

The Ohio State University

PROJECT 5: SORTINGMACHINE WITH HEAPSORT

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SW 2: Dev & Dsgn

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```
1 import java.util.Comparator;
2 import java.util.Iterator;
3 import java.util.NoSuchElementException;
4
5 import components.queue.Queue;
6 import components.queue.Queue1L;
7 import components.sortingmachine.SortingMachine;
8 import components.sortingmachine.SortingMachineSecondary;
9
10 /**
11  * {@code SortingMachine} represented as a {@code Queue} and an
12  * array (using an
13  * embedding of heap sort), with implementations of primary
14  * methods.
15  *
16  * @param <T>
17  *     type of {@code SortingMachine} entries
18  * @mathdefinitions <pre>
19  * IS_TOTAL_PREORDER (
20  *   r: binary relation on T
21  * ) : boolean is
22  *   for all x, y, z: T
23  *     ((r(x, y) or r(y, x)) and
24  *      (if (r(x, y) and r(y, z)) then r(x, z)))
25  *
26  * SUBTREE_IS_HEAP (
27  *   a: string of T,
28  *   start: integer,
29  *   stop: integer,
30  *   r: binary relation on T
31  * ) : boolean is
32  *   [the subtree of a (when a is interpreted as a complete
33  *    binary tree) rooted
34  *    at index start and only through entry stop of a satisfies
35  *    the heap
36  *    ordering property according to the relation r]
37  *
38  * SUBTREE_ARRAY_ENTRIES (
39  *   a: string of T,
```

```
36 *   start: integer,
37 *   stop: integer
38 * ) : finite multiset of T is
39 * [the multiset of entries in a that belong to the subtree of
   a
40 *   (when a is interpreted as a complete binary tree) rooted
   at
41 *   index start and only through entry stop]
42 * </pre>
43 * @convention <pre>
44 * IS_TOTAL_PREORDER([relation computed by
   $this.machineOrder.compare method] and
45 * if $this.insertionMode then
46 *   $this.heapSize = 0
47 * else
48 *   $this.entries = <> and
49 *   for all i: integer
50 *     where (0 <= i and i < |$this.heap|)
51 *       ([entry at position i in $this.heap is not null]) and
52 *       SUBTREE_IS_HEAP($this.heap, 0, $this.heapSize - 1,
53 *       [relation computed by $this.machineOrder.compare
   method]) and
54 *   0 <= $this.heapSize <= |$this.heap|
55 * </pre>
56 * @correspondence <pre>
57 * if $this.insertionMode then
58 *   this = (true, $this.machineOrder,
   multiset_entries($this.entries))
59 * else
60 *   this = (false, $this.machineOrder,
   multiset_entries($this.heap[0, $this.heapSize]))
61 * </pre>
62 *
63 * @author Daniil Gofman, Ansh Pachauri
64 *
65 */
66 public class SortingMachine5a<T> extends
   SortingMachineSecondary<T> {
67
```

```
68      /*
69      * Private members
70      */
71
72      /**
73      * Order.
74      */
75      private Comparator<T> machineOrder;
76
77      /**
78      * Insertion mode.
79      */
80      private boolean insertionMode;
81
82      /**
83      * Entries.
84      */
85      private Queue<T> entries;
86
87      /**
88      * Heap.
89      */
90      private T[] heap;
91
92      /**
93      * Heap size.
94      */
95      private int heapSize;
96
97      /**
98      * Exchanges entries at indices {@code i} and {@code j} of
99      * {@code array}.
100     *
101     * @param <T>
102     *         type of array entries
103     * @param array
104     *         the array whose entries are to be exchanged
105     * @param i
```

```
105      *           one index
106      * @param j
107      *           the other index
108      * @updates array
109      * @requires 0 <= i < |array| and 0 <= j < |array|
110      * @ensures array = [#array with entries at indices i and j
    exchanged]
111      */
112      private static <T> void exchangeEntries(T[] array, int i,
    int j) {
113          assert array != null : "Violation of: array is not
    null";
114          assert 0 <= i : "Violation of: 0 <= i";
115          assert i < array.length : "Violation of: i < |array|";
116          assert 0 <= j : "Violation of: 0 <= j";
117          assert j < array.length : "Violation of: j < |array|";
118
119          if (i != j) {
120              T tmp = array[i];
121              array[i] = array[j];
122              array[j] = tmp;
123          }
124      }
125
126      /**
127       * Given an array that represents a complete binary tree
    and an index
128       * referring to the root of a subtree that would be a heap
    except for its
129       * root, sifts the root down to turn that whole subtree
    into a heap.
130       *
131       * @param <T>
132       *           type of array entries
133       * @param array
134       *           the complete binary tree
135       * @param top
136       *           the index of the root of the "subtree"
137       * @param last
```

