

Type-safe Web Programming Using Routed Multiparty Session Types in TypeScript

Anson Miu

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Second Marker: Dr. Iain Phillips

With thanks to Fangyi Zhou and Dr. Francisco Ferreira

June 22, 2020

Contributions

Type-safe Web Programming Using Routed Multiparty Session Types in TypeScript

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Targets standard industrial strength technologies and idiomatic web programming practices
2. **ROUTEDSESSIONS**: a New Theory of Multiparty Session Types with Routed Communication
Formalised new theory, proved correctness, implemented in SessionTS to support peer-to-peer interactions over server-centric network structures

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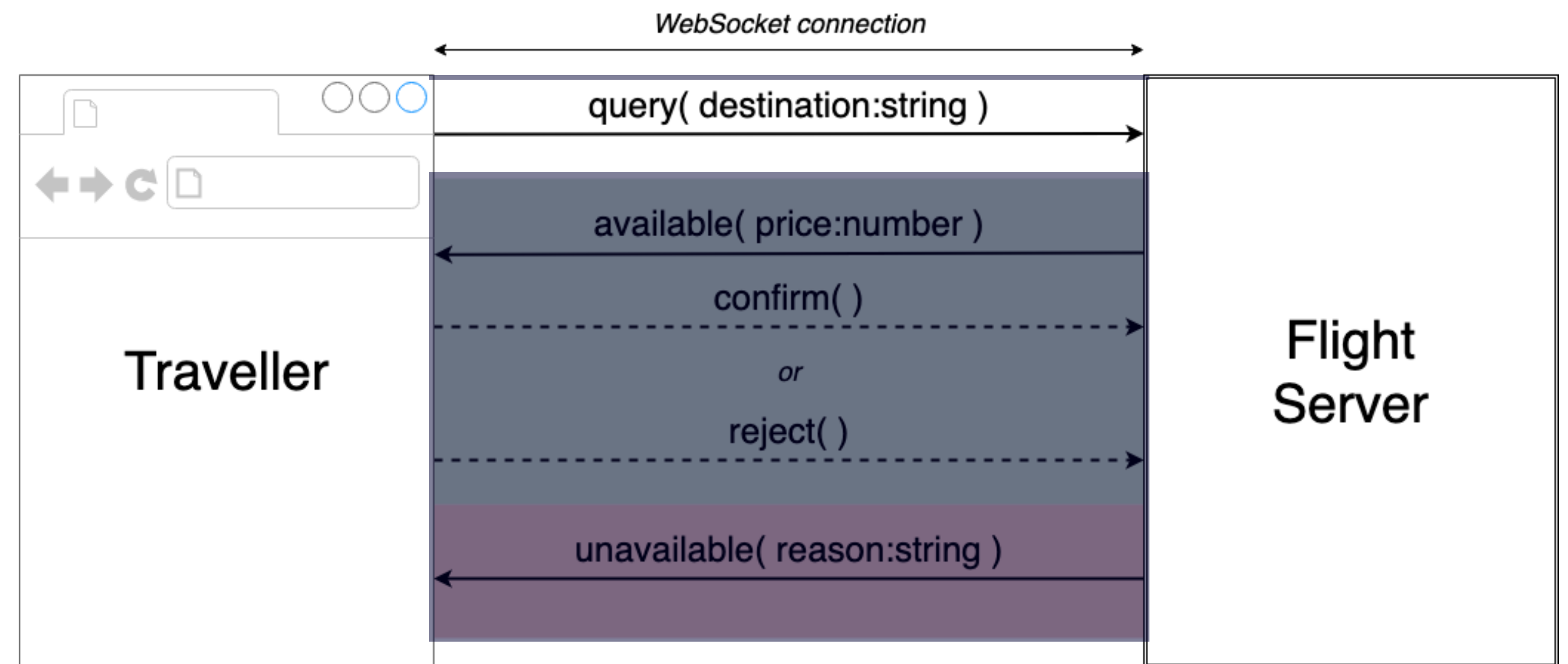
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Problem

Communication Safety in Interactive Web Applications

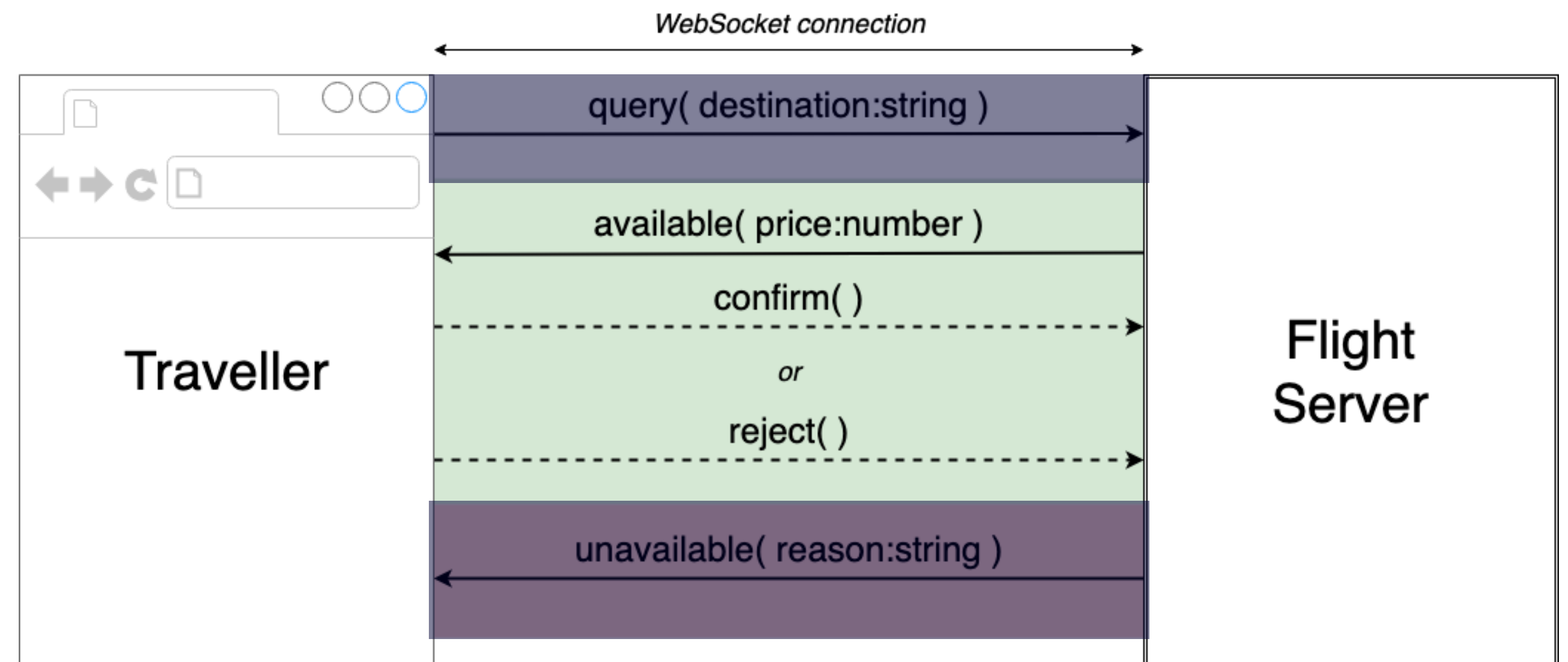
Example: Flight Booking Service

- Traveller asks Server about flight details for a particular destination.
- If available:
 - Server reserves seat
 - Server responds with price
 - Traveller responds with decision
 - If Traveller rejects, server releases seat
- Otherwise, Traveller can try again.



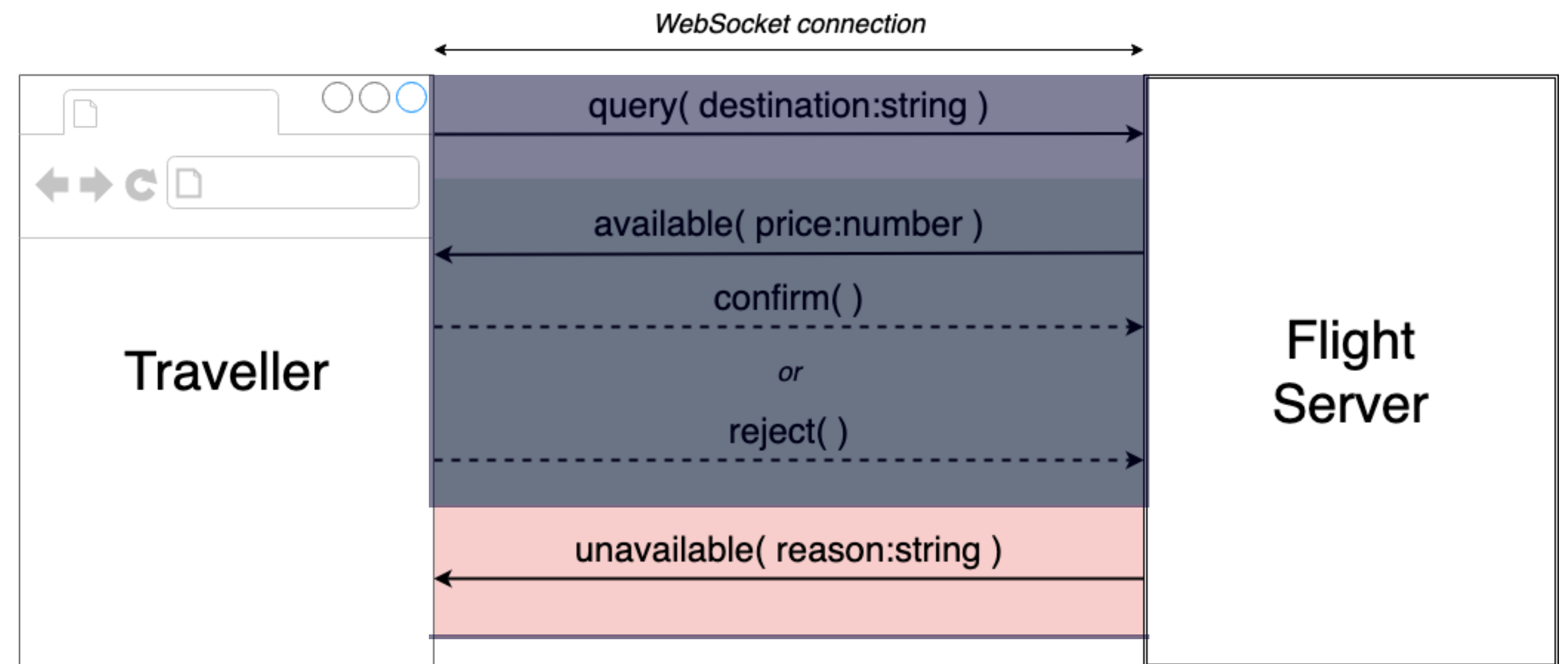
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Deadlocks

What if Traveller is waiting for quote whilst Server is waiting for destination?

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Communication Mismatch

What if Server sends *string*, but Traveller expects *number*?

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Channel Linearity Violation

What if Traveller sends query twice?
How many seats will be reserved?

