Boring but important disclaimers:

- ▶ If you are not getting this from the GitHub repository or the associated Canvas page (e.g. CourseHero, Chegg etc.), you are probably getting the substandard version of these slides Don't pay money for those, because you can get the most updated version for free at

    https://github.com/julianmak/academic-notes

    The repository principally contains the compiled products rather than the source for size reasons.

- ▶ Associated Python code (as Jupyter notebooks mostly) will be held on the same repository. The source data however might be big, so I am going to be naughty and possibly just refer you to where you might get the data if that is the case (e.g. JRA-55 data). I know I should make properly reproducible binders etc., but I didn't...

- ▶ I do not claim the compiled products and/or code are completely mistake free (e.g. I know I don't write Pythonic code). Use the material however you like, but use it at your own risk.

- ▶ As said on the repository, I have tried to honestly use content that is self made, open source or explicitly open for fair use, and citations should be there. If however you are the copyright holder and you want the material taken down, please flag up the issue accordingly and I will happily try and swap out the relevant material.

<u>OCES 3301</u> :
basic Data Analysis in ocean sciences

Session 7: fairly basic time-series analysis

Outline

(Just overview here; for actual content see Jupyter notebooks)

- ▶ time-series data
  - → recall: frequency, wavelength, wavenumbers etc.
- ▶ basic manipulations
  - → filtering (high and low pass) and kernels
  - → trends (just regression)
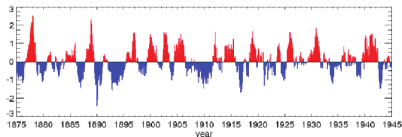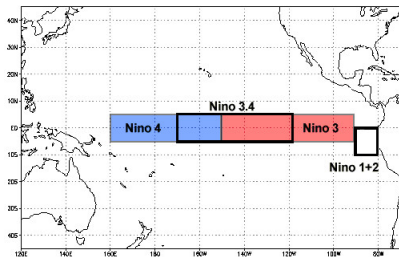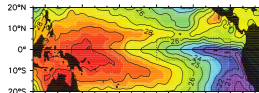 - → lag analysis (also just regression)

Time-series data
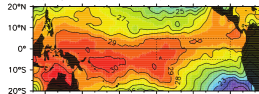

Figure: The eternal bendy boi.

Time-series data

- recall El-Niño data (lec 02)

  → SST data over time
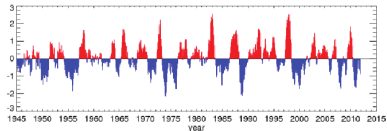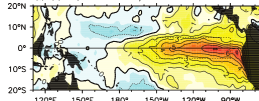
- detrended averaged signal here
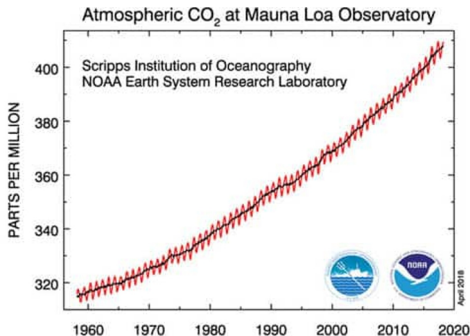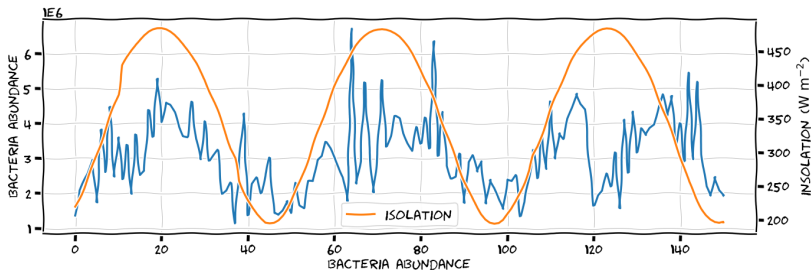
Time-series data

- Keeling curve
  → atmospheric CO_2 concentration at one spot
- rolling average given as black line
  → non-linear trend?

