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(2063)

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B.Tech 2nd Semester Examination

Engineering Mathematics-II (NS)

NS-104

Time : 3 Hours

Max. Marks : 50

The candidates shall limit their answers precisely within the answer-book (40 pages) issued to them and no supplementary/continuation sheet will be issued.

Note : Attempt five questions in all selecting one question from each sections A, B, C and D of the question paper and all subparts of the question in section E. Use of non-programmable calculators are allowed.

SECTION - A

1. (a) Test the series for convergence.

$$\frac{2}{2.3.4} + \frac{4}{3.4.5} + \frac{6}{4.5.6} + \dots \quad (5)$$

- (b) Discuss the convergence of series

$$\frac{1}{2} + \frac{2}{3}x + \left(\frac{3}{4}\right)^2 x^2 + \left(\frac{4}{3}\right)^3 x^3 + \dots \infty \quad (5)$$

2. (a) Using Integral test, show that the series

$$\sum n e^{-n^2} \text{ converges} \quad (5)$$

- (b) Examine the convergence of the series

$$\frac{1}{2^3} - \frac{1}{3^3}(1+2) + \frac{1}{4^3}(1+2+3) - \left(\frac{1}{5^3}(1+2+3)+4\right) + \dots \quad (5)$$

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SECTION - B

3. (a) Obtain the Fourier series for $f(x)=e^{-x}$ in the interval $0 < x < 2\pi$. (5)
- (b) Expand in series of sines and cosines of multiple angles of x , the periodic function $f(x)$ with period 2π defined as $f(x)=\begin{cases} -1 & \text{for } -\pi < x < 0 \\ 1 & \text{for } 0 \leq x \leq \pi \end{cases}$ Also calculate the sum of the series at $x=0, \pm \pi$. (5)
4. (a) Obtain the half range series for e^x in $0 < x < 1$. (5)
- (b) If the Fourier series $\frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$ of $f(x)$ converges to $f(x)$ at every point of the closed interval $[0, 2\pi]$, then prove that
- $$\frac{1}{\pi} \int_0^{2\pi} [f(x)]^2 dx = \frac{a_0^2}{2} + \sum_{n=1}^{\infty} (a_n^2 + b_n^2) \quad (5)$$

SECTION - C

5. (a) Solve $\frac{dy}{dx} + y \sec x + \tan x$ (5)
- (b) Solve $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = \log x \sin(\log x)$ (5)
6. (a) Using method of variation of parameter solve $\frac{d^2y}{dx^2} + 16y = 32 \sec x$ (5)

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- (b) Solve $x^2p^2 + xyp - 6y^2 = 0$, where $b = \frac{dy}{dx}$ (5)

SECTION - D

7. (a) Prove that $\nabla \times (\nabla \times A) = \nabla(\nabla \cdot A) - \nabla^2 A$, where ∇ is a vector differentiable operator and A is a differentiable vector function. (5)
- (b) Evaluate by stoke's Theorem $\oint_C (e^x dx + 2y dy - dz)$ where C is the curve $x^2 + y^2 = 4, z = 2$. (5)
8. (a) Evaluate $\oint_C [(x^2 - \cosh y) dx + (y + \sin x) dy]$ using Green's theorem, where C is the rectangle with vertices (0, 0), (π , 0), (π , 1), (0, 1). (5)
- (b) Evaluate $\iiint_V \phi dv$, where, $\phi = 45x^2y$ and V is the closed region bounded by the planes $4x + 2yz = 8, x = 0, y = 0, z = 0$. (5)

SECTION - E

9. (a) Show the series $\sum_{n=1}^{\infty} \frac{1}{2^{n-1}}$ is convergent and converges to 2. (1)
- (b) Define power series and its interval of convergence. (1)

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(c)	Discus Fourier series for even and odd functions.	(1)
(d)	Expand in a Fourier series, the function $f(x)=x$ in the interval $[-\pi, \pi]$	(1)
(e)	Solve: $\frac{d^4y}{dx^4} + 4x = 0$	(1)
(f)	Define Clairaut equation and also find its solution.	(1)
(g)	If $\vec{r} = x\hat{i} + y\hat{j} + 3\hat{k}$, show that $\text{div}\vec{r} = 3$	(1)
(h)	Define irrotational vectors field.	(1)
(i)	Find the particular integral of $\frac{d^3y}{dx^3} - 3\frac{dy}{dx} + 2y = e^{2x}$	(1)
(j)	State Leibnitz's Rule for the convergence of an alternating infinite series.	(1)