Approach

using Multiparty Session Types

- (1) Specify Communication
- (2) Generate APIs from Specification

(1) Scribble Protocol Specification

```
type <typescript> "Credentials" from "./Payment" as Cred;
global protocol FlightService(role Traveller, role Server) {
  Destination(string) from Traveller to Server;
  choice at Server {
    Available(number) from Server to Traveller;
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    } or { Reject() from Traveller to Server; }
  } or {
    Full() from Server to Traveller;
    do FlightService(Traveller, Server);
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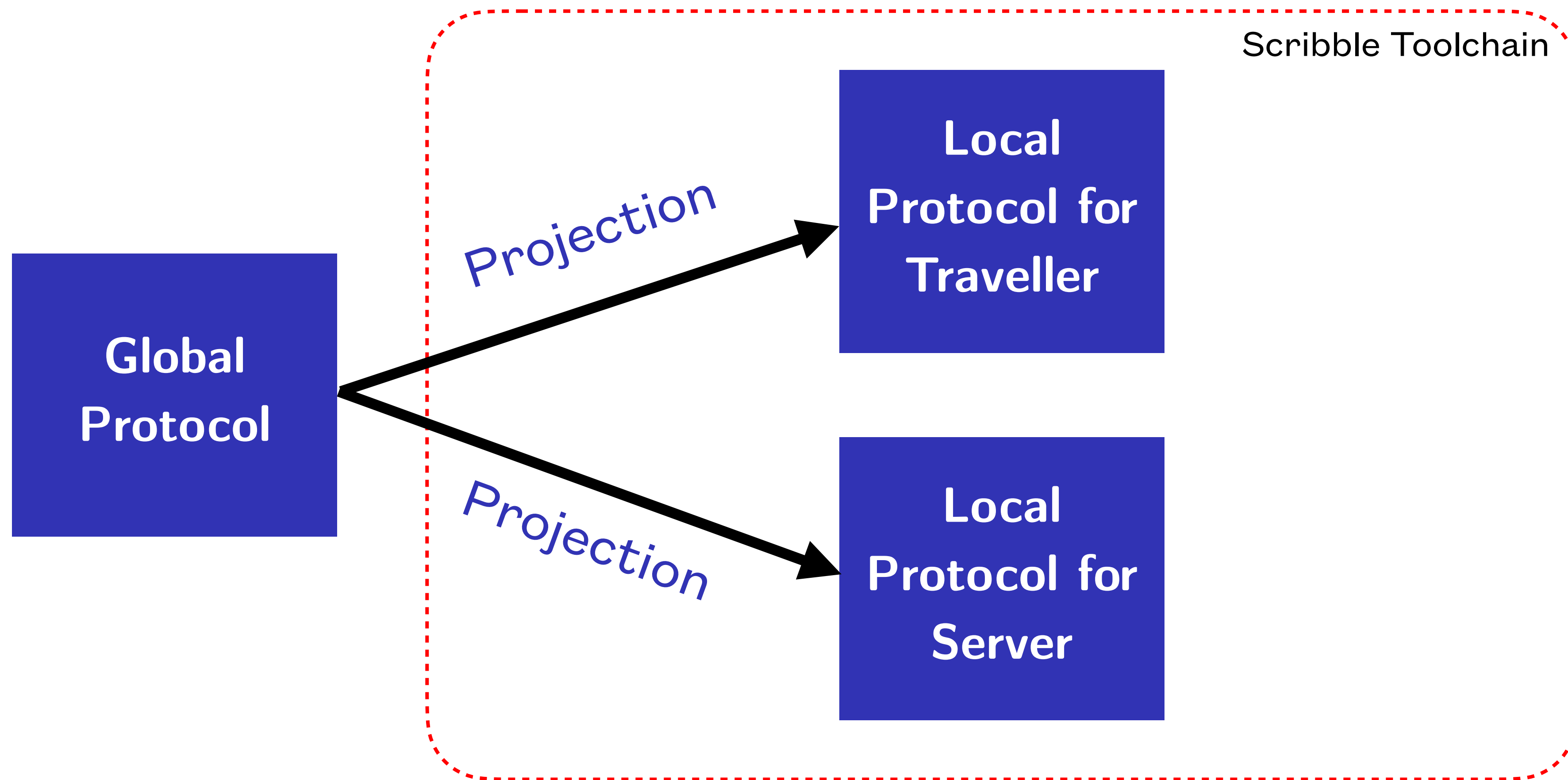
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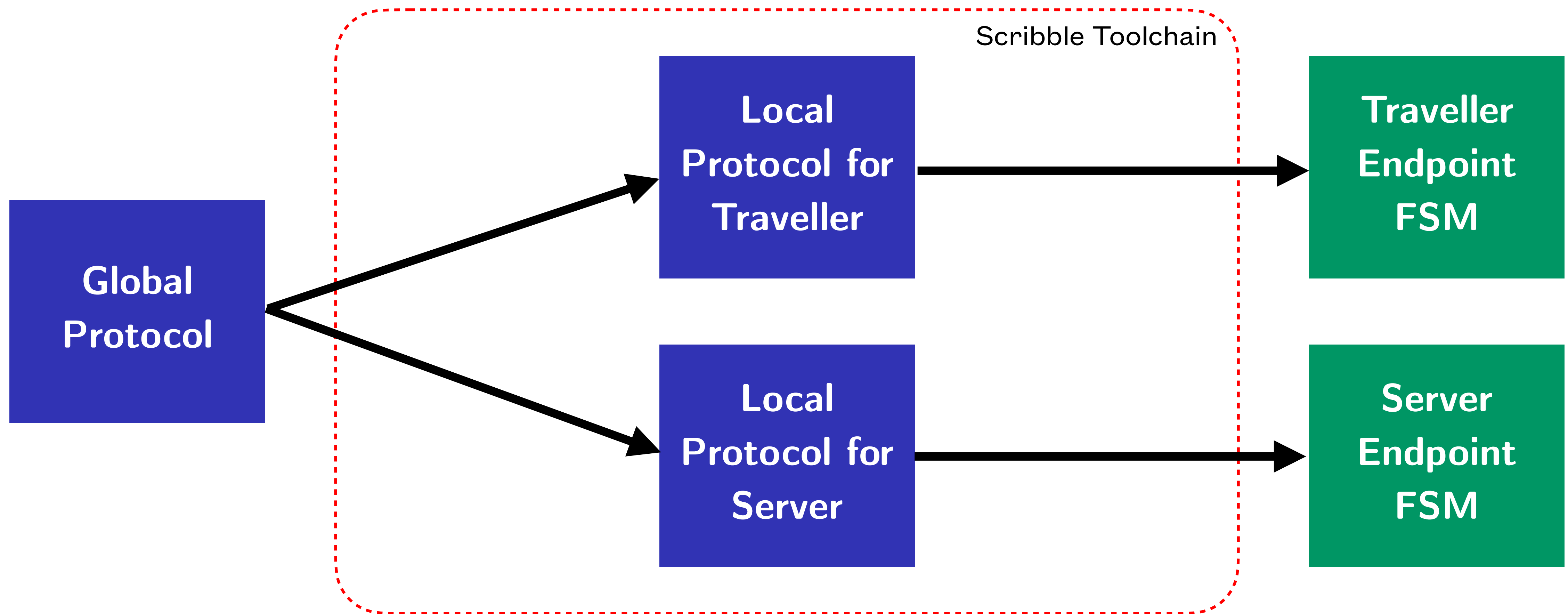
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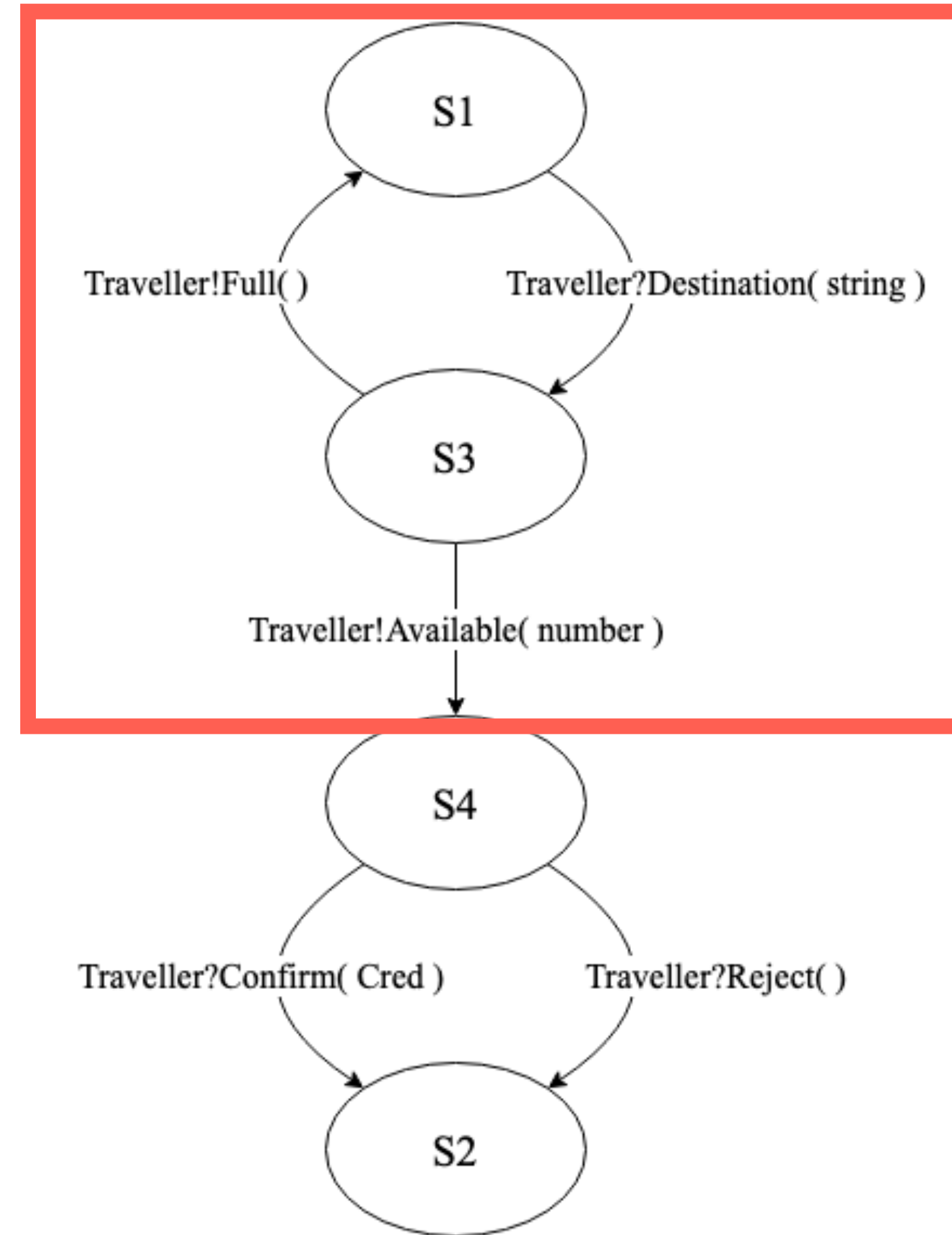


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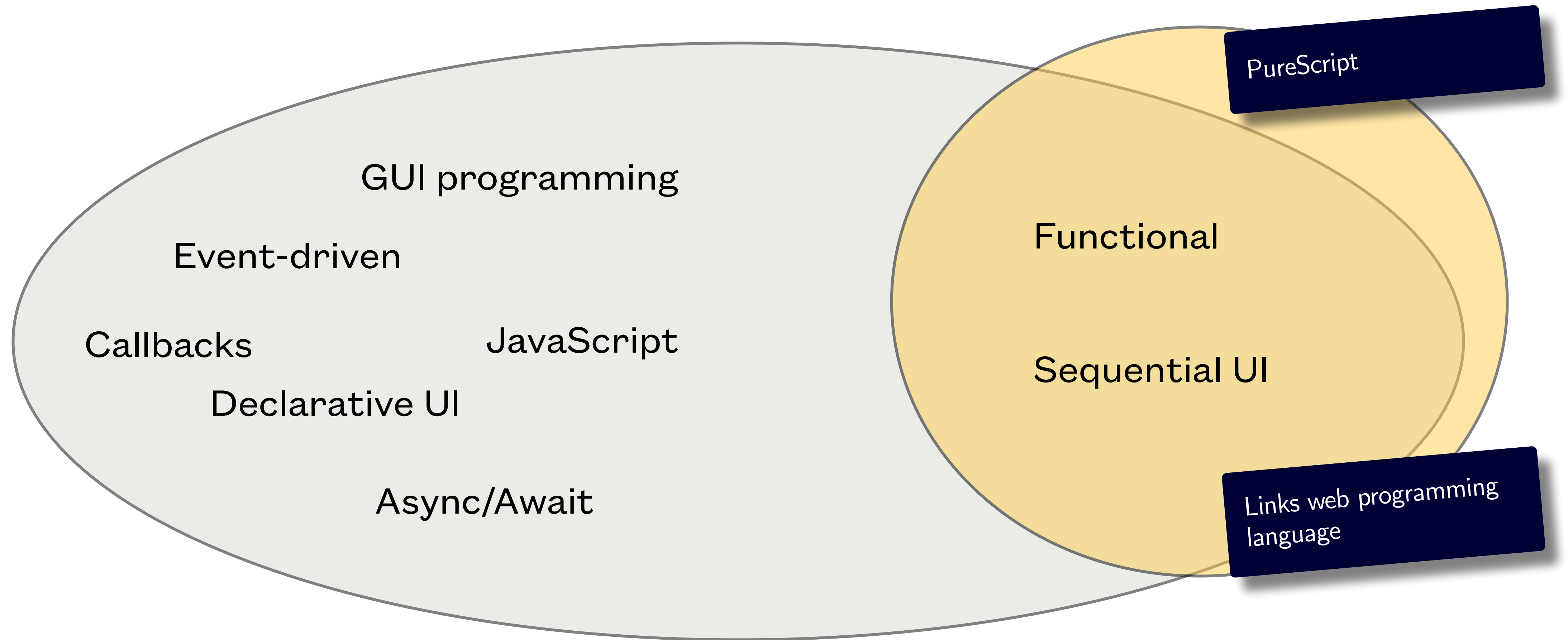
**Server
Endpoint
FSM**

Limitations of State of the Art

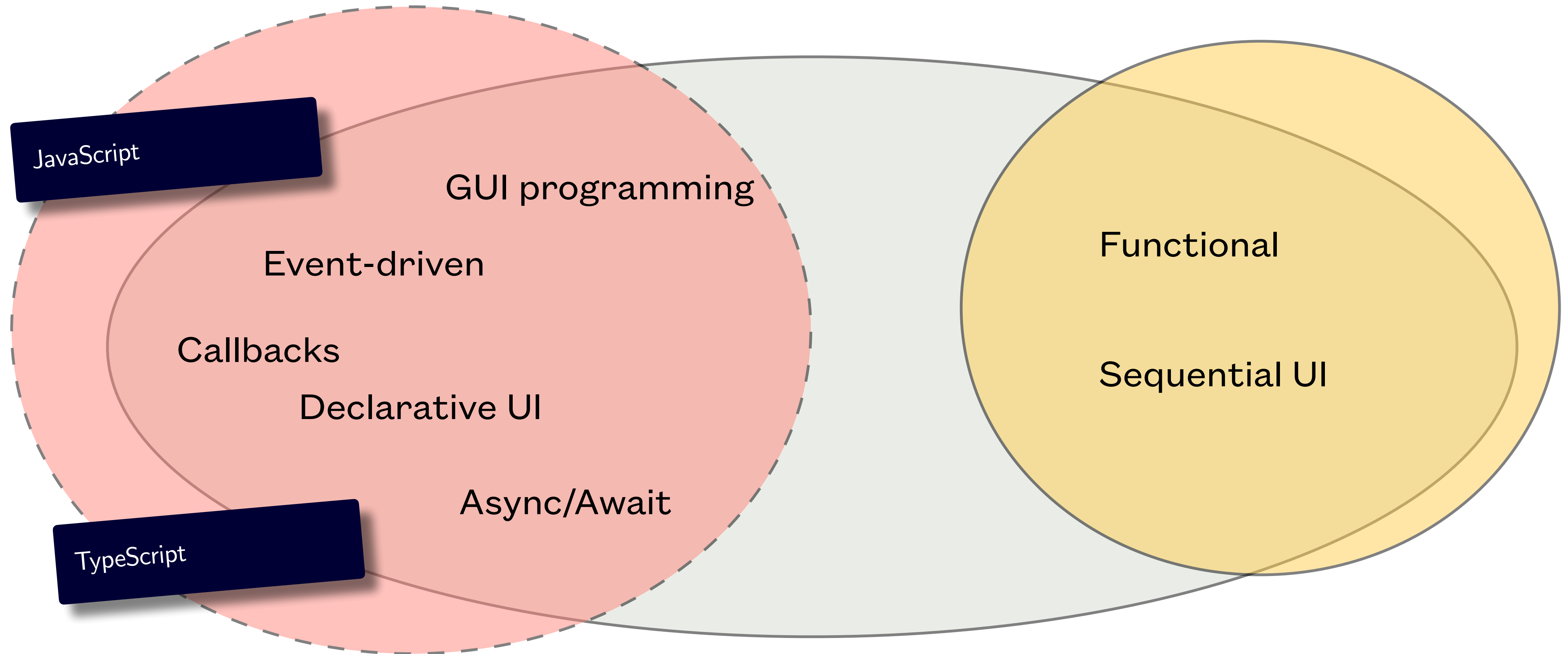
Not Widely Used

Only Server-Centric Protocols

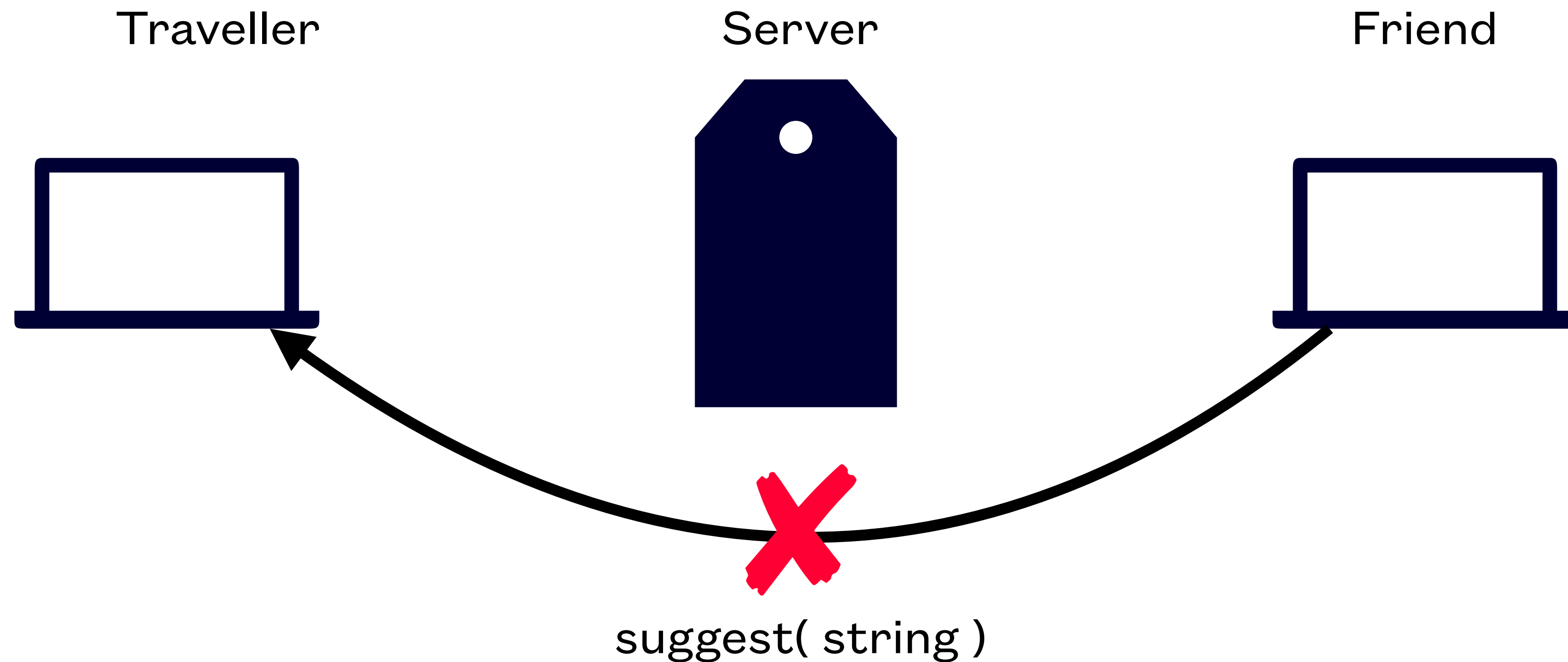
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Limitation 2: Only Server-Centric Protocols



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SessionTS

A Session Type API Code Generation Toolchain for
Modern Web Programming

Initial Work

- Accepted to the 12th International Workshop on Programming Language Approaches to Concurrency- & Communication-cEntric Software (PLACES 2020)
- Published in the *Electronic Proceedings in Theoretical Computer Science* (EPTCS)

Generating Interactive WebSocket Applications in TypeScript

Anson Miu
Imperial College London

Francisco Ferreira
Imperial College London

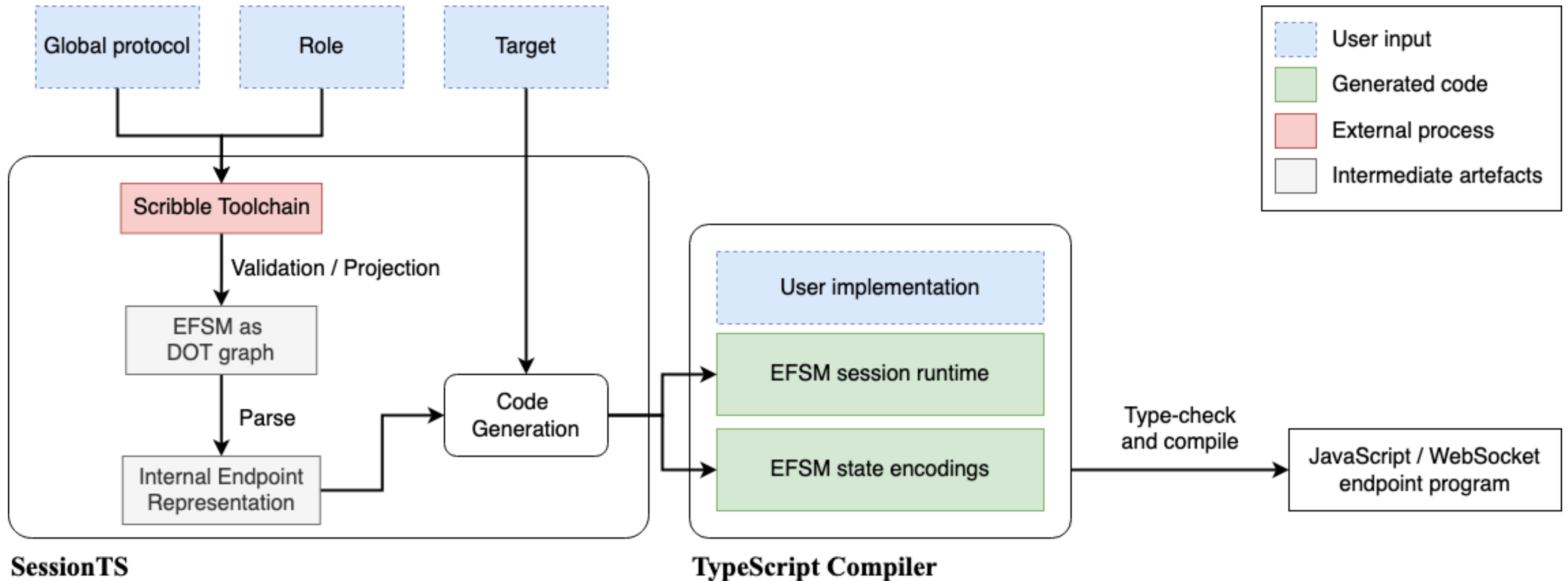
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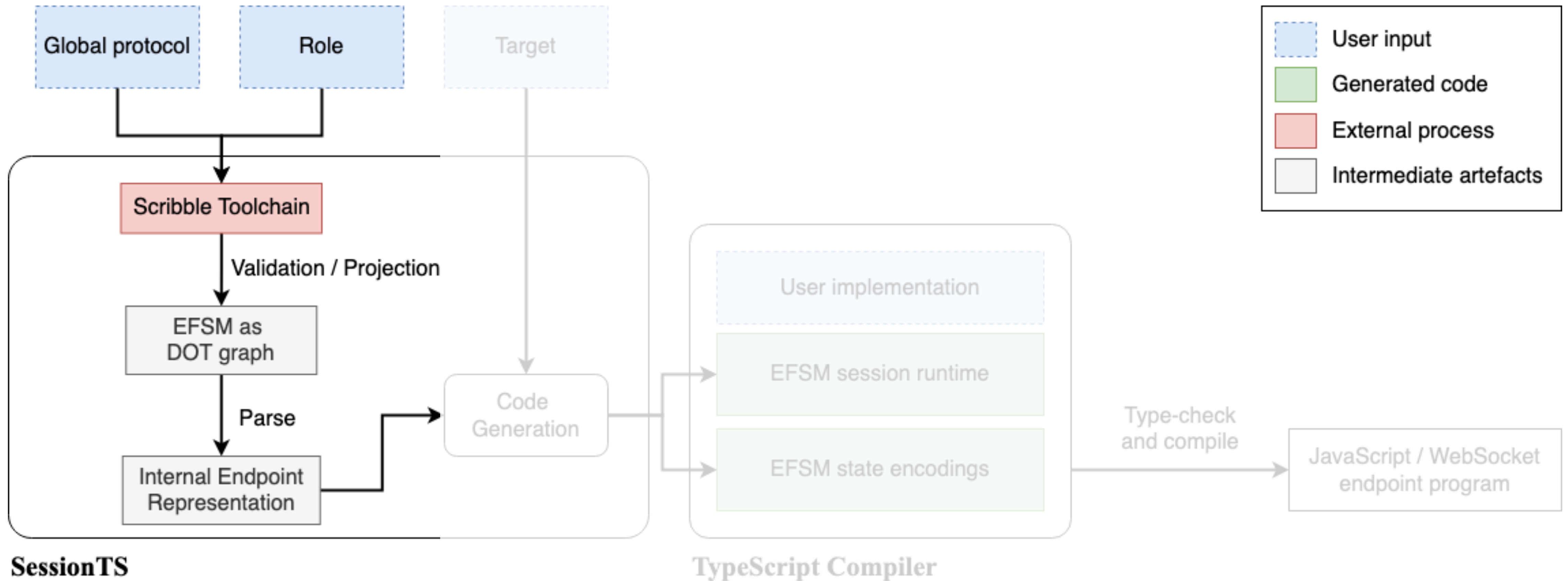
Advancements in mobile device computing power have made interactive web applications possible, allowing the web browser to render contents dynamically and support low-latency communication with the server. This comes at a cost to the developer, who now needs to reason more about correctness of communication patterns in their application as web applications support more complex communication patterns.

Multiparty session types (MPST) provide a framework for verifying conformance of implementations to their prescribed communication protocol. Existing proposals for applying the MPST framework in application developments either neglect the event-driven nature of web applications, or lack compatibility with industry tools and practices, which discourages mainstream adoption by web developers.

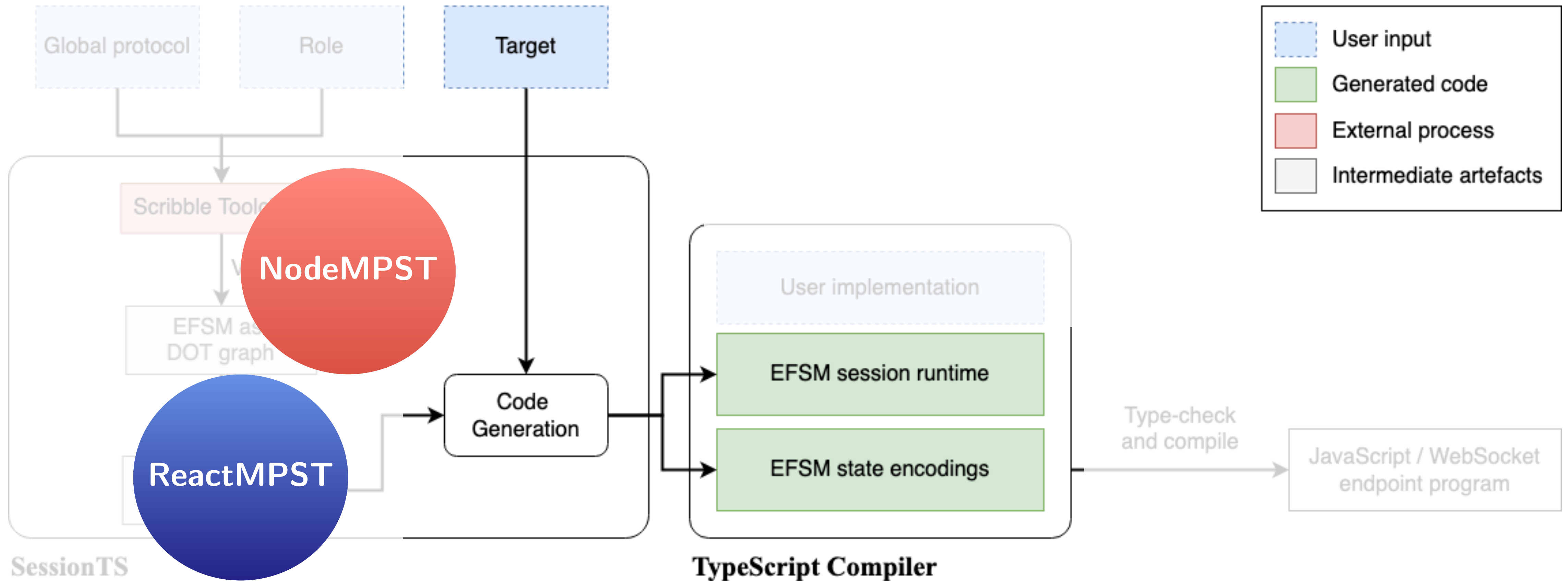
Workflow



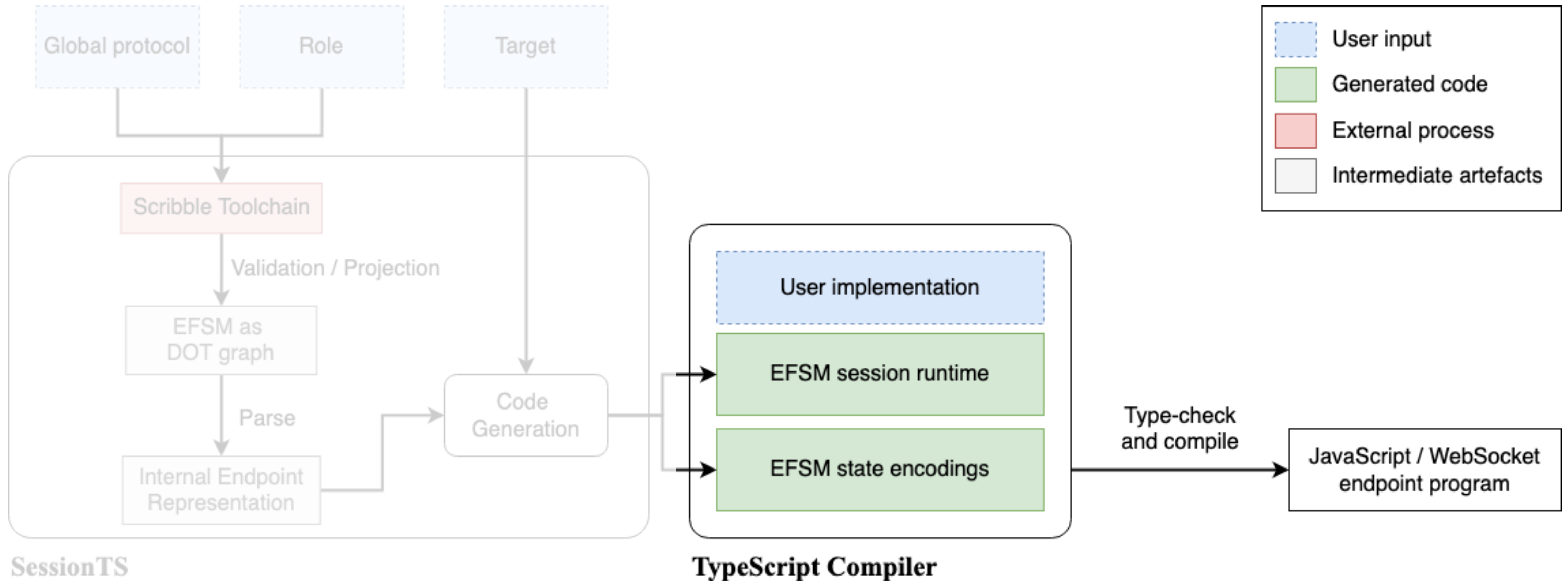
(1) Obtain EFSM from Protocol



(2) Generate APIs



(3) Implement APIs and Compile



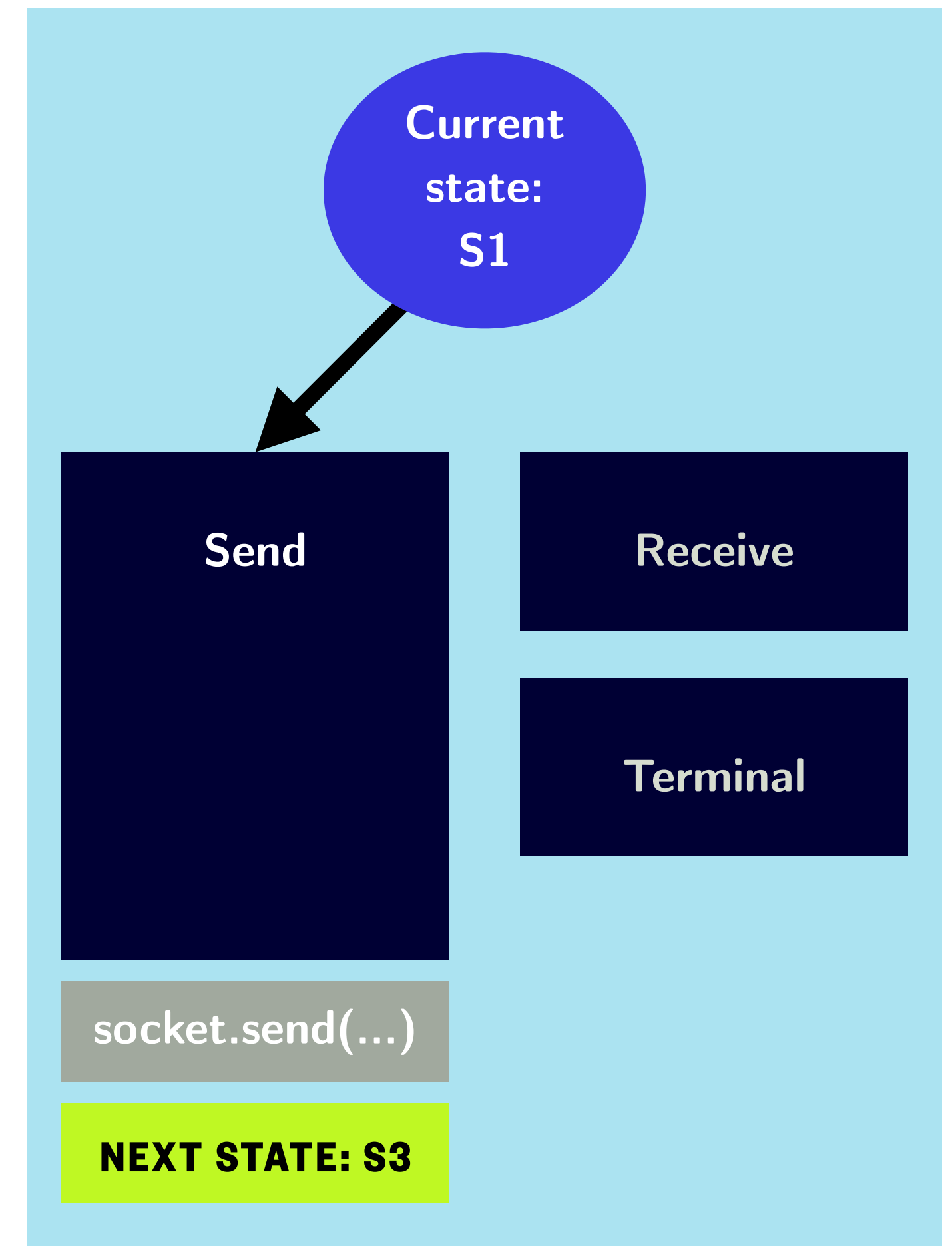
Demo

Type-safe Flight Booking Service

Design Philosophy

- We generate the session runtime to execute EFSM
 - Performs I/O action for current state
- We construct types for injecting business logic
 - What to send? How to handle receive?
- Developer instantiates session runtime with custom implementations

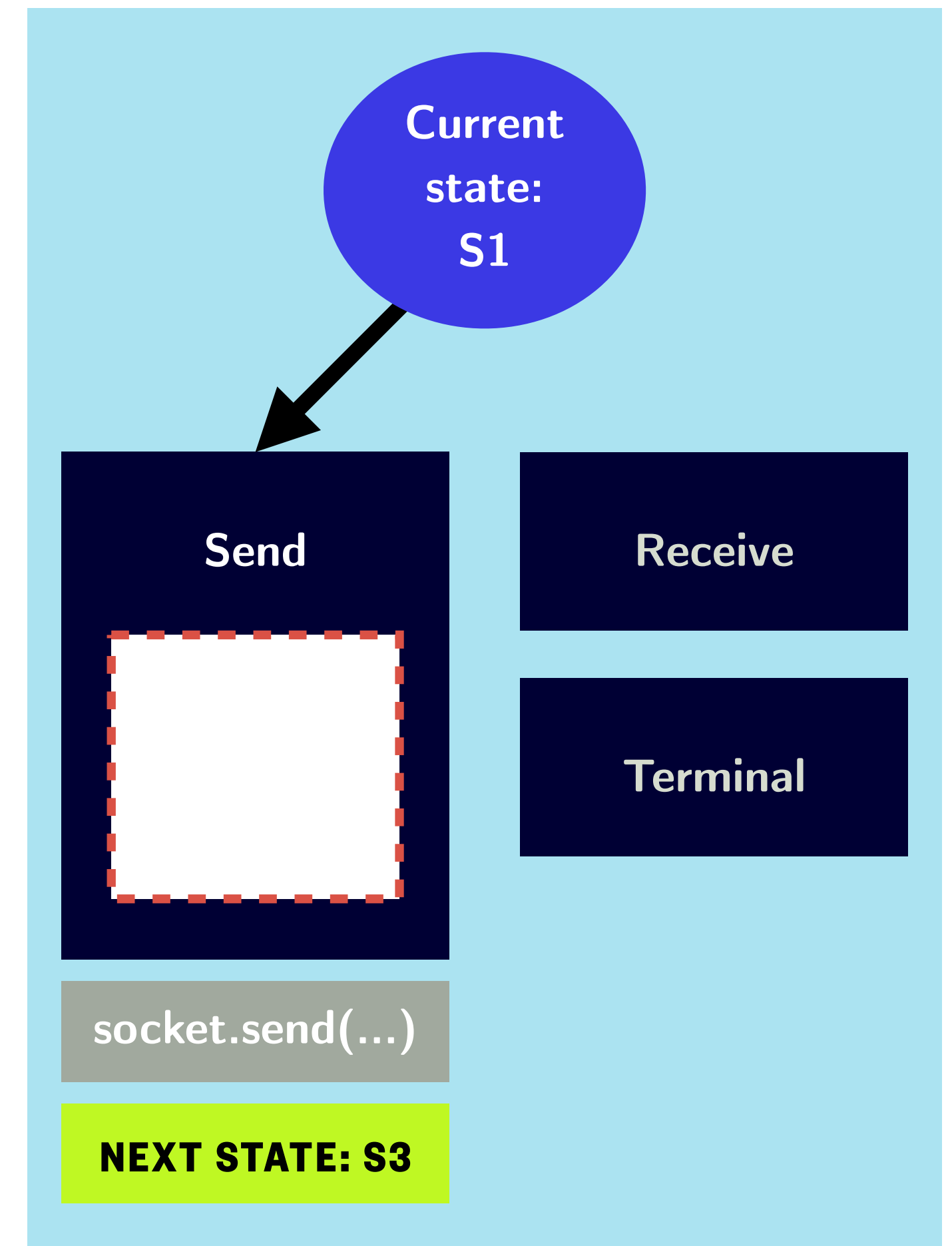
Runtime



Design Philosophy

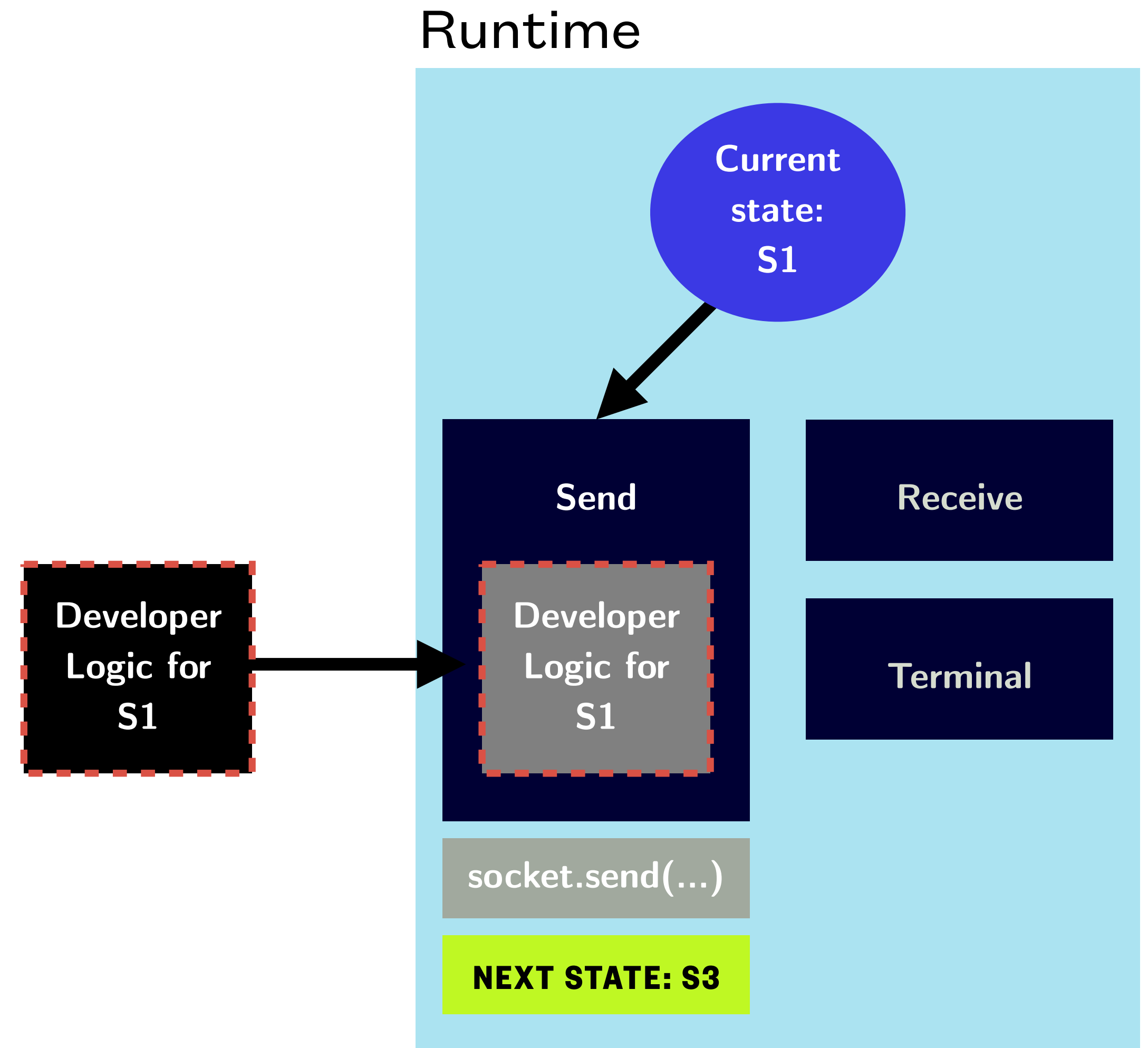
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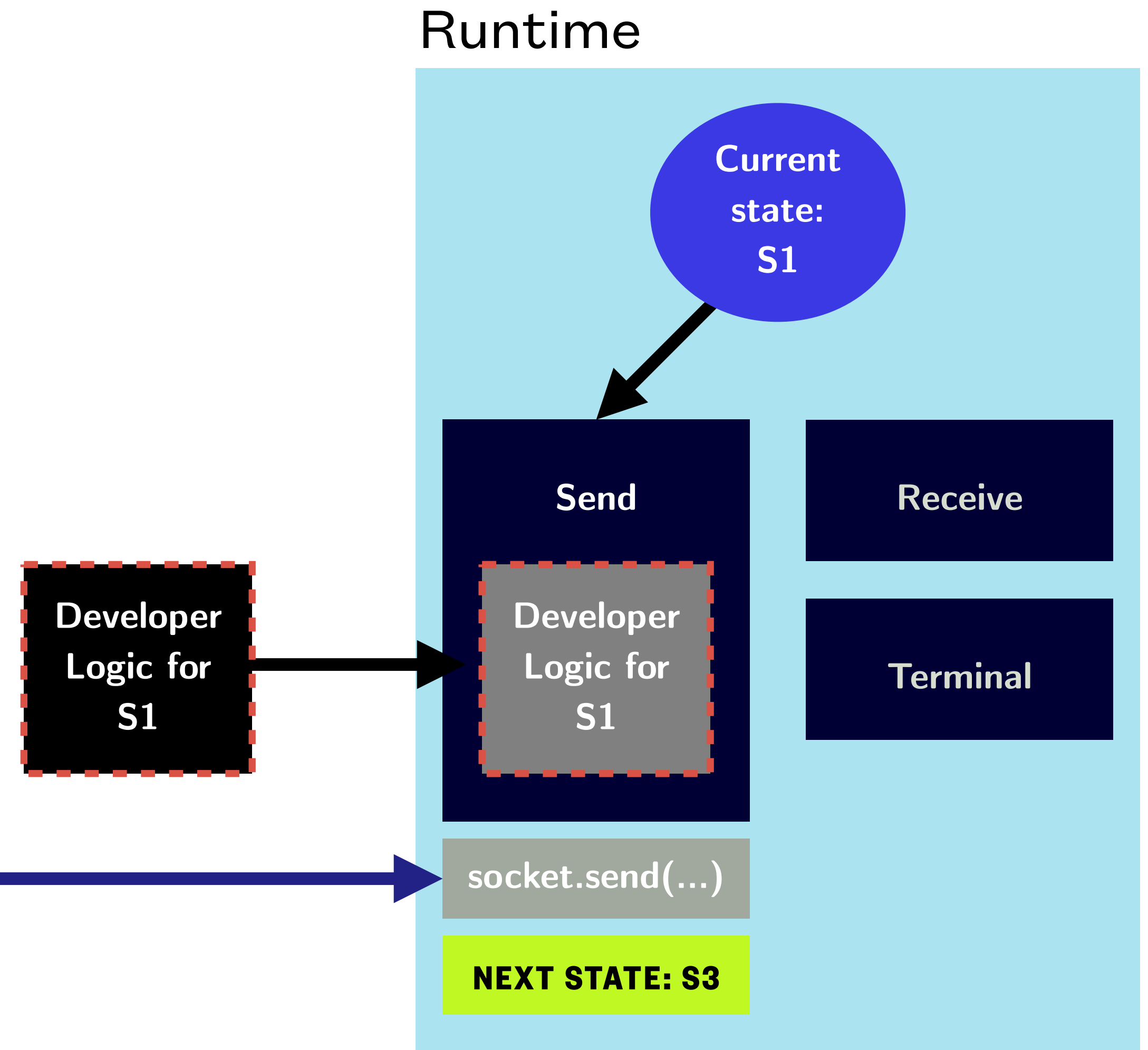
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Channel resources are not exposed, so channel reuse is **impossible** by construction.



EFSM in Node

- Send states = an union of selections
 - Selection :: (label, payload, successor)
- Receive states = labelled handlers
 - Handler :: payload → Successor

