

- ④ List name of the employees who have salary more than 10000 & Less 25000;

$\pi_{ename} (\sigma_{salary > 10000 \wedge salary < 25000} (Emp))$

- ⑤ Salary more than 10000 or Less than 25000

$\pi_{ename} (\sigma_{salary > 10000 \vee salary < 25000} (Emp))$

04/03/2024

Union \Rightarrow

$\Rightarrow \pi_{c.name} (depositor) \cup \pi_{c.name} (loan)$

Customer name from depositor or loan

\rightarrow Arity of both ^{no. of columns} ~~columns~~ queries must be same

\rightarrow Domain of Respective Columns must be same

eg $\rightarrow \pi_{c.name} (depositor) \cup \pi_{balance} (loan)$

(X)

\Rightarrow Set-difference $(-)$

$\phi \rightarrow$ List all the depositors who do not have any loan.

$\rightarrow \pi_{c.name} (depositor) - \pi_{c.name} (loan)$

\Rightarrow Cartesian Product (\times)

eid	ename	desig
1	A	101
2	B	102
3	C	101

did	dname
101	CS
102	IT

\Rightarrow ~~Renam~~

Emp \times Dept

eid	ename	desig	did	dname
1	A	101	101	CS
1	A	101	102	IT
2	B	102	101	CS
2	B	102	102	IT
3	C	101	101	CS
3	C	101	102	IT

\Rightarrow Rename $\rho_x (E)$

Could be an ~~old~~ Table name or expression/query as well

In case of table name $\rho_x (E)$ will be renamed as x

In case of expression $\Rightarrow E$ will be represented as x

Additional Operations

⇒ Intersection (\cap)

$$R \cap S = R - (R - S)$$

R	S	$R \cap S$	$R - S$
A	G	B	AC
B	H	A	E
C	B	D	F
D	A		
E	P		
F	X		

$R - (R - S)$

B
A
D

⇒ Natural Join (\bowtie)

$$(R \bowtie S) = \text{result}$$

$$\pi_{R \cup S} \left(\sigma_{r.attr1 = s.attr1 \wedge r.attr2 = s.attr2 \wedge \dots} (R \times S) \right)$$

Emp		
Empid	ename	did
1	A	101
2	B	102
3	C	101

Dept		
did	dname	
101	CS	
102	IT	
103	Mech	

Emp \bowtie Dept

eid	ename	did	did	dname
1	A	101	101	CS
2	B	102	102	IT
3	C	101	101	CS

⇒ Division operation (\div)

Q → List all the customers who have accounts in all branches of jaipur.

$$(R1 \div R2) = R1 \text{ where } R1 = \text{all the branches of jaipur}$$

$$R1 = \pi_{bname} \left(\sigma_{b.city = \text{jaipur}} (branch) \right)$$

$$R2 = \pi_{cname, bname} (depositor \bowtie loan)$$

5/3/2021

Extended Relational Algebra Operations

$$\Rightarrow \pi_{ename, basic + da + HRA} (Emp)$$

$$\Rightarrow \pi_{ename, (basic + da + HRA) \text{ as salary}} (Emp)$$

also

We can use Aggregate function

$$\Rightarrow \sigma_{sum(salary)} (Emp)$$

Outer Joins \Rightarrow

① Left Outer Join (\bowtie)

② Right Outer Join (\ltimes)

③ Full Outer Join (\ltimes)

Operation with Null values \Rightarrow

\rightarrow All arithmetic operations with null returns null.

$< <= > >= \neq \Rightarrow$ Returns Unknown

Boolean Logical Operations

AND \Rightarrow True & Unknown \Rightarrow Unknown

false & unknown \Rightarrow false

unknown & unknown \Rightarrow Unknown

OR \Rightarrow

True ^{or} unknown \Rightarrow True

false ^{or} unknown \Rightarrow Unknown

Unknown ^{or} unknown \Rightarrow Unknown

Not \Rightarrow

not (unknown) \Rightarrow Unknown

Assignment Operator \Rightarrow

eg \rightarrow \leftarrow

$$\left\{ \begin{array}{l} R \\ T \end{array} \right\} \leftarrow \pi_{ename, salary} (Emp)$$

Temporary table in which we want to store the result.

Relation

$$(r \leftarrow r - E)$$

eg →

$Emp \leftarrow Emp - (\sigma_{ename='RAM'}(Emp))$

$loan \leftarrow loan - (\sigma_{amount \geq 0 \wedge amount \leq 1000}^{(loan)})$

Insertion ⇒

$\{r \leftarrow r \cup E\}$

eg ⇒

$Emp \leftarrow Emp \cup \{101, 'RAM', 50000\}$

Deletion • Update ⇒

$account \leftarrow \Pi_{a_number, a_name, balance \neq 1.05}^{(account)}$

Operations deals with Null ⇒

⇒ select

$\sigma_{salary > 30000}(Emp)$

1	A	50000
2	B	45000
4	D	35000

Emp		
eid	ename	Salary
1	A	50000
2	B	45000
3	C	null
4	D	35000
5	E	null
6	F	30000
7		

$\sigma_p(E) \Rightarrow$ If P's value is false or unknown then there will be no result.

