## i

$$x_{1} \times x_{1} : (1,2) \times (1,2) = 1 \times 1 + 2 \times 2 = 5$$

$$x_{1} \times x_{2} : (1,2) \times (-2,1) = 1 \times -2 + 2 \times 1 = 0$$

$$x_{1} \times x_{3} : (1,2) \times (-1,-2) = 1 \times -1 + 2 \times -2 = -5$$

$$x_{1} \times x_{4} : (1,2) \times (2,-1) = 1 \times 2 + 2 \times -1 = 0$$

$$x_{2} \times x_{1} : (-2,1) \times (1,2) = -2 \times 1 + 1 \times 2 = 0$$

$$x_{2} \times x_{2} : (-2,1) \times (-2,1) = -2 \times -2 + 1 \times 1 = 5$$

$$x_{2} \times x_{3} : (-2,1) \times (-1,-2) = -2 \times -1 + 1 \times -2 = 0$$

$$x_{2} \times x_{4} : (-2,1) \times (2,-1) = -2 \times 2 + 1 \times -1 = -5$$

$$x_{3} \times x_{1} : (-1,-2) \times (1,2) = -1 \times 1 + -2 \times 2 = -5$$

$$x_{3} \times x_{2} : (-1,-2) \times (-2,1) = -1 \times -2 + -2 \times 1 = 0$$

$$\Rightarrow \begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 5 & 0 & -5 \\ -5 & 0 & 5 & 0 \\ 0 & -5 & 0 & 5 \end{bmatrix}$$

$$x_4 \times x_1 : (2, -1) \times (1, 2) = 2 \times 1 + -1 \times 2 = 0$$
  
 $x_4 \times x_2 : (2, -1) \times (-2, 1) = 2 \times -2 + -1 \times 1 = -5$   
 $x_4 \times x_3 : (2, -1) \times (-1, -2) = 2 \times -1 + -1 \times -2 = 0$   
 $x_4 \times x_4 : (2, -1) \times (2, -1) = 2 \times 2 + -1 \times -1 = 5$ 

 $x_3 \times x_3 : (-1, -2) \times (-1, -2) = -1 \times -1 + -2 \times -2 = 5$  $x_3 \times x_4 : (-1, -2) \times (2, -1) = -1 \times 2 + -2 \times -1 = 0$ 

ii — anotherthing anotherthing