Thomas H. Jørgensen

2023

# Plan for today

Introduction

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 Dynamic labor supply of couples Borella, De Nardi and Yang (forthcoming): "Are Marriage-Related Taxes and Social Security Benefits Holding Back Female Labor Supply?"

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#### Reading guide:

- 1. What are the main research questions?
- 2. What is the (empirical) motivation?

3. What are the central mechanisms in the model?

4. What is the *simplest model* in which we could capture these?

# Plan for today

Introduction

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Dynamic labor supply of couples
 Borella, De Nardi and Yang (forthcoming): "Are Marriage-Related
 Taxes and Social Security Benefits Holding Back Female Labor Supply?"

#### Reading guide:

- 1. What are the main research questions?
  - How does household-level taxes and transfers affect labor supply?
  - Could individual taxes/transfers increase welfare?
- 2. What is the (empirical) motivation?

3. What are the central mechanisms in the model?

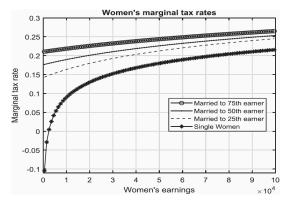
4. What is the simplest model in which we could capture these?

- High marginal tax rates for secondary earner (often women historically)
  - → labor supply discouraged
  - $\rightarrow$  specialization

Introduction

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→ intra-household inequality

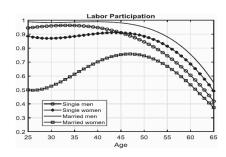


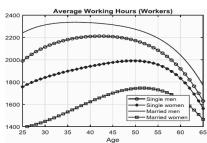
# Empirical Motivation: II

Introduction

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## Outline

Model and Mechanisms

Simulation Results

Simple Mode

## Model Overview

## Three stages

- 1. Working (25–61)
- 2. Early retirement (62-65)
- 3. Retirement (66-99)

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  - Singles + couples,  $j \in \{1, 2\}$  (1 =single) Random transitions

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#### Choices:

Labor supply of both members,  $n_t^i$ ,  $i \in \{1, 2\}$  (1 = man) Consumption/Savings,  $c_t$ ,  $a_{t+1}$ 

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#### States:

Savings, at Income shocks of both,  $\epsilon_t'$ Human capital of both,  $\overline{y}_t^i$ 

## **Preferences**

Individual preferences are [my notation]

