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## **Assignment 1**

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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**12.13.6.7: Question**. A die is thrown again and again until three sixes are obtained. Find the probability of obtaining the third six in the sixth throw of the die.

[: The events  $E_1$  and  $E_2$  are independent]

$$P(E_1E_2) = P(X=2) \times \frac{1}{6}$$

$$P(E_1 E_2) = \frac{625}{23328}$$

**Answer:**  $\frac{625}{23328}$ .

## **Solution**:

Parameter	Description	Value
X	Random variable representing number of sixes obtained in the first five throws of the die	-
p	Probability of getting a 6 in the throw of a die	$\frac{1}{6}$
n	number of trials	5

$$x \in \{0, 1, 2, 3, 4, 5\}$$

where x is the possible value of X.

$$P(X = x) = {}^{n}C_{x} \times p^{x} \times (1 - p)^{(n-x)}$$

$$P(X = x) = {}^{5}C_{x} \times (\frac{1}{6})^{x} \times (\frac{5}{6})^{(5-x)}$$

$$P(X = x) = \begin{cases} \frac{3125}{7776} & x = 0\\ \frac{3125}{7776} & x = 1\\ \frac{625}{3888} & x = 2\\ \frac{125}{3888} & x = 3\\ \frac{25}{7776} & x = 4\\ \frac{1}{7776} & x = 5 \end{cases}$$

Let  $E_1$ : Event that two sixes are obtained in first five throws of the die

 $E_2$ : Event that a six is obtained at the sixth throw of the die

Event that both  $E_1$  and  $E_2$  occur is favourable

$$P(E_1E_2) = P(E_1) \times P(E_2)$$