```

138     *           the index of the last entry in the heap
139     * @param order
140     *           total preorder for sorting
141     * @updates array
142     * @requires <pre>
143     * 0 <= top and last < |array| and
144     * for all i: integer
145     *   where (0 <= i and i < |array|)
146     *   ([entry at position i in array is not null]) and
147     *   [subtree rooted at {@code top} is a complete binary
148     *   tree] and
149     *   SUBTREE_IS_HEAP(array, 2 * top + 1, last,
150     *   [relation computed by order.compare method]) and
151     *   SUBTREE_IS_HEAP(array, 2 * top + 2, last,
152     *   [relation computed by order.compare method]) and
153     *   IS_TOTAL_PREORDER([relation computed by order.compare
154     *   method])
155     * </pre>
156     * @ensures <pre>
157     * SUBTREE_IS_HEAP(array, top, last,
158     * [relation computed by order.compare method]) and
159     * perms(array, #array) and
160     * SUBTREE_ARRAY_ENTRIES(array, top, last) =
161     * SUBTREE_ARRAY_ENTRIES(#array, top, last) and
162     * [the other entries in array are the same as in #array]
163     * </pre>
164     */
165     private static <T> void siftDown(T[] array, int top, int
166     last,
167     Comparator<T> order) {
168     assert array != null : "Violation of: array is not
169     null";
170     assert order != null : "Violation of: order is not
171     null";
172     assert 0 <= top : "Violation of: 0 <= top";
173     assert last < array.length : "Violation of: last < |
174     array|";
175     for (int i = 0; i < array.length; i++) {
176     assert array[i] != null : ""

```

```
171             + "Violation of: all entries in array are
    not null";
172         }
173         assert isHeap(array, 2 * top + 1, last, order) : ""
174             + "Violation of: SUBTREE_IS_HEAP(array, 2 * top
    + 1, last,"
175             + " [relation computed by order.compare
    method])";
176         assert isHeap(array, 2 * top + 2, last, order) : ""
177             + "Violation of: SUBTREE_IS_HEAP(array, 2 * top
    + 2, last,"
178             + " [relation computed by order.compare
    method])";
179         /*
180         * Impractical to check last requires clause; no need
    to check the other
181         * requires clause, because it must be true when using
    the array
182         * representation for a complete binary tree.
183         */
184
185         int left = 2 * top + 1;
186         int right = 2 * top + 2;
187         if (left <= last) {
188             if (right <= last) {
189                 int smallest = left;
190                 if (order.compare(array[left], array[right]) >
    0) {
191                     smallest = right;
192                 }
193
194                 if (order.compare(array[top], array[smallest])
    > 0
195                     && smallest == left) {
196                     exchangeEntries(array, top, left);
197                     siftDown(array, left, last, order);
198                 } else if (order.compare(array[top],
    array[smallest]) > 0
199                     && smallest == right) {
```

```
200         exchangeEntries(array, top, smallest);
201         siftDown(array, right, last, order);
202     }
203     } else {
204         if (order.compare(array[top], array[left]) > 0)
205     {
206         exchangeEntries(array, top, (2 * top + 1));
207     }
208     }
209 }
210 }
211
212 /**
213  * Heapifies the subtree of the given array rooted at the
214  * given {@code top}.
215  *
216  * @param <T>
217  *         type of array entries
218  * @param array
219  *         the complete binary tree
220  * @param top
221  *         the index of the root of the "subtree" to
222  *         heapify
223  * @param order
224  *         the total preorder for sorting
225  * @updates array
226  * @requires <pre>
227  *         0 <= top and
228  *         for all i: integer
229  *             where (0 <= i and i < |array|)
230  *             ([entry at position i in array is not null]) and
231  *             [subtree rooted at {@code top} is a complete binary
232  *             tree] and
233  *         IS_TOTAL_PREORDER([relation computed by order.compare
234  *         method])
235  * </pre>
236  * @ensures <pre>
237  *         SUBTREE_IS_HEAP(array, top, |array| - 1,
```