Atmospheric CO_2 at Mauna Loa Observatory

Scripps Institution of Oceanography
NOAA Earth System Research Laboratory

Time-series data

- ▶ bacteria data from Charmaine (see assignment 2)
    - → some oscillation period/frequency?
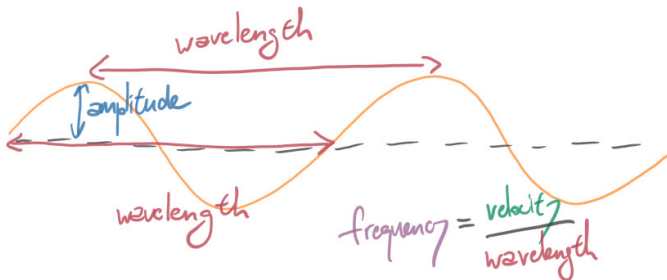   - → some correlation?

Recall: waves

Figure: Schematic of wave features. Box length $L = 2\pi$ for simplicity.

▶ displacement η described by (could also be sine)

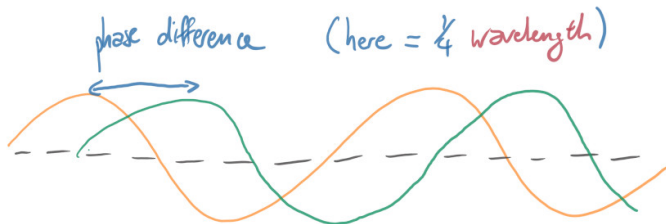$$\eta \sim A\cos(x - vt), \qquad \gamma = v/\lambda$$

Recall: waves

Figure: Schematic of wave features. Box length $L = 2\pi$ for simplicity.

▶ displacement η described by (could also be sine)

$$\eta \sim A\cos(x), \qquad \eta \sim A\cos(x - \lambda/4)$$
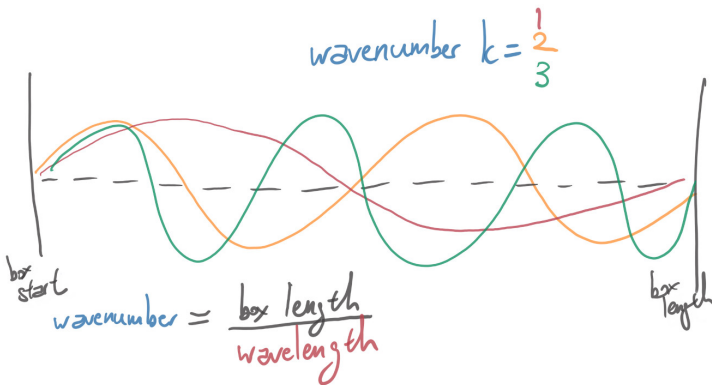
Recall: waves

Figure: Schematic of wave features. Box length $L = 2\pi$ for simplicity.

▶ displacement η described by (could also be sine)

$$\eta \sim A\cos(2x), \qquad \eta \sim A\cos(1x), \qquad \eta \sim A\cos(3x)$$

Recall: waves

$$\gamma = \frac{v}{\lambda}, \qquad k = \frac{2\pi}{\lambda}$$

- ▶ γ the frequency (units: $s^{-1} = Hz$)

  $\rightarrow$ how quickly the wave oscillates
- ▶ $v = c_p$ the **phase** velocity

  $\rightarrow$ how fast the wave itself moves around
- ▶ λ the wavelength

  $\rightarrow$ how long the wave is
- ▶ k the wavenumber

  $\rightarrow$ intuitively how many waves can you fit in a box (so $k \sim \lambda^{-1}$)