$$v(c_t, l_t, i, j) = \frac{[(c_t/\eta^{i,j})^{\omega} l_t^{1-\omega}]^{1-\gamma} - 1}{1-\gamma}$$

```
where l_t^{i,j} = L^{i,j} - n_t^i - \Phi_t^{i,j} \mathbf{1}(n_t^i > 0) is leisure. (4 parameters estimated for each gender/marital status) \eta^{i,j} is equivalence scales \omega is the Cobb-Douglas input elasticity \gamma is the CRRA coefficient
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• Utility of a single man and woman is  $v(c_t, l_t, 1, 1)$  and  $v(c_t, l_t, 2, 1)$ .

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- Utility of a single man and woman is  $v(c_t, l_t, 1, 1)$  and  $v(c_t, l_t, 2, 1)$ .
- Utility of a couple is

$$w(c_t, l_t^1, l_t^2) = v(c_t, l_t^1, 1, 2) + v(c_t, l_t^2, 2, 2)$$

# Human Capital and Wages

• Human capital is previous avg. earnings, approximated as

$$\overline{y}_{t+1}^{i} = \frac{\overline{y}_{t}^{i}(t-t_{0}) + \min(Y_{t}^{i}, \tilde{y}_{t})}{t+1-t_{0}}$$
 (1)

where  $Y_t^i = w_t^i n_t^i$  is labor earnings  $\tilde{y}_t$  is Social Security cap  $t_0 = 25$ .

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• Wages are

$$w_t^i = e_t^i(\overline{y}_t^i)\epsilon_t^i$$

where

$$e_t^i(\overline{y}_t^i)$$
: age, gender and HC. Table 1 in Appendix  $\log \epsilon_{t+1}^i = 
ho_\epsilon^i \log \epsilon_t^i + v_{i+1}^i, \ v_{i+1}^i \sim \mathcal{N}(0, (\sigma_v^i)^2)$ 

(2)

## Government: Taxes and Transfers

Labor income taxes are approximated as

$$T(Y, i, j, t) = (1 - \lambda_t^{i,j} Y^{-\tau_t^{i,j}}) \cdot Y$$

where

 $Y = ra_t + Y_t^1 + Y_t^2$  is total household income  $\lambda_{\star}^{i,j}$  and  $\tau_{\star}^{i,j}$  are gender/marital specific tax-parameters (not reported).

- Payroll tax:  $min(Y, \tilde{y}_t)\tau_t^{SS}$
- Consumption floor, c(j). See table 10 in Appendix.

## Children

• Exogenous/Perfect foresight and continuous. Only women + couples.

- **Exogenous/Perfect foresight** and continuous. Only women + couples. •  $f^{0,5}(i,j,t)$ : number of children in age-group 0-5
  - $\tau_c^{0.5}$ : child care cost, pct of income (estimated)
- $f^{6,11}(i,j,t)$ : number of children in age-group 6-11  $\tau_c^{6,11}$ : child care cost, pct of income (estimated)
- f(1, 1, t) = 0 (single men)

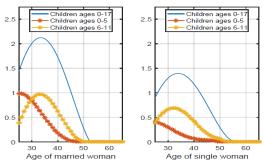


Figure: Figure 5 in Online Appendix. 1945 cohort.

## viarriage and Divorce

Marriage probability depends on wage-shock

$$v_{t+1}(i, \epsilon_t^i) = \Pr(j_{t+1} = 2|j_t = 1, t, i, \epsilon_t^i)$$

• Probability of matching a partner with states  $(a_{t+1}^p, \overline{y}_{t+1}^p, \epsilon_{t+1}^p)$ :

$$\Pr(\mathbf{a}_{t+1}^p, \overline{\mathbf{y}}_{t+1}^p, \boldsymbol{\epsilon}_{t+1}^p | \boldsymbol{\epsilon}_t^i, i) = \boldsymbol{\theta}_{t+1}(\mathbf{a}_{t+1}^p, \overline{\mathbf{y}}_{t+1}^p | \boldsymbol{\epsilon}_{t+1}^p) \cdot \boldsymbol{\xi}_{t+1}(\boldsymbol{\epsilon}_{t+1}^p | \boldsymbol{\epsilon}_t^i, i)$$



## • Marriage probability depends on wage-shock

 $v_{t+1}(i, \epsilon_{t}^{i}) = \Pr(j_{t+1} = 2|j_{t} = 1, t, i, \epsilon_{t}^{i})$ 

• Probability of matching a partner with states  $(a_{t+1}^p,\overline{y}_{t+1}^p,\epsilon_{t+1}^p)$ :

$$\Pr(\mathbf{a}_{t+1}^{p},\overline{\mathbf{y}}_{t+1}^{p},\epsilon_{t+1}^{p}|\epsilon_{t}^{i},i) = \theta_{t+1}(\mathbf{a}_{t+1}^{p},\overline{\mathbf{y}}_{t+1}^{p}|\epsilon_{t+1}^{p}) \cdot \xi_{t+1}(\epsilon_{t+1}^{p}|\epsilon_{t}^{i},i)$$

• Divorce probability depends on both members wage shocks

$$\zeta_{t+1}(\epsilon_t^1, \epsilon_t^2) = \Pr(j_{t+1} = 1 | j_t = 2, t, \epsilon_t^1, \epsilon_t^2)$$

• Wealth equally split + no alimony.

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• Bellman Equation for couple is (subject to (1) and (2))

