colon notation is used to convert any vector or matrix to a column vector.

Example:

```
>> x = 1:4;
>> y = x(:)
y =
1
2
3
4
```

Colon notation converts a matrix to a column vector by appending the columns of the input matrix

```
>> A = rand(2,3);

>> v = A(:)

v =

0.9501

0.2311

0.6068

0.4860

0.8913

0.7621

0.4565
```

Note: The rand function generates random elements between zero and one.

Repeating the preceding statements will, in all likelihood, produce different numerical values for the elements of v.

Exercise: Generating complex functions

- Generate a complex function f(t) = 3ej3πt for t ranging from 0 to 1 in 0.001 increments.
- Step1: create a time variable,
 - t = 0.0.001.1;
- Step2: construct the vector,
 - f = 3*exp(j*3*pi*t);
- Step3: plot (t,f)

Additional Types of Variables

Matrix elements can either be numeric values or characters. Numeric elements can either be real or complex (imaginary).

More general variable types are available: n-dimensional arrays (where n>2), structs, cell arrays, and objects. Numeric (real and complex) and string arrays of dimension two or less will be sufficient for our purposes.

Consider some simple variations on numeric and string matrices:

- Complex Numbers
- Strings
- Polynomials

Complex Numbers

MATLAB automatically performs complex arithmetic

Unit Imaginary Numbers (1)

```
i and j are ordinary MATLAB variables preassigned with the value \sqrt{-1}. >> i^2
```

ans = -1

Both or either i and j can be reassigned

Unit Imaginary Numbers (2)

The i and j variables are often used for array subscripting. Set i (or j) to an integer value that is also a valid array subscript.

Note: When working with complex numbers, it is a good idea to reserve either i or j for the unit imaginary value $\sqrt{-1}$.

Functions for Complex Arithmetic (1)

Function	Operation			
abs	Compute the magnitude of a number abs(z) is equivalent to sqrt(real(z)^2 + imag(z)^2)			
angle	Angle of complex number in Euler notation			
exp	If x is real, $\exp(x) = e^x$			
	If z is complex, $\exp(z) = e^{\operatorname{Re}(z)}(\cos(\operatorname{Im}(z) + i\sin(\operatorname{Im}(z)))$			
conj	Complex conjugate of a number			
imag	Extract the imaginary part of a complex number			
real	Extract the real part of a complex number			

Functions for Complex Arithmetic

Examples:

```
>> zeta = 5; theta = pi/3; >> x = real(z)
>> z = zeta*exp(i*theta)
                                  x =
                                       2.5000
Z =
   2.5000 + 4.3301i
                                   >> y = imag(z)
>> abs(z)
                                       4.3301
ans =
     5
                                   >> angle(z)*180/pi
>> sqrt(z*conj(z))
                                  ans =
                                     60.0000
ans =
     5
```

Remember: There is no "degrees" mode in MATLAB. All angles are in radians.

Exercise 1

Evaluating complex variables and Expressions

- Express the following complex numbers in Cartesian form. Plot it in the complex plane
- a) $y = je^{j11\pi/4}$
- b) $y=(1-j)^{10}$

plot(y,'x')

Strings

- Strings are matrices with character elements.
- String constants are enclosed in single quotes
- Colon notation and subscript operations apply

Examples:

```
>> first = 'John';
>> last = 'Coltrane';
>> name = [first,' ',last]
name =
John Coltrane

>> length(name)
ans =
    13

>> name(9:13)
ans =
trane
```

Functions for String Manipulation (1)

Functions for String Manipulation (1)

Function	Operation			
char	Converts an integer to the character using ASCII codes, or combines characters into a character matrix			
findstr	Finds one string in another string			
length	Returns the number of characters in a string			
num2str	Converts a number to string			
str2num	Converts a string to a number			
strcmp	Compares two strings			
strmatch	Identifies rows of a character array that begin with a string			
strncmp	Compares the first n elements of two strings			
sprintf	Converts strings and numeric values to a string			

Functions for String Manipulation (2)

num2str converts a number to a string

```
>> msg1 = ['There are ',num2str(100/2.54),' inches in a meter']
msg1 =
There are 39.3701 inches in a meter
```

For greater control over format of the number-to-string conversion, use sprintf

```
>> msg2 = sprintf('There are %5.2f cubic inches in a liter',1000/2.54^3)
msg2 =
There are 61.02 cubic inches in a liter
```

The Matlab sprintf function is similar to the C function of the same name, but it uses single quotes for the format string.

