

Unit - 1

INTRODUCTION

Ever since computers were invented, we have wondered whether they might be made to learn. If we could understand how to program them to learn-to improve automatically with experience-the impact would be dramatic.

- Imagine computers learning from medical records which treatments are most effective for new diseases
- Houses learning from experience to optimize energy costs based on the particular usage patterns of their occupants.
- Personal software assistants learning the evolving interests of their users in order to highlight especially relevant stories from the online morning newspaper

A successful understanding of how to make computers learn would open up many new uses of computers and new levels of competence and customization

Some successful applications of machine learning

- Learning to recognize spoken words
- Learning to drive an autonomous vehicle
- Learning to classify new astronomical structures
- Learning to play world-class backgammon

Why is Machine Learning Important?

- Some tasks cannot be defined well, except by examples (e.g., recognizing people).
- Relationships and correlations can be hidden within large amounts of data. Machine Learning/Data Mining may be able to find these relationships.
- Human designers often produce machines that do not work as well as desired in the environments in which they are used.
- The amount of knowledge available about certain tasks might be too large for explicit encoding by humans (e.g., medical diagnostic).
- Environments change over time.
- New knowledge about tasks is constantly being discovered by humans. It may be difficult to continuously re-design systems “by hand”.

WELL-POSED LEARNING PROBLEMS

Definition: A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E.

To have a well-defined learning problem, three features need to be identified:

1. The class of tasks
2. The measure of performance to be improved
3. The source of experience

Examples

1. **Checkers game:** A computer program that learns to play *checkers* might improve its performance as measured by its ability to win at the class of tasks involving playing checkers games, through experience obtained by playing games against itself.

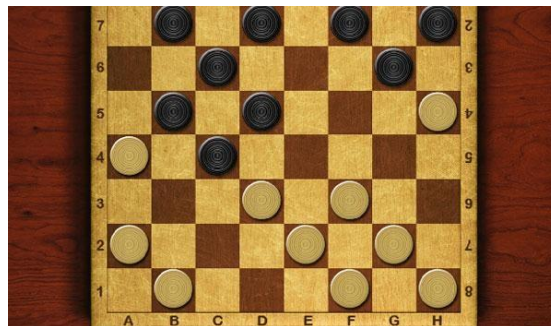


Fig: Checker game board

A checkers learning problem:

- Task T: playing checkers
- Performance measure P: percent of games won against opponents
- Training experience E: playing practice games against itself

2. A handwriting recognition learning problem:

- Task T: recognizing and classifying handwritten words within images
- Performance measure P: percent of words correctly classified
- Training experience E: a database of handwritten words with given classifications

3. A robot driving learning problem:

- Task T: driving on public four-lane highways using vision sensors
- Performance measure P: average distance travelled before an error (as judged by human overseer)
- Training experience E: a sequence of images and steering commands recorded while observing a human driver

DESIGNING A LEARNING SYSTEM

The basic design issues and approaches to machine learning are illustrated by designing a program to learn to play checkers, with the goal of entering it in the world checkers tournament

1. Choosing the Training Experience
2. Choosing the Target Function
3. Choosing a Representation for the Target Function
4. Choosing a Function Approximation Algorithm
 1. Estimating training values
 2. Adjusting the weights
5. The Final Design

1. Choosing the Training Experience

- The first design choice is to choose the type of training experience from which the system will learn.
- The type of training experience available can have a significant impact on success or failure of the learner.

There are three attributes which impact on success or failure of the learner

1. Whether the training experience provides *direct or indirect feedback* regarding the choices made by the performance system.

For example, in checkers game:

In learning to play checkers, the system might learn from *direct training examples* consisting of *individual checkers board states* and *the correct move for each*.

Indirect training examples consisting of the *move sequences* and *final outcomes* of various games played. The information about the correctness of specific moves early in the game must be inferred indirectly from the fact that the game was eventually won or lost.

Here the learner faces an additional problem of *credit assignment*, or determining the degree to which each move in the sequence deserves credit or blame for the final outcome. Credit assignment can be a particularly difficult problem because the game can be lost even when early moves are optimal, if these are followed later by poor moves.

Hence, learning from direct training feedback is typically easier than learning from indirect feedback.

2. The degree to which the *learner controls the sequence of training examples*

For example, in checkers game:

The learner might depend on the *teacher* to select informative board states and to provide the correct move for each.

Alternatively, the learner might itself propose board states that it finds particularly confusing and ask the teacher for the correct move.

The learner may have complete control over both the board states and (indirect) training classifications, as it does when it learns by playing against itself with *no teacher present*.

3. How well it represents the *distribution of examples* over which the final system performance P must be measured

For example, in checkers game:

In checkers learning scenario, the performance metric P is the percent of games the system wins in the world tournament.

If its training experience E consists only of games played against itself, there is a danger that this training experience might not be fully representative of the distribution of situations over which it will later be tested.

It is necessary to learn from a distribution of examples that is different from those on which the final system will be evaluated.

2. Choosing the Target Function

The next design choice is to determine exactly what type of knowledge will be learned and how this will be used by the performance program.

Let's consider a checkers-playing program that can generate the legal moves from any board state.

The program needs only to learn how to choose the best move from among these legal moves. We must learn to choose among the legal moves, the most obvious choice for the type of information to be learned is a program, or function, that chooses the best move for any given board state.

1. Let *ChooseMove* be the target function and the notation is

$$\text{ChooseMove} : B \rightarrow M$$

which indicate that this function accepts as input any board from the set of legal board states B and produces as output some move from the set of legal moves M.

ChooseMove is a choice for the target function in checkers example, but this function will turn out to be very difficult to learn given the kind of indirect training experience available to our system

2. An alternative target function is an *evaluation function* that assigns a *numerical score* to any given board state

Let the target function V and the notation

$$V : B \rightarrow R$$

which denote that V maps any legal board state from the set B to some real value.

Intend for this target function V to assign higher scores to better board states. If the system can successfully learn such a target function V , then it can easily use it to select the best move from any current board position.

Let us define the target value $V(b)$ for an arbitrary board state b in B , as follows:

- If b is a final board state that is won, then $V(b) = 100$
- If b is a final board state that is lost, then $V(b) = -100$
- If b is a final board state that is drawn, then $V(b) = 0$
- If b is not a final state in the game, then $V(b) = V(b')$,

Where b' is the best final board state that can be achieved starting from b and playing optimally until the end of the game

3. Choosing a Representation for the Target Function

Let's choose a simple representation - for any given board state, the function c will be calculated as a linear combination of the following board features:

- x_1 : the number of black pieces on the board
- x_2 : the number of red pieces on the board
- x_3 : the number of black kings on the board
- x_4 : the number of red kings on the board
- x_5 : the number of black pieces threatened by red (i.e., which can be captured on red's next turn)
- x_6 : the number of red pieces threatened by black

Thus, learning program will represent as a linear function of the form

$$\hat{V}(b) = w_0 + w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4 + w_5x_5 + w_6x_6$$

Where,

- w_0 through w_6 are numerical coefficients, or weights, to be chosen by the learning algorithm.
- Learned values for the weights w_1 through w_6 will determine the relative importance of the various board features in determining the value of the board
- The weight w_0 will provide an additive constant to the board value

4. Choosing a Function Approximation Algorithm

In order to learn the target function f we require a set of training examples, each describing a specific board state b and the training value $V_{\text{train}}(b)$ for b .

Each training example is an ordered pair of the form $(b, V_{\text{train}}(b))$.