```
234     *      [relation computed by order.compare method]) and
235     * perms(array, #array)
236     * </pre>
237     */
238     private static <T> void heapify(T[] array, int top,
Comparator<T> order) {
239         assert array != null : "Violation of: array is not
null";
240         assert order != null : "Violation of: order is not
null";
241         assert 0 <= top : "Violation of: 0 <= top";
242         for (int i = 0; i < array.length; i++) {
243             assert array[i] != null : ""
244                 + "Violation of: all entries in array are
not null";
245         }
246         /*
247         * Impractical to check last requires clause; no need
to check the other
248         * requires clause, because it must be true when using
the array
249         * representation for a complete binary tree.
250         */
251
252         int left = 2 * top + 1;
253         int right = 2 * top + 2;
254
255         if (left < array.length) {
256             heapify(array, left, order);
257             heapify(array, right, order);
258             siftDown(array, top, array.length - 1, order);
259         }
260     }
261 }
262
263 /**
264     * Constructs and returns an array representing a heap with
the entries from
265     * the given {@code Queue}.
```

```
266      *
267      * @param <T>
268      *           type of {@code Queue} and array entries
269      * @param q
270      *           the {@code Queue} with the entries for the
    heap
271      * @param order
272      *           the total preorder for sorting
273      * @return the array representation of a heap
274      * @clears q
275      * @requires IS_TOTAL_PREORDER([relation computed by
    order.compare method])
276      * @ensures <pre>
277      * SUBTREE_IS_HEAP(buildHeap, 0, |buildHeap| - 1) and
278      * perms(buildHeap, #q) and
279      * for all i: integer
280      *   where (0 <= i and i < |buildHeap|)
281      *   ([entry at position i in buildHeap is not null]) and
282      * </pre>
283      */
284      @SuppressWarnings("unchecked")
285      private static <T> T[] buildHeap(Queue<T> q, Comparator<T>
    order) {
286          assert q != null : "Violation of: q is not null";
287          assert order != null : "Violation of: order is not
    null";
288          /*
289           * Impractical to check the requires clause.
290           */
291          /*
292           * With "new T[...]" in place of "new Object[...]" it
    does not compile;
293           * as shown, it results in a warning about an unchecked
    cast, though it
294           * cannot fail.
295           */
296          T[] heap = (T[]) (new Object[q.length()]);
297
298          // Copy elements from the queue to the heap array
```

```
299     int index = 0;
300     while (q.length() > 0) {
301         T element = q.dequeue();
302         heap[index] = element;
303         index++;
304     }
305
306     // Build the heap by ensuring the heap property
307     for (int i = (heap.length - 1) / 2; i >= 0; i--) {
308         heapify(heap, i, order);
309     }
310
311     return heap;
312 }
313
314 /**
315  * Checks if the subtree of the given {@code array} rooted
  at the given
316  * {@code top} is a heap.
317  *
318  * @param <T>
319  *         type of array entries
320  * @param array
321  *         the complete binary tree
322  * @param top
323  *         the index of the root of the "subtree"
324  * @param last
325  *         the index of the last entry in the heap
326  * @param order
327  *         total preorder for sorting
328  * @return true if the subtree of the given {@code array}
  rooted at the
329  *         given {@code top} is a heap; false otherwise
330  * @requires <pre>
331  * 0 <= top and last < |array| and
332  * for all i: integer
333  *     where (0 <= i and i < |array|)
334  *     ([entry at position i in array is not null]) and
335  * [subtree rooted at {@code top} is a complete binary
```

```
tree]
336     * </pre>
337     * @ensures <pre>
338     * isHeap = SUBTREE_IS_HEAP(array, top, last,
339     *     [relation computed by order.compare method])
340     * </pre>
341     */
342     private static <T> boolean isHeap(T[] array, int top, int
last,
343         Comparator<T> order) {
344         assert array != null : "Violation of: array is not
null";
345         assert 0 <= top : "Violation of: 0 <= top";
346         assert last < array.length : "Violation of: last < |
array|";
347         for (int i = 0; i < array.length; i++) {
348             assert array[i] != null : ""
349                 + "Violation of: all entries in array are
not null";
350         }
351         /*
352         * No need to check the other requires clause, because
it must be true
353         * when using the Array representation for a complete
binary tree.
354         */
355         int left = 2 * top + 1;
356         boolean isHeap = true;
357         if (left <= last) {
358             isHeap = (order.compare(array[top], array[left]) <=
0)
359                 && isHeap(array, left, last, order);
360             int right = left + 1;
361             if (isHeap && (right <= last)) {
362                 isHeap = (order.compare(array[top],
array[right]) <= 0)
363                     && isHeap(array, right, last, order);
364             }
365         }
```

