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## PROJECT 4: SET ON BINARY SEARCH TREES

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```
1 import java.util.Iterator;
 2
 3 import components.binarytree.BinaryTree;
 4import components.binarytree.BinaryTree1;
 5 import components.set.Set;
 6 import components.set.SetSecondary;
 7
 8 / * *
9 * {@code Set} represented as a {@code BinaryTree} (maintained as a binary
10 * search tree) of elements with implementations of primary methods.
11 *
12 * @param <T>
13 *
                type of {@code Set} elements
14 * @mathdefinitions 
15 * IS BST(
16 * tree: binary tree of T
17 * ): boolean satisfies
18 * [tree satisfies the binary search tree properties as described in the
19 *
      slides with the ordering reported by compareTo for T, including that
20 *
       it has no duplicate labels]
21 * 
22 * @convention IS_BST($this.tree)
23 * @correspondence this = labels($this.tree)
24 *
25 * @author Daniil Gofman, Ansh Pachauri
26 *
27 */
28 public class Set3a<T extends Comparable<T>> extends SetSecondary<T> {
29
30
31
      * Private members
32
      */
33
34
35
       * Elements included in {@code this}.
36
37
      private BinaryTree<T> tree;
38
      /**
39
40
       * Returns whether {@code x} is in {@code t}.
41
42
       * @param <T>
43
                    type of {@code BinaryTree} labels
       * @param t
44
45
                    the {@code BinaryTree} to be searched
       * @param x
46
47
                    the label to be searched for
48
       * @return true if t contains x, false otherwise
49
       * @requires IS BST(t)
```

```
* @ensures isInTree = (x is in labels(t))
50
51
      private static <T extends Comparable<T>> boolean isInTree(BinaryTree<T>
52
  t,
53
               T x) {
          assert t != null : "Violation of: t is not null";
54
55
          assert x != null : "Violation of: x is not null";
56
           // initialize variables
57
          boolean result = false;
58
          // check if tree is empty
59
           if (t.size() > 0) {
               BinaryTree<T> left = t.newInstance();
60
61
               BinaryTree<T> right = t.newInstance();
62
               T root = t.disassemble(left, right);
63
               // compare x with the root and check for x in the
64
               // appropriate node
65
               if (root.equals(x)) {
66
                   result = true;
67
               } else if (root.compareTo(x) < 0) {</pre>
68
                   result = isInTree(right, x);
69
               } else {
70
                   result = isInTree(left, x);
71
               }
72
               // reassemble tree
73
               t.assemble(root, left, right);
74
75
          // return if x is in the tree
76
          return result;
77
      }
78
79
      /**
80
       * Inserts {@code x} in {@code t}.
81
82
       * @param <T>
83
                     type of {@code BinaryTree} labels
84
         @param t
85
                     the {@code BinaryTree} to be searched
       * @param x
86
87
                     the label to be inserted
88
       * @aliases reference {@code x}
89
       * @updates t
90
       * @requires IS BST(t) and x is not in labels(t)
91
       * @ensures IS BST(t) and labels(t) = labels(#t) union {x}
92
93
      private static <T extends Comparable<T>> void insertInTree
  (BinaryTree<T> t,
94
               T x) {
95
          assert t != null : "Violation of: t is not null";
          assert x != null : "Violation of: x is not null";
96
97
          // Initialize variables
```

```
98
           BinaryTree<T> left = t.newInstance();
           BinaryTree<T> right = t.newInstance();
99
100
           // Check if the tree is empty
101
           if (t.size() > 0) {
102
               T root = t.disassemble(left, right);
103
               // Check if the root is greater than,
104
               // Or less than x and add to the appropriate node.
105
               if (root.compareTo(x) > 0) {
106
                   insertInTree(left, x);
107
               } else {
108
                   insertInTree(right, x);
109
               }
110
               // Reassemble the tree
111
               t.assemble(root, left, right);
112
               // If the tree is empty
113
           } else {
114
               // Reassemble the tree with x as the root
115
               t.assemble(x, left, right);
116
           }
117
118
       }
119
120
       /**
121
        * Removes and returns the smallest (left-most) label in {@code t}.
122
123
        * @param <T>
124
                     type of {@code BinaryTree} labels
125
          @param t
126
                     the {@code BinaryTree} from which to remove the label
        * @return the smallest label in the given {@code BinaryTree}
127
128
        * @updates t
129
        * @requires IS BST(t) and |t| > 0
130
        * @ensures 
        * IS BST(t) and removeSmallest = [the smallest label in #t]
131
132
        * labels(t) = labels(#t) \ {removeSmallest}
133
        * 
        */
134
135
       private static <T> T removeSmallest(BinaryTree<T> t) {
136
           assert t != null : "Violation of: t is not null";
137
           assert t.size() > 0 : "Violation of: |t| > 0";
138
139
           // Initialize variables to store left and right children
140
           BinaryTree<T> left = t.newInstance();
           BinaryTree<T> right = t.newInstance();
141
142
           // Get root of the tree
143
           T root = t.disassemble(left, right);
144
           T smallest = root;
           if (left.size() > 0) {
145
               smallest = removeSmallest(left);
146
147
               t.assemble(root, left, right);
```