```
const logic = new Implementation.Initial({
  [Labels.S17.Destination]: async (dest) => {
    const result = await checkAvailable(dest);
    if (result.available) {
      return new Implementation.S19([
        Labels.S19.Available, [result.price], ...
      ]);
    } else {
      return new Implementation.S19([
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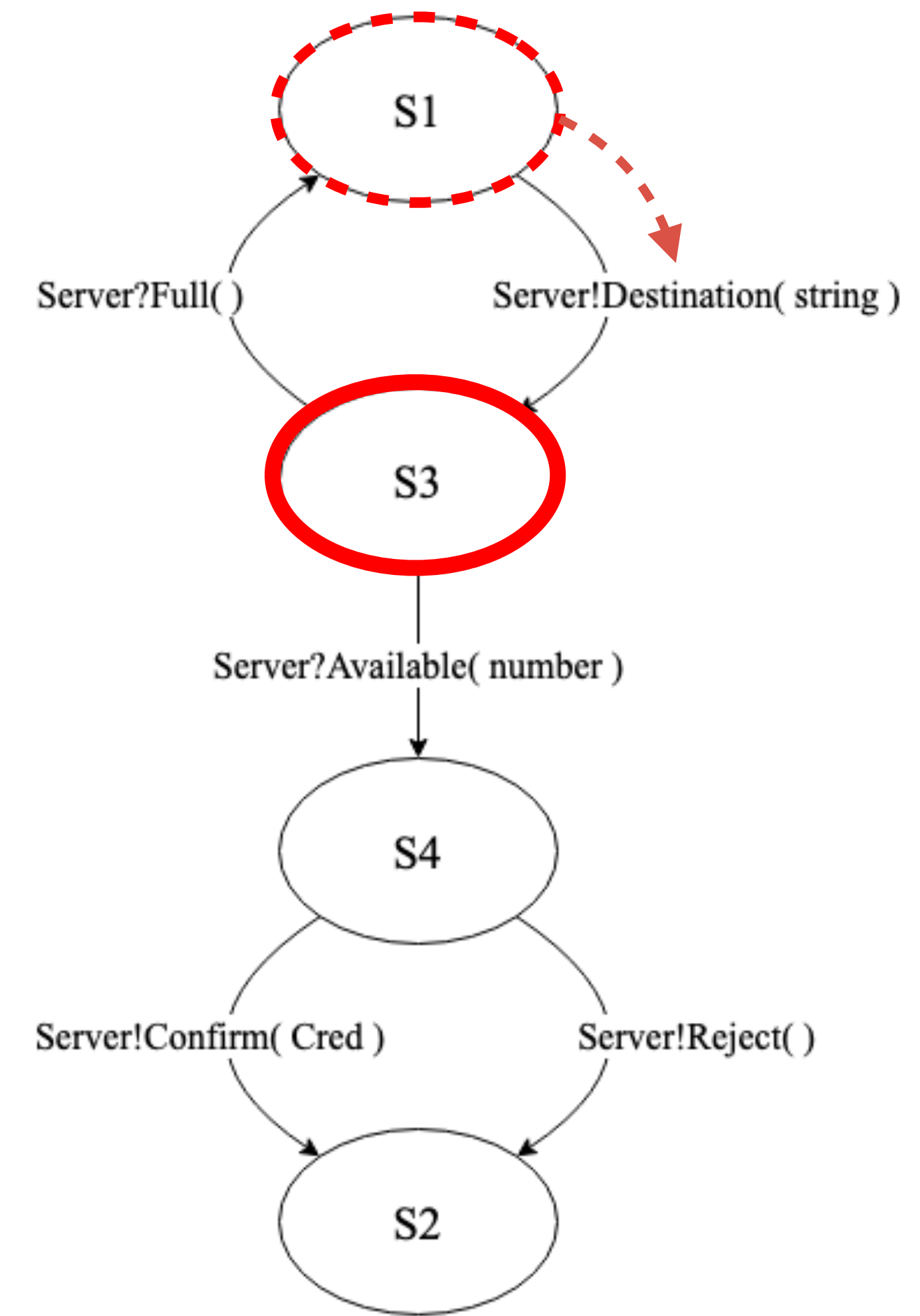
Session Types for GUI

- Channel actions triggered by user interaction
 - User clicks button
 - User presses “Enter” on their keyboard
 - User hovers over HTML element, etc.

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How to guarantee that user respects channel linearity?



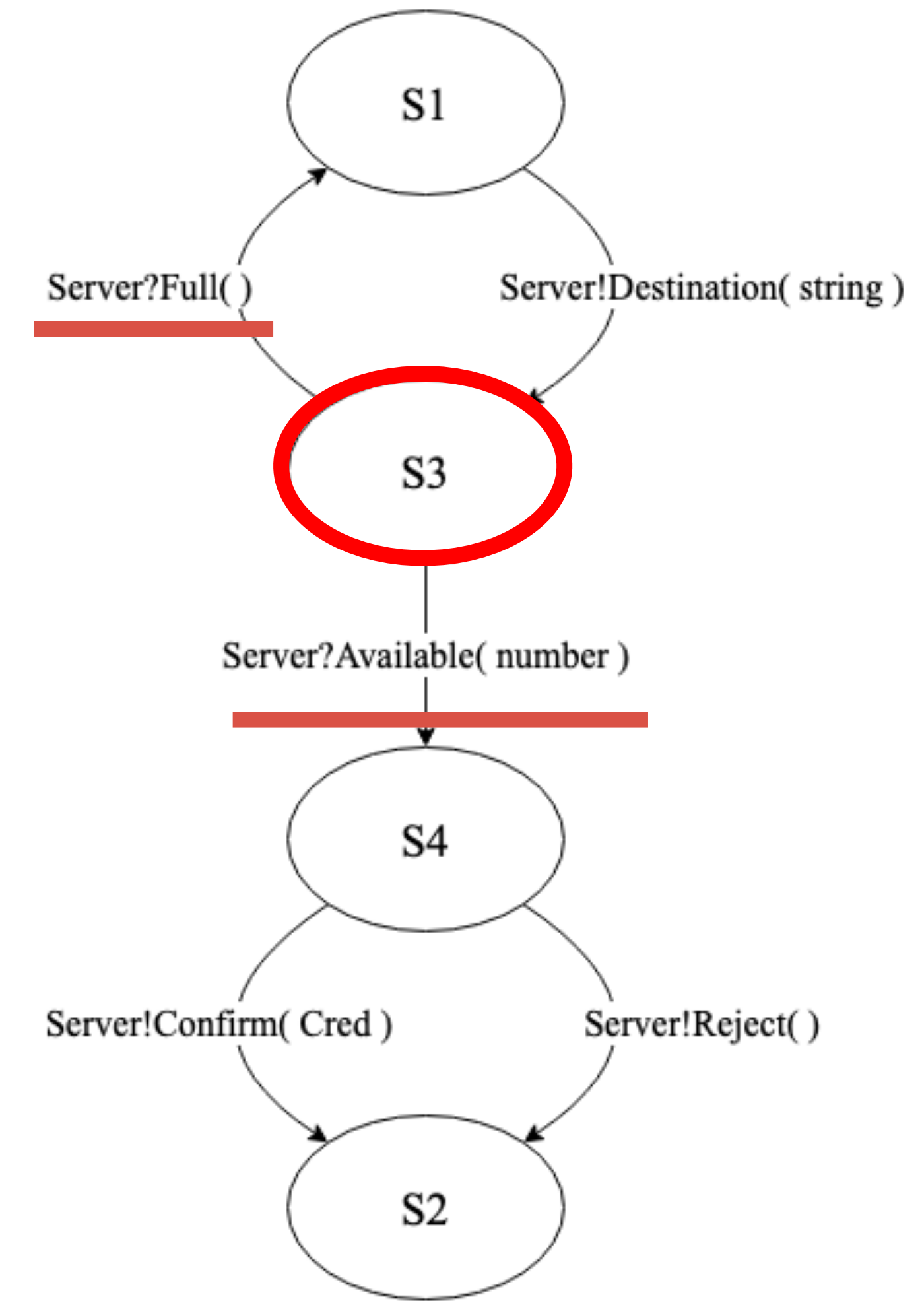
Model-View-Update (MVU)

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- Each model **uniquely** defines:
 - Set of messages (e.g. “onClick”)
 - View function (UI)
- The update function defines valid transitions (model x message) to other model types

Correspondence between MVU, EFSM and React Components

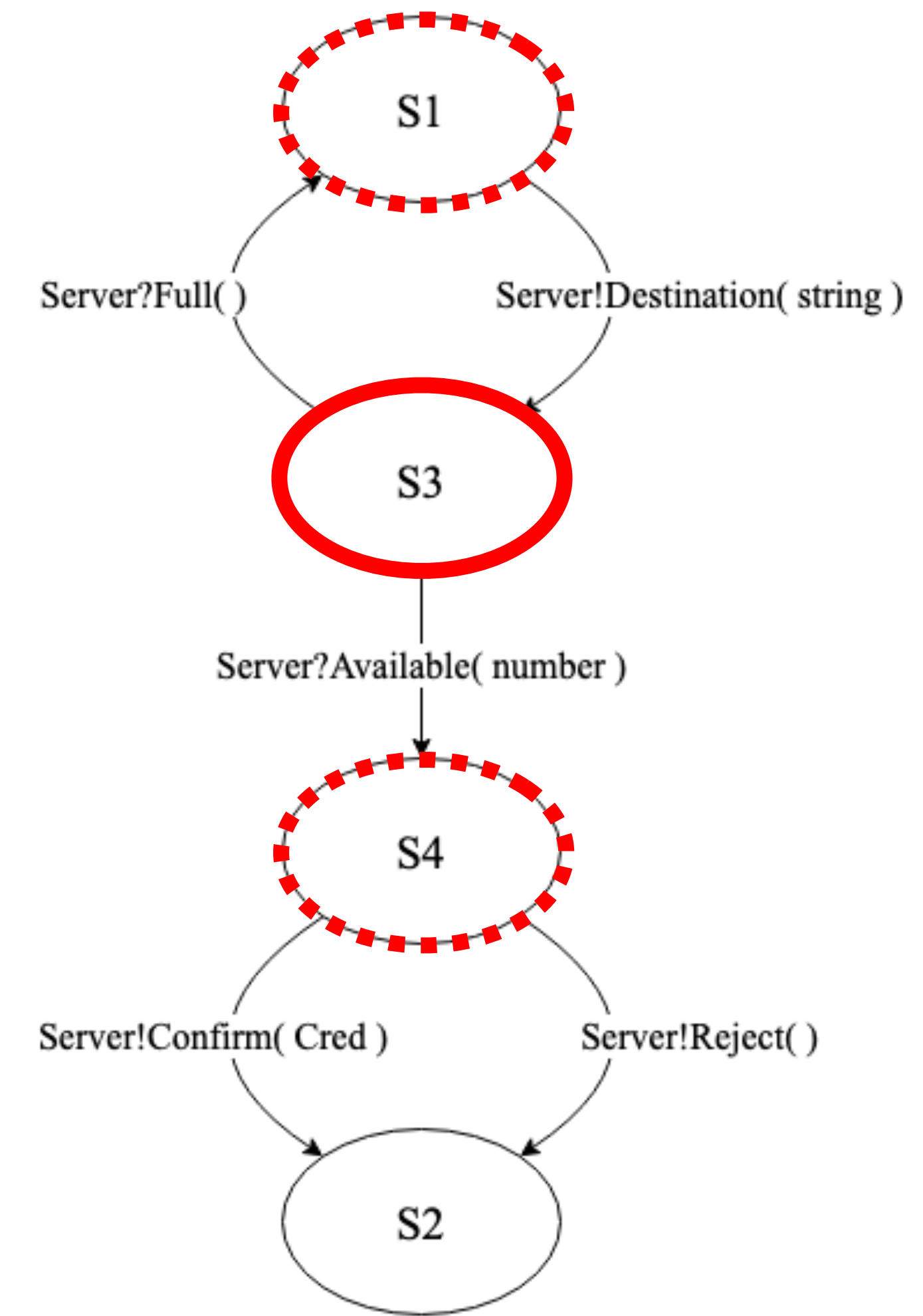
MVU + Endpoint FSM

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MVU + React

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```
export default class Terminal
  extends React.Component {
  render() {
    return <Typography variant='h2'>
      Thank you for using our service!
    </Typography>;
  }
}
```

EFSM in React

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 - Developer implements the view function
- Send action = component factory
 - I/O bound to UI event on component
- Receive action = callback
 - Abstract method

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const London = this.Destination('onClick', ev => {
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return (<div>
  ...
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```
export default class Waiting extends S8 {  
  
  Available(price: number) {  
    console.log('OK!');  
    this.context.setPrice(price);  
  }  
  
  Full() {  
    console.log('Full!');  
    this.context.setError(...);  
    this.context.setDestination('');  
  }  
  
  render() { ... }  
  
}
```

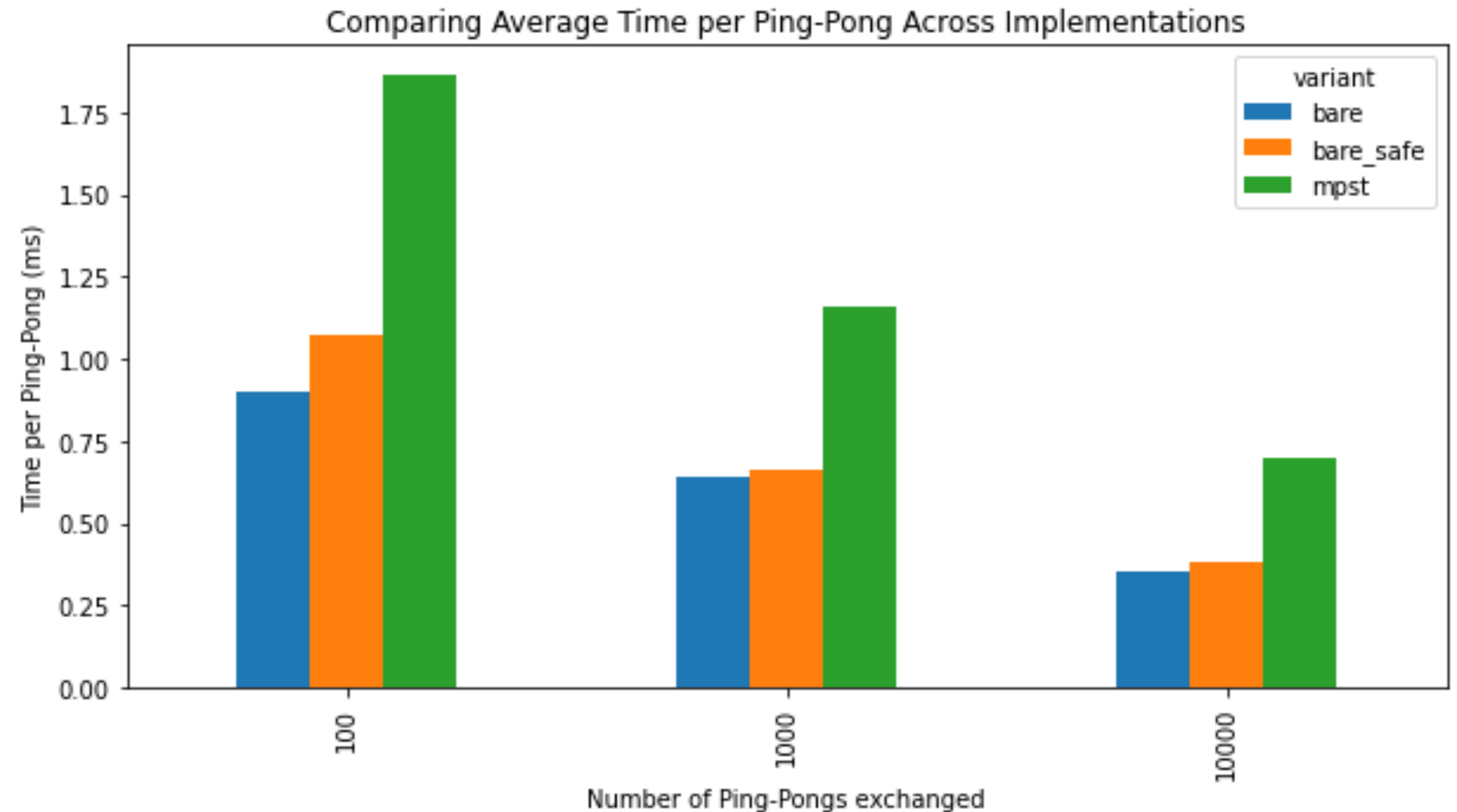
Evaluation

- **Expressiveness**

- Flight Booking Service
- Noughts and Crosses

- **Performance**

- Micro-benchmarks of Ping Pong protocol with varying number of round trips
- Overhead in message processing time