```
366         return isHeap;
367     }
368
369     /**
370      * Checks that the part of the convention repeated below
371      holds for the
372      * current representation.
373      * @return true if the convention holds (or if assertion
374      checking is off);
375      * otherwise reports a violated assertion
376      * @convention <pre>
377      * if $this.insertionMode then
378      *   $this.heapSize = 0
379      * else
380      *   $this.entries = <> and
381      *   for all i: integer
382      *     where (0 <= i and i < |$this.heap|)
383      *       ([entry at position i in $this.heap is not null])
384      and
385      *   SUBTREE_IS_HEAP($this.heap, 0, $this.heapSize - 1,
386      *     [relation computed by $this.machineOrder.compare
387      method]) and
388      *   0 <= $this.heapSize <= |$this.heap|
389      * </pre>
390      */
391     private boolean conventionHolds() {
392         if (this.insertionMode) {
393             assert this.heapSize == 0 : ""
394                 + "Violation of: if $this.insertionMode
395 then $this.heapSize = 0";
396         } else {
397             assert this.entries.length() == 0 : ""
398                 + "Violation of: if not $this.insertionMode
399 then $this.entries = <>";
400             assert 0 <= this.heapSize : ""
401                 + "Violation of: if not $this.insertionMode
402 then 0 <= $this.heapSize";
403             assert this.heapSize <= this.heap.length : ""
```

```
398             + "Violation of: if not $this.insertionMode
then"
399             + " $this.heapSize <= |$this.heap|";
400         for (int i = 0; i < this.heap.length; i++) {
401             assert this.heap[i] != null : ""
402             + "Violation of: if not
$this.insertionMode then"
403             + " all entries in $this.heap are not
null";
404         }
405         assert isHeap(this.heap, 0, this.heapSize - 1,
406             this.machineOrder) : ""
407             + "Violation of: if not
$this.insertionMode then"
408             + " SUBTREE_IS_HEAP($this.heap, 0,
$this.heapSize - 1,"
409             + " [relation computed by
$this.machineOrder.compare"
410             + " method])";
411     }
412     return true;
413 }
414
415 /**
416  * Creator of initial representation.
417  *
418  * @param order
419  *         total preorder for sorting
420  * @requires IS_TOTAL_PREORDER([relation computed by
order.compare method]
421  * @ensures <pre>
422  * $this.insertionMode = true and
423  * $this.machineOrder = order and
424  * $this.entries = <> and
425  * $this.heapSize = 0
426  * </pre>
427  */
428 private void createNewRep(Comparator<T> order) {
429
```

```
430         // Set up insertion mode according to contract
431         this.insertionMode = true;
432         // Set up comparator
433         this.machineOrder = order;
434         // Create representation variable
435         this.entries = new Queue1L<T>();
436         // Set the number of elements in a queue
437         this.heapSize = 0;
438         // Build heap
439         this.heap = buildHeap(this.entries, order);
440
441     }
442
443     /*
444     * Constructors
445     */
446
447     /**
448     * Constructor from order.
449     *
450     * @param order
451     *         total preorder for sorting
452     */
453     public SortingMachine5a(Comparator<T> order) {
454         this.createNewRep(order);
455         assert this.conventionHolds();
456     }
457
458     /*
459     * Standard methods
460     */
461
462     @SuppressWarnings("unchecked")
463     @Override
464     public final SortingMachine<T> newInstance() {
465         try {
466             return
```

```
        this.getClass().getConstructor(Comparator.class)
467            .newInstance(this.machineOrder);
468    } catch (ReflectiveOperationException e) {
469        throw new AssertionError(
470            "Cannot construct object of type " +
        this.getClass());
471    }
472 }
473
474 @Override
475 public final void clear() {
476     this.createNewRep(this.machineOrder);
477     assert this.conventionHolds();
478 }
479
480 @Override
481 public final void transferFrom(SortingMachine<T> source) {
482     assert source != null : "Violation of: source is not
    null";
483     assert source != this : "Violation of: source is not
    this";
484     assert source instanceof SortingMachine5a<?> : ""
485         + "Violation of: source is of dynamic type
    SortingMachine5a<?>";
486     /*
487      * This cast cannot fail since the assert above would
    have stopped
488      * execution in that case: source must be of dynamic
    type
489      * SortingMachine5a<?>, and the ? must be T or the call
    would not have
490      * compiled.
491      */
492     SortingMachine5a<T> localSource = (SortingMachine5a<T>)
    source;
493     this.insertionMode = localSource.insertionMode;
494     this.machineOrder = localSource.machineOrder;
495     this.entries = localSource.entries;
496     this.heap = localSource.heap;
```