```
Set3a.java
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148
           } else {
149
               t.transferFrom(right);
150
151
           // Return the smallest element
152
           return smallest;
153
       }
154
       /**
155
        * Finds label {@code x} in {@code t}, removes it from {@code t}, and
156
157
        * returns it.
158
        * @param <T>
159
160
                     type of {@code BinaryTree} labels
161
        * @param t
162
                     the {@code BinaryTree} from which to remove label {@code
   x}
        * @param x
163
164
                     the label to be removed
165
        * @return the removed label
166
        * @updates t
        * @requires IS BST(t) and x is in labels(t)
167
168
        * @ensures 
169
        * IS BST(t) and removeFromTree = x and
        * labels(t) = labels(#t) \ {x}
170
171
        * 
        */
172
173
       private static <T extends Comparable<T>> T removeFromTree(BinaryTree<T>
   t,
174
               T x) {
           assert t != null : "Violation of: t is not null";
175
           assert x != null : "Violation of: x is not null";
176
177
           assert t.size() > 0 : "Violation of: x is in labels(t)";
178
179
           // Create new binary trees for the left and right subtrees.
180
           BinaryTree<T> right = t.newInstance();
181
           BinaryTree<T> left = t.newInstance();
182
183
           // Disassemble the original tree 't' and get the root element.
184
           T root = t.disassemble(left, right);
185
           // Create a variable to store the element that will be removed.
186
187
           T remove = root;
188
189
           // Check if the root element is equal to the element 'x'.
           if (root.equals(x)) {
190
191
               // If 'x' is found at the root, handle the removal case.
192
               // If the right subtree is not empty, find the smallest element
               // in the right subtree and set it as the new root.
193
194
               if (right.size() > 0) {
195
                   root = removeSmallest(right);
```

```
Set3a.java
                                              Friday, September 29, 2023, 7:06 PM
196
                    t.assemble(root, left, right);
197
                } else {
198
                    // If the right subtree is empty, transfer the left subtree
   to 't'.
199
                    t.transferFrom(left);
200
                }
201
           } else {
202
                // If 'x' is not equal to the root element, recursively search
   for 'x'
203
                // in either the left or right subtree based on the comparison.
204
205
                if (root.compareTo(x) < 0) {</pre>
206
                    // If 'x' is greater than the root element, search in the
   right subtree.
207
                    remove = removeFromTree(right, x);
                } else {
208
209
                    // If 'x' is less than the root element, search in the left
   subtree.
210
                    remove = removeFromTree(left, x);
211
                }
212
213
                // Assemble the tree after the recursive call.
214
                t.assemble(root, left, right);
215
           }
216
217
           // Return the element that was removed.
218
           return remove;
219
       }
220
221
222
        * Creator of initial representation.
223
        */
224
       private void createNewRep() {
225
226
           // Create new representation
227
           this.tree = new BinaryTree1<T>();
228
       }
229
230
231
        * Constructors
232
        */
233
       /**
234
        * No-argument constructor.
235
236
        */
237
       public Set3a() {
238
239
           // Default constructor
240
           this.createNewRep();
```

```
Set3a.java
                                             Friday, September 29, 2023, 7:06 PM
241
       }
242
243
244
        * Standard methods
245
246
247
       @SuppressWarnings("unchecked")
248
       @Override
249
       public final Set<T> newInstance() {
250
           try {
               return this.getClass().getConstructor().newInstance();
251
252
           } catch (ReflectiveOperationException e) {
253
               throw new AssertionError(
254
                        "Cannot construct object of type " + this.getClass());
255
           }
256
       }
257
258
       @Override
259
       public final void clear() {
260
           this.createNewRep();
261
       }
262
263
       @Override
264
       public final void transferFrom(Set<T> source) {
           assert source != null : "Violation of: source is not null";
265
           assert source != this : "Violation of: source is not this";
266
           assert source instanceof Set3a<?> : ""
267
                   + "Violation of: source is of dynamic type Set3<?>";
268
269
270
            * This cast cannot fail since the assert above would have stopped
271
            * execution in that case: source must be of dynamic type Set3a<?>,
   and
272
            * the ? must be T or the call would not have compiled.
273
            */
274
           Set3a<T> localSource = (Set3a<T>) source;
275
           this.tree = localSource.tree;
276
           localSource.createNewRep();
277
       }
278
279
280
        * Kernel methods
281
       */
282
283
       @Override
284
       public final void add(T x) {
           assert x != null : "Violation of: x is not null";
285
           assert !this.contains(x) : "Violation of: x is not in this";
286
287
```

```
Set3a.java
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288
           // Inserts element x into a BST
289
           insertInTree(this.tree, x);
290
       }
291
292
       @Override
       public final T remove(T x) {
293
294
           assert x != null : "Violation of: x is not null";
295
           assert this.contains(x) : "Violation of: x is in this";
296
297
           // Remove and return element from the tree
298
           return removeFromTree(this.tree, x);
299
       }
300
301
       @Override
302
       public final T removeAny() {
           assert this.size() > 0 : "Violation of: this /= empty_set";
303
           // Removes the smallest term from the tree
304
           return removeSmallest(this.tree);
305
306
       }
307
308
       @Override
       public final boolean contains(T x) {
309
310
           assert x != null : "Violation of: x is not null";
           // checks if x is in the tree
311
           return isInTree(this.tree, x);
312
313
       }
314
315
       @Override
316
       public final int size() {
317
           // return the size of the tree
318
           return this.tree.size();
319
       }
320
       @Override
321
322
       public final Iterator<T> iterator() {
323
           return this.tree.iterator();
324
       }
325
326 }
327
```