For instance, the following training example describes a board state b in which black has won the game (note $x_2 = 0$ indicates that red has no remaining pieces) and for which the target function value $V_{\text{train}}(b)$ is therefore $+100$.

$$((x_1=3, x_2=0, x_3=1, x_4=0, x_5=0, x_6=0), +100)$$

Function Approximation Procedure

1. Derive training examples from the indirect training experience available to the learner
2. Adjusts the weights w_i to best fit these training examples

1. Estimating training values

A simple approach for estimating training values for intermediate board states is to assign the training value of $V_{\text{train}}(b)$ for any intermediate board state b to be $V(\text{Successor}(b))$

Where ,

- V is the learner's current approximation to V
- $\text{Successor}(b)$ denotes the next board state following b for which it is again the program's turn to move

Rule for estimating training values

$$V_{\text{train}}(b) \leftarrow V(\text{Successor}(b))$$

2. Adjusting the weights

Specify the learning algorithm for choosing the weights w_i to best fit the set of training examples $\{(b, V_{\text{train}}(b))\}$

A first step is to define what we mean by the bestfit to the training data.

One common approach is to define the best hypothesis, or set of weights, as that which minimizes the squared error E between the training values and the values predicted by the hypothesis.

$$E \equiv \sum_{\langle b, V_{\text{train}}(b) \rangle \in \text{training examples}} (V_{\text{train}}(b) - \hat{V}(b))^2$$

Several algorithms are known for finding weights of a linear function that minimize E . One such algorithm is called the *least mean squares, or LMS training rule*. For each observed training example it adjusts the weights a small amount in the direction that reduces the error on this training example

LMS weight update rule :- For each training example $(b, V_{\text{train}}(b))$

Use the current weights to calculate $V(b)$

For each weight w_i , update it as

$$w_i \leftarrow w_i + \eta (V_{\text{train}}(b) - V(b)) x_i$$

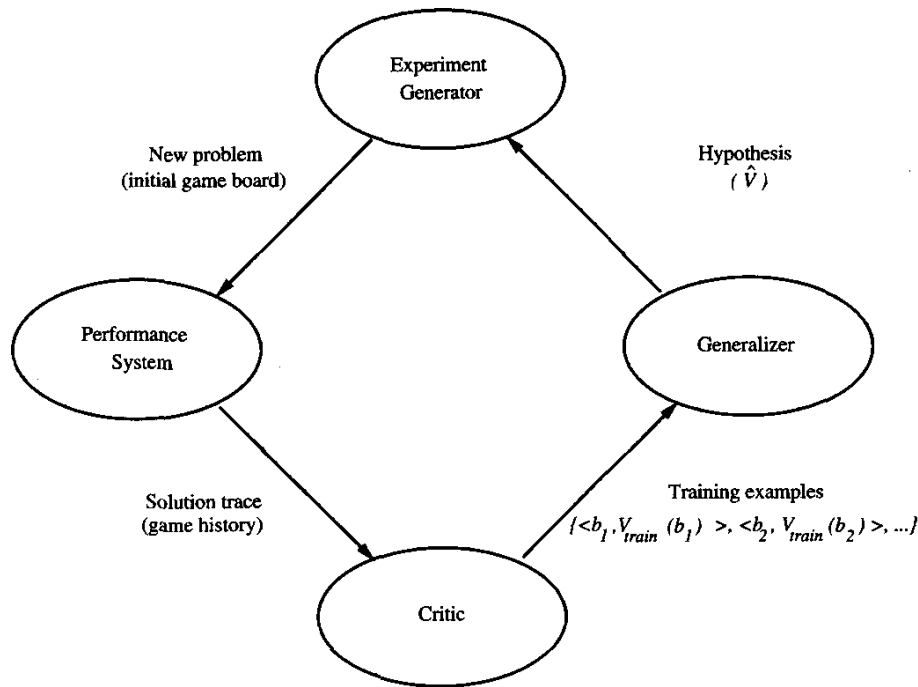
Here η is a small constant (e.g., 0.1) that moderates the size of the weight update.

Working of weight update rule

- When the error $(V_{\text{train}}(b) - V(b))$ is zero, no weights are changed.
- When $(V_{\text{train}}(b) - V(b))$ is positive (i.e., when $V(b)$ is too low), then each weight is increased in proportion to the value of its corresponding feature. This will raise the value of $V(b)$, reducing the error.
- If the value of some feature x_i is zero, then its weight is not altered regardless of the error, so that the only weights updated are those whose features actually occur on the training example board.

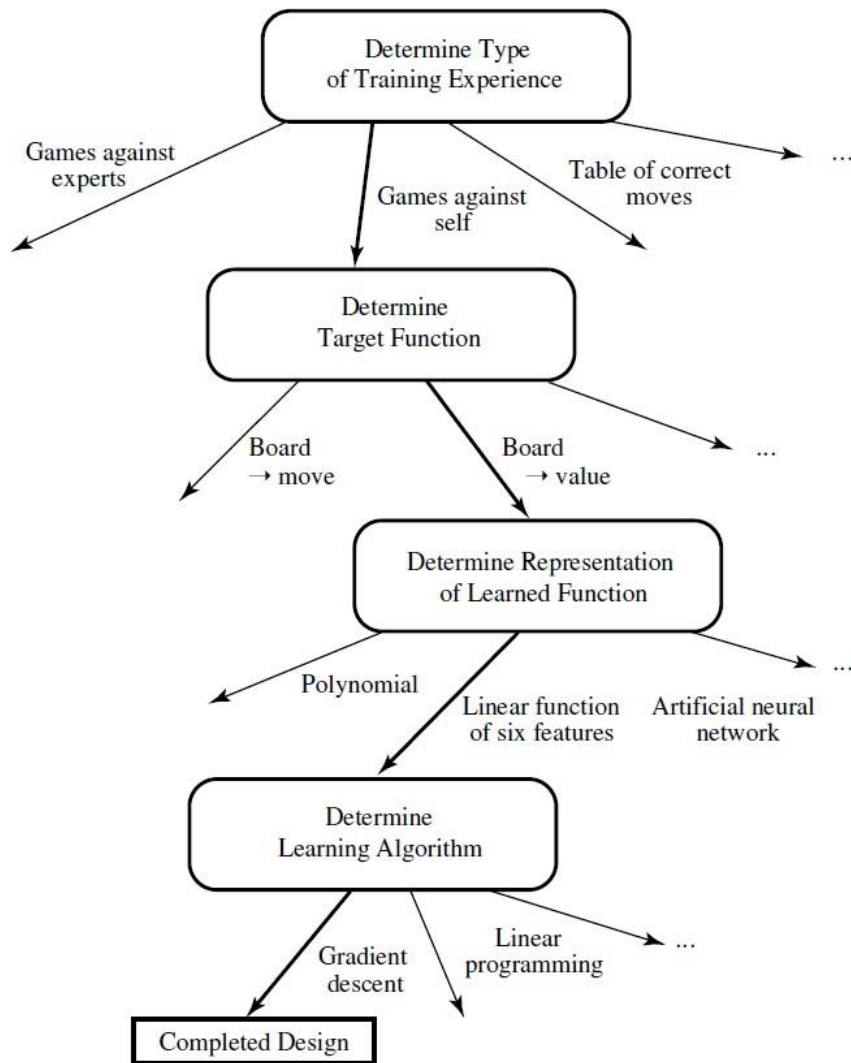
5. The Final Design

The final design of checkers learning system can be described by four distinct program modules that represent the central components in many learning systems



1. **The Performance System** is the module that must solve the given performance task by using the learned target function(s). It takes an instance of a new problem (new game) as input and produces a trace of its solution (game history) as output.
2. **The Critic** takes as input the history or trace of the game and produces as output a set of training examples of the target function
3. **The Generalizer** takes as input the training examples and produces an output hypothesis that is its estimate of the target function. It generalizes from the specific training examples, hypothesizing a general function that covers these examples and other cases beyond the training examples.
4. **The Experiment Generator** takes as input the current hypothesis and outputs a new problem (i.e., initial board state) for the Performance System to explore. Its role is to pick new practice problems that will maximize the learning rate of the overall system.