Functions for String Manipulation (3)

The char function can be used to combine strings

```
>> both = char(msg1,msg2)
both =
There are 39.3701 inches in a meter
There are 61.02 cubic inches in a liter
```

or to refer to individual characters by their ASCII codes¹

```
>> char(49)
ans =
1
>> char([77 65 84 76 65 66])
ans =
MATLAB
```

ode	HEX	Symbol	HTML Number	HTML Name	HTML Name2	Name
65	41	Α	A			Uppercase
66	42	В	B			Uppercase
67	43	С	C			Uppercase
68	44	D	D			Uppercase
69	45	Е	E			Uppercase
70	46	F	F			Uppercase
71	47	G	G			Uppercase
72	48	Н	H			Uppercase
73	49	1	I			Uppercase
74	4A	J	J			Uppercase
75	4B	К	K			Uppercase
76	4C	L	L			Uppercase
77	4D	М	M			Uppercase
78	4E	N	N			Uppercase
79	4F	0	O			Uppercase
80	50	Р	P			Uppercase
81	51	Q	Q			Uppercase
82	52	R	R			Uppercase
83	53	S	S			Uppercase
84	54	Т	T			Uppercase
85	55	U	U			Uppercase
86	56	V	V			Uppercase
87	57	W	W			Uppercase
88	58	X	X			Uppercase
89	59	Υ	Y			Uppercase
90	5A	Z	Z			Uppercase

ASCII Character Category

¹See e.g., www.asciicodes.com or wikipedia.org/wiki/ASCII.

Polynomials

 ${
m Matlab}$ polynomials are stored as vectors of coefficients. The polynomial coefficients are stored in decreasing powers of x

$$P_n(x) = c_1 x^n + c_2 x^{n-1} + \dots + c_n x + c_{n+1}$$

Example: Evaluate $x^3 - 2x + 12$ at x = -1.5

Store the coefficients of the polynomial in vector c:

$$>> c = [1 \ 0 \ -2 \ 12];$$

Use the built-in polyval function to evaluate the polynomial.

```
>> polyval(c,1.5)
ans =
12.3750
```

Functions for Manipulating Polynomials

Function	Operations performed		
conv	Product (convolution) of two polynomials		
deconv	Division (deconvolution) of two polynomials		
poly	Create a polynomial having specified roots		
polyder	Differentiate a polynomial		
polyval	Evaluate a polynomial		
polyfit	Polynomial curve fit		
roots	Find roots of a polynomial		

Vector Addition and Subtraction

Vector and addition and subtraction are element-by-element operations.

Example:

```
>> u = [10 9 8]; (u and v are row vectors)
>> v = [1 2 3];
>> u+v
ans =
11 11 11
>> u-v
ans =
9 7 5
```

Vectorization

- Vectorization is the use of single, compact expressions that operate on all elements of a vector without explicitly writing the code for a loop.
 The loop is executed by the MATLAB kernel, which is much more efficient at evaluating a loop in interpreted MATLAB code.
- Vectorization allows calculations to be expressed succintly so that programmers get a high level (as opposed to detailed) view of the operations being performed.
- Vectorization is important to make MATLAB operate efficiently².

²Recent versions of MATLAB have improved the efficiency for some non-vectorized code.

Vectorization of Built-in Functions

Most built-in function support *vectorized* operations. If the input is a scalar the result is a scalar. If the input is a vector or matrix, the output is a vector or matrix with the same number of rows and columns as the input.