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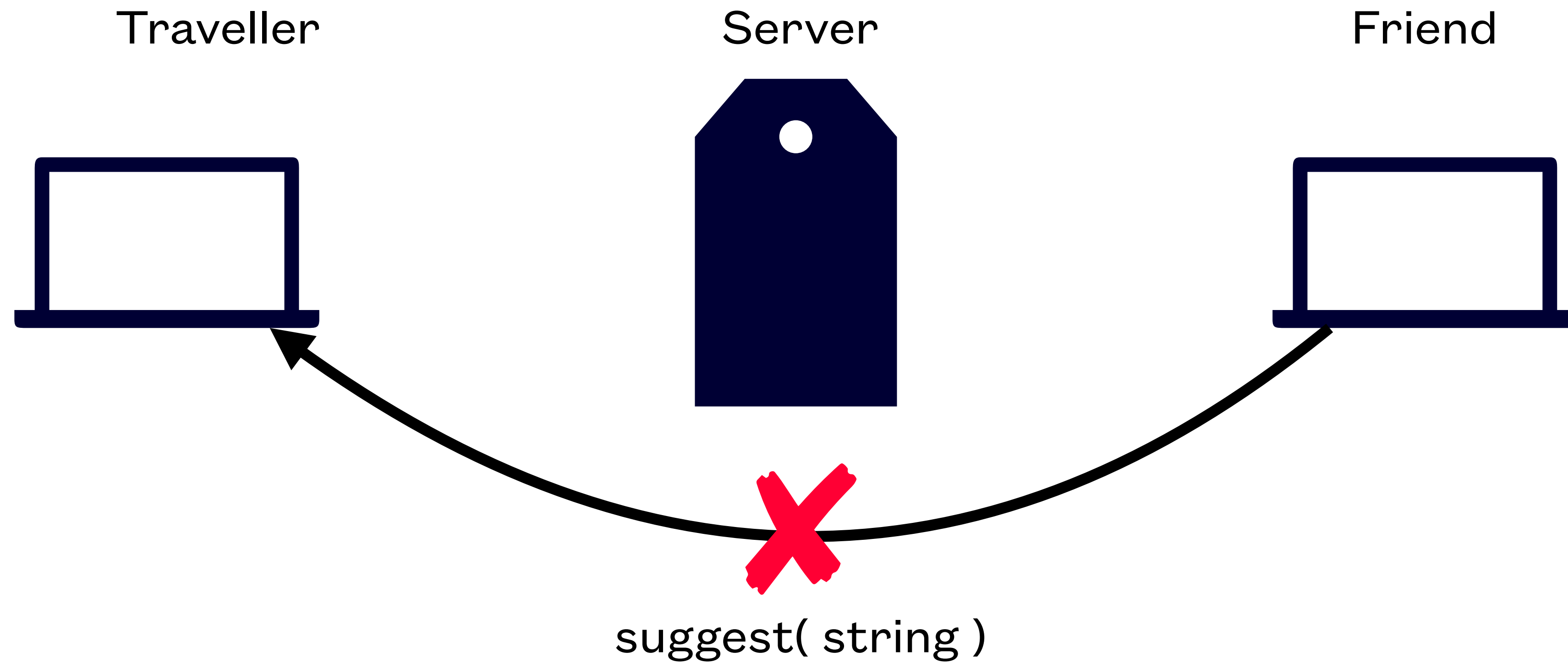
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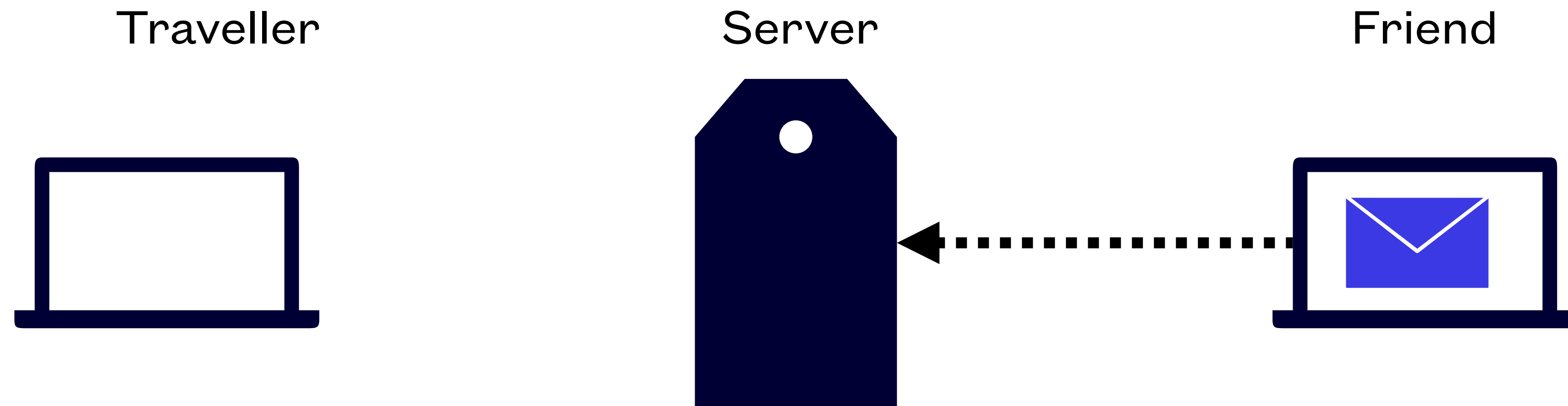
ROUTEDSESSIONS

A New Theory of Multiparty Session Types with
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Intuition

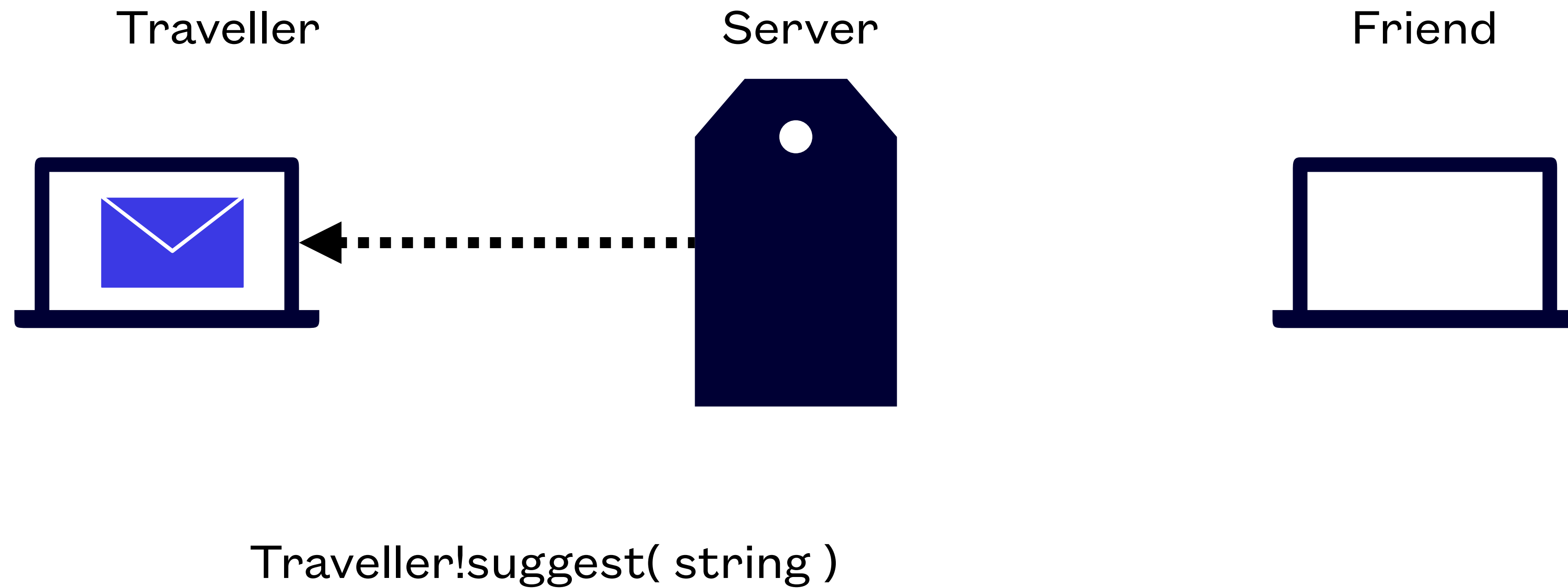


Intuition



Traveller!suggest(string)

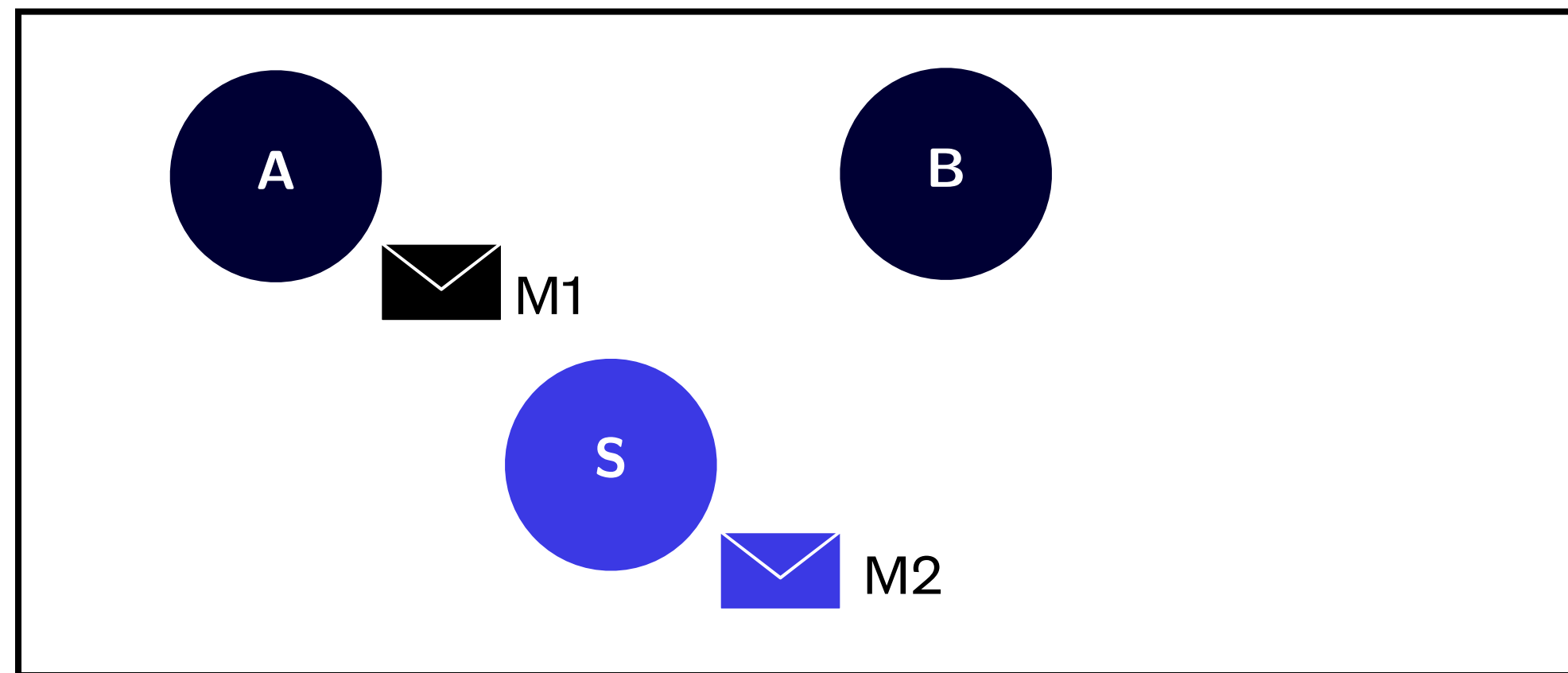
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Challenges in Formalising “Routing”

“Original communication”

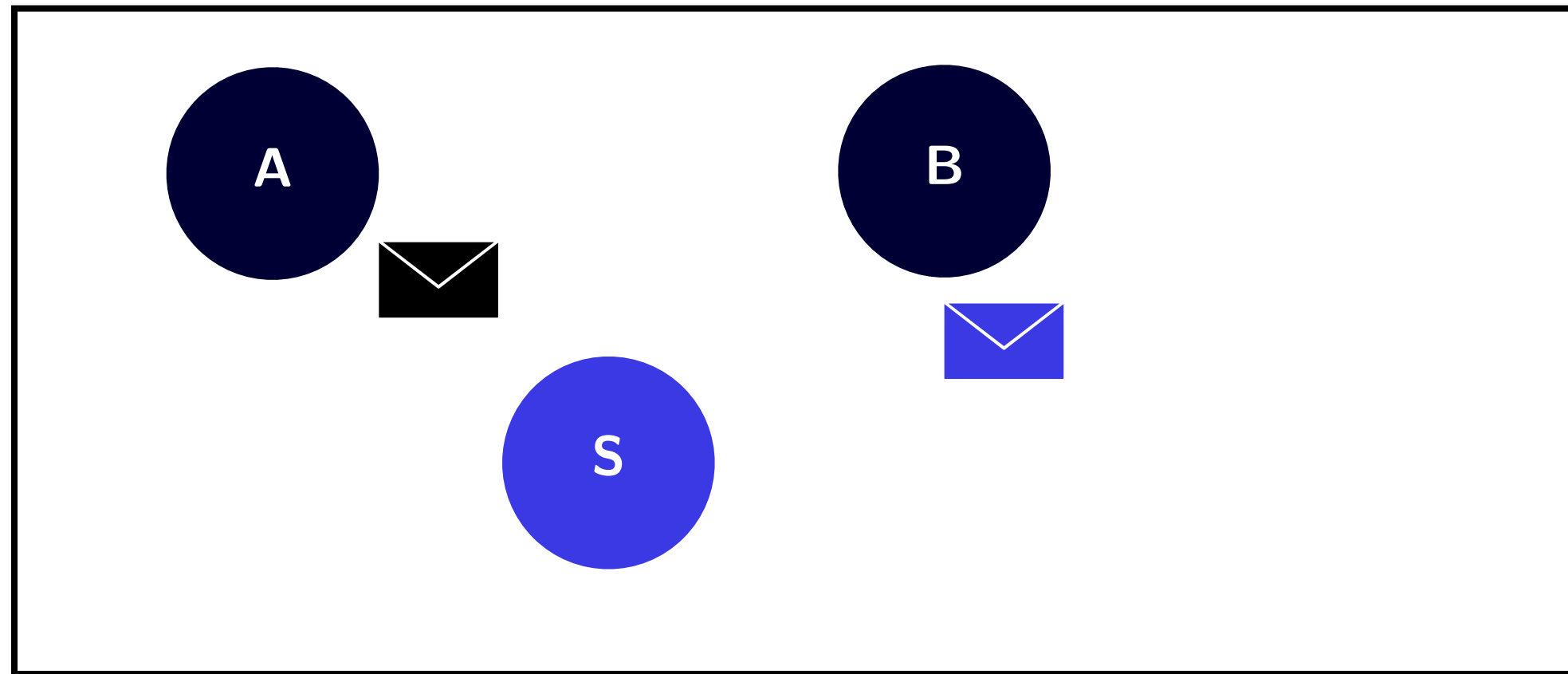
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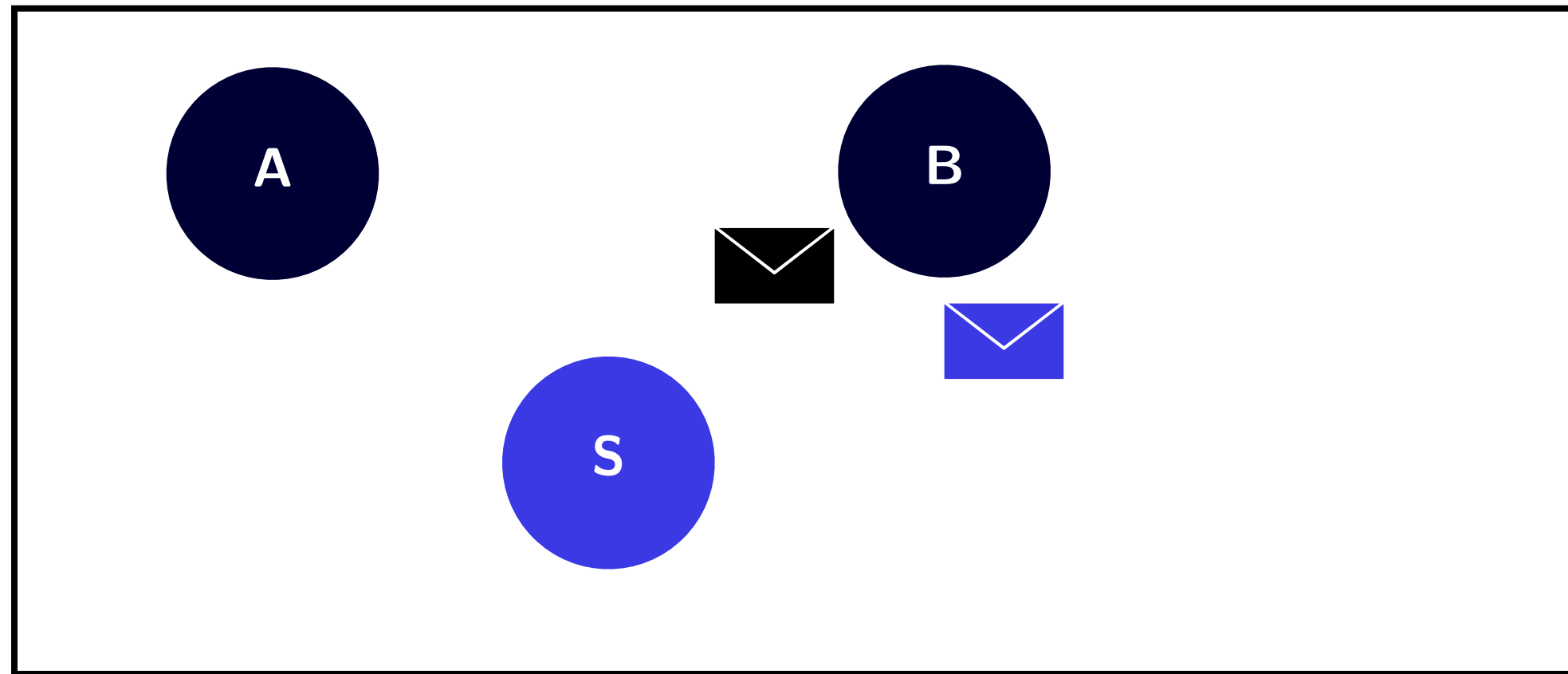
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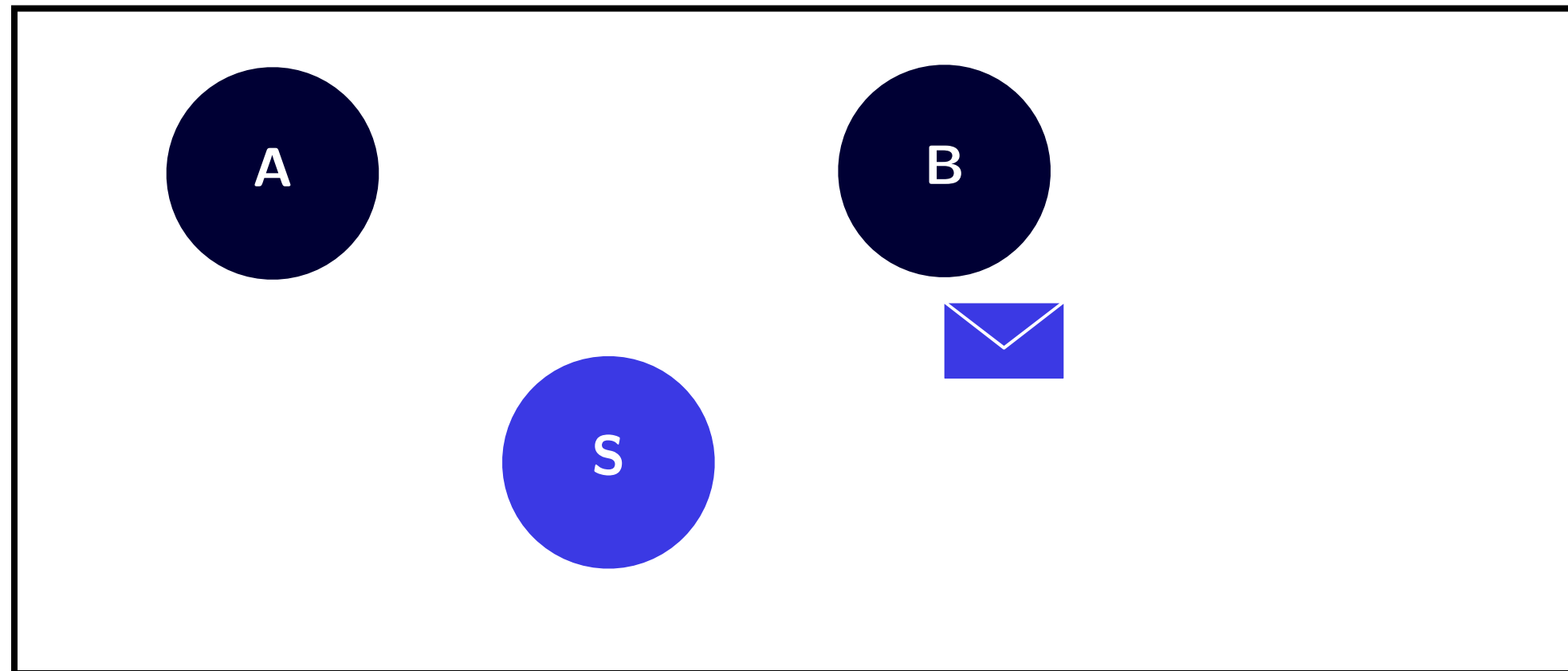
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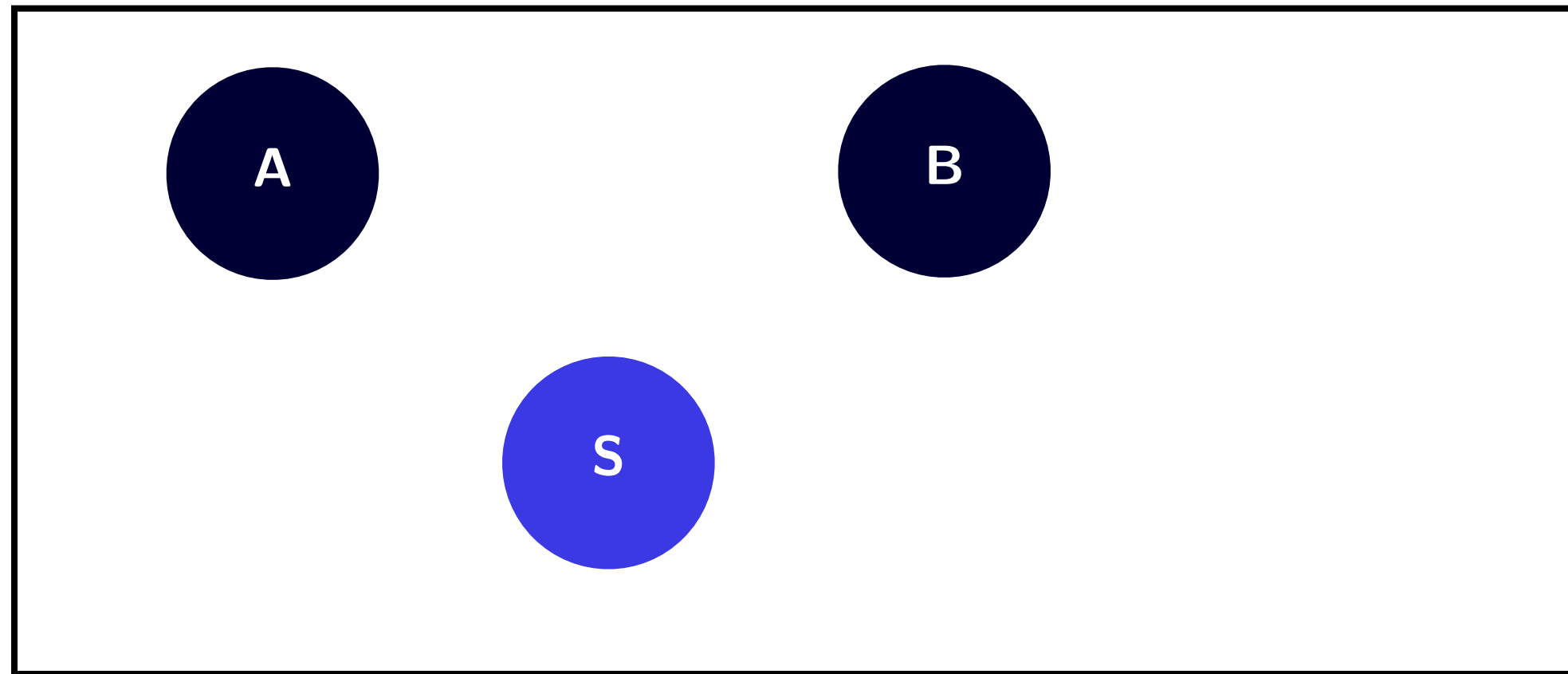
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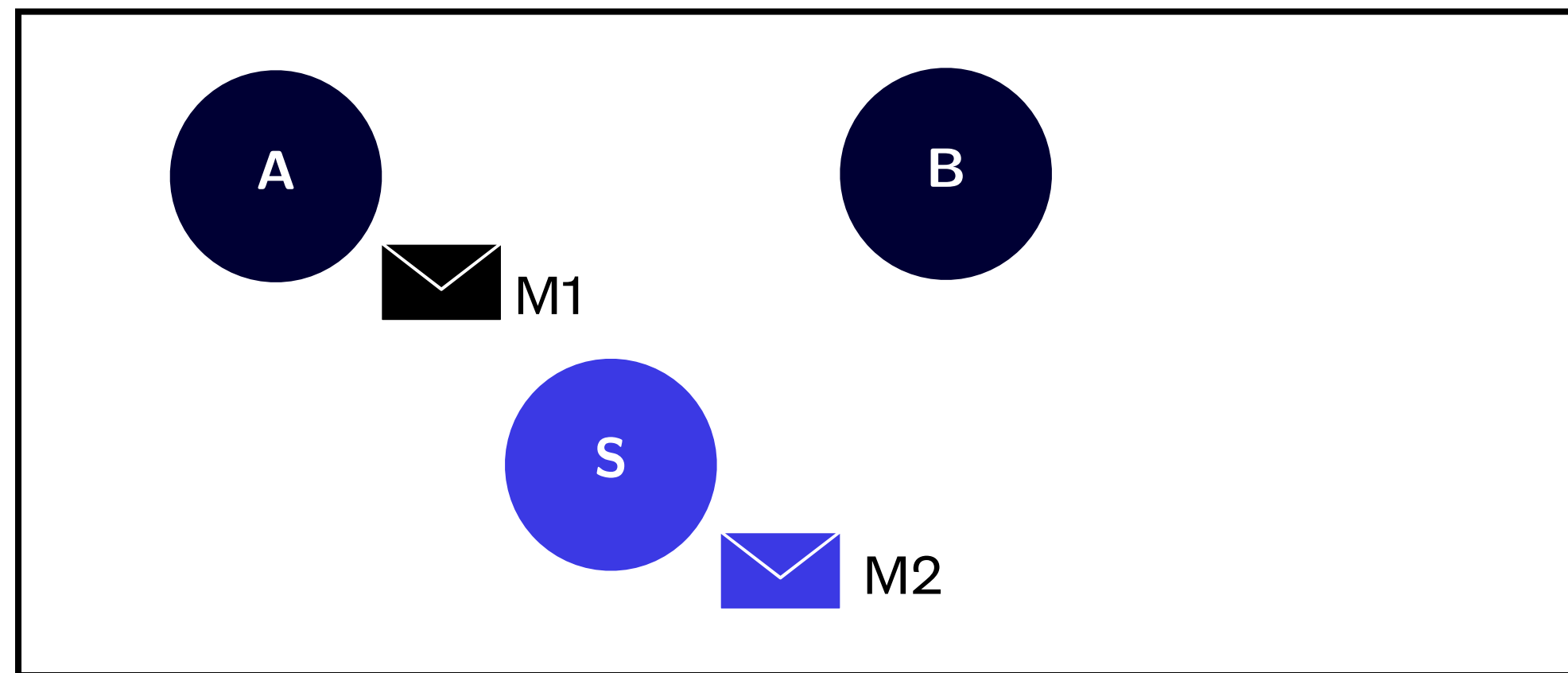
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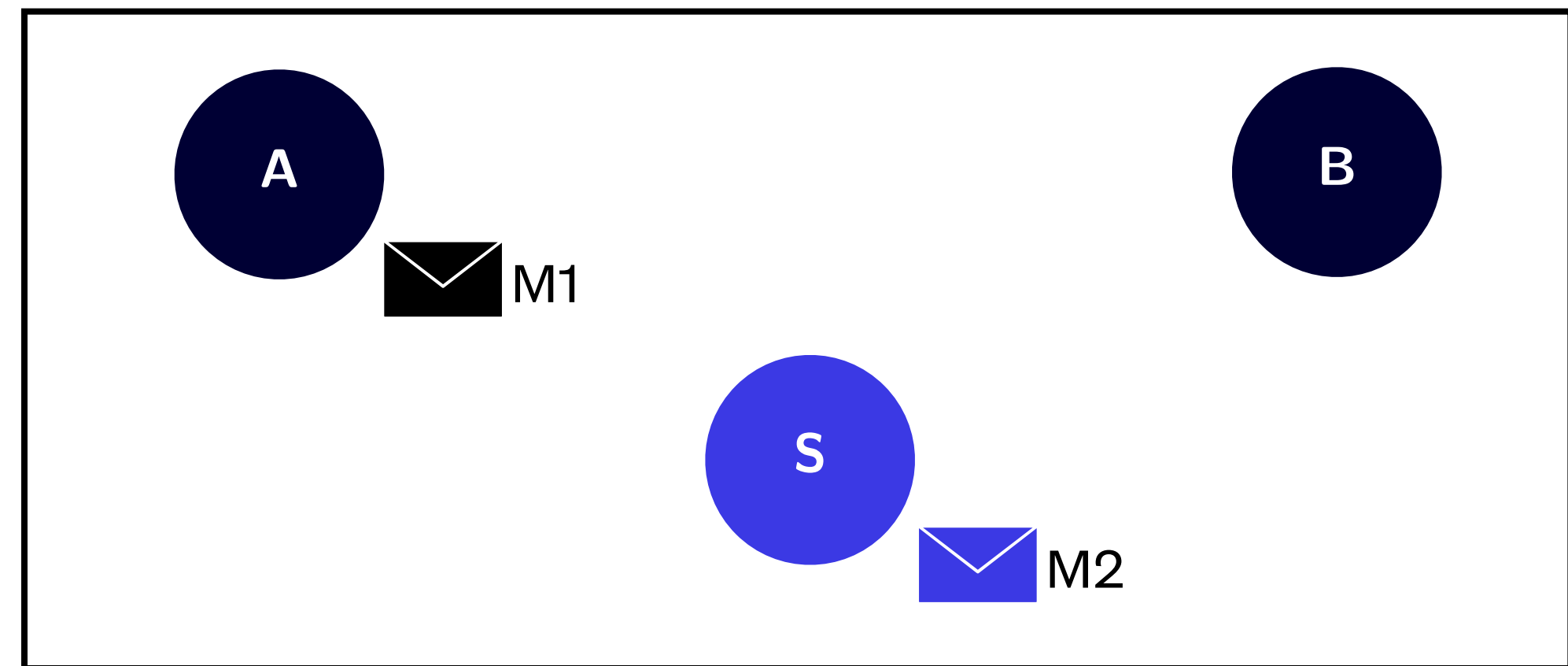
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“Naive Routed Communication”