The sequence of design choices made for the checkers program is summarized in below figure



PERSPECTIVES AND ISSUES IN MACHINE LEARNING

Issues in Machine Learning

The field of machine learning, and much of this book, is concerned with answering questions such as the following

- What algorithms exist for learning general target functions from specific training examples? In what settings will particular algorithms converge to the desired function, given sufficient training data? Which algorithms perform best for which types of problems and representations?
- How much training data is sufficient? What general bounds can be found to relate the confidence in learned hypotheses to the amount of training experience and the character of the learner's hypothesis space?

- When and how can prior knowledge held by the learner guide the process of generalizing from examples? Can prior knowledge be helpful even when it is only approximately correct?
- What is the best strategy for choosing a useful next training experience, and how does the choice of this strategy alter the complexity of the learning problem?
- What is the best way to reduce the learning task to one or more function approximation problems? Put another way, what specific functions should the system attempt to learn? Can this process itself be automated?
- How can the learner automatically alter its representation to improve its ability to represent and learn the target function?

CONCEPT LEARNING

- Learning involves acquiring general concepts from specific training examples. Example: People continually learn general concepts or categories such as "bird," "car," "situations in which I should study more in order to pass the exam," etc.
- Each such concept can be viewed as describing some subset of objects or events defined over a larger set
- Alternatively, each concept can be thought of as a Boolean-valued function defined over this larger set. (Example: A function defined over all animals, whose value is true for birds and false for other animals).

Definition: Concept learning - Inferring a Boolean-valued function from training examples of its input and output

A CONCEPT LEARNING TASK

Consider the example task of learning the target concept "Days on which *Aldo* enjoys his favorite water sport"

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

Table: Positive and negative training examples for the target concept *EnjoySport*.

The task is to learn to predict the value of *EnjoySport* for an arbitrary day, based on the values of its other attributes?

What hypothesis representation is provided to the learner?

- Let's consider a simple representation in which each hypothesis consists of a conjunction of constraints on the instance attributes.
- Let each hypothesis be a vector of six constraints, specifying the values of the six attributes *Sky*, *AirTemp*, *Humidity*, *Wind*, *Water*, and *Forecast*.

For each attribute, the hypothesis will either

- Indicate by a "?" that any value is acceptable for this attribute,
- Specify a single required value (e.g., Warm) for the attribute, or
- Indicate by a " Φ " that no value is acceptable

If some instance x satisfies all the constraints of hypothesis h , then h classifies x as a positive example ($h(x) = 1$).

The hypothesis that **PERSON** enjoys his favorite sport only on cold days with high humidity is represented by the expression

(?, Cold, High, ?, ?, ?)

The most general hypothesis-that every day is a positive example-is represented by

(?, ?, ?, ?, ?, ?)

The most specific possible hypothesis-that no day is a positive example-is represented by

(Φ , Φ , Φ , Φ , Φ , Φ)

Notation

- The set of items over which the concept is defined is called the *set of instances*, which is denoted by X .

Example: X is the set of all possible days, each represented by the attributes: Sky, AirTemp, Humidity, Wind, Water, and Forecast

- The concept or function to be learned is called the *target concept*, which is denoted by c . c can be any Boolean valued function defined over the instances X

$$c: X \rightarrow \{0, 1\}$$

Example: The target concept corresponds to the value of the attribute *EnjoySport* (i.e., $c(x) = 1$ if *EnjoySport* = Yes, and $c(x) = 0$ if *EnjoySport* = No).

- Instances for which $c(x) = 1$ are called *positive examples*, or members of the target concept.
- Instances for which $c(x) = 0$ are called *negative examples*, or non-members of the target concept.
- The ordered pair $(x, c(x))$ to describe the training example consisting of the instance x and its target *concept value* $c(x)$.
- D to denote the set of available training examples

- The symbol H to denote the set of all possible hypotheses that the learner may consider regarding the identity of the target concept. Each hypothesis h in H represents a Boolean-valued function defined over X

$$h: X \rightarrow \{0, 1\}$$

The goal of the learner is to find a hypothesis h such that $h(x) = c(x)$ for all x in X .

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- Given:
 - Instances X : Possible days, each described by the attributes
 - *Sky* (with possible values Sunny, Cloudy, and Rainy),
 - *AirTemp* (with values Warm and Cold),
 - *Humidity* (with values Normal and High),
 - *Wind* (with values Strong and Weak),
 - *Water* (with values Warm and Cool),
 - *Forecast* (with values Same and Change).
 - Hypotheses H : Each hypothesis is described by a conjunction of constraints on the attributes *Sky*, *AirTemp*, *Humidity*, *Wind*, *Water*, and *Forecast*. The constraints may be "?" (any value is acceptable), "Φ" (no value is acceptable), or a specific value.
 - Target concept c : *EnjoySport* : $X \rightarrow \{0, 1\}$
 - Training examples D : Positive and negative examples of the target function
 - Determine:
 - A hypothesis h in H such that $h(x) = c(x)$ for all x in X .
-

Table: The *EnjoySport* concept learning task.

The inductive learning hypothesis

Any hypothesis found to approximate the target function well over a sufficiently large set of training examples will also approximate the target function well over other unobserved examples.

CONCEPT LEARNING AS SEARCH

- Concept learning can be viewed as the task of searching through a large space of hypotheses implicitly defined by the hypothesis representation.
- The goal of this search is to find the hypothesis that best fits the training examples.

Example:

Consider the instances X and hypotheses H in the *EnjoySport* learning task. The attribute *Sky* has three possible values, and *AirTemp*, *Humidity*, *Wind*, *Water*, *Forecast* each have two possible values, the instance space X contains exactly

$$3 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 = 96 \text{ distinct instances}$$

$$5 \cdot 4 \cdot 4 \cdot 4 \cdot 4 \cdot 4 = 5120 \text{ syntactically distinct hypotheses within } H.$$

Every hypothesis containing one or more " Φ " symbols represents the empty set of instances; that is, it classifies every instance as negative.

$$1 + (4 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3) = 973. \text{ Semantically distinct hypotheses}$$

