

## 2.4 Format of a recursive function

```
if (test for a base case)
    return (base case value)
else if (test for another base case)
    return (other base case value)
else // recursive case
    return (some work and recursive call)
```

### (i) Calculate factorial of a positive integer

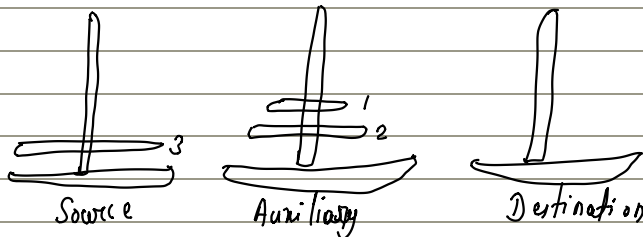
```
int fact(n) {
    if (n == 0)
        return 1;
    else if (n == 1)
        return 1;
    else
        return n * fact(n-1);
}
```

## 2.9 Recursion: Problems and Solutions

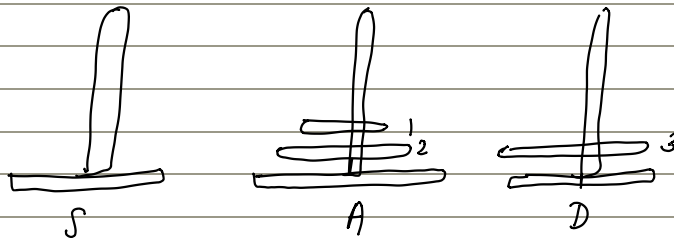
### P1. Towers of Hanoi

#### Algorithms:

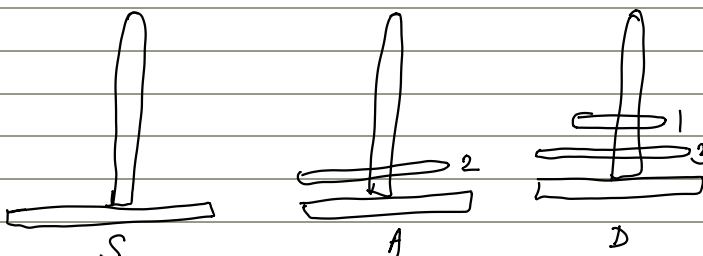
(i) Move the top  $n-1$  disks from source to auxiliary tower.



(ii) Move the  $n^{\text{th}}$  disk from source to destination tower



(iii) Move the  $n-1$  disks from auxiliary tower to destination tower



Code:

```
void towers-of-hanoi(int n, source, auxiliary, destination) {
    if (n == 1) {
        cout << "Move disk 1 from " << source << " tower to "
            << destination << " tower" << endl;
        return;
    }
    else {
        // Move top n-1 disks from source to auxiliary tower
        towers-of-hanoi(n-1, source, destination, auxiliary);

        // Move nth disk from source to destination tower
        cout << "Move disk " << n << " from " << source << " tower to "
            << destination << " tower" << endl;

        // Move n-1 disks from auxiliary to destination tower
        towers-of-hanoi(n-1, auxiliary, source, destination);
    }
}
```

P2. To check whether an array is sorted

Code:

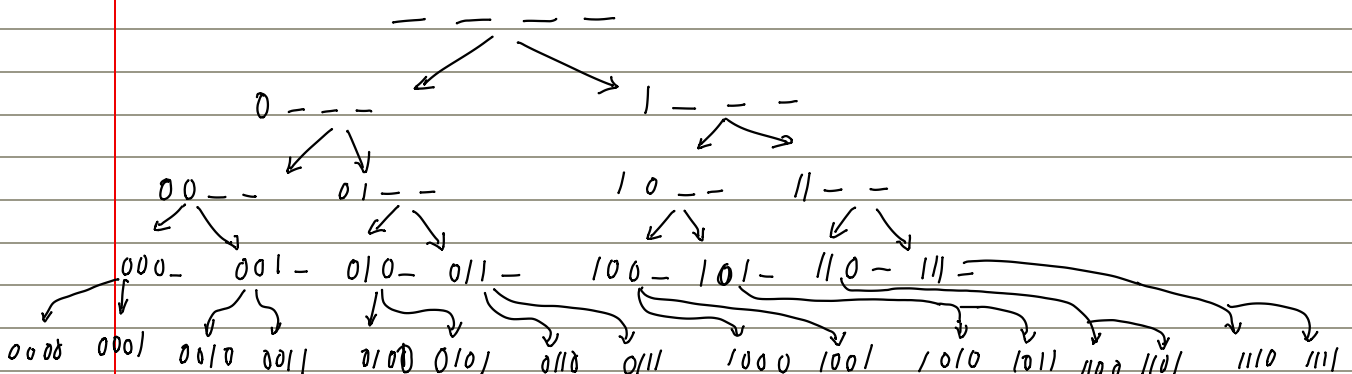
```
bool is-array-sorted(int arr[], int n) {
    if (n == 1) {
        return true;
    }
    else {
        return (arr[n-1] > arr[n-2]) ? is-array-sorted(arr, n-1) : false;
    }
}
```

## 2.12 Backtracking: problems and solutions

P3. Generate all strings of  $n$  bits

Algorithm:

Ex: if  $n = 4$



code :

```
void generate-n-bits (int i, bool arr[], int n) {  
    if (i == n) {  
        for (int j = 0; j < n; j++) {  
            cout << arr[j] << " ";  
        }  
        return;  
    }  
    else {  
        arr[i] = 0;  
        generate-n-bits (i+1, arr, n);  
        arr[i] = 1;  
        generate-n-bits (i+1, arr, n);  
    }  
}
```