  $\rightarrow$ does not necessarily have to be an integer
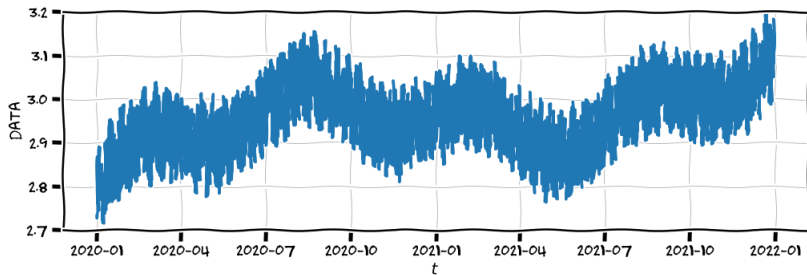
Idealised example

Figure: A dense signal.

Idealised example

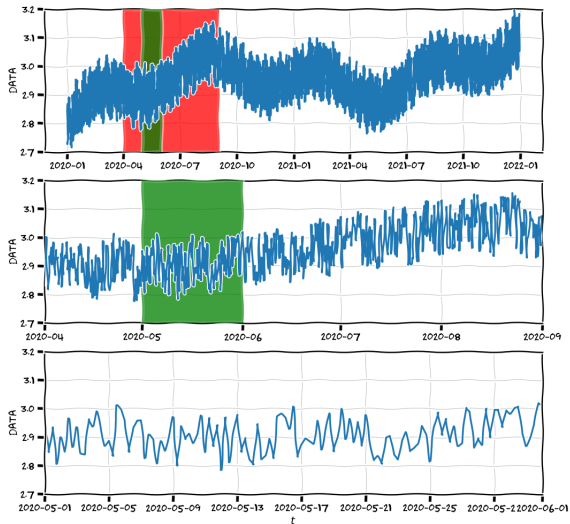**Figure:** A dense signal: zoomed in.

Idealised example: filtering

▶ noise/fluctuations coexisting with 'real' signal (cf. 05, 06)

$\rightarrow$ how to pick these out?

$\rightarrow$ average over some window?
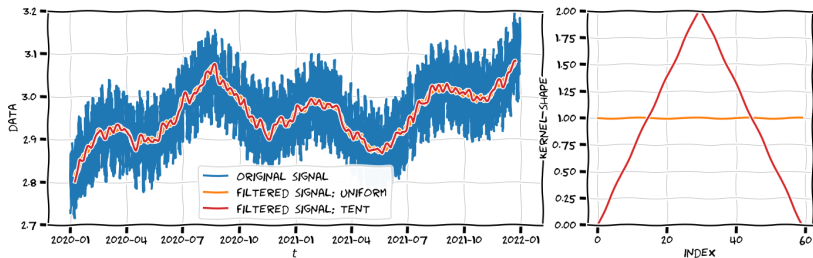
Idealised example: filtering

Figure: A dense signal: moving window average.

- ▶ uniform window (moving boxcar)
- ▶ tent
- ▶ others

Idealised example: convolution with kernel

▶ low-pass filtering is when you filter out the high frequencies (so leaving the low frequencies intact) by some averaging etc.

▶ formally down through a convolution

$$f^<(t) = (f * G)(t) = \int f(\tau)G(t - \tau) \, d\tau,$$

$\rightarrow G$ is the kernel

$\rightarrow$ averaging $\sim$ integral (sums)

$\rightarrow$ boxcar is taking $G \equiv 1/T$ in some interval of length T, and 0 outside of interval

▶ $f = f^> + f^<$, the high-passed and low-passed signal respectively

$\rightarrow$ low pass filter kills the high frequencies, and vice-versa
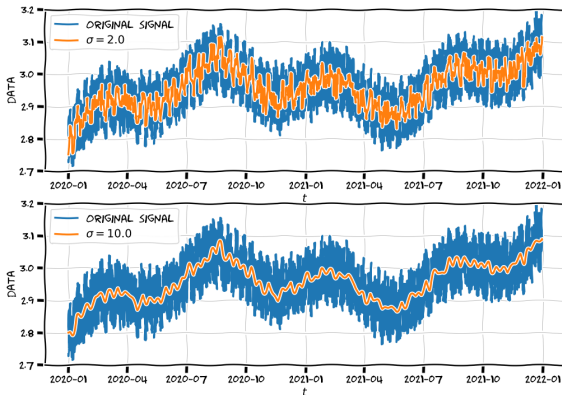
Idealised example: filtering

Figure: A dense signal: Gaussian filter.

