🍰 **Interview Cake**

Write a method to find the 2nd largest element in a binary search tree.↴

Here's a sample binary tree node class:

```java
public class BinaryTreeNode {

    public int value;
    public BinaryTreeNode left;
    public BinaryTreeNode right;

    public BinaryTreeNode(int value) {
        this.value = value;
    }

    public BinaryTreeNode insertLeft(int leftValue) {
        this.left = new BinaryTreeNode(leftValue);
        return this.left;
    }

    public BinaryTreeNode insertRight(int rightValue) {
        this.right = new BinaryTreeNode(rightValue);
        return this.right;
    }
}
```

Java ▾

Gotchas

Our first thought might be to do an in-order traversal of the BST↴ and return the second-to-last item. This means looking at *every node in the* BST. That would take $O(n)$ time and $O(h)$ space, where h is the max *height* of the tree (which is $lg(n)$ if the tree is balanced,↴ but could be as much as n if not).

We can do better than $O(n)$ time and $O(h)$ space.

We can do this in *one* walk from top to bottom of our BST. This means $O(h)$ time (again, that's $O(\lg n)$ if the tree is balanced, $O(n)$ otherwise).

A clean recursive implementation will take $O(h)$ space in the call stack, but we can bring our algorithm down to $O(1)$ space overall.

Breakdown

Let's start by solving a simplified version of the problem and see if we can adapt our approach from there. **How would we find *the largest* element in a BST?**

A reasonable guess is to say **the largest element is simply the "rightmost" element**.

So maybe we can start from the root and just step down right child pointers until we can't anymore (until the right child is `null`). At that point the current node is the largest in the whole tree.

Is this sufficient? We can prove it is by contradiction:

If the largest element *were not* the "rightmost," then the largest element would either:

1. be in some ancestor node's left subtree, or
2. have a right child.

But each of these leads to a contradiction:

1. If the node is in some ancestor node's left subtree it's *smaller* than that ancestor node, so it's not the largest.
2. If the node has a right child that child is larger than it, so it's not the largest.

So the "rightmost" element *must be* the largest.

How would we formalize getting the "rightmost" element in code?

We can use a simple recursive approach. At each step:

1. If there is a right child, that node and the subtree below it are all greater than the current node. So step down to this child and recurse.
2. Else there is no right child and we're already at the "rightmost" element, so we return its value.

```java
public static int findLargest(BinaryTreeNode rootNode) {

    if (rootNode.right != null) {

        return findLargest(rootNode.right);

    }

    return rootNode.value;

}
```
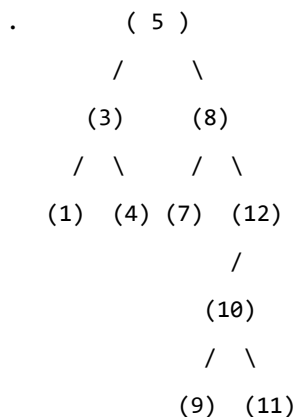
Okay, so we can find the largest element. **How can we adapt this approach to find the *second* largest element?**

Our first thought might be, "it's simply the parent of the largest element!" That seems obviously true when we imagine a nicely balanced tree like this one:

```
.        ( 5 )
        /      \
     (3)       (8)
    /  \      /  \
  (1)  (4) (7)  (9)
```
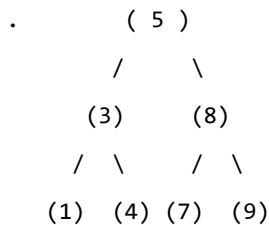
But what if the largest element itself has a left subtree?

```
.        ( 5 )
        /      \
     (3)       (8)
    /  \      /  \
  (1)  (4) (7)  (12)
                  /
               (10)
               /  \
            (9)   (11)
```

Here the parent of our largest is 8, but the second largest is 11.

Drat, okay so the second largest isn't necessarily the parent of the largest...back to the drawing board...

Wait. No. The second largest *is* the parent of the largest *if the largest does not have a left subtree.* If we can handle the case where the largest *does* have a left subtree, we can handle all cases, and we have a solution.

So let's try sticking with this. **How do we find the second largest when the largest has a left subtree?**

It's the *largest* item in that left subtree! Whoa, we freaking *just wrote* a method for finding the largest element in a tree. We could use that here!