$$\begin{split} W^{c}_{t}(a_{t}, \epsilon^{1}_{t}, \epsilon^{2}_{t}, \overline{y}^{1}_{t}, \overline{y}^{2}_{t}) &= \max_{c_{t}, n^{1}_{t}, n^{2}_{t}} w(c_{t}, l^{1}_{t}, l^{2}_{t}) \\ &+ (1 - \zeta_{t+1}) \beta \mathbb{E}_{t}[W^{c}_{t+1}(a_{t+1}, \epsilon^{1}_{t+1}, \epsilon^{2}_{t+1}, \overline{y}^{1}_{t+1}, \overline{y}^{2}_{t+1})] \\ &+ \zeta_{t+1} \beta \sum_{i=1}^{2} \mathbb{E}_{t}[W^{s}_{t+1}(i, a_{t+1}/2, \epsilon^{i}_{t+1}, \overline{y}^{i}_{t+1})] \\ &\text{s.t.} \end{split}$$

$$a_{t+1} = (1+r)a_t + Y_t^1 + Y_t^2(1-\tau_c(2,2,t)) - c_t$$

$$-\tau_t^{SS} \sum_{i=1}^2 \min(Y_t^i, \tilde{y}_t) - T(ra_t + Y_t^1 + Y_t^2, 2, t)$$

where

 $W_{t+1}^{s}(\bullet)$  is value of being single

$$\mathbb{E}_t[W_{t+1}^t(\mathbf{a}_{t+1}, \epsilon_{t+1}^1, \epsilon_{t+1}^2, \overline{V}_{t+1}^1]$$

$$\mathbb{E}_{t}[W_{t+1}^{c}(a_{t+1}, \epsilon_{t+1}^{1}, \epsilon_{t+1}^{2}, \overline{y}_{t+1}^{1}, \overline{y}_{t+1}^{2})] = \int W_{t+1}^{c}(\bullet, \exp(\rho_{\epsilon}^{1} \log \epsilon_{t}^{1} + v_{t+1}^{1}), \exp(\rho_{\epsilon}^{2} \log \epsilon_{t}^{2} + v_{t+1}^{1}))$$

## Outline

Simulation Results

# Labor Supply Elasticities

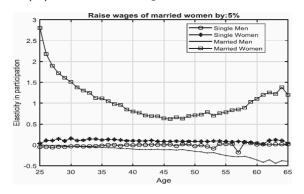
#### • Frisch: Anticipated transitory income changes

TABLE 4
Model-implied elasticities of labour supply

	Participation				Hours among workers				
	Married		Single		Mai	ried	Single		
	W	M	W	M	W	M	W	M	
30	1.0	0.0	0.5	0.2	0.2	0.3	0.4	0.4	
40	0.7	0.1	0.4	0.2	0.4	0.5	0.4	0.5	
50	0.6	0.2	0.4	0.5	0.4	0.5	0.8	0.5	
60	1.1	0.8	1.8	1.4	0.3	0.3	0.5	0.4	

- Highest for women
- Extensive margin important

• Marshall: permanent increase in wages of women from age 25  $(t_0)$ , I think, i.e. "regime shift".



- Large for married women
- U-shaped
  - Small negative cross-elasticity for men.

## Counterfactual Policy Simulations

Remove the Joint taxation.

Unclear exactly how, but I think it is like

$$a_{t+1} = (1+r)a_t + Y_t^1 + Y_t^2(1 - \tau_c(2, 2, t)) - c_t - \tau_t^{SS} \sum_{i=1}^{2} \min(Y_t^i, \tilde{y}_t) - T(ra_t/2 + Y_t^1, 1, 1, t) - T(ra_t/2 + Y_t^2, 2, 1, t)$$

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• Balance government budget by changing  $\lambda_t^{i,j}$  in

$$T(Y, i, j, t) = (1 - \lambda_t^{i,j} Y^{-\tau_t^{i,j}}) \cdot Y$$

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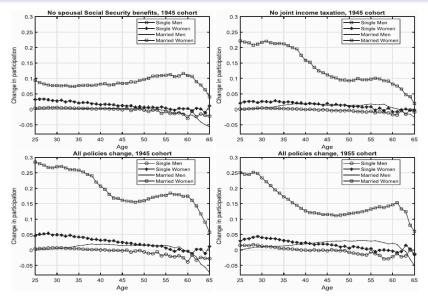
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Also: Remove spousal dependence on social and survivor benefits
 Only affects in later life stages (ignore a bit here)



## Simulation Results: Welfare

• Welfare effects: Level of wealth at age 25  $(t_0)$  in the baseline model that makes individuals indifferent between the baseline and the new

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- Let the alternative value be (all couples here)

$$V^{reform} = \frac{1}{s} \sum_{s=1}^{s} V_{t_0}(a_{s,t_0}, \epsilon_{s,t_0}^1, \epsilon_{s,t_0}^2, \overline{y}_{s,t_0}^1, \overline{y}_{s,t_0}^2; reform)$$

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Let baseline value be

$$V^{base}(a) = \frac{1}{s} \sum_{s=1}^{s} V_{t_0}(a_{s,t_0} + a, \epsilon_{s,t_0}^1, \epsilon_{s,t_0}^2, \overline{y}_{s,t_0}^1, \overline{y}_{s,t_0}^2)$$

as a function of additional initial wealth, a.

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as a function of additional initial wealth, a.

Asset compensation required

$$a^* = \{a : V^{reform} - V^{base}(a) = 0\}$$

(normalized by avg income:  $\frac{1}{2}a^{\star}/(\overline{y}_{s,t_0}^1+\overline{y}_{s,t_0}^2)$  (?))

## Simulation Results: Welfare

TABLE 7 Asset compensation required for staying in the benchmark economy, normalized as a fraction of average income