General-to-Specific Ordering of Hypotheses

Consider the two hypotheses

$$h_1 = (\text{Sunny}, ?, ?, \text{Strong}, ?, ?)$$

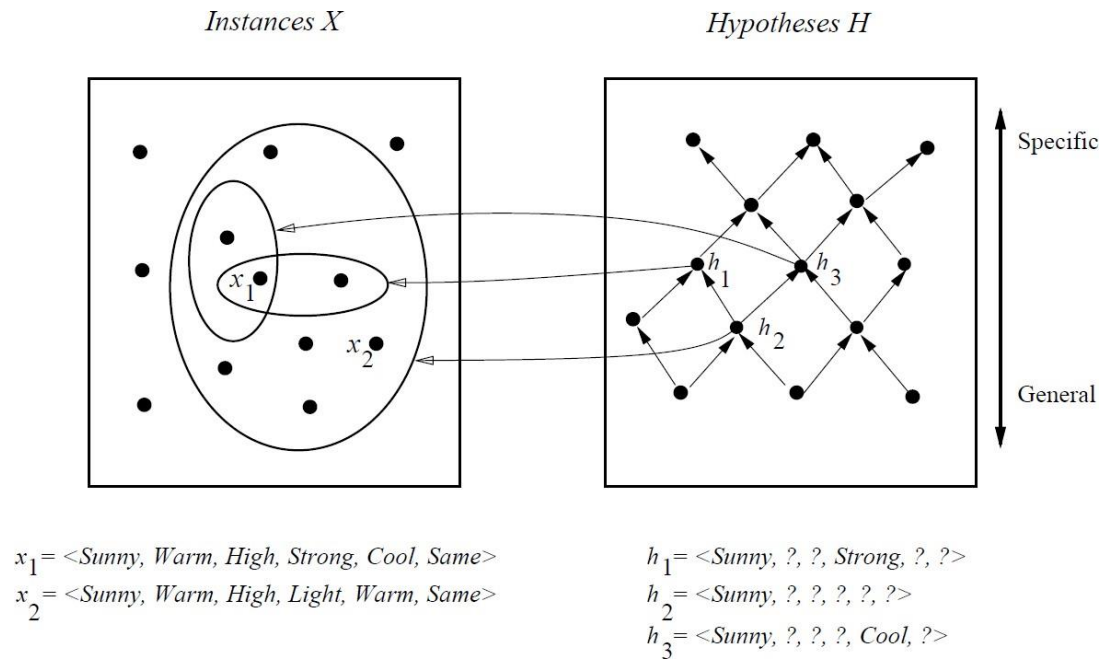
$$h_2 = (\text{Sunny}, ?, ?, ?, ?, ?)$$

- Consider the sets of instances that are classified positive by h_1 and by h_2 .
- h_2 imposes fewer constraints on the instance, it classifies more instances as positive. So, any instance classified positive by h_1 will also be classified positive by h_2 . Therefore, h_2 is more general than h_1 .

Given hypotheses h_j and h_k , h_j is more-general-than or- equal to h_k if and only if any instance that satisfies h_k also satisfies h_j

Definition: Let h_j and h_k be Boolean-valued functions defined over X . Then h_j is **more general-than-or-equal-to** h_k (written $h_j \geq h_k$) if and only if

$$(\forall x \in X) [(h_k(x) = 1) \rightarrow (h_j(x) = 1)]$$



- In the figure, the box on the left represents the set X of all instances, the box on the right the set H of all hypotheses.
- Each hypothesis corresponds to some subset of X —the subset of instances that it classifies positive.
- The arrows connecting hypotheses represent the more - general -than relation, with the arrow pointing toward the less general hypothesis.
- Note the subset of instances characterized by h_2 subsumes the subset characterized by h_1 , hence h_2 is more - general— than h_1

FIND-S: FINDING A MAXIMALLY SPECIFIC HYPOTHESIS

FIND-S Algorithm

1. Initialize h to the most specific hypothesis in H
2. For each positive training instance x
 - For each attribute constraint a_i in h
 - If the constraint a_i is satisfied by x
 - Then do nothing
 - Else replace a_i in h by the next more general constraint that is satisfied by x
3. Output hypothesis h

To illustrate this algorithm, assume the learner is given the sequence of training examples from the *EnjoySport* task

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

- The first step of FIND-S is to initialize h to the most specific hypothesis in H
 $h = (\emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset)$

- Consider the first training example

$$x_1 = \langle \text{Sunny Warm Normal Strong Warm Same} \rangle, +$$

Observing the first training example, it is clear that hypothesis h is too specific. None of the " \emptyset " constraints in h are satisfied by this example, so each is replaced by the next *more general constraint* that fits the example

$$h_1 = \langle \text{Sunny Warm Normal Strong Warm Same} \rangle$$

- Consider the second training example

$$x_2 = \langle \text{Sunny, Warm, High, Strong, Warm, Same} \rangle, +$$

The second training example forces the algorithm to further generalize h , this time substituting a "?" in place of any attribute value in h that is not satisfied by the new example

$$h_2 = \langle \text{Sunny Warm ? Strong Warm Same} \rangle$$

- Consider the third training example

$$x_3 = \langle \text{Rainy, Cold, High, Strong, Warm, Change} \rangle, -$$

Upon encountering the third training the algorithm makes no change to h . The FIND-S algorithm simply ignores every negative example.

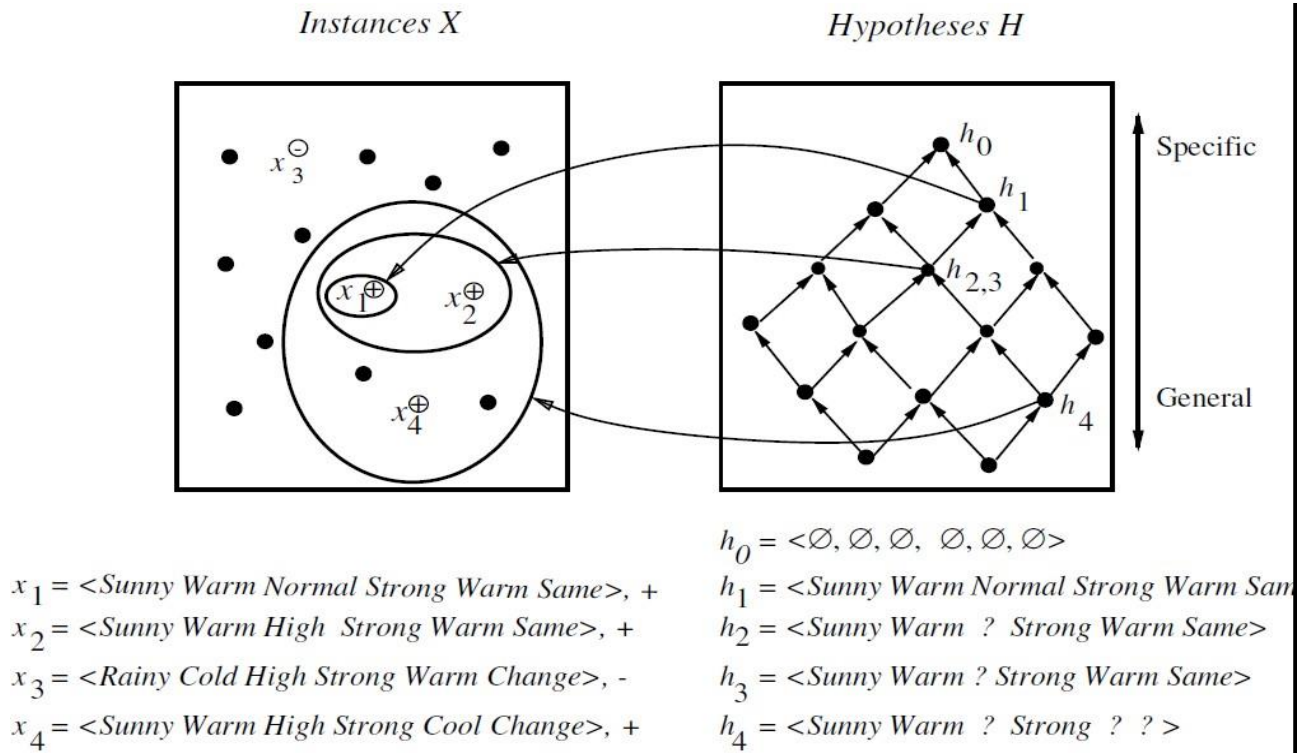
$$h_3 = \langle \text{Sunny Warm ? Strong Warm Same} \rangle$$

- Consider the fourth training example

$$x_4 = \langle \text{Sunny Warm High Strong Cool Change} \rangle, +$$

The fourth example leads to a further generalization of h

$$h_4 = \langle \text{Sunny Warm ? Strong ? ?} \rangle$$



The key property of the FIND-S algorithm

- FIND-S is guaranteed to output the most specific hypothesis within H that is consistent with the positive training examples
- FIND-S algorithm's final hypothesis will also be consistent with the negative examples provided the correct target concept is contained in H, and provided the training examples are correct.