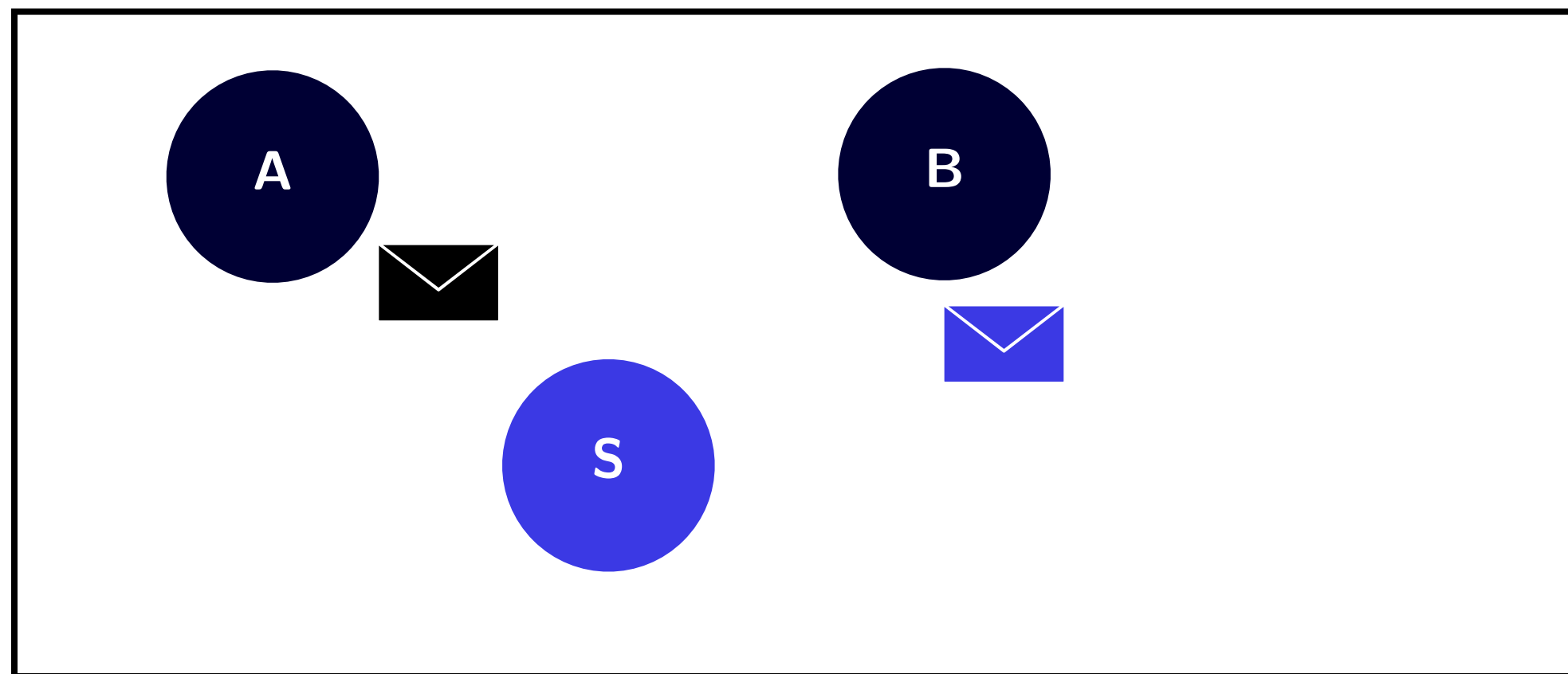
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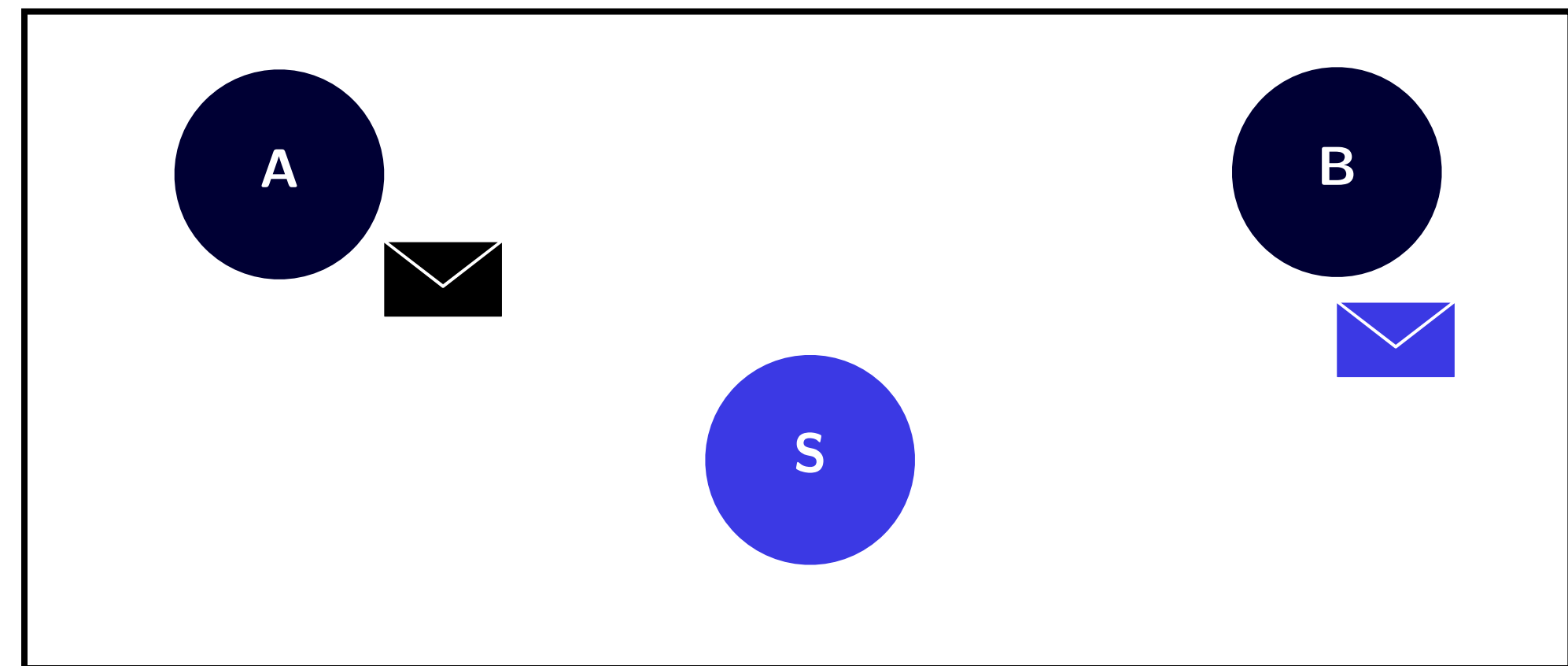
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- S sends M2 to B.



“Naive Routed Communication”

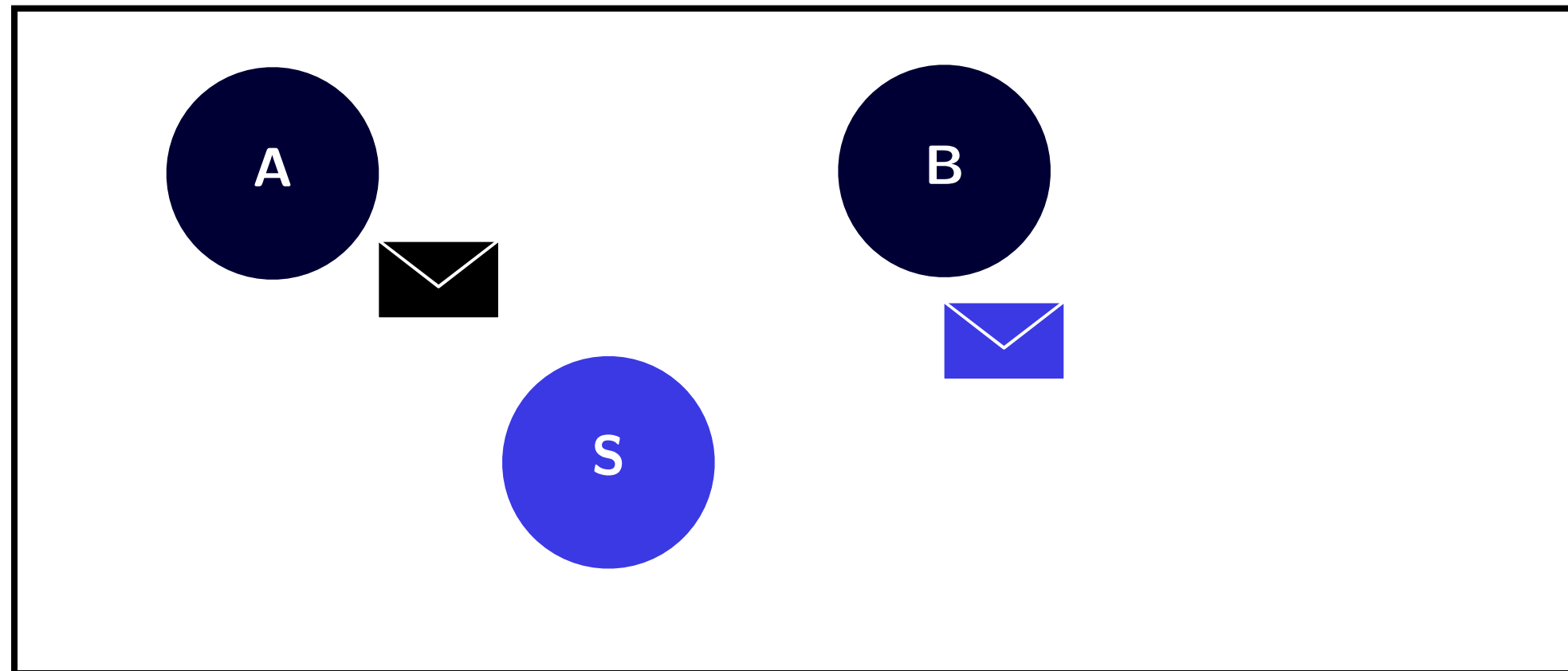
- A sends M1 to S.
- S sends M1 to B.
- S sends M2 to B.



Challenges in Formalising “Routing”

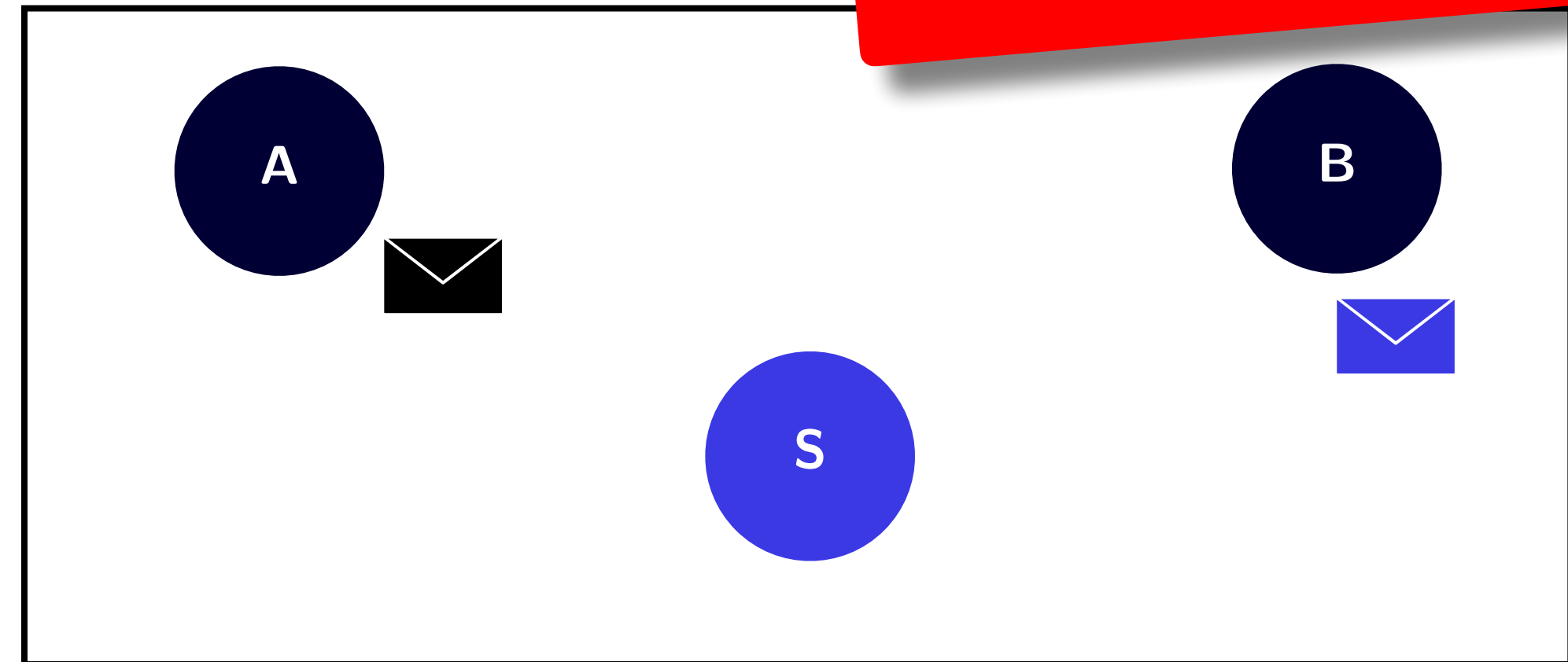
“Original communication”

- A sends M1 to B.
- S sends M2 to B.



“Naive Routed Communication”

- A sends M1 to S.
- S sends M1 to B.
- S sends M2 to B.

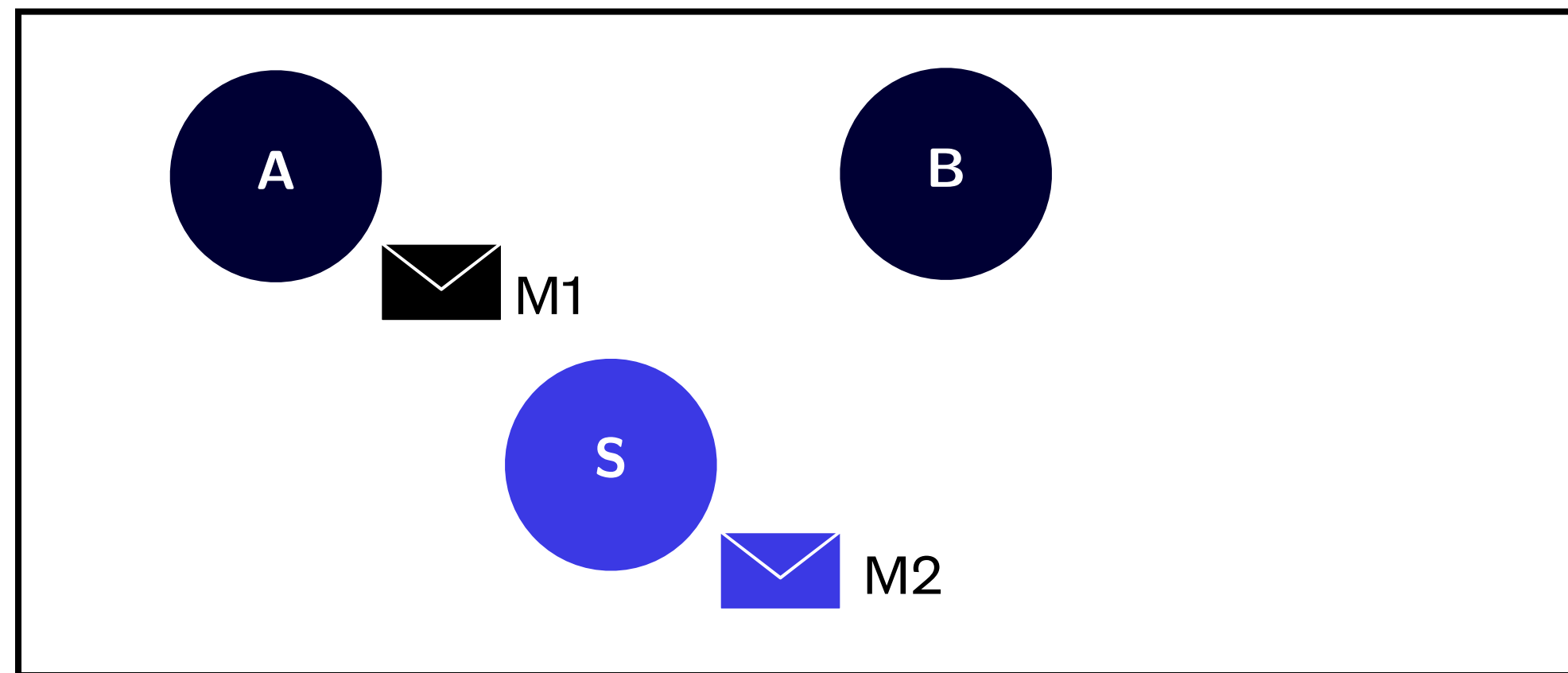


Not Possible!