▶ Gaussian kernel here (cf. lec05; see two slides)

→ often used in image processing (e.g. 'blurring')

Idealised example: trends

▶ normally *linear trends*
  → just linear regression...
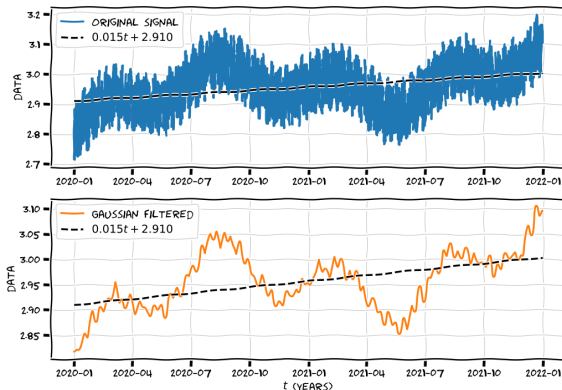 → preserved by filtering?

Figure: A dense signal: linear trend.

Idealised example: trends

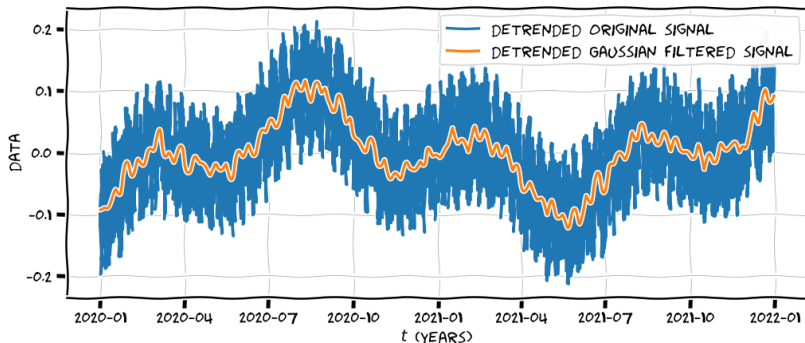▶ detrend to get anomalies with respect to the linear trend

→ come back to this in 08

Figure: A dense signal: linear trend.

Idealised example: correlations

▶ again, just linear correlations
  $\rightarrow$ compare two data at the same time
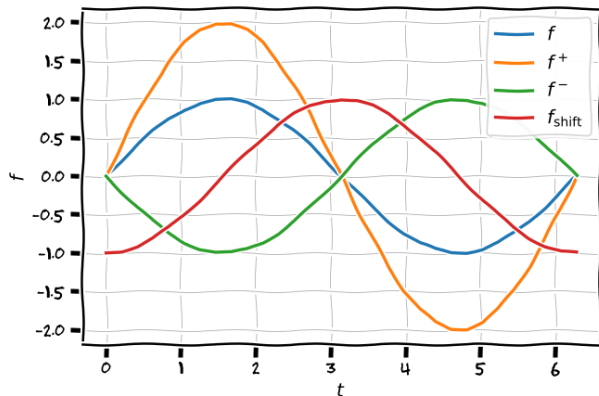