Join Operations ⇒

$r \bowtie s$

$t_s \in S$

$t_r \in R$

If both are null that will not match

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(÷)

Enrolled ÷ Course

sid
1

Enrolled	
sid	cid
1	DBMS
2	DBMS
1	OS
3	OS

cid
DBMS
OS

$R(x, y) \div S(y)$

⇒ Attributes of S must be proper subset of attributes of R.

⇒ For each corresponding value of y above notation will return value of x from tuple $\langle x, y \rangle$ which exists ~~everywhere~~ for each y of S.

Database Design

Normalisation

we need to first understand.

⇒ Functional dependencies

$eid \rightarrow ename$
 { If ⁱⁿ any two rows eid is same then $ename$ will also be same. }

$eid \rightarrow design \times$

$design \rightarrow gradeP. \checkmark$

eid	ename	design	gradeP.
1	A	IA	2800
2	B	Prog.	4800
1	A	Prog	4800
3	C	IA	2800

→ $ename$ is functionally determined by eid .

→ eid functionally determine $ename$

→ $ename$ is functionally dependent upon eid .

$x \rightarrow y$
 if $U(x) = V(x)$
 then $U(y) = V(y)$

	x	y
U		
V		

Inference Rules →

① Reflexive →

if $Y \subseteq X$ then X will determine Y $\{X \rightarrow Y\}$
^{Superset}
_{Subset}

② Augmentation →

If $X \rightarrow Y$ ^{than} $XZ \rightarrow YZ$

$X = eid, ename$

$Y = ename$

Reflexive ⇒ $\{X \rightarrow Y \text{ because } Y \subseteq X\}$

Emp

cid	ename	dob
1	A	3-2-90
2	B	5-6-85
1	A	3-2-90
4	C	8-3-89
2	B	5-6-85
6	D	2-3-87

$\{eid, \cancel{dob} \rightarrow ename \text{ then } cid, \cancel{ename} \rightarrow ename, dob\}$

Augmentation.

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③ Transitive \Rightarrow

If $x \rightarrow y$ & $y \rightarrow z$ then

$$x \rightarrow z$$

$eid \rightarrow ename$ &

$ename \rightarrow mob$ then

$$\underline{eid \rightarrow mob}$$

Emp		
eid	ename	mob
1	A	—
2	B	—
3	C	—
4	D	—
5	E	—
2	B	—
3	C	—
1	A	—

~~Armstrong~~

Armstrong Rule

- Reflexive
- Augmentation
- Transitive

④ Additive/ Union Rule

$$\left. \begin{array}{l} x \rightarrow y \\ x \rightarrow z \end{array} \right\} \underline{x \rightarrow yz}$$

⑤ Decomposition / Productive Rule

$$x \rightarrow yz \quad \left\{ \begin{array}{l} x \rightarrow y \\ x \rightarrow z \end{array} \right.$$

⑥ Pseudo Transitive Rule

$$\left. \begin{array}{l} x \rightarrow y \\ yz \rightarrow w \end{array} \right\} \underline{xz \rightarrow w}$$

Fully Functional Dependency

\Rightarrow If $x \rightarrow y$ then y will be functionally dependent on x , but will not be dependent on any proper subset of x .

$$ename, \text{dob} \rightarrow G.P.$$

If $ename, \text{dob}$ is fully determining $G.P$ then

$$ename \not\rightarrow G.P$$

$$\text{dob} \not\rightarrow G.P$$

Partial Functional Dependency

\Rightarrow If R is a relation and K is its candidate key, if X is proper subset of K and $X \rightarrow A$ means A is a partial functional dependent on K .

Prime Attributes

\Rightarrow If an attribute is part of any candidate key, this is known as prime attribute.

\Rightarrow An attribute which is not part of any candidate key, is known as non-prime attributes.

Trivial Dependency

$A \rightarrow B$ is known as trivial dependency

if B is subset of A {same as reflexive rule}

$$\downarrow$$
$$B \subseteq A$$

Closure \Rightarrow is set of all implied / inferred functional dependencies of F is known as closure of F . and represented by F^+ .

$$F^+ = \underbrace{F}_{\text{Set of FD}} \cup \underbrace{F'}_{\substack{\text{Set of FD} \\ \text{inferred from } F}}$$

Normalization

\Rightarrow Process to analyse ~~data~~ existing relations by functional dependencies to minimise redundancy and updation anomalies.

\Rightarrow we ~~do not~~ sub divide tables which is known as decomposition.