Challenges in Formalising “Routing”

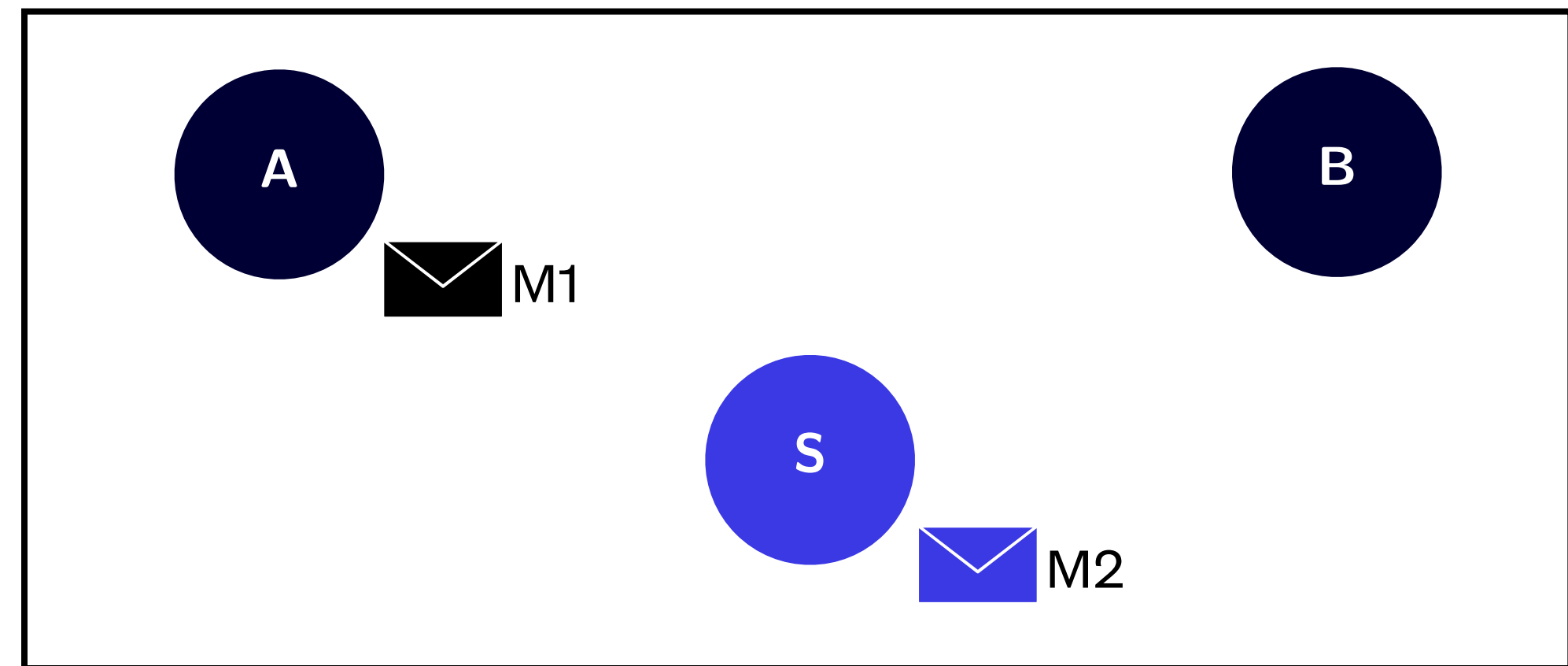
“Original communication”

- A sends M1 to B.
- S sends M2 to B.



ROUTEDSESSIONS

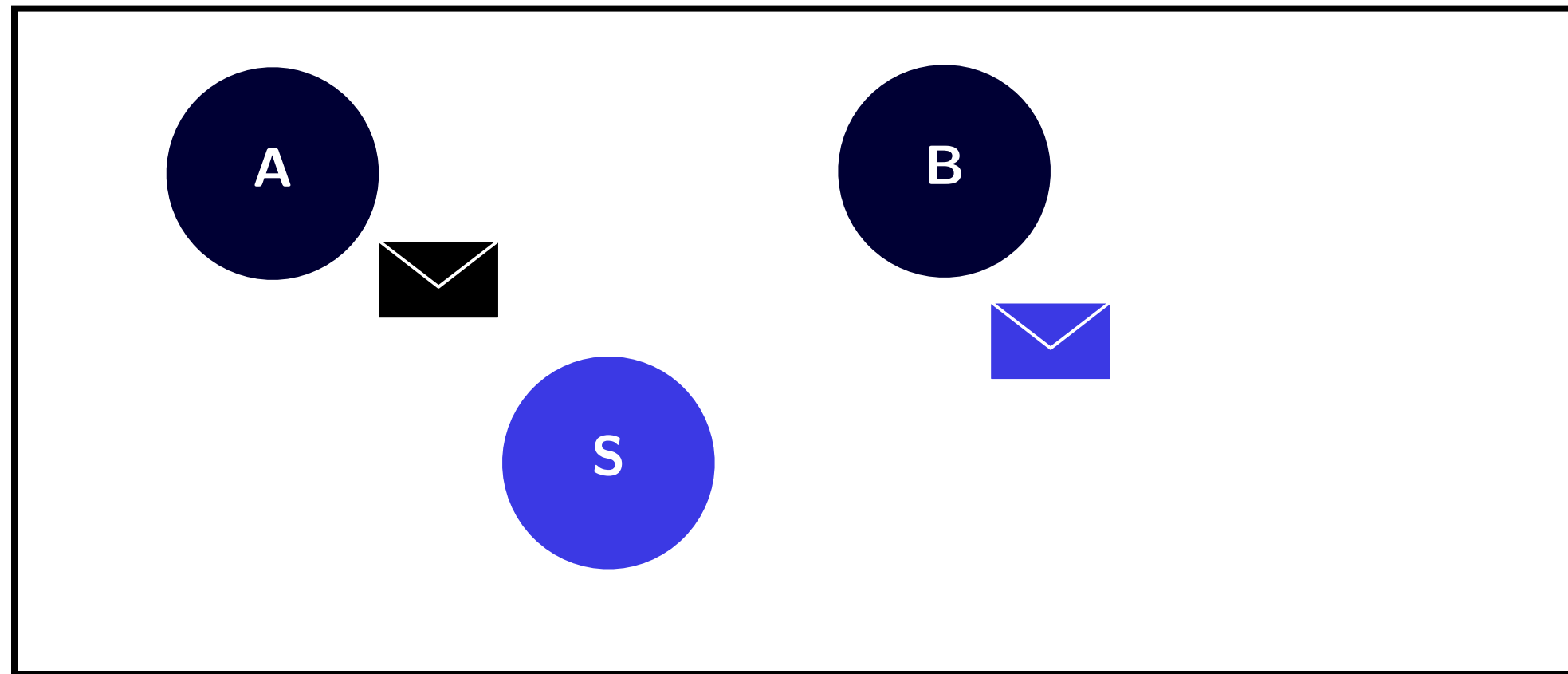
- A sends M1 to B via S.
- S sends M2 to B.



Challenges in Formalising “Routing”

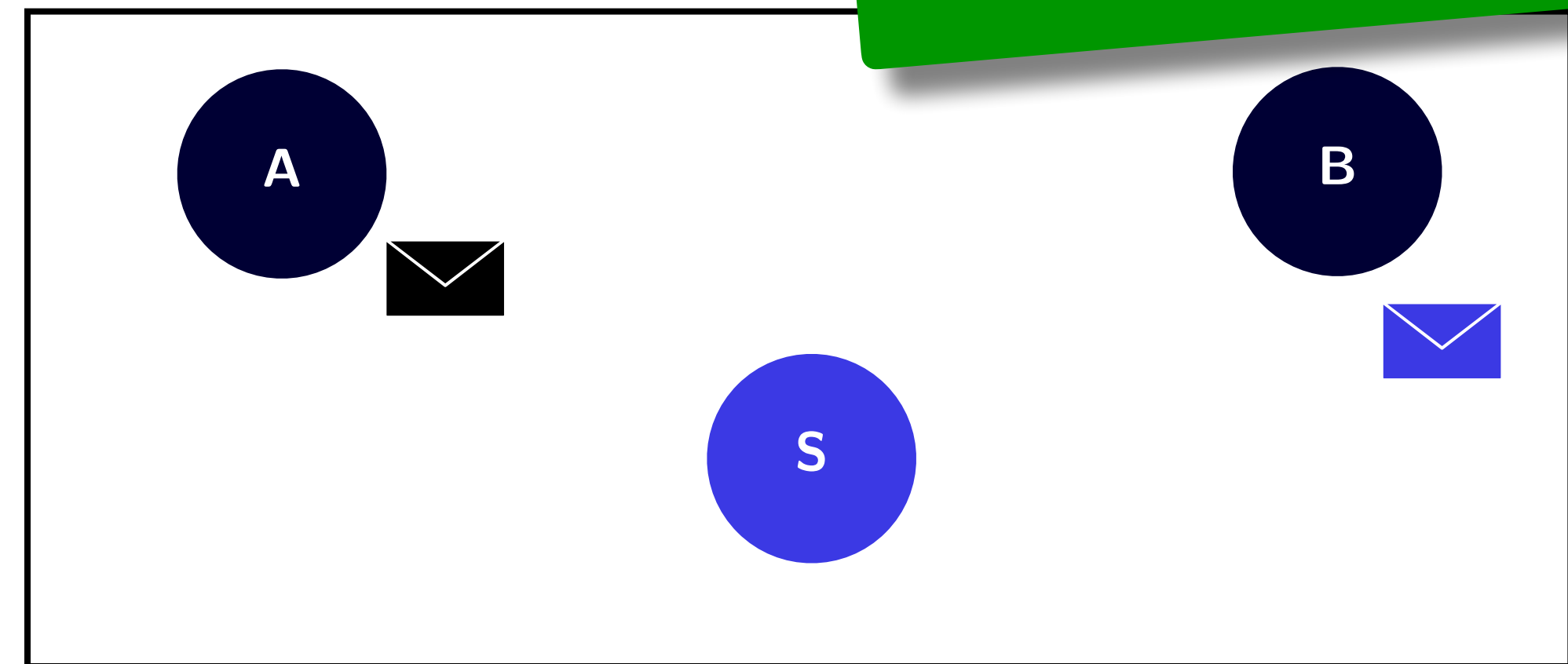
“Original communication”

- A sends M1 to B.
- S sends M2 to B.



ROUTEDSESSIONS

- A sends M1 to B via S.
- S sends M2 to B.



via S allows this

Formalising Routed Communication

“Original communication”

- A sends M1 to B.
- S sends M2 to B.

ROUTEDSESSIONS

- A sends M1 to B via S.
- S sends M2 to B.

Define new theory for
ROUTEDSESSIONS

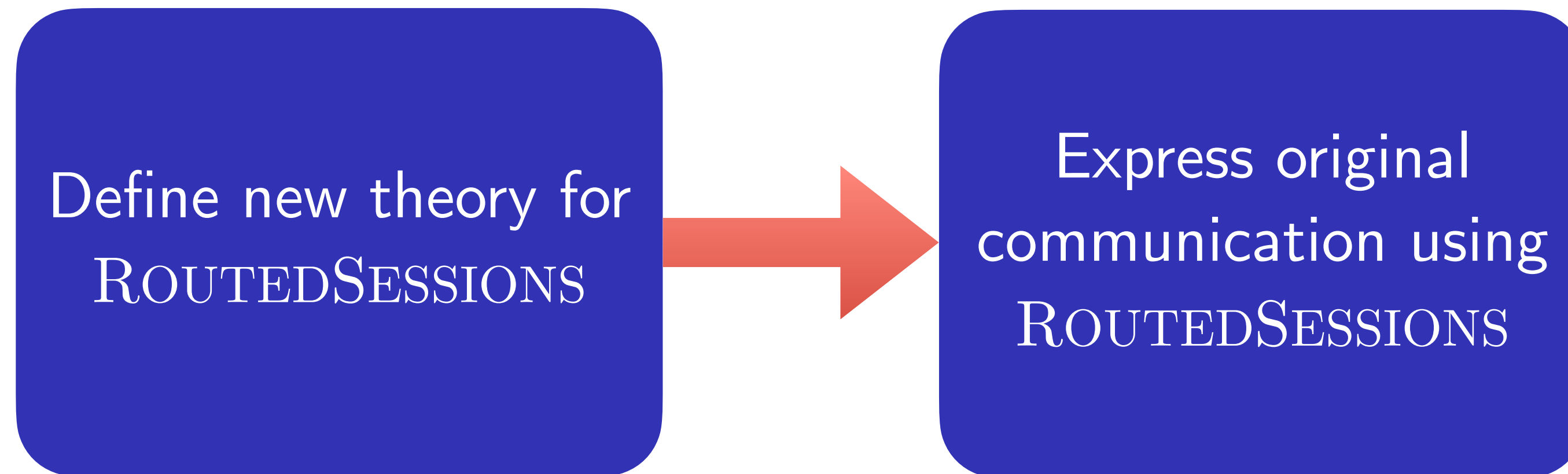
Formalising Routed Communication

“Original communication”

- A sends M1 to B.
- S sends M2 to B.

ROUTEDSESSIONS

- A sends M1 to B via S.
- S sends M2 to B.



Formalising Routed Communication

“Original communication”

- A sends M1 to B.
- S sends M2 to B.

ROUTEDSESSIONS

- A sends M1 to B via S.
- S sends M2 to B.



Global Types

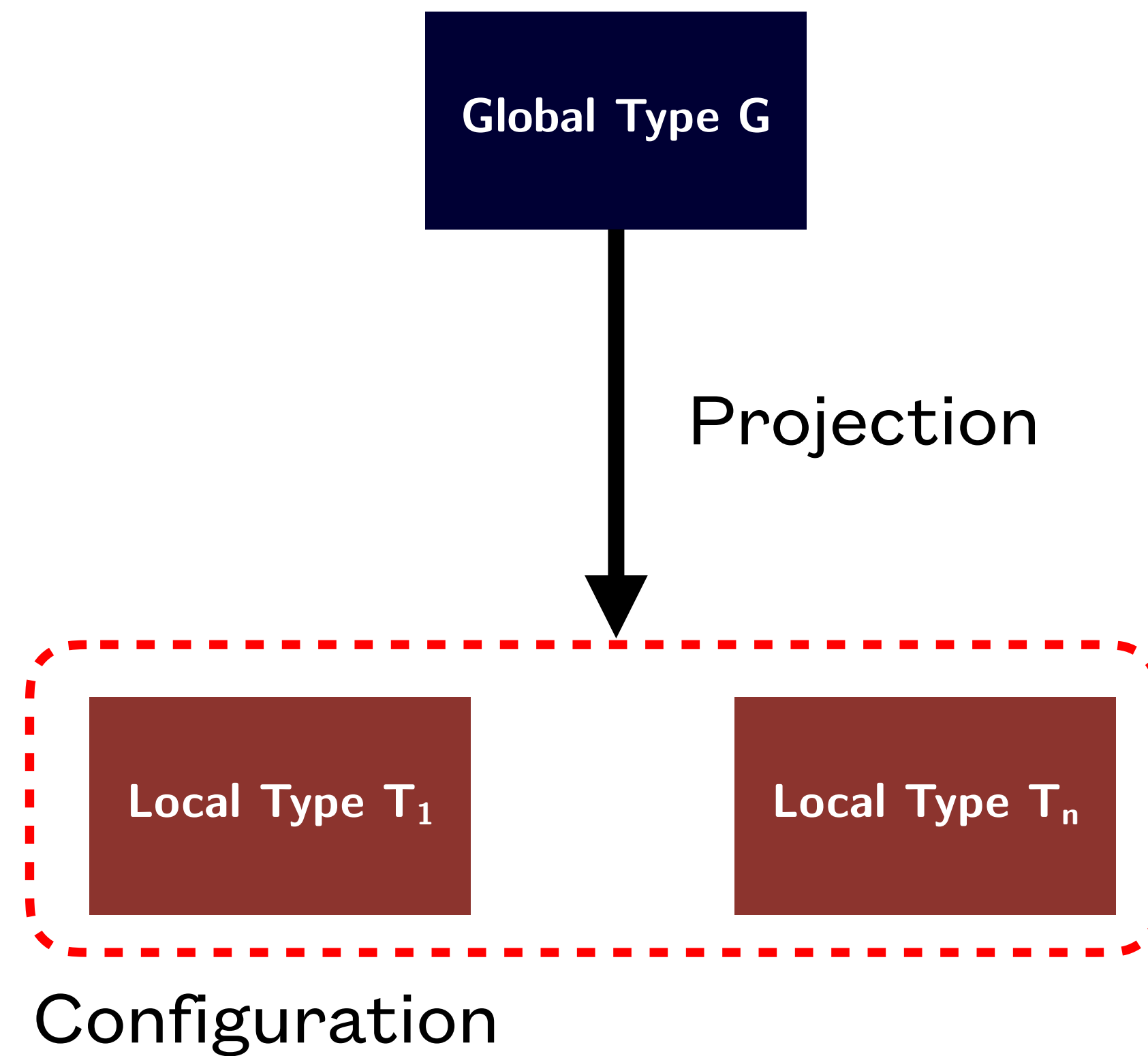
Syntax

| $G ::=$ | Global Types |
|---|----------------------|
| end | Termination |
| t | Type Variable |
| $\mu t. G$ | Recursive Type |
| $p \rightarrow q : \{l_i : G_i\}_{i \in I}$ | Direct Communication |
| $p \xrightarrow{s} q : \{l_i : G_i\}_{i \in I}$ | Routed Communication |

“via S”

Figure 8.1: Global Types in ROUTEDSESSIONS

Projection



Local Types

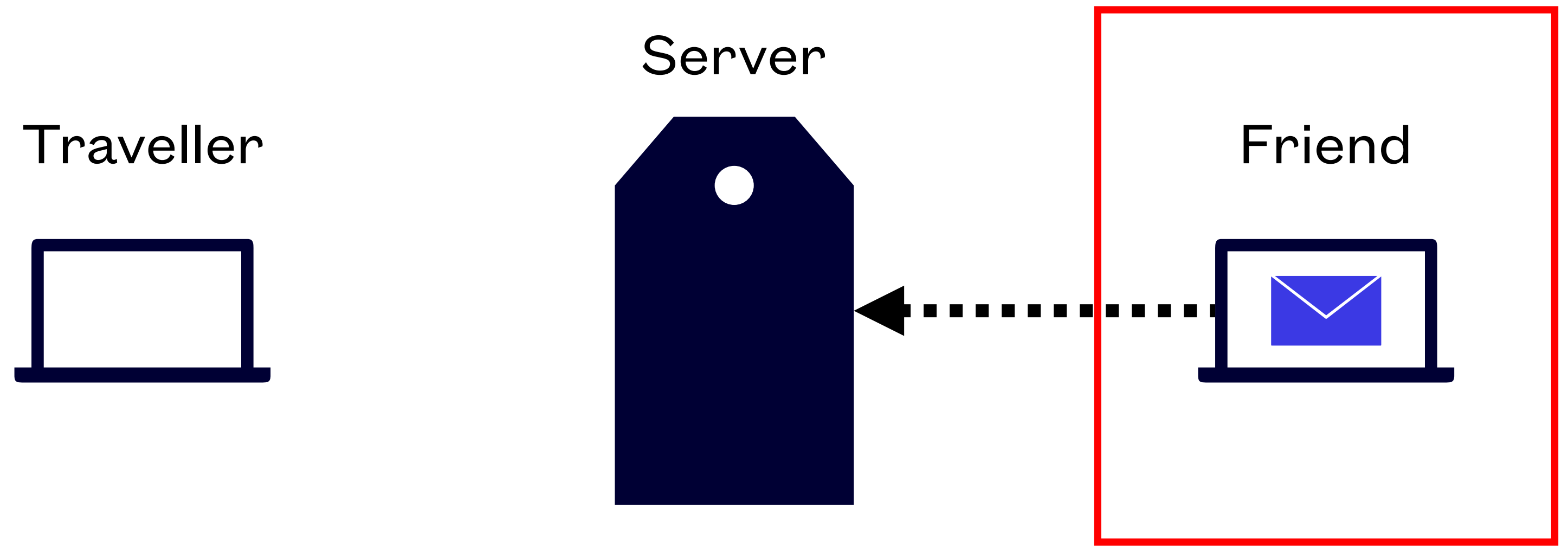
| $T ::=$ | Local Types |
|---|-----------------------|
| end | Termination |
| t | Type Variable |
| $\mu t. T$ | Recursive Type |
| $p \oplus \{l_i : T_i\}_{i \in I}$ | Selection |
| $p \& \{l_i : T_i\}_{i \in I}$ | Branching |
| $p \hookrightarrow q : \{l_i : T_i\}_{i \in I}$ | Routing Communication |
| $p_q \oplus \{l_i : T_i\}_{i \in I}$ | Routed Selection |
| $p_q \& \{l_i : T_i\}_{i \in I}$ | Routed Branching |

Figure 8.2: Local Types in ROUTEDSESSIONS

Local Types

Syntax

| $T ::=$ | Local Types |
|---|-----------------------|
| end | Termination |
| t | Type Variable |
| $\mu t. T$ | Recursive Type |
| $p \oplus \{l_i : T_i\}_{i \in I}$ | Selection |
| $p \& \{l_i : T_i\}_{i \in I}$ | Branching |
| $p \hookrightarrow q : \{l_i : T_i\}_{i \in I}$ | Routing Communication |
| $p_q \oplus \{l_i : T_i\}_{i \in I}$ | Routed Selection |
| $p_q \& \{l_i : T_i\}_{i \in I}$ | Routed Branching |



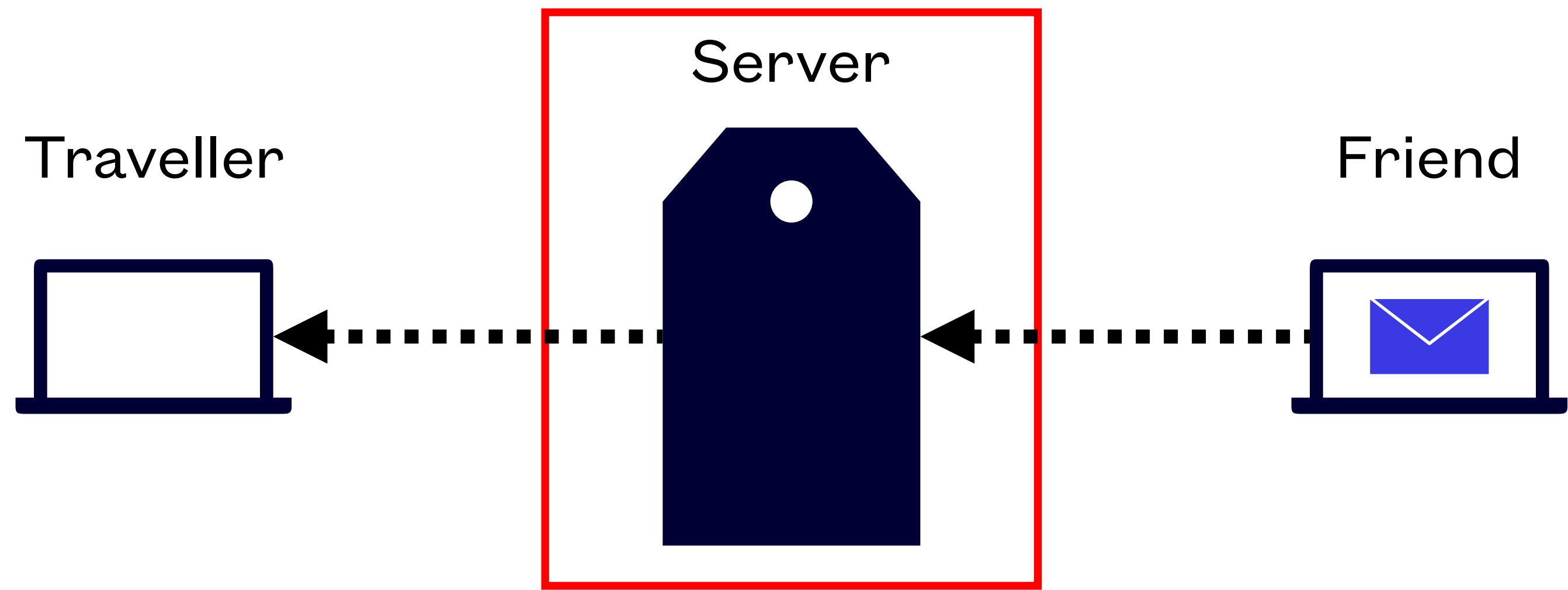
$\text{Traveller}_{\text{Server}} \oplus M1$

Figure 8.2: Local Types in ROUTEDSESSIONS

Local Types

Syntax

| $T ::=$ | Local Types |
|---|-----------------------|
| end | Termination |
| t | Type Variable |
| $\mu t. T$ | Recursive Type |
| $p \oplus \{l_i : T_i\}_{i \in I}$ | Selection |
| $p \& \{l_i : T_i\}_{i \in I}$ | Branching |
| $p \hookrightarrow q : \{l_i : T_i\}_{i \in I}$ | Routing Communication |
| $p_q \oplus \{l_i : T_i\}_{i \in I}$ | Routed Selection |
| $p_q \& \{l_i : T_i\}_{i \in I}$ | Routed Branching |



“I am routing a message from Friend intended for Traveller”

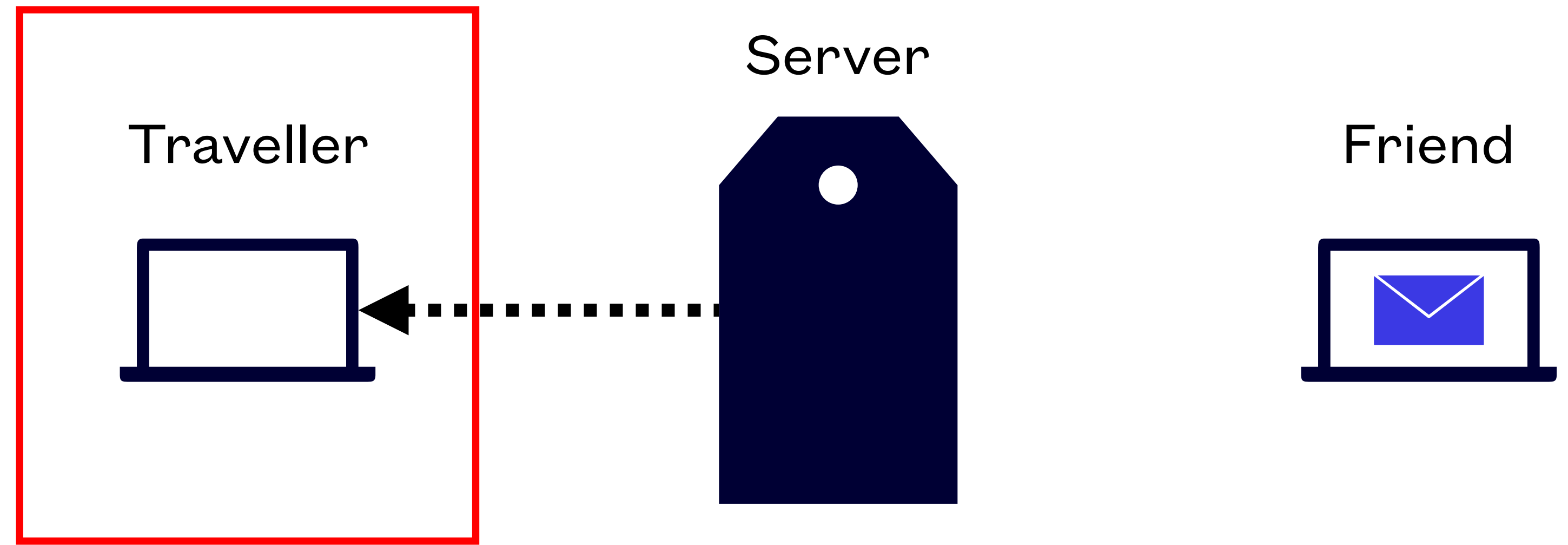
Friend \hookrightarrow Traveller : M1

Figure 8.2: Local Types in ROUTEDSESSIONS

Local Types

Syntax

| $T ::=$ | Local Types |
|---|-----------------------|
| end | Termination |
| t | Type Variable |
| $\mu t. T$ | Recursive Type |
| $p \oplus \{l_i : T_i\}_{i \in I}$ | Selection |
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| $p \hookrightarrow q : \{l_i : T_i\}_{i \in I}$ | Routing Communication |
| $p_q \oplus \{l_i : T_i\}_{i \in I}$ | Routed Selection |
| $p_q \& \{l_i : T_i\}_{i \in I}$ | Routed Branching |