Unanswered by FIND-S

1. Has the learner converged to the correct target concept?
2. Why prefer the most specific hypothesis?
3. Are the training examples consistent?
4. What if there are several maximally specific consistent hypotheses?

VERSION SPACES AND THE CANDIDATE-ELIMINATION ALGORITHM

The key idea in the CANDIDATE-ELIMINATION algorithm is to output a description of the set of all *hypotheses consistent with the training examples*

Representation

Definition: consistent- A hypothesis h is **consistent** with a set of training examples D if and only if $h(x) = c(x)$ for each example $(x, c(x))$ in D .

$$\text{Consistent}(h, D) \equiv (\forall \langle x, c(x) \rangle \in D) h(x) = c(x)$$

Note difference between definitions of *consistent* and *satisfies*

- An example x is said to **satisfy** hypothesis h when $h(x) = 1$, regardless of whether x is a positive or negative example of the target concept.
- An example x is said to **consistent** with hypothesis h iff $h(x) = c(x)$

Definition: version space- The **version space**, denoted $VS_{H, D}$ with respect to hypothesis space H and training examples D , is the subset of hypotheses from H consistent with the training examples in D

$$VS_{H, D} \equiv \{h \in H \mid \text{Consistent}(h, D)\}$$

The LIST-THEN-ELIMINATION algorithm

The LIST-THEN-ELIMINATE algorithm first initializes the version space to contain all hypotheses in H and then eliminates any hypothesis found inconsistent with any training example.

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1. **VersionSpace** \leftarrow a list containing every hypothesis in H
 2. For each training example, $(x, c(x))$
 remove from **VersionSpace** any hypothesis h for which $h(x) \neq c(x)$
 3. Output the list of hypotheses in **VersionSpace**
-

The LIST-THEN-ELIMINATE Algorithm

- List-Then-Eliminate works in principle, so long as version space is finite.
- However, since it requires exhaustive enumeration of all hypotheses in practice it is not feasible.

A More Compact Representation for Version Spaces

The version space is represented by its most general and least general members. These members form general and specific boundary sets that delimit the version space within the partially ordered hypothesis space.

Definition: The **general boundary** G , with respect to hypothesis space H and training data D , is the set of maximally general members of H consistent with D

$$G \equiv \{g \in H \mid \text{Consistent}(g, D) \wedge (\neg \exists g' \in H)[(g' \underset{g}{>} g) \wedge \text{Consistent}(g', D)]\}$$

Definition: The **specific boundary** S , with respect to hypothesis space H and training data D , is the set of minimally general (i.e., maximally specific) members of H consistent with D .

$$S \equiv \{s \in H \mid \text{Consistent}(s, D) \wedge (\neg \exists s' \in H)[(s \underset{s'}{>} s') \wedge \text{Consistent}(s', D)]\}$$

Theorem: Version Space representation theorem

Theorem: Let X be an arbitrary set of instances and Let H be a set of Boolean-valued hypotheses defined over X . Let $c: X \rightarrow \{0, 1\}$ be an arbitrary target concept defined over X , and let D be an arbitrary set of training examples $\{(x, c(x))\}$. For all X, H, c , and D such that S and G are well defined,

$$VS_{H,D} = \{h \in H \mid (\exists s \in S) (\exists g \in G) (g \underset{g}{\geq} h \underset{s}{\geq} s)\}$$

To Prove:

1. Every h satisfying the right hand side of the above expression is in $VS_{H,D}$
2. Every member of $VS_{H,D}$ satisfies the right-hand side of the expression

Sketch of proof:

1. let g, h, s be arbitrary members of G, H, S respectively with $g \underset{g}{\geq} h \underset{s}{\geq} s$
 - By the definition of S , s must be satisfied by all positive examples in D . Because $h \underset{s}{\geq} s$, h must also be satisfied by all positive examples in D .
 - By the definition of G , g cannot be satisfied by any negative example in D , and because $g \underset{g}{\geq} h$, h cannot be satisfied by any negative example in D . Because h is satisfied by all positive examples in D and by no negative examples in D , h is consistent with D , and therefore h is a member of $VS_{H,D}$.
2. It can be proven by assuming some h in $VS_{H,D}$, that does not satisfy the right-hand side of the expression, then showing that this leads to an inconsistency

CANDIDATE-ELIMINATION Learning Algorithm

The CANDIDATE-ELIMINATION algorithm computes the version space containing all hypotheses from H that are consistent with an observed sequence of training examples.

Initialize G to the set of maximally general hypotheses in H

Initialize S to the set of maximally specific hypotheses in H

For each training example d , do

- If d is a positive example
 - Remove from G any hypothesis inconsistent with d
 - For each hypothesis s in S that is not consistent with d
 - Remove s from S
 - Add to S all minimal generalizations h of s such that
 - h is consistent with d , and some member of G is more general than h
 - Remove from S any hypothesis that is more general than another hypothesis in S
- If d is a negative example
 - Remove from S any hypothesis inconsistent with d
 - For each hypothesis g in G that is not consistent with d
 - Remove g from G
 - Add to G all minimal specializations h of g such that
 - h is consistent with d , and some member of S is more specific than h
 - Remove from G any hypothesis that is less general than another hypothesis in G

CANDIDATE- ELIMINATION algorithm using version spaces

An Illustrative Example

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

CANDIDATE-ELIMINATION algorithm begins by initializing the version space to the set of all hypotheses in H ;

Initializing the G boundary set to contain the most general hypothesis in H

$$G_0 \langle ?, ?, ?, ?, ?, ? \rangle$$

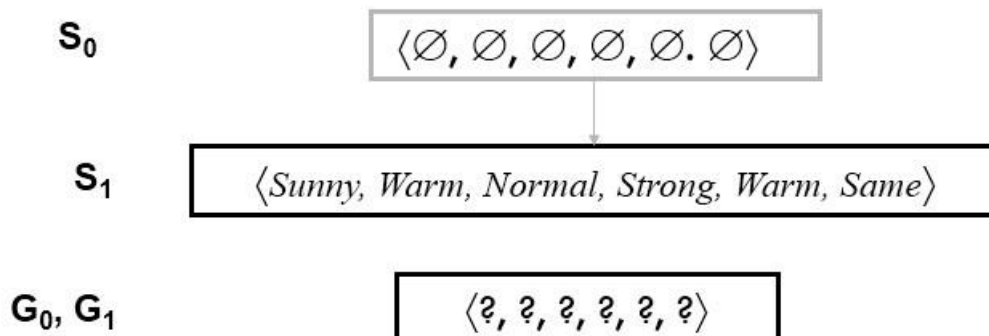
Initializing the S boundary set to contain the most specific (least general) hypothesis

$$S_0 \langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset \rangle$$

- When the first training example is presented, the CANDIDATE-ELIMINATION algorithm checks the S boundary and finds that it is overly specific and it fails to cover the positive example.
- The boundary is therefore revised by moving it to the least more general hypothesis that covers this new example
- No update of the G boundary is needed in response to this training example because G_0 correctly covers this example