```
497         this.heapSize = localSource.heapSize;
498         localSource.createNewRep(localSource.machineOrder);
499         assert this.conventionHolds();
500         assert localSource.conventionHolds();
501     }
502
503     /*
504     * Kernel methods
505     */
506
507     @Override
508     public final void add(T x) {
509         assert x != null : "Violation of: x is not null";
510         assert this.isInInsertionMode() : "Violation of:
this.insertion_mode";
511
512         this.entries.enqueue(x);
513
514         assert this.conventionHolds();
515     }
516
517     @Override
518     public final void changeToExtractionMode() {
519         assert this.isInInsertionMode() : "Violation of:
this.insertion_mode";
520
521         this.insertionMode = false;
522
523         this.heap = buildHeap(this.entries, this.machineOrder);
524         this.heapSize = this.heap.length;
525
526         assert this.conventionHolds();
527     }
528
529     @Override
530     public final T removeFirst() {
531         assert !this
532             .isInInsertionMode() : "Violation of: not
```

```
        this.insertion_mode";
533         assert this.size() > 0 : "Violation of: this.contents /
    = {}";
534
535         T x = this.heap[0];
536         // switch root with last entry in heap
537         exchangeEntries(this.heap, 0, this.heapSize - 1);
538         this.heapSize--;
539         siftDown(this.heap, 0, this.heapSize - 1,
    this.machineOrder);
540
541         assert this.conventionHolds();
542         // Fix this line to return the result after checking
    the convention.
543
544         return x;
545
546     }
547
548     @Override
549     public final boolean isInInsertionMode() {
550         assert this.conventionHolds();
551         return this.insertionMode;
552     }
553
554     @Override
555     public final Comparator<T> order() {
556         assert this.conventionHolds();
557         return this.machineOrder;
558     }
559
560     @Override
561     public final int size() {
562
563         assert this.conventionHolds();
564
565         int result = this.heapSize;
566         if (this.insertionMode) {
567             result = this.entries.length();
```

```
568     }
569
570     return result;
571
572 }
573
574 @Override
575 public final Iterator<T> iterator() {
576     return new SortingMachine5aIterator();
577 }
578
579 /**
580  * Implementation of {@code Iterator} interface for
581  * {@code SortingMachine5a}.
582  */
583 private final class SortingMachine5aIterator implements
584     Iterator<T> {
585     /**
586      * Representation iterator when in insertion mode.
587      */
588     private Iterator<T> queueIterator;
589
590     /**
591      * Representation iterator count when in extraction
592      mode.
593      */
594     private int arrayCurrentIndex;
595
596     /**
597      * No-argument constructor.
598      */
599     private SortingMachine5aIterator() {
600         if (SortingMachine5a.this.insertionMode) {
601             this.queueIterator =
602                 SortingMachine5a.this.entries.iterator();
603         } else {
604             this.arrayCurrentIndex = 0;
605         }
606     }
607 }
```

```
604         assert SortingMachine5a.this.conventionHolds();
605     }
606
607     @Override
608     public boolean hasNext() {
609         boolean hasNext;
610         if (SortingMachine5a.this.insertionMode) {
611             hasNext = this.queueIterator.hasNext();
612         } else {
613             hasNext = this.arrayCurrentIndex <
SortingMachine5a.this.heapSize;
614         }
615         assert SortingMachine5a.this.conventionHolds();
616         return hasNext;
617     }
618
619     @Override
620     public T next() {
621         assert this.hasNext() : "Violation of:
~this.unseen != <>";
622         if (!this.hasNext()) {
623             /*
624              * Exception is supposed to be thrown in this
        case, but with
625              * assertion-checking enabled it cannot happen
        because of assert
626              * above.
627              */
628             throw new NoSuchElementException();
629         }
630         T next;
631         if (SortingMachine5a.this.insertionMode) {
632             next = this.queueIterator.next();
633         } else {
634             next =
SortingMachine5a.this.heap[this.arrayCurrentIndex];
635             this.arrayCurrentIndex++;
636         }
637         assert SortingMachine5a.this.conventionHolds();
```

```
638         return next;
639     }
640
641     @Override
642     public void remove() {
643         throw new UnsupportedOperationException(
644             "remove operation not supported");
645     }
646
647 }
648
649 }
650
```