There are 2 desirable conditions for decomposition

① Lossless join decomposition

② dependency preservation.

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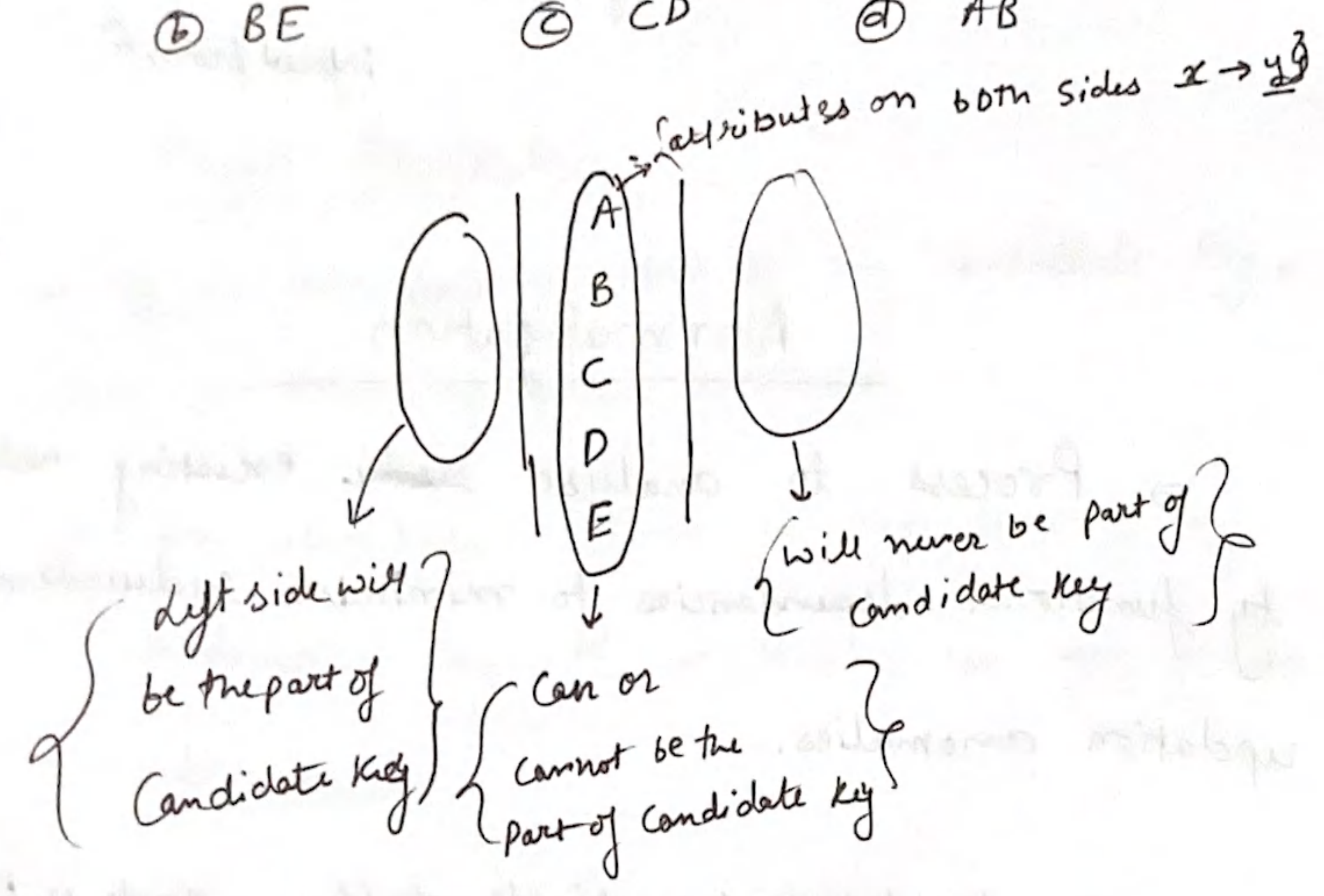
Q → If R is a relational Schema $R(A, B, C, D, E)$ with the following functional dependencies

$AD \rightarrow C, B \rightarrow A, C \rightarrow E, E \rightarrow BD$

Which of following is ^{not} a Candidate Key of R.

- (a) AD (b) BE (c) CD (d) AB

Method 1 →



Method 2 → use options → $(AD)^+ \Rightarrow \{A, B, C, E, D\}$ ✓
 This will be one of the candidate key.

$(BE)^+ \Rightarrow \{B, E, A, D, C\}$ ✓
 This one is also candidate key

$(CD)^+ \Rightarrow \{C, D, E, B, A\}$ ✓

$$(AB)^+ \Rightarrow \{A, B\}$$

Answer → AB is not a Candidate Key of R.

Q. $R(A, B, C, D, E, F, G, H, I, J)$