	All			Winners			Losers		
	Couples	SW	SM	Couples	sw	SM	Couples	SW	SM
1945 cohort									
(1) Remove Socia	l Security spo	ousal benefi	ts, unbala	nced budget					
Average	-0.24	-0.20	0.25	0.00	0.00	0.25	-0.24	-0.20	-0.02
Percentage				0.0	0.0	100.0	100.0	100.0	0.0
(2) Remove Socia	1 Security spo	ousal benefi	ts, balanc	ed budget					
Average	0.66	0.19	1.15	0.66	0.20	1.15	0.00	-0.03	0.00
Percentage				100.0	92.5	100.0	0.0	7.5	0.0
(3) Remove joint	income taxati	on, unbalan	iced budg	et					
Average	0.06	-0.18	0.81	0.29	0.06	0.81	-0.19	-0.19	0.00
Percentage				52.8	4.9	100.0	47.2	95.1	0.0
(4) Remove joint	income taxati	on, balance	d budget						
Average	0.31	-0.08	1.06	0.42	0.12	1.06	-0.09	-0.13	0.00
Percentage				78.8	20.6	100.0	21.2	79.4	0.0
(5) Remove all ma	arital-related	policies, ba	lanced bu	dget					
Average	0.80	0.05	1.97	0.80	0.33	1.97	-0.03	-0.12	0.00
Percentage				98.8	37.4	100.0	1.2	62.6	0.0
1955 cohort									
(6) Remove all ma	arital-related	policies, ba	lanced bu	dget					
Average	0.73	0.21	1.14	0.74	0.30	1.14	-0.04	-0.04	-0.03
Percentage				98.2	74.1	100.0	1.8	25.9	0.0

Notes: Top line for each experiment: average welfare gain or loss. Bottom line for each experiment: fraction in that group gaining or losing welfare. SM, single men; SW, single women.

## Outline

Model and Mechanisms

Simulation Results

3 Simple Model

## Our simple model

- Dual-earner model
- Simplifications:

No savings Couple cannot divorce (no singlehood) Deterministic (no shocks)

- Taxes:
  - On household level
- **Reform** of interest: Individual taxation

Simple Model 0000

## Recursive formulation

$$\begin{split} V_t(K_{1,t},K_{2,t}) &= \max_{h_{1,t},h_{2,t}} U(c_t,h_{1,t},h_{2,t}) + \beta V_{t+1}(K_{1,t+1},K_{2,t+1}) \\ c_t &= \sum_{j=1}^2 w_{j,t}h_{j,t} - T(w_{1,t}h_{1,t},w_{2,t}h_{2,t}) \\ \log w_{j,t} &= \alpha_{j,0} + \alpha_{j,1}K_{j,t}, \ j \in \{1,2\} \\ K_{j,t+1} &= (1-\delta)K_{j,t} + h_{j,t}, \ j \in \{1,2\} \end{split}$$

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Preferences are sum of individual

$$U(c_t, h_{1,t}, h_{2,t}) = 2 \frac{(c_t/2)^{1+\eta}}{1+\eta} - \rho_1 \frac{h_{1,t}^{1+\gamma}}{1+\gamma} - \rho_2 \frac{h_{2,t}^{1+\gamma}}{1+\gamma}$$

#### Recursive formulation

$$V_{t}(K_{1,t}, K_{2,t}) = \max_{h_{1,t}, h_{2,t}} U(c_{t}, h_{1,t}, h_{2,t}) + \beta V_{t+1}(K_{1,t+1}, K_{2,t+1})$$

$$c_{t} = \sum_{j=1}^{2} w_{j,t} h_{j,t} - T(w_{1,t} h_{1,t}, w_{2,t} h_{2,t})$$

$$\log w_{j,t} = \alpha_{j,0} + \alpha_{j,1} K_{j,t}, j \in \{1, 2\}$$

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Taxes are

$$T(Y_1, Y_2) = (1 - \lambda(Y_1 + Y_2)^{-\tau}) \cdot (Y_1 + Y_2)$$

## Next Time

#### Next time:

Labor supply and children.

#### Literature:

Guner, Kaygusuz and Ventura (2020): "Child-Related Transfers, Household Labor Supply and Welfare"

- Read before lecture
- Reading guide:

(focus on types child-related transfers + policy experiments)

Section 1: Introduction + topic. Super important - Read.

Section 2: Background, US. Read.

Section 3: Model. Complex. Get the idea. Focus on married couples and childcare costs.

Section 4: Calibrations Skim

Section 5: Understanding childcare subsidies. Key - read.

Section 6: Counterfactual policies. Key - read.

## References I

- BORELLA, M., M. DE NARDI AND F. YANG (forthcoming): "Are Marriage-Related Taxes and Social Security Benefits Holding Back Female Labor Supply?," *Review of Economic Studies*.
- Guner, N., R. Kaygusuz and G. Ventura (2020): "Child-Related Transfers, Household Labor Supply and Welfare," *Review of Economic Studies*, 87(5), 2290–2321.