

## TUTORIAL-2

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Sec - CST - SPL 2

Roll No. - 40

Que 1

```
void fun (int n) {  
    int j=1, i=0;  
    while (i<n) {  
        i+=j; j++; }  
}
```

for  $j=1$        $i=1$ ;  
      $j=2$        $i=1+2$ ;  
      $j=3$        $i=1+2+3$ ;  
      $\vdots$            $\vdots$   
                 (m levels)

for  $i$

$$\therefore 1+2+3+\dots < n$$

$$\therefore 1+2+\dots m < n$$

$$\therefore \frac{m(m+1)}{2} < n$$

$$m \approx \sqrt{n}$$

$\therefore$  by summation method

$$O \sum_{i=1}^m 1 \quad O \quad 1+1+\dots \sqrt{n} \text{ times}$$

$$\therefore \boxed{T(n) \approx \sqrt{n}}$$

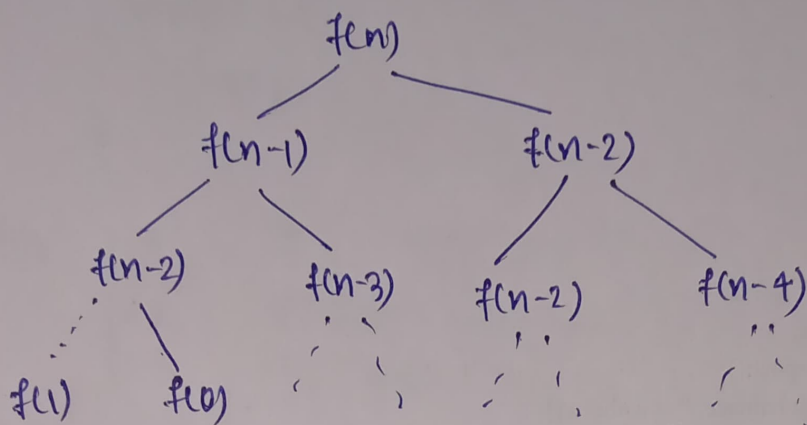
Rathi

Que 2. for fibonacci series -

$$f(n) = f(n-1) + f(n-2)$$

$$f(0) = 0 \quad f(1) = 1$$

By forming tree -



At every function call we get 2 function calls -

$\therefore$  for  $n$  levels -

we have,  $2 \times 2 \times \dots n$  times

$$\therefore \boxed{T(n) = 2^n}$$

Maximum space -

considering recursive stack,

no. of calls maximum =  $n$

For each call we have space complexity  $O(1)$

$$\therefore \boxed{T(n) = O(n)}$$

without considering recursive stack,

for each call we have time complexity  $O(1)$

$$\therefore \boxed{T(n) = O(1)}$$

Ravi

Que 3:

Q) merge

quick sort

```
void quicksort (int arr[], int low, int high)
```

```
{
```

```
    if (low < high)
```

```
    {
```

```
        int pi = pos partition (arr, low, high);
```

```
        quicksort (arr, low, pi-1);
```

```
        quicksort (arr, pi+1, high);
```

```
    }
```

```
}
```

```
int partition (int arr[], int low, int high)
```

```
{
```

```
    int pivot = arr[high]
```

```
    int i = (low-1);
```

```
    for (int j = low; j < high-1; j++)
```

```
    {
```

```
        if (arr[j] < pivot)
```

```
        {
```

```
            i++;
```

```
            swap (arr[i], arr[j]);
```

```
        }
```

```
    }
```

```
    swap (arr[i+1], arr[high]);
```

```
    return (i+1);
```

```
}
```

Pathi

②  $n^3$

multiplication of two square matrix

for  $i=0; i < r1; i++$  {

for  $j=0; j < c2; j++$  {

for  $k=0; k < c1; k++$

{

$res[i][j] += a[i][k] * b[k][j];$

}

}

③  $\log(\log n)$

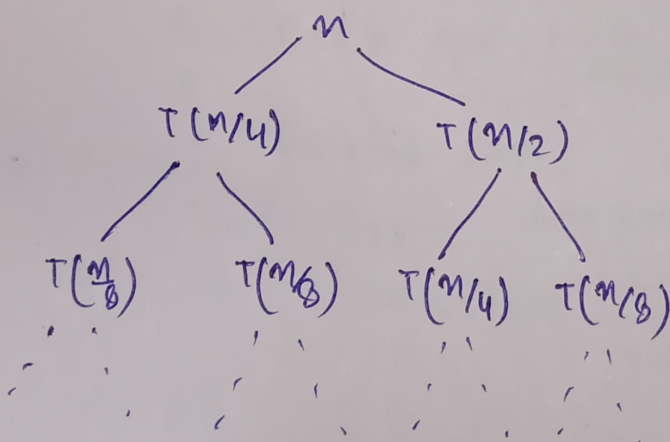
for  $i=2; i < n; i = i * i$

{

count++;