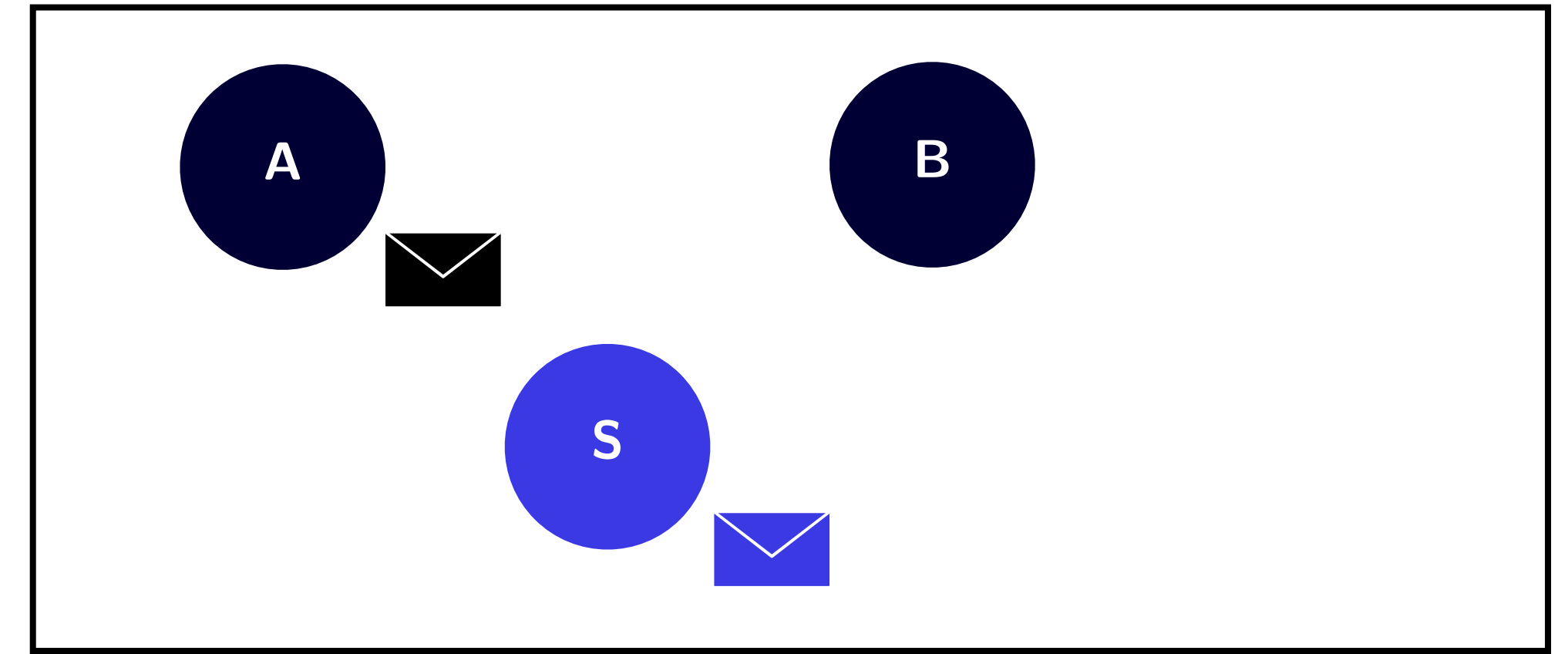
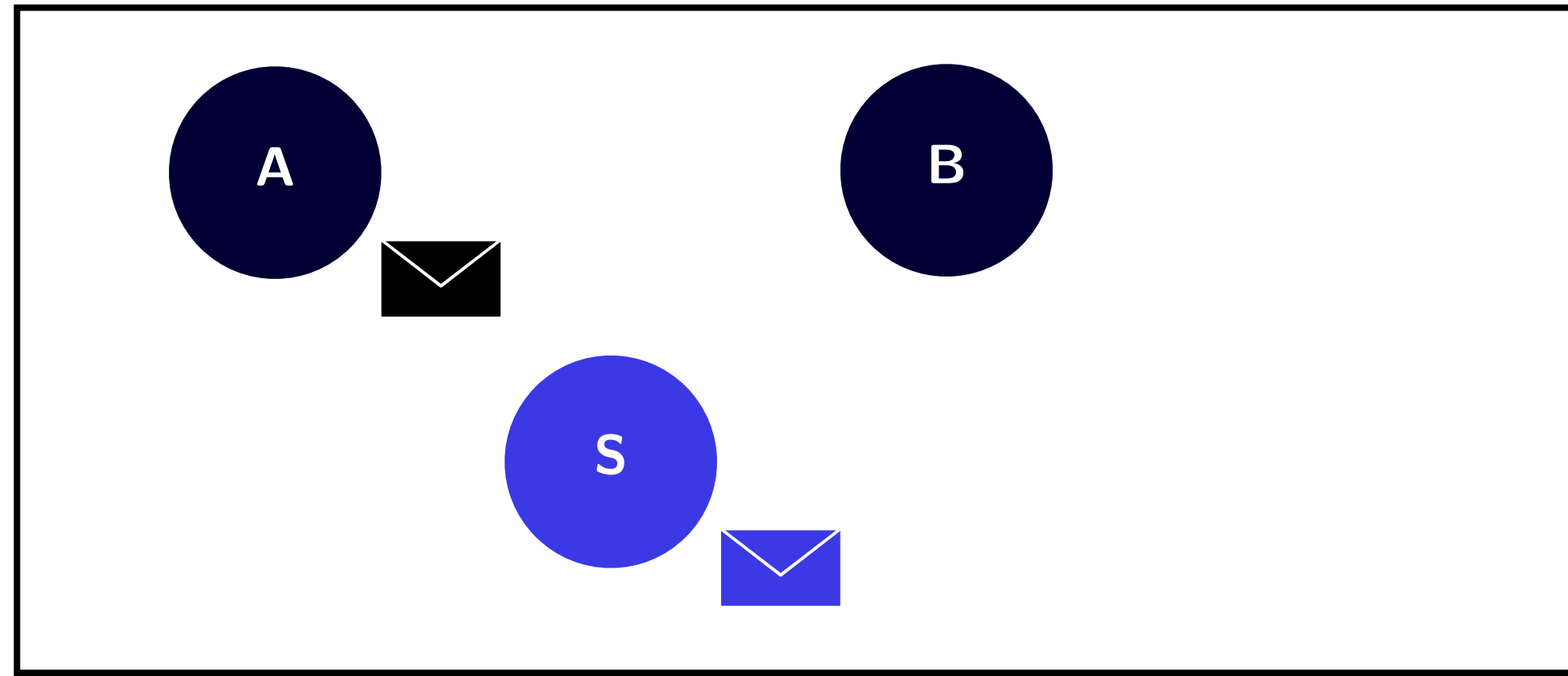


“I am receiving a message from Server, **originally from Friend**”

Friend_{Server} & M1

Figure 8.2: Local Types in ROUTEDSESSIONS

Semantics



Semantics

Semantics

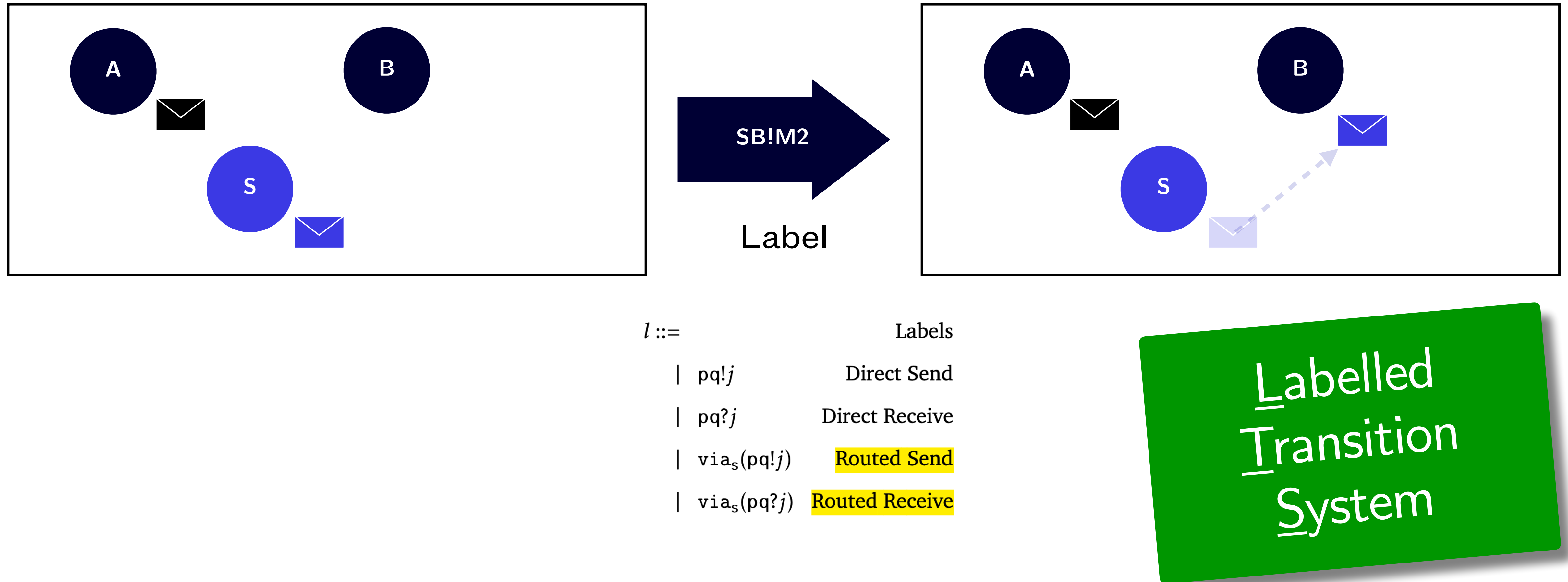


Figure 8.3: LTS Labels in ROUTEDSESSIONS

Semantics

$$\begin{array}{c}
 \frac{}{p \rightarrow q : \{l_i : G_i\}_{i \in I} \xrightarrow{pq!j} p \rightsquigarrow q. j : \{l_i : G_i\}_{i \in I}} \text{[GR1]} \\
 \\
 \frac{}{p \rightsquigarrow q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{pq?j} G_j} \text{[GR2]} \\
 \\
 \frac{G[\mu t. G/t] \xrightarrow{l} G'}{\mu t. G \xrightarrow{l} G'} \text{[GR3]} \\
 \\
 \frac{\forall i \in I. G_i \xrightarrow{l} G'_i \quad \text{subj}(l) \notin \{p, q\}}{p \rightarrow q : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \rightarrow q : \{l_i : G'_i\}_{i \in I}} \text{[GR4]} \\
 \\
 \frac{G_j \xrightarrow{l} G'_j \quad \text{subj}(l) \neq q \quad \forall i \in I \setminus \{j\}. G'_i = G_i}{p \rightsquigarrow q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \rightsquigarrow q. j : \{l_i : G'_i\}_{i \in I}} \text{[GR5]} \\
 \\
 \frac{}{p \xrightarrow{s} q : \{l_i : G_i\}_{i \in I} \xrightarrow{\text{via}_s(pq!j)} p \rightsquigarrow_s q. j : \{l_i : G_i\}_{i \in I}} \text{[GR6]} \\
 \\
 \frac{}{p \rightsquigarrow_s q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{\text{via}_s(pq?j)} G_j} \text{[GR7]} \\
 \\
 \frac{\forall i \in I. G_i \xrightarrow{l} G'_i \quad \text{subj}(l) \notin \{p, q\}}{p \xrightarrow{s} q : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \xrightarrow{s} q : \{l_i : G'_i\}_{i \in I}} \text{[GR8]} \\
 \\
 \frac{G_j \xrightarrow{l} G'_j \quad \text{subj}(l) \neq q \quad \forall i \in I \setminus \{j\}. G'_i = G_i}{p \rightsquigarrow_s q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \rightsquigarrow_s q. j : \{l_i : G'_i\}_{i \in I}} \text{[GR9]}
 \end{array}$$

Figure 8.4: LTS Semantics over Global Types in ROUTEDSESSIONS

| $l ::=$ | Labels |
|----------------------|----------------|
| $pq!j$ | Direct Send |
| $pq?j$ | Direct Receive |
| $\text{via}_s(pq!j)$ | Routed Send |
| $\text{via}_s(pq?j)$ | Routed Receive |

Figure 8.3: LTS Labels in ROUTEDSESSIONS

$$\begin{array}{c}
 \frac{}{q \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{pq!j} T_j} \text{[LR1]} \\
 \\
 \frac{}{q \& \{l_i : T_i\}_{i \in I} \xrightarrow{qp?j} T_j} \text{[LR2]} \\
 \\
 \frac{T[\mu t. T/t] \xrightarrow{l} T'}{\mu t. T \xrightarrow{l} T'} \text{[LR3]} \\
 \\
 \frac{}{q_s \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{\text{via}_s(pq!j)} T_j} \text{[LR4]} \\
 \\
 \frac{}{q_s \& \{l_i : T_i\}_{i \in I} \xrightarrow{\text{via}_s(qp?j)} T_j} \text{[LR5]} \\
 \\
 \frac{}{p \hookrightarrow q : \{l_i : T_i\}_{i \in I} \xrightarrow{\text{via}_s(pq!j)} p \leftrightarrow q. j : \{l_i : T_i\}_{i \in I}} \text{[LR6]} \\
 \\
 \frac{}{p \leftrightarrow q. j : \{l_i : T_i\}_{i \in I} \xrightarrow{\text{via}_s(pq?j)} T_j} \text{[LR7]} \\
 \\
 \frac{\forall i \in I. T_i \xrightarrow{l} T'_i \quad \text{subj}(l) \notin \{p, q\}}{p \hookrightarrow q : \{l_i : T_i\}_{i \in I} \xrightarrow{l} p \hookrightarrow q : \{l_i : T'_i\}_{i \in I}} \text{[LR8]} \\
 \\
 \frac{T_j \xrightarrow{l} T'_j \quad \text{subj}(l) \neq q \quad \forall i \in I \setminus \{j\}. T'_i = T_i}{p \leftrightarrow q. j : \{l_i : T_i\}_{i \in I} \xrightarrow{l} p \leftrightarrow q. j : \{l_i : T'_i\}_{i \in I}} \text{[LR9]} \\
 \\
 \frac{l = \text{via}_s(\cdot) \quad \text{subj}(l) \neq q \quad \forall i \in I. T_i \xrightarrow{l} T'_i}{q \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{l} q \oplus \{l_i : T'_i\}_{i \in I}} \text{[LR10]} \\
 \\
 \frac{l = \text{via}_s(\cdot) \quad \text{subj}(l) \neq q \quad \forall i \in I. T_i \xrightarrow{l} T'_i}{q \& \{l_i : T_i\}_{i \in I} \xrightarrow{l} q \& \{l_i : T'_i\}_{i \in I}} \text{[LR11]}
 \end{array}$$

Figure 8.5: LTS over Local Types in ROUTEDSESSIONS

Semantics

$$\frac{}{p \rightarrow q : \{l_i : G_i\}_{i \in I} \xrightarrow{pq!j} p \rightsquigarrow q. j : \{l_i : G_i\}_{i \in I}} \text{[GR1]}$$

$$\frac{}{p \rightsquigarrow q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{pq?j} G_j} \text{[GR2]}$$

$$\frac{G[\mu t. G/t] \xrightarrow{l} G'}{\mu t. G \xrightarrow{l} G'} \text{[GR3]}$$

$$\frac{}{q \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{pq!j} T_j} \text{[LR1]}$$

$$\frac{}{q \& \{l_i : T_i\}_{i \in I} \xrightarrow{qp?j} T_j} \text{[LR2]}$$

$$\frac{T[\mu t. T/t] \xrightarrow{l} T'}{\mu t. T \xrightarrow{l} T'} \text{[LR3]}$$

$$\text{[LR4]}$$

$$\frac{l = \text{via}_s(\cdot) \quad \text{subj}(l) \neq q \quad \forall i \in I. T_i \xrightarrow{l} T'_i}{q \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{l} q \oplus \{l_i : T'_i\}_{i \in I}} \text{[LR10]}$$

Figure 8.3: LTS Labels in ROUTEDSESSIONS

$$\frac{\forall i \in I. G_i \xrightarrow{l} G'_i \quad \text{subj}(l) \notin \{p, q\}}{p \xrightarrow{s} q : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \xrightarrow{s} q : \{l_i : G'_i\}_{i \in I}} \text{[GR8]}$$

$$\frac{G_j \xrightarrow{l} G'_j \quad \text{subj}(l) \neq q \quad \forall i \in I \setminus \{j\}. G'_i = G_i}{p \rightsquigarrow_s q. j : \{l_i : G_i\}_{i \in I} \xrightarrow{l} p \rightsquigarrow_s q. j : \{l_i : G'_i\}_{i \in I}} \text{[GR9]}$$

$$\frac{T_j \xrightarrow{l} T'_j \quad \text{subj}(l) \neq q \quad \forall i \in I \setminus \{j\}. T'_i = T_i}{p \rightsquigarrow q. j : \{l_i : T_i\}_{i \in I} \xrightarrow{l} p \rightsquigarrow q. j : \{l_i : T'_i\}_{i \in I}} \text{[LR9]}$$

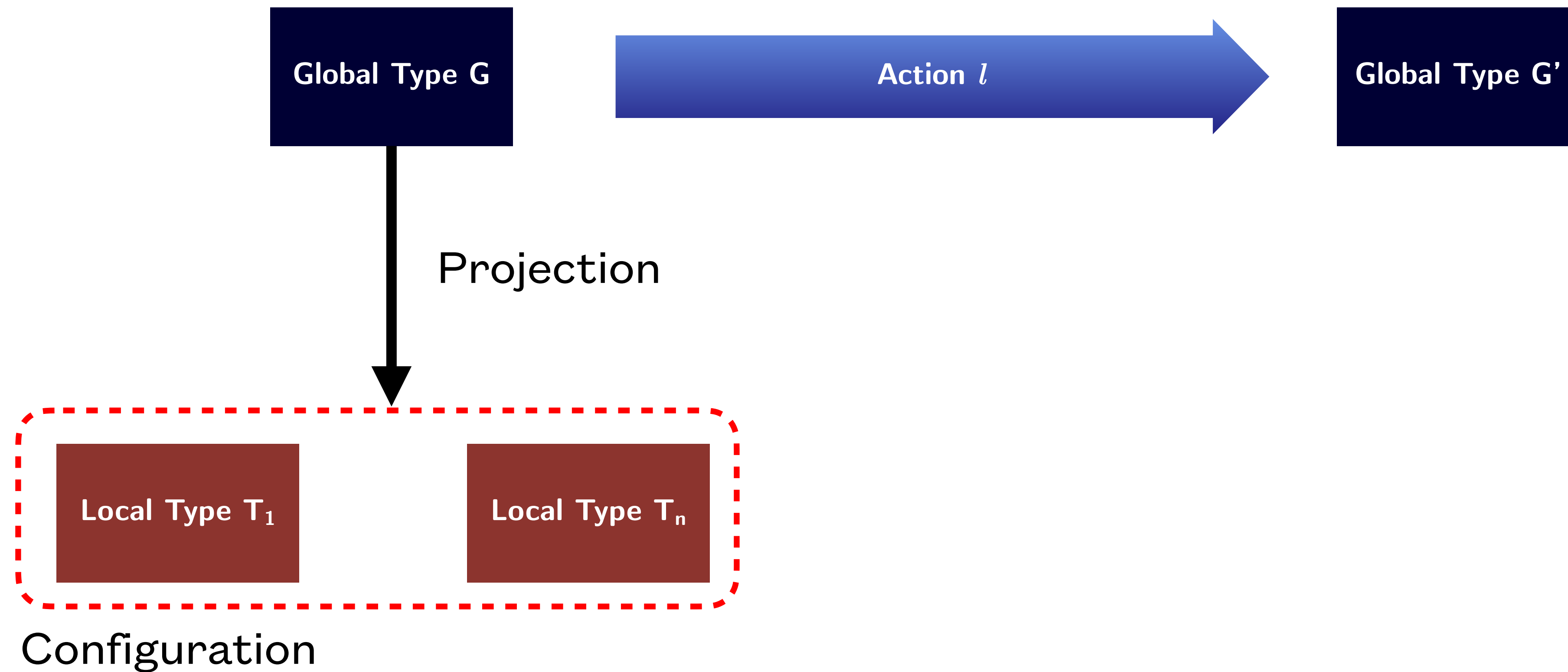
$$\frac{l = \text{via}_s(\cdot) \quad \text{subj}(l) \neq q \quad \forall i \in I. T_i \xrightarrow{l} T'_i}{q \oplus \{l_i : T_i\}_{i \in I} \xrightarrow{l} q \oplus \{l_i : T'_i\}_{i \in I}} \text{[LR10]}$$

$$\frac{l = \text{via}_s(\cdot) \quad \text{subj}(l) \neq q \quad \forall i \in I. T_i \xrightarrow{l} T'_i}{q \& \{l_i : T_i\}_{i \in I} \xrightarrow{l} q \& \{l_i : T'_i\}_{i \in I}} \text{[LR11]}$$

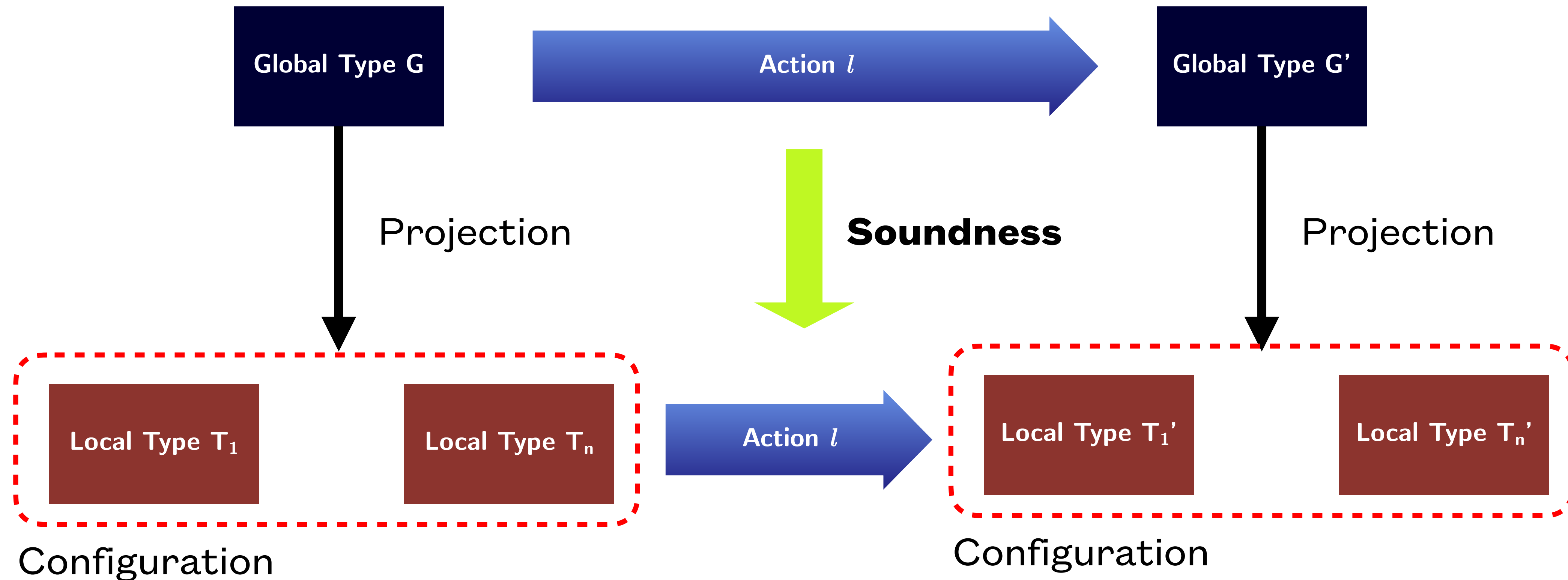
Figure 8.4: LTS Semantics over Global Types in ROUTEDSESSIONS

Figure 8.5: LTS over Local Types in ROUTEDSESSIONS

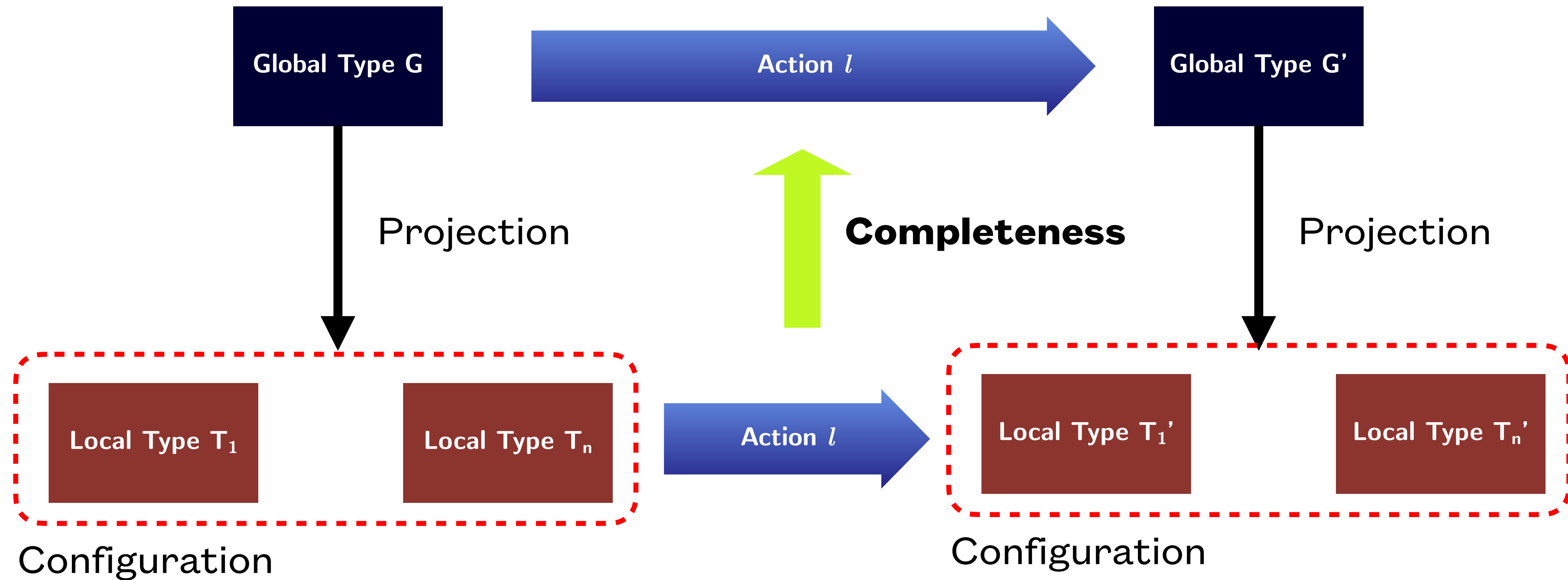
Semantics



Soundness



Completeness



Soundness & Completeness

Lemma 8.1 (Step Equivalence). *For all global types G and configurations s , if $\langle G \rangle < s$, then $G \xrightarrow{l} G' \iff s \xrightarrow{l} s'$ such that $\langle G' \rangle < s'$.*

Proof. By induction on the possible transitions in the LTSs over global types (to prove \implies , i.e. *soundness*) and configurations (to prove \impliedby , i.e. *completeness*).