Example:

```
>> x = 0:pi/4:pi (define a row vector)

x = 0 0.7854 1.5708 2.3562 3.1416

>> y = cos(x) (evaluate cosine of each x(i))

y = 1.0000 0.7071 0 -0.7071 -1.0000
```

Vectorized Calculations (6)

More examples

```
>> A = pi*[ 1 2; 3 4]
                                      >> B = A/2
                                       B =
A =
    3.1416
             6.2832
                                          1.5708
                                                    3.1416
    9.4248
            12.5664
                                          4.7124
                                                    6.2832
>> S = sin(A)
                                      >> T = sin(B)
S =
                                      T =
     0
          0
                                           1
                                                 0
     0
           0
                                           -1
                                                 0
```

Array Operators

Array operators support element-by-element operations that are not defined by the rules of linear algebra.

Array operators have a period prepended to a standard operator.

Symbol	Operation		
.*	element-by-element multiplication		
./	element-by-element "right" division		
.\	element-by-element "left" division		
.^	element-by-element exponentiation		

Array operators are a very important tool for writing vectorized code.

Using Array Operators (1)

Examples: Element-by-element multiplication and division

```
>> u = [1 2 3];

>> v = [4 5 6];

Use .* and ./ for element-by-element multiplication and division

>> w = u.*v

w =

4 10 18

>> x = u./v

x =

0.2500 0.4000 0.5000
```

Using Array Operators (1)

Examples: Element-by-element multiplication and division

Using Array Operators (2)

Examples: Application to matrices

The last statement causes an error because the number of columns in ${\tt A}$ is not equal to the number of rows in ${\tt B}$ — a requirement for ${\tt A}$ and ${\tt B}$ to be compatible for matrix multiplication.

Using Array Operators (3)

```
>> A = [1 2 3 4; 5 6 7 8];

>> B = [8 7 6 5; 4 3 2 1];

>> A*B'

ans =

60 20

164 60
```

The number of columns in A is equal to the number of rows in B^T , so A*B, is a legal matrix-matrix multiplication.

Array operators also apply to matrix powers.

Built-in Functions

Many standard mathematical functions, such as sin, cos, log, and log10, are built-in.

Example:

```
log(x) computes the natural logarithm of x log10(x) is the base 10 logarithm log2(x) is the base 2 logarithm
```

```
>> log(256)
ans =
5.5452
>> log10(256) ans =
2.4082
>> log2(256) ans =
8
```

Ways to Get Help

- Use on-line help to request info on a specific function
- >> help sqrt
- In Matlab version 6 and later the doc function opens the on-line version of the manual. This is very helpful for more complex commands.
- >> doc plot
- Use lookfor to find functions by keywords
- >> lookfor functionName

On-line Help (1)

```
Syntax:
```

help functionName

Example:

>> help log

produces

LOG Natural logarithm.

LOG(X) is the natural logarithm of the elements of X.

Complex results are produced if X is not positive.

See also LOG2, LOG10, EXP, LOGM.

The help function provides a compact summary of how to use a command. Use the doc function to get more in-depth information.

On-line Help (2)

The help browser opens when you type a doc command:

>> doc plot



Looking for Functions

Syntax:

lookfor string

searches first line of function descriptions for "string".

Example:

>> lookfor cosine

produces

ACOS Inverse cosine.

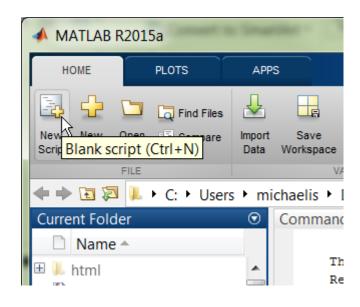
ACOSH Inverse hyperbolic cosine.

COS Cosine.

COSH Hyperbolic cosine.

Creating a MATLAB Program/Script

- Click on "New Script" at the upper left corner of the "Home" tab to create a new script (*.m) file.
- The MATLAB editor window is opened whenever a new script is created or an existing one is opened.



Scripts with input and output

```
% This script calculates the area of a circle
% It prompts the user for the radius
% Prompt the user for the radius and calculate
% the area based on that radius
radius = input('Please enter the radius: ');
area = pi * (radius^2);
% Print all variables in a sentence format
fprintf('For a circle with a radius of %.2f,',radius)
fprintf('the area is %.2f\n',area)
```