For training example d ,

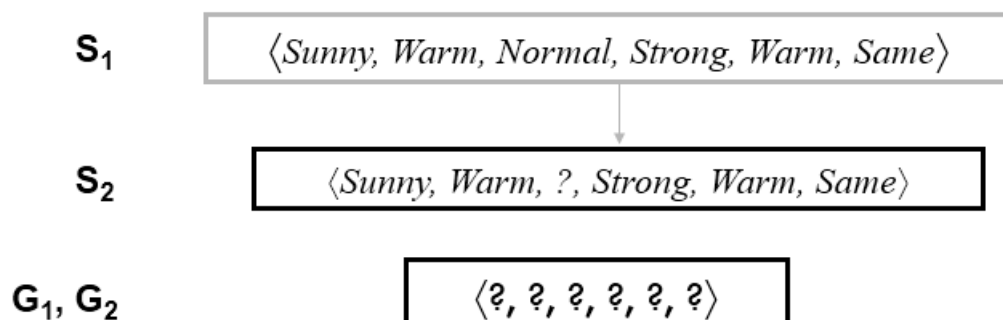
$\langle \text{Sunny, Warm, Normal, Strong, Warm, Same} \rangle +$



- When the second training example is observed, it has a similar effect of generalizing S further to S_2 , leaving G again unchanged i.e., $G_2 = G_1 = G_0$

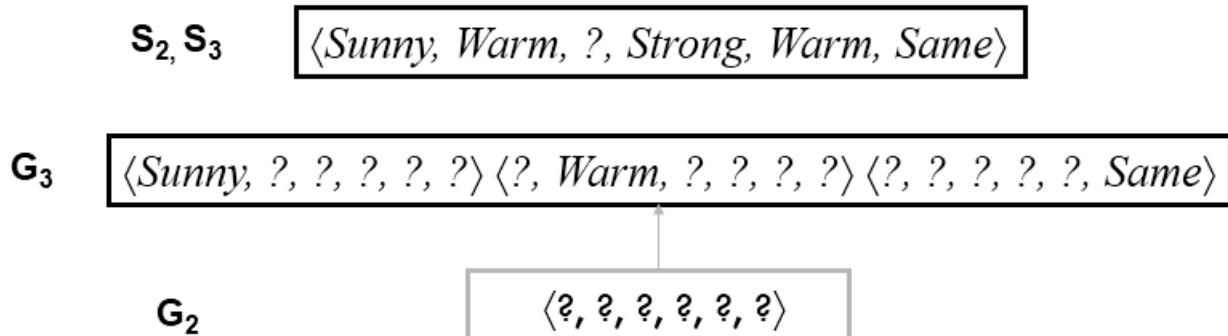
For training example d ,

$\langle \text{Sunny, Warm, High, Strong, Warm, Same} \rangle +$



- Consider the third training example. This negative example reveals that the G boundary of the version space is overly general, that is, the hypothesis in G incorrectly predicts that this new example is a positive example.
- The hypothesis in the G boundary must therefore be specialized until it correctly classifies this new negative example

For training example d, $\langle \text{Rainy, Cold, High, Strong, Warm, Change} \rangle -$

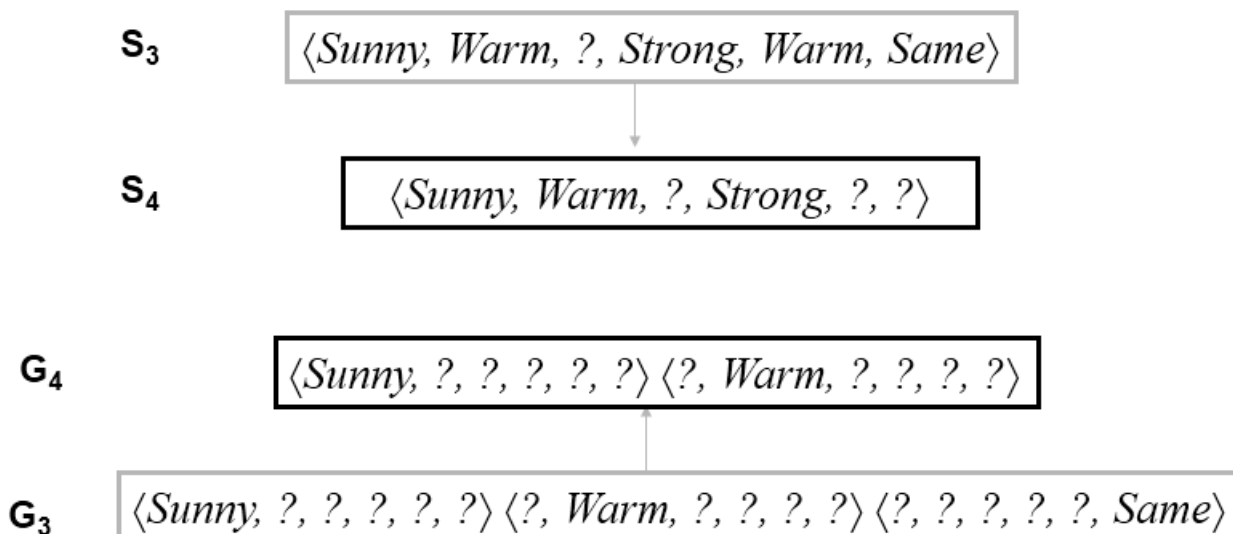


Given that there are six attributes that could be specified to specialize G_2 , why are there only three new hypotheses in G_3 ?

For example, the hypothesis $h = \langle \text{?, ?, Normal, ?, ?, ?} \rangle$ is a minimal specialization of G_2 that correctly labels the new example as a negative example, but it is not included in G_3 . The reason this hypothesis is excluded is that it is inconsistent with the previously encountered positive examples

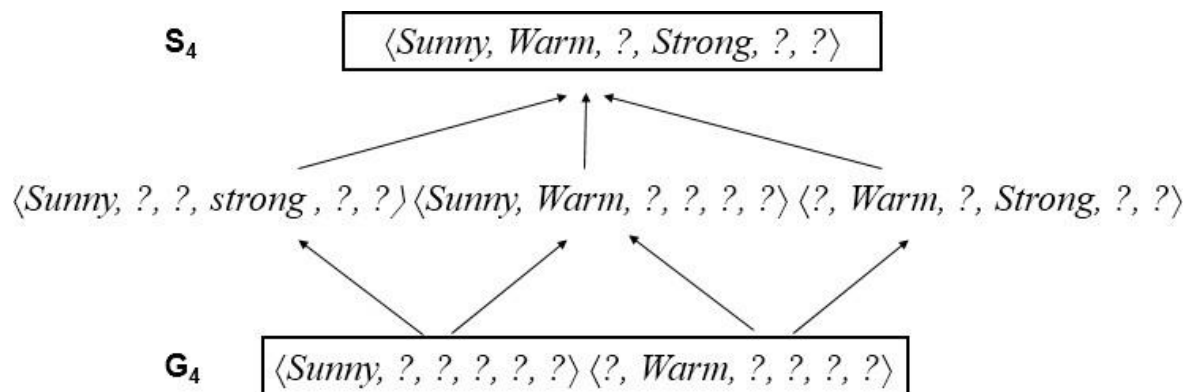
- Consider the fourth training example.

For training example d, $\langle \text{Sunny, Warm, High, Strong, Cool Change} \rangle +$



- This positive example further generalizes the S boundary of the version space. It also results in removing one member of the G boundary, because this member fails to cover the new positive example

After processing these four examples, the boundary sets S_4 and G_4 delimit the version space of all hypotheses consistent with the set of incrementally observed training examples.