Theorem 8.1 (Trace Equivalence). *Let G be a global type with participants $\mathcal{P} = \text{pt}(G)$, and let $\vec{T} = \{G \upharpoonright p\}_{p \in \mathcal{P}}$ be the local types projected from G . Then $G \approx (\vec{T}, \vec{e})$.*

Proof. Direct consequence of Lemma 8.1. □

Local Type T

Configurati

Towards ROUTEDSESSIONS

Definition 8.9 (Encoding on Global Types).

$$\begin{aligned} \llbracket \text{end}, s \rrbracket &= \text{end} && [\text{ENC-G-END}] \\ \llbracket t, s \rrbracket &= t && [\text{ENC-G-RECVAR}] \\ \llbracket \mu t. G, s \rrbracket &= \mu t. \llbracket G, s \rrbracket && [\text{ENC-G-REC}] \\ \llbracket p \rightarrow q : \{l_i : G_i\}_{i \in I}, s \rrbracket &= \begin{cases} p \rightarrow q : \{l_i : \llbracket G_i, s \rrbracket\}_{i \in I} & \text{if } s \in \{p, q\} \\ p \xrightarrow{s} q : \{l_i : \llbracket G_i, s \rrbracket\}_{i \in I} & \text{otherwise} \end{cases} && [\text{ENC-G-COMM}] \end{aligned}$$

`encode :: RouterRole -> CanonicalTheory -> NewTheory`

Towards ROUTEDSESSIONS

Definition 8.9 (Encoding on Global Types).

$$\llbracket \text{end}, s \rrbracket = \text{end} \quad [\text{ENC-G-END}]$$

$$\llbracket t, s \rrbracket = t \quad [\text{ENC-G-RECVAR}]$$

$$\llbracket \mu t. G, s \rrbracket = \mu t. \llbracket G, s \rrbracket \quad [\text{ENC-G-REC}]$$

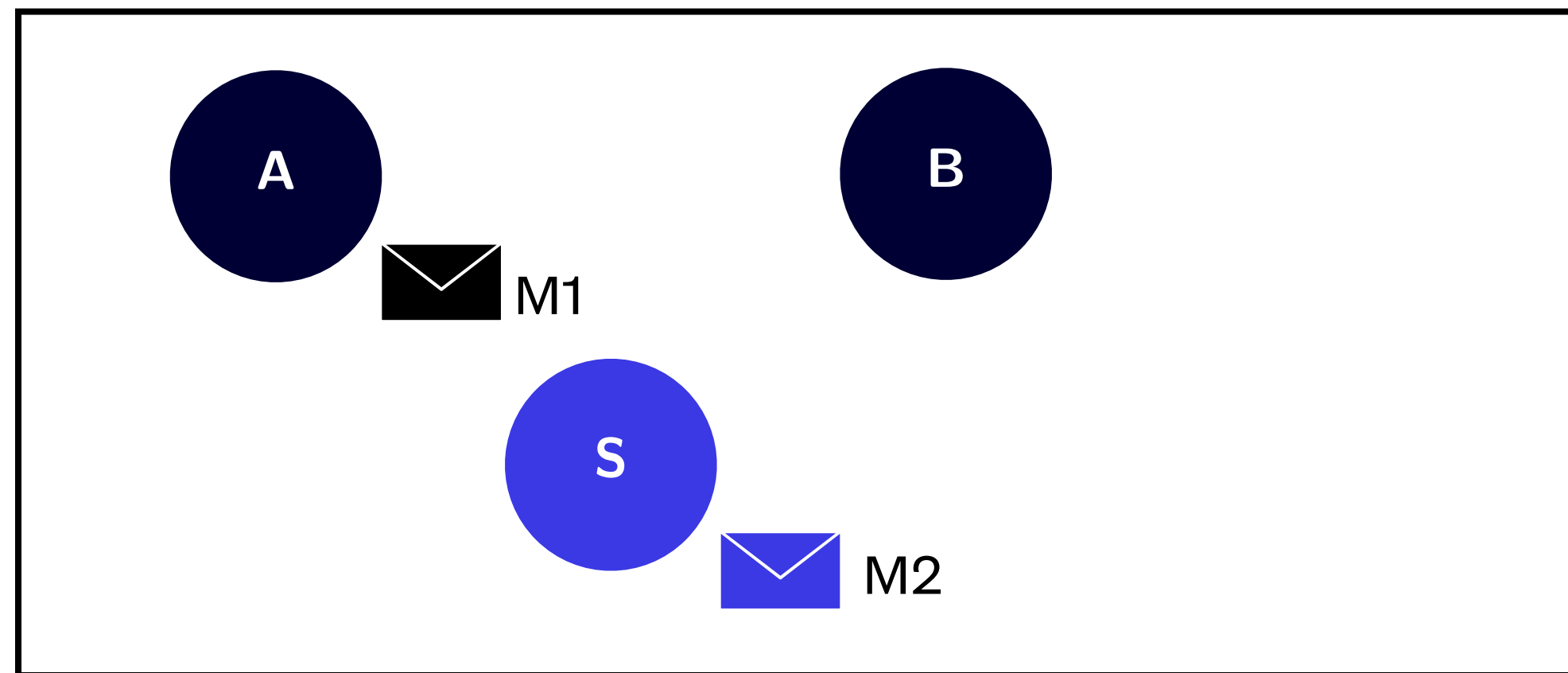
$$\llbracket p \rightarrow q : \{l_i : G_i\}_{i \in I}, s \rrbracket = \begin{cases} p \rightarrow q : \{l_i : \llbracket G_i, s \rrbracket\}_{i \in I} & \text{if } s \in \{p, q\} \\ p \xrightarrow{s} q : \{l_i : \llbracket G_i, s \rrbracket\}_{i \in I} & \text{otherwise} \end{cases} \quad [\text{ENC-G-COMM}]$$

`encode :: RouterRole -> CanonicalTheory -> NewTheory`

Encoding Preserves Semantics

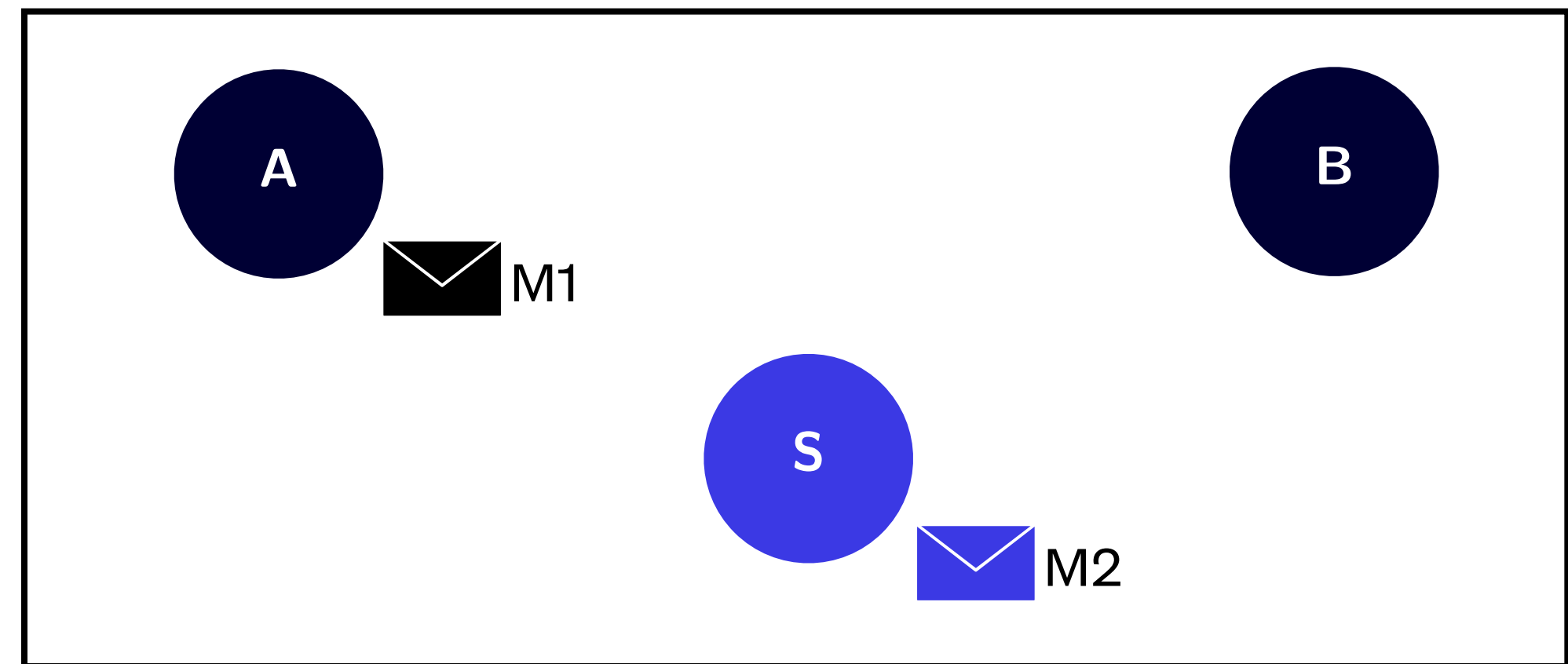
“Original communication”

- A sends M1 to B.
- S sends M2 to B.



ROUTEDSESSIONS

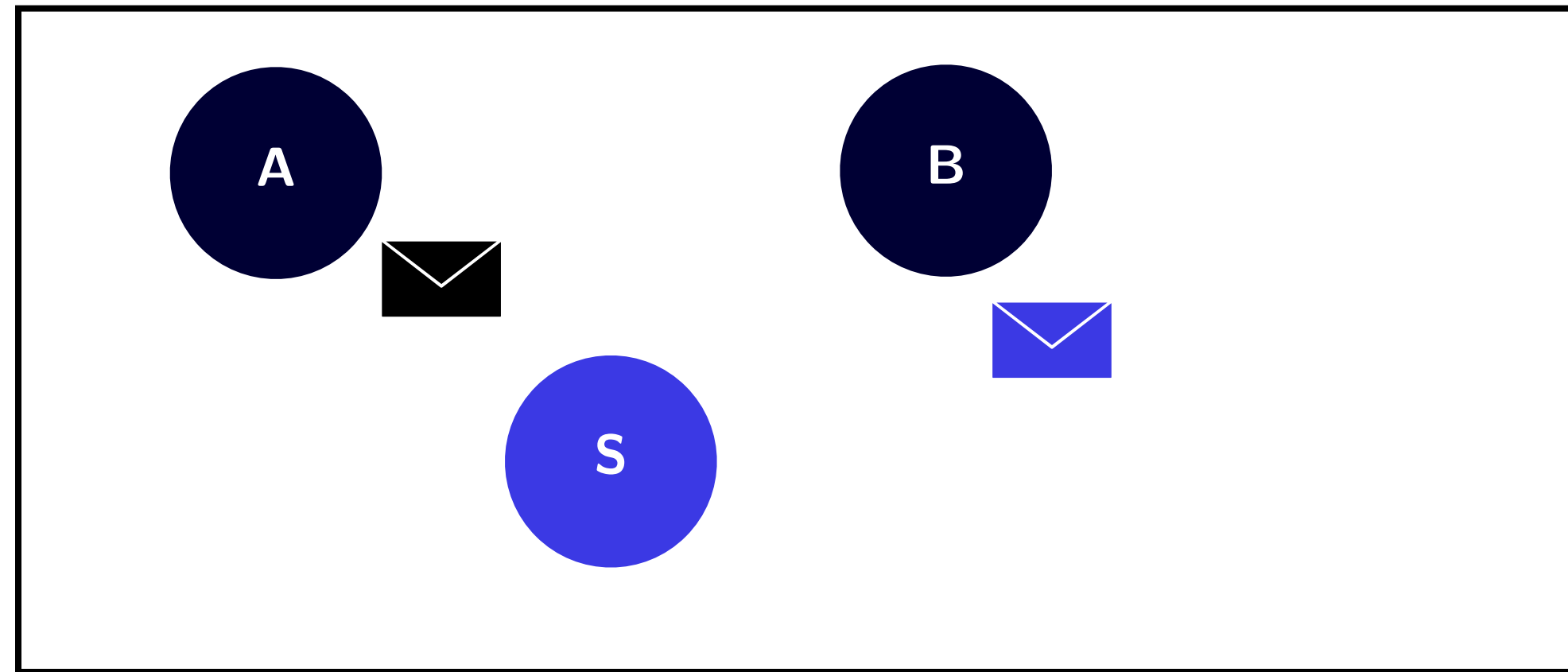
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Encoding Preserves Semantics

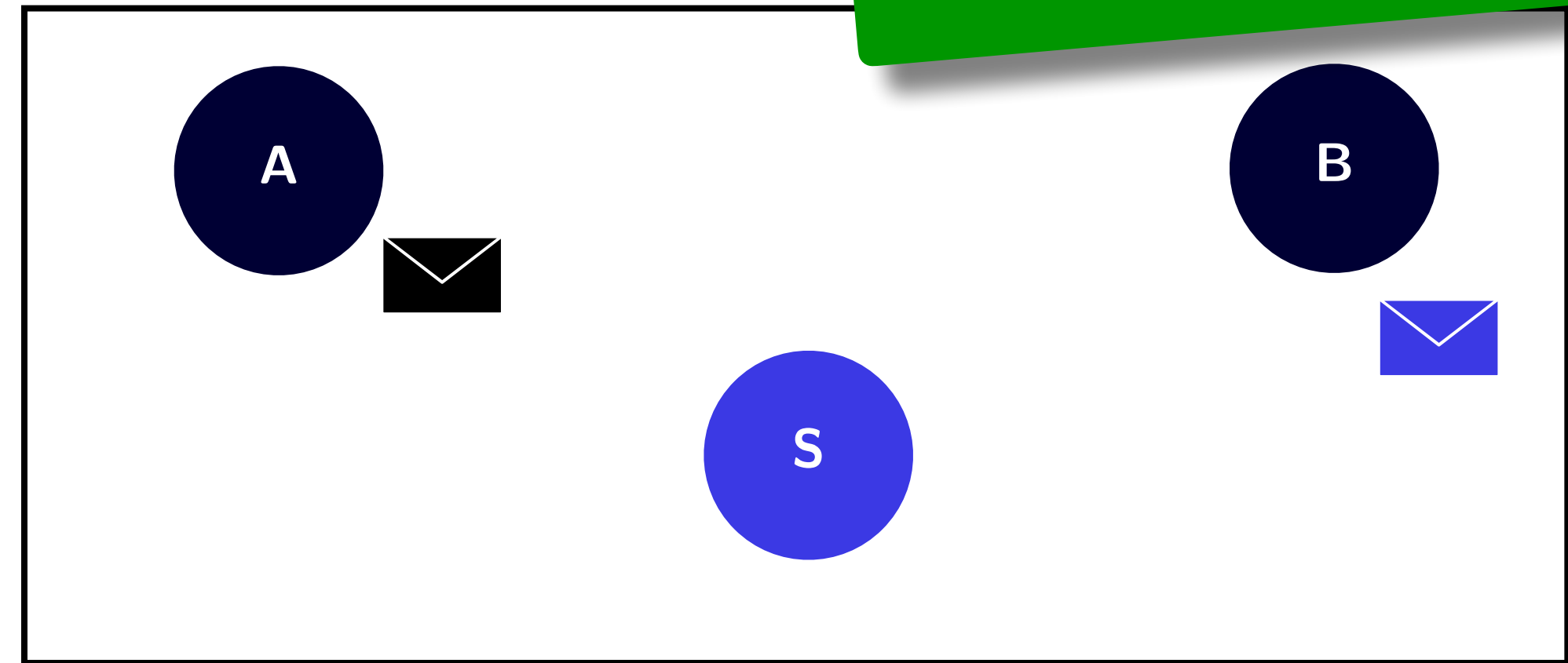
“Original communication”

- A sends M1 to B.
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ROUTEDSESSIONS

- A sends M1 to B via S.
- S sends M2 to B.



via S allows this

Encoding Preserves Semantics

“Original communication”

ROUTEDSESSIONS

- A
 - S
- Theorem 8.4** (Encoding Preserves Semantics). *Let G, G' be global types such that $G \xrightarrow{l} G'$ for some label l .*

$$\forall l, s. \left(G \xrightarrow{l} G' \implies \llbracket G, s \rrbracket \xrightarrow{\llbracket l, s \rrbracket} \llbracket G', s \rrbracket \right)$$

S

S

- **Theorem 8.1: Trace Equivalence**

Extended semantics on routed multiparty session types is sound and complete w.r.t. projection.

- **Theorem 8.2: Deadlock Freedom**

Well-formed communication protocols do not get stuck.

- **Theorem 8.3: Encoding Preserves Well-formedness**

If the original communication is well-formed, so is the encoded routed communication.

- **Theorem 8.4: Encoding Preserves Semantics**

If the global type makes a step, the encoded global type makes a compatible step.

Evaluation

- **Theorem 8.1: Trace Equivalence**

Extended semantics on routed multiparty session types is sound and complete w.r.t. projection.

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Evaluation

- Lemma 8.1: Step Equivalence
- Lemma 8.2: (LTS) Preservation of Well-formedness
- Lemma 8.3: Progress for Well-formed Global Types
- Lemma 8.5: Encoding Preserves Projection
- Lemma A.1: Local LTS Preserves Merge
- Lemma A.3: Commutativity between Encoding and Substitution
- Lemma A.8: Encoding on Global Types Preserves Merge

Concluding Remarks

Communication Safety in Modern Web Programming

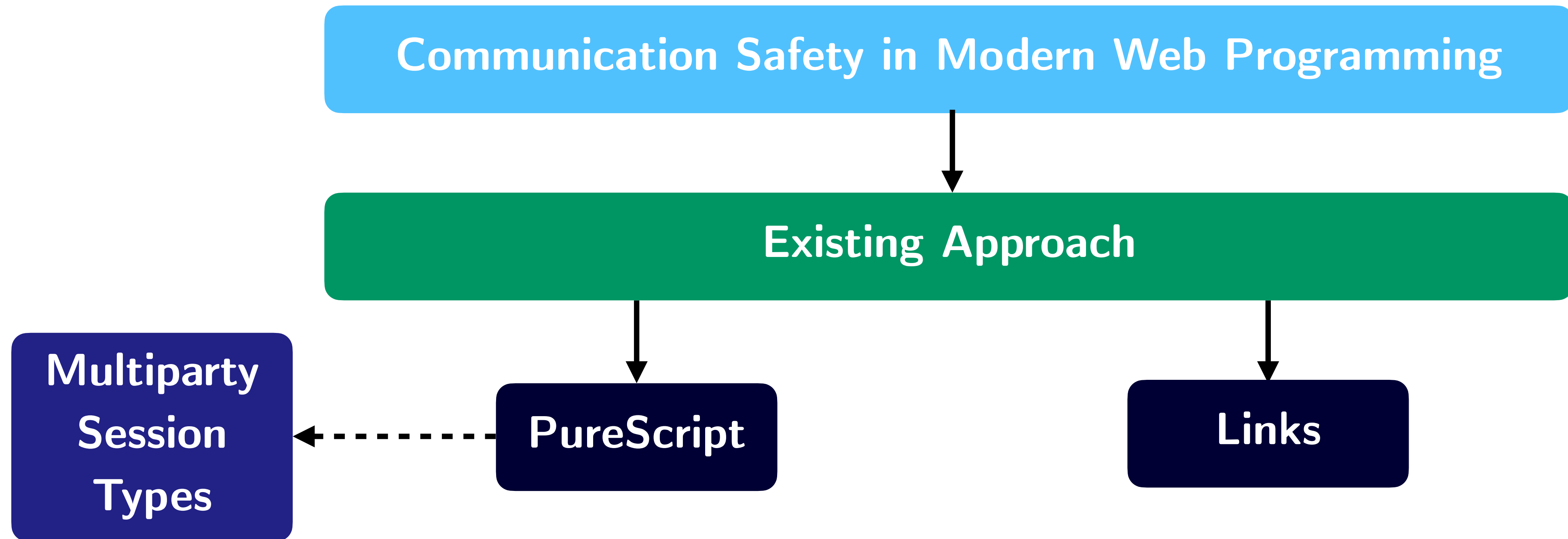
Communication Safety in Modern Web Programming

Existing Approach

Multiparty
Session
Types

PureScript

Links



Communication Safety in Modern Web Programming

Existing Approach

Multiparty
Session
Types

PureScript

Links

Limitations of Current State of the Art

Not Widely Used

Only Server-Centric
Protocol

Communication Safety in Modern Web Programming



Limitations of Current State of the Art



Not Widely Used



**Only Server-Centric
Protocol**

Communication Safety in Modern Web Programming

```
graph TD; A[Communication Safety in Modern Web Programming] --> B[Limitations of Current State of the Art]; B --> C[Not Widely Used]; B --> D[Only Server-Centric Protocol]; C --> E["SessionTS<br/>Same communication guarantees as state of the art, but specifically targets modern web programming."];
```

Limitations of Current State of the Art

Not Widely Used

Only Server-Centric Protocol

SessionTS

Same communication guarantees as state of the art, but specifically targets modern web programming.

Communication Safety in Modern Web Programming

Limitations of Current State of the Art

Not Widely Used

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Same communication guarantees as state of the art, but specifically targets modern web programming.

Only Server-Centric Protocol

ROUTEDSESSIONS

Formalise routed communication, prove that peer-to-peer client interactions over server-centric topology preserves semantics and communication safety.

Communication Safety in Modern Web Programming

Limitations of Current State of the Art

Not Widely Used

SessionTS

Same communication guarantees as state of the art, but specifically targets modern web programming.

Only Server-Centric Protocol

ROUTEDSESSIONS

Formalise routed communication, prove that peer-to-peer client interactions over server-centric topology preserves semantics and communication safety.