How would we code this up?

Java ▾

```java
    private static int findLargest(BinaryTreeNode rootNode) {

        if (rootNode == null) {
            throw new IllegalArgumentException("Tree must have at least 1 node");
        }
        if (rootNode.right != null)  {
            return findLargest(rootNode.right);
        }
        return rootNode.value;
    }


    public static int findSecondLargest(BinaryTreeNode rootNode) {
        if (rootNode == null || (rootNode.left == null
                && rootNode.right == null)) {
            throw new IllegalArgumentException("Tree must have at least 2 nodes");
        }

        // case: we're currently at largest, and largest has a left subtree,
        // so 2nd largest is largest in said subtree
        if (rootNode.left != null && rootNode.right == null) {
            return findLargest(rootNode.left);
        }

        // case: we're at parent of largest, and largest has no left subtree,
        // so 2nd largest must be current node
        if (rootNode.right != null
                && rootNode.right.left == null
                && rootNode.right.right == null) {
            return rootNode.value;
        }

        // otherwise: step right
        return findSecondLargest(rootNode.right);
    }
```

Okay awesome. This'll work. It'll take $O(h)$ time (where h is the height of the tree) and $O(h)$ space.

But that h space in the call stack is avoidable. **How can we get this down to constant space?**

Solution

We start with a method for getting **the largest** value. The largest value is simply the "rightmost" one, so we can get it in one walk down the tree by traversing rightward until we don't have a right child anymore:

```java
public static int findLargest(BinaryTreeNode rootNode) {

    BinaryTreeNode largest = null;
    BinaryTreeNode current = rootNode;


    while (current != null) {
        if (current.right == null) {
            largest = current;
        }
        current = current.right;
    }
    return largest.value;

}
```

With this in mind, we can also find the *second largest* in one walk down the tree. At each step, we have a few cases:

1. **If we have a left subtree but not a right subtree**, then the current node is the largest overall (the "rightmost") node. The second largest element must be the largest element in the left subtree. We use our `findLargest()` method above to find the largest in that left subtree!
2. **If we have a right child, but that right child node doesn't have any children**, then the right child must be *the largest element* and our current node must be *the second largest element*!
3. **Else, we have a right subtree with more than one element**, so the largest and second largest are somewhere in that subtree. So we step right.

Java ▼

```java
private static int findLargest(BinaryTreeNode rootNode) {

    BinaryTreeNode current = rootNode;

    while (current.right != null) {

        current = current.right;

    }

    return current.value;

}


public static int findSecondLargest(BinaryTreeNode rootNode) {

    if (rootNode == null || (rootNode.left == null

            && rootNode.right == null)) {

        throw new IllegalArgumentException("Tree must have at least 2 nodes");

    }


    BinaryTreeNode current = rootNode;


    while (true) {


        // case: current is largest and has a left subtree

        // 2nd largest is the largest in that subtree

        if (current.left != null && current.right == null) {

            return findLargest(current.left);

        }


        // case: current is parent of largest, and largest has no children,

        // so current is 2nd largest

        if (current.right != null &&

                current.right.left == null &&

                current.right.right == null) {

            return current.value;

        }


        current = current.right;

    }

}
```

Complexity

We're doing *one* walk down our BST, which means $O(h)$ time, where h is the height of the tree (again, that's $O(\lg n)$ if the tree is balanced, $O(n)$ otherwise). $O(1)$ space.

What We Learned

Here we used a **"simplify, solve, and adapt" strategy**.

The question asks for a method to find the *second* largest element in a BST, so we started off by *simplifying* the problem: we thought about how to find the *first* largest element.

Once we had a strategy for that, we *adapted* that strategy to work for finding the *second* largest element.

It may seem counter-intuitive to start off by solving the *wrong* question. But starting off with a simpler version of the problem is often *much* faster, because it's easier to wrap our heads around right away.

One more note about this one:

Breaking things down into *cases* is another strategy that really helped us here.

Notice how simple finding the second largest node got when we divided it into two cases:

1. The largest node has a left subtree.
2. The largest node *does not* have a left subtree.

Whenever a problem is starting to feel complicated, try breaking it down into cases.

It can be really helpful to actually draw out sample inputs for those cases. This'll keep your thinking organized and also help get your interviewer on the same page.

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