INDUCTIVE BIAS

The fundamental questions for inductive inference

1. What if the target concept is not contained in the hypothesis space?
2. Can we avoid this difficulty by using a hypothesis space that includes every possible hypothesis?
3. How does the size of this hypothesis space influence the ability of the algorithm to generalize to unobserved instances?
4. How does the size of the hypothesis space influence the number of training examples that must be observed?

These fundamental questions are examined in the context of the CANDIDATE-ELIMINATION algorithm

A Biased Hypothesis Space

- Suppose the target concept is not contained in the hypothesis space H , then obvious solution is to enrich the hypothesis space to include every possible hypothesis.
- Consider the *EnjoySport* example in which the hypothesis space is restricted to include only conjunctions of attribute values. Because of this restriction, the hypothesis space is unable to represent even simple disjunctive target concepts such as
"Sky = Sunny or Sky = Cloudy."
- The following three training examples of disjunctive hypothesis, the algorithm would find that there are zero hypotheses in the version space

⟨Sunny Warm Normal Strong Cool Change⟩	Y
⟨Cloudy Warm Normal Strong Cool Change⟩	Y
⟨Rainy Warm Normal Strong Cool Change⟩	N

- If Candidate Elimination algorithm is applied, then it end up with empty Version Space. After first two training example

$$S = \langle ? \text{ Warm Normal Strong Cool Change} \rangle$$

- This new hypothesis is overly general and it incorrectly covers the third negative training example! So H does not include the appropriate c .
- In this case, a more expressive hypothesis space is required.

An Unbiased Learner

- The solution to the problem of assuring that the target concept is in the hypothesis space H is to provide a hypothesis space capable of representing every teachable concept that is representing every possible subset of the instances X .
- The set of all subsets of a set X is called the power set of X
- In the *EnjoySport* learning task the size of the instance space X of days described by the six attributes is 96 instances.
- Thus, there are 2^{96} distinct target concepts that could be defined over this instance space and learner might be called upon to learn.
- The conjunctive hypothesis space is able to represent only 973 of these - a biased hypothesis space indeed
- Let us reformulate the *EnjoySport* learning task in an unbiased way by defining a new hypothesis space H' that can represent every subset of instances
- The target concept "Sky = Sunny or Sky = Cloudy" could then be described as

$$(\text{Sunny}, ?, ?, ?, ?, ?) \vee (\text{Cloudy}, ?, ?, ?, ?, ?)$$

The Futility of Bias-Free Learning

Inductive learning requires some form of prior assumptions, or inductive bias

Definition:

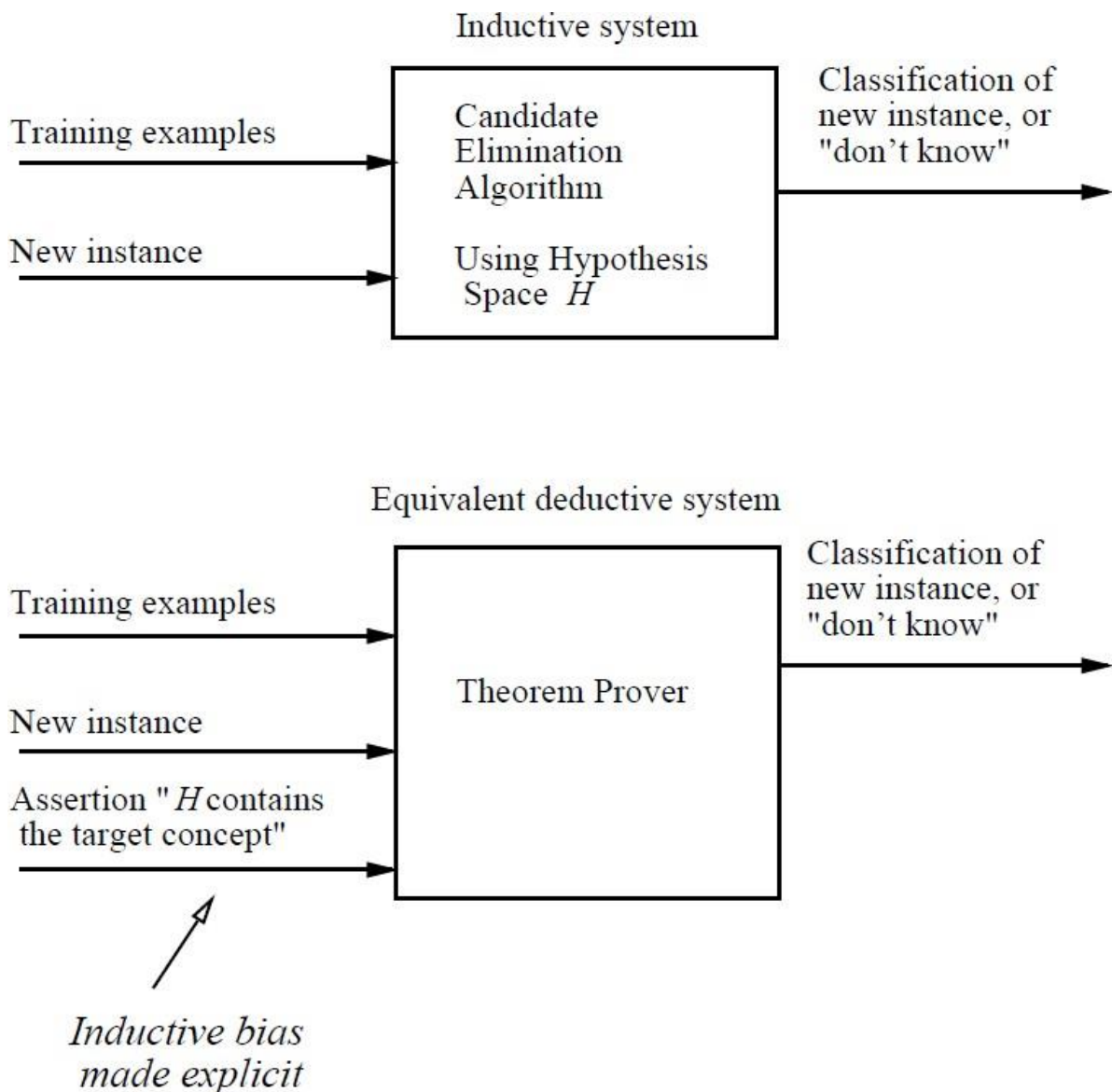
Consider a concept learning algorithm L for the set of instances X .

- Let c be an arbitrary concept defined over X
- Let $D_c = \{(x, c(x))\}$ be an arbitrary set of training examples of c .
- Let $L(x_i, D_c)$ denote the classification assigned to the instance x_i by L after training on the data D_c .
- The inductive bias of L is any minimal set of assertions B such that for any target concept c and corresponding training examples D_c

$$(\forall \langle x_i \in X \rangle [(B \wedge D_c \wedge x_i) \vdash L(x_i, D_c)])$$

The below figure explains

- Modelling inductive systems by equivalent deductive systems.
- The input-output behavior of the CANDIDATE-ELIMINATION algorithm using a hypothesis space H is identical to that of a deductive theorem prover utilizing the assertion " H contains the target concept." This assertion is therefore called the inductive bias of the CANDIDATE-ELIMINATION algorithm.
- Characterizing inductive systems by their inductive bias allows modelling them by their equivalent deductive systems. This provides a way to compare inductive systems according to their policies for generalizing beyond the observed training data.

