

1.

- a) If you pass the course, then you did not miss the final exam.
- b) you will fail the course if and only if you miss the final exam.
- c) You do not have a cold or you missed the final exam.
- d) If, you missed the exam and passed the course, then you didnt have a have a cold if and only if you passed the course.

2.

- a) The given proposition is a tautology so the semantics are: True for all values.
- b) The negation of this proposition is a contradiction so the semantics are: False for all values.

3.

a) semantics of  $T \rightarrow ((\neg p \rightarrow q) \rightarrow p)$ :

p	q	$T \rightarrow ((\neg p \rightarrow q) \rightarrow p)$
T	T	F
T	F	F
F	T	T
F	F	F

b) The above proposition is logically equivalent to "F or (p or q) and (not p)"

4.

- a)
- b)

$$\begin{aligned}
 4. \quad & (p \wedge ((\neg p \vee \neg q) \wedge (p \vee q))) \vee (q \wedge ((\neg p \vee \neg q) \wedge (p \vee q))) \\
 \equiv & (p \wedge (p \vee q) \wedge (\neg p \vee \neg q)) \vee (q \wedge (p \vee q) \wedge (\neg p \vee \neg q)) \\
 \equiv & (p \wedge (\neg p \vee \neg q)) \vee (q \wedge (\neg p \vee \neg q)) \\
 \equiv & (p \vee q) \wedge (\neg p \vee \neg q) \\
 \equiv & (q \vee p) \wedge (\neg p \vee \neg q) \\
 \equiv & (\neg q \rightarrow p) \wedge (p \rightarrow \neg q) \\
 \equiv & (\neg q \leftrightarrow p) \quad \boxed{II}
 \end{aligned}$$

5.  $\leftrightarrow \neg \vee \wedge \equiv$

$$\begin{aligned}
 & w \rightarrow ((r \rightarrow u) \wedge (u \rightarrow \neg w) \wedge (w \rightarrow r)) \\
 \equiv & w \rightarrow ((\neg r \vee u) \wedge (\neg u \vee \neg w) \wedge (\neg w \vee r)) \\
 \equiv & w \rightarrow \neg(\neg w \wedge \neg w) \\
 \equiv & w \rightarrow (w \vee w) \\
 \equiv & \neg w \vee (w \vee w) \\
 \equiv & \neg w \vee w
 \end{aligned}$$

Therefore it is a tautology

6.

a)  $p = F, q = T$

b)  $p = T, q = T$

c)  $p = T, q = T, r = F$

7.

a)  $(r \rightarrow (p \vee q) \wedge (p \rightarrow (q \rightarrow r)))$

b)  $(\text{not } r (p \text{ or } q)) \text{ and } (\text{not } p \text{ or } (\text{not } q \text{ or } r))$

8.

$R = (b_0 \rightarrow b_2) \wedge (b_2 \rightarrow b_0)$