}

Que 4:  $T(n) = T(n/4) + T(n/2) + cn^2$



At level -

$$0 \rightarrow cn^2$$

$$1 \rightarrow \frac{n^2}{4^2} + \frac{n^2}{2^2} = \frac{5n^2}{16}$$

$$2 \rightarrow \frac{n^2}{8^2} + \frac{n^2}{16^2} + \frac{n^2}{4^2} + \frac{n^2}{8^2} = \left(\frac{5}{16}\right)^2 n^2$$

*Patni*

$$\text{max levels} = \frac{n}{2^k} = 1$$

$$2) k = \log_2 n$$

$$\therefore T(n) = c(n^2 + (5/16)n^2 + (5/16)^2 n^2 + \dots + (5/16)^{\log_2 n} n^2)$$

$$= cn^2 [1 + (5/16) + (5/16)^2 + \dots + (5/16)^{\log_2 n}]$$

$$= cn^2 \times 1 \times \left( \frac{1 - (5/16)^{\log_2 n}}{1 - 5/16} \right)$$

$$= cn^2 \times \frac{11}{5} (1 - (5/16)^{\log_2 n})$$

$$\therefore \boxed{T(n) = O(n^2 c)}$$

Ans:

```
int fun(int n) {
```

```
    for (i=1; i<=n; i++)
```

```
        for (j=1; j<=n; j++)
```

```
            // O(1)
```

```
    }
```

for

i

j

j = (n-1)/i times

1

1

2

1+3+5

3

1+4+7

⋮

⋮

n

⋮

$$\sum_{i=1}^n \frac{(n-1)}{i}$$

Latika

$$\therefore T(n) = \frac{(n-1)}{1} + \frac{(n-1)}{2} + \frac{(n-1)}{3} + \dots + \frac{(n-1)}{n}$$

$$T(n) = n \left[ 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right] - 1 \left[ 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right]$$

$$= n \log n - \log n \log n$$

$$\therefore \underline{\underline{T(n) = O(n \log n)}}$$

Ques 6. for (i=2; i<=n; i=pow(i,k))

{

    O(1)

}

for

    2<sup>1</sup>

    2<sup>k</sup>

    2<sup>k<sup>2</sup></sup>

    2<sup>k<sup>3</sup></sup>

    ⋮

    2<sup>k<sup>m</sup></sup>

where,  $2^{k^m} \leq n$

$$k^m = \log_2 n$$

$$m = \log_k \log_2 n$$

$$\therefore \sum_{i=1}^m 1$$

⇒ 1 + 1 + 1 + ... m times

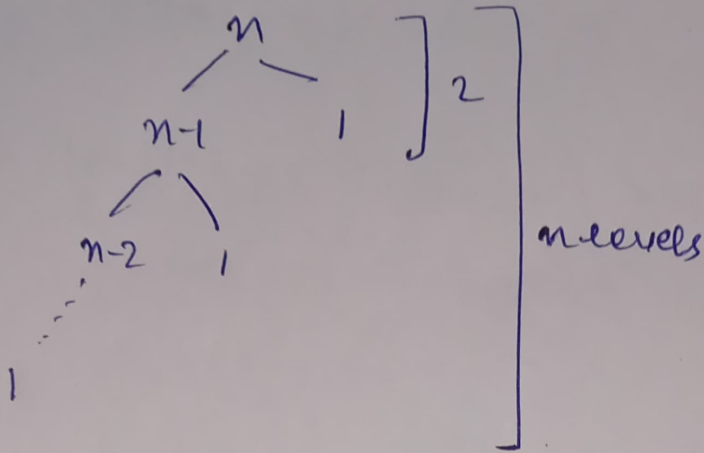
$$\therefore \boxed{T(n) = O(\log_k \log n)}$$

Qatir



Que 7: Given algo divides array in 99% & 1% part

$$\therefore T(n) = T(n-1) + O(1)$$



'n' work is done at each level for merging.

$$T(n) = (T(n-1) + T(n-2) + \dots + T(1) + O(1)) \times n$$
$$\geq n \times n$$

$$\therefore \boxed{T(n) \geq O(n^2)}$$

Lowest height  $\geq 2$

Highest height  $= n$

$$\therefore \boxed{\text{difference} \geq n-2} \quad n > 1$$

The given algo produces linear result.

*gauri*

Ques 8. Considering for large values of 'n'

$$(a) 1.00 < \log \log n < \log n < (\log n)^2 < \sqrt{n} < n < n \log n < \log(n!) < n^2 < 2^n < 4^n < 2^{2^n}$$

$$(b) 1 < \log \log n < \sqrt{\log n} < \log n < \log 2n < 2 \log n < n < n \log n < 2n < 4n < \log(n!) < n^2 < n! < 2^{2^n}$$

$$(c) 96 < \log_6 n < \log_2 n < 5n < n \log_6 n < n \log_2 n < \log(n!) < 6n^2 < 7n^3 < n! < 2^{2^n}$$

Patti