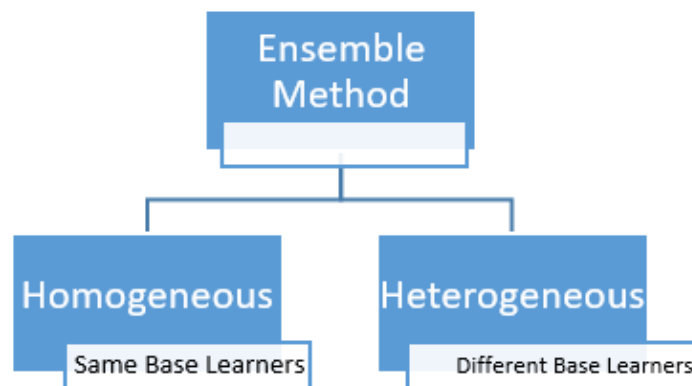


Ensemble Learning

Ensemble Learning Techniques in Machine Learning, Machine learning models suffer bias and/or variance. Bias is the difference between the predicted value and actual value by the model. Bias is introduced when the model doesn't consider the variation of data and creates a simple model. The simple model doesn't follow the patterns of data, and hence the model gives errors in predicting training as well as testing data i.e. the model with high bias and high variance. When the model follows even random quirks of data, as pattern of data, then the model might do very well on training dataset i.e. it gives low bias, but it fails on test data and gives high variance.

Therefore, to improve the accuracy (estimate) of the model, ensemble learning methods are developed. Ensemble is a machine learning concept, in which several models are trained using machine learning algorithms. It combines low performing classifiers (also called as weak learners or base learner) and combine individual model prediction for the final prediction.

On the basis of type of base learners, ensemble methods can be categorized as homogeneous and heterogeneous ensemble methods. If base learners are same, then it is a homogeneous ensemble method. If base learners are different then it is a heterogeneous ensemble method.



Ensemble Learning Methods

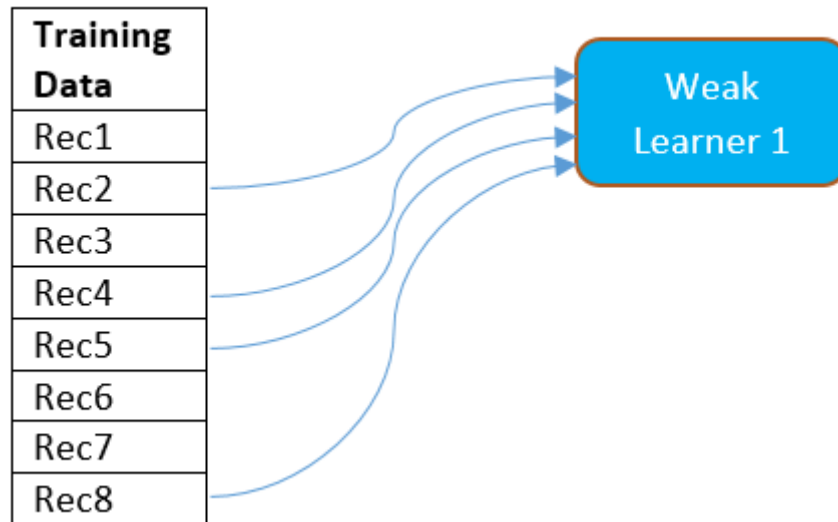
Ensemble techniques are classified into three types:

1. Bagging
2. Boosting
3. Stacking
4. Bagging

Consider a scenario where you are looking at the users' ratings for a product. Instead of approving one user's good/bad rating, we consider average rating given to the product. With average rating, we can be considerably sure of quality of the product. Bagging makes use of this principle. Instead of depending on one model, it runs the data through multiple models in parallel, and average them out as model's final output.

What is Bagging? How it works?

Bagging is an acronym for **Bootstrapped Aggregation**. Bootstrapping means random selection of records with replacement from the training dataset. 'Random selection with replacement' can be explained as follows:

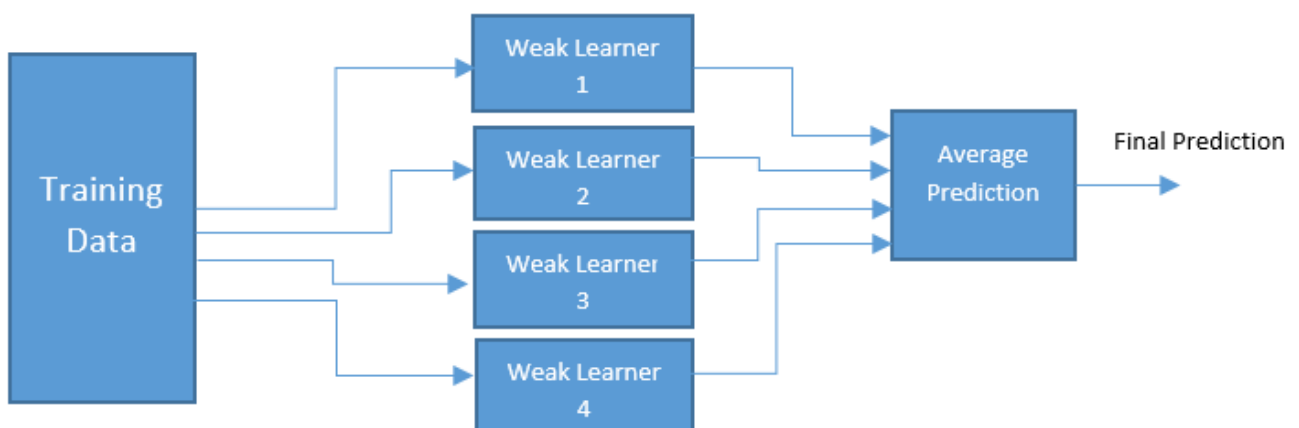


Consider that there are 8 samples in the training dataset. Out of these 8 samples, every weak learner gets 5 samples as training data for the model. These 5 samples need not be unique, or non-repetitive.

The model (weak learner) is allowed to get a sample multiple times. For example, as shown in the figure, Rec5 is selected 2 times by the model. Therefore, weak learner1 gets Rec2, Rec5, Rec8, Rec5, Rec4 as training data.

All the samples are available for selection to next weak learners. Thus all 8 samples will be available for next weak learner and any sample can be selected multiple times by next weak learners.

Bagging is a **parallel method**, which means several weak learners learn the data pattern independently and simultaneously. This can be best shown in the below diagram:



The output of each weak learner is averaged to generate final output of the model.

Since the weak learner's outputs are averaged, this mechanism helps to reduce variance or variability in the predictions. However, it does not help to reduce bias of the model.

Since final prediction is an average of output of each weak learner, it means that each weak learner has equal say or weight in the final output.

To summarize:

- Bagging is Bootstrapped Aggregation
- It is Parallel method
- Final output is calculated by averaging the outputs produced by individual weak learner
- Each weak learner has equal say
- Bagging reduces variance

Boosting

We saw that in bagging every model is given equal preference, but if one model predicts data more correctly than the other, then higher weightage should be given to this model over the other. Also, the model should attempt to reduce bias. These concepts are applied in the second ensemble method that we are going to learn, that is Boosting.

What is Boosting?

To start with, boosting assigns equal weights to all data points as all points are equally important in the beginning. For example, if a training dataset has N samples, it assigns weight $= 1/N$ to each sample.

The weak learner classifies the data. The weak classifier classifies some samples correctly, while making mistake in classifying others.

After classification, sample weights are changed. Weight of correctly classified sample is reduced, and weight of incorrectly classified sample is increased. Then the next weak classifier is run.

This process continues until model as a whole gives strong predictions.