Figure: What is the expected linear correlation here (with respect to f)?
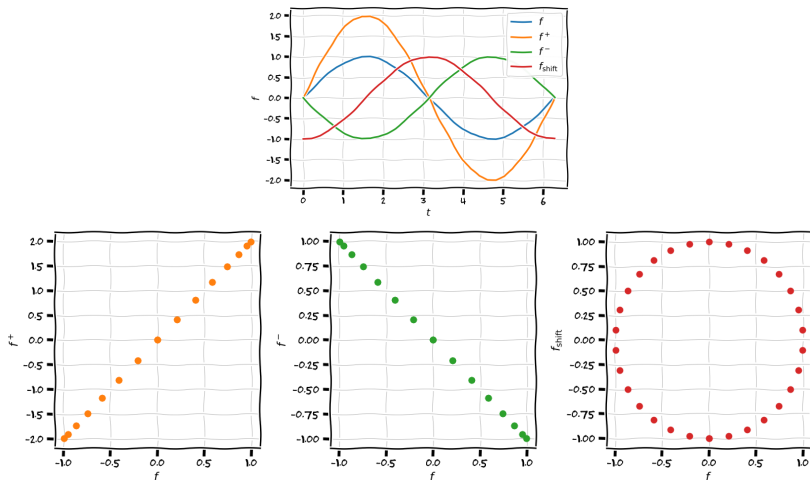
Idealised example: correlations

Figure: As above figure but shown in a slightly different way, might be easier to see...
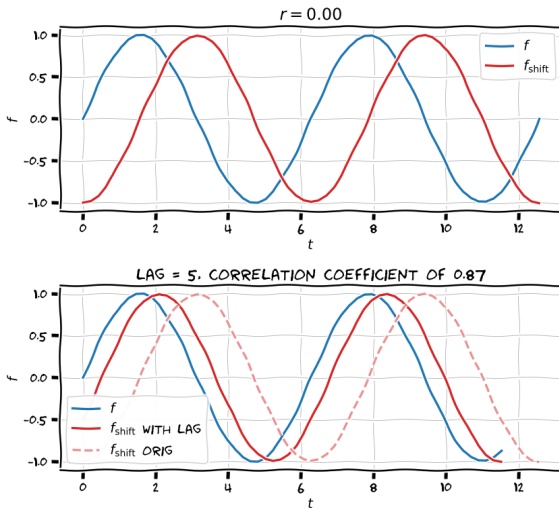
Idealised example: lag correlations

Figure: Correlation of original and shifted signals.

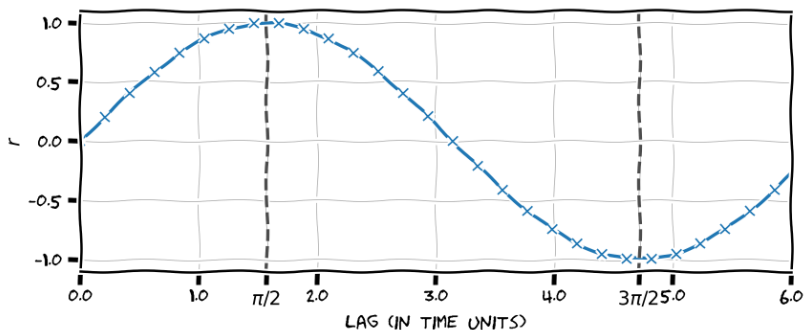# Idealised example: lag correlations

Figure: Correlation of above signal as a function of lag (are max and min values consistent with expectations?)

Idealised example: auto-correlations

▶ **auto** means 'self'

  → correlation of lagged versions of itself

▶ one interpretation of how 'predictable' something is

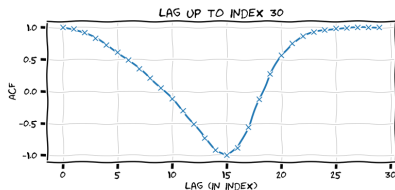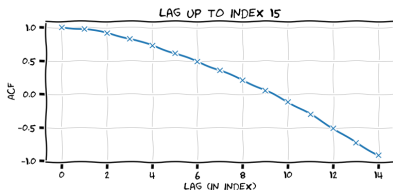 → the `statsmodel` version does something slightly different

Figure: Auto-correlation of a simple signal (why is there an apparent asymmetry?)

Jupyter notebook

go to 07 Jupyter notebook to get some code practise

- ▶ with above and El-Niño 3.4 data
- ▶ could also try it with the bacteria data in assignment 2
  $\rightarrow$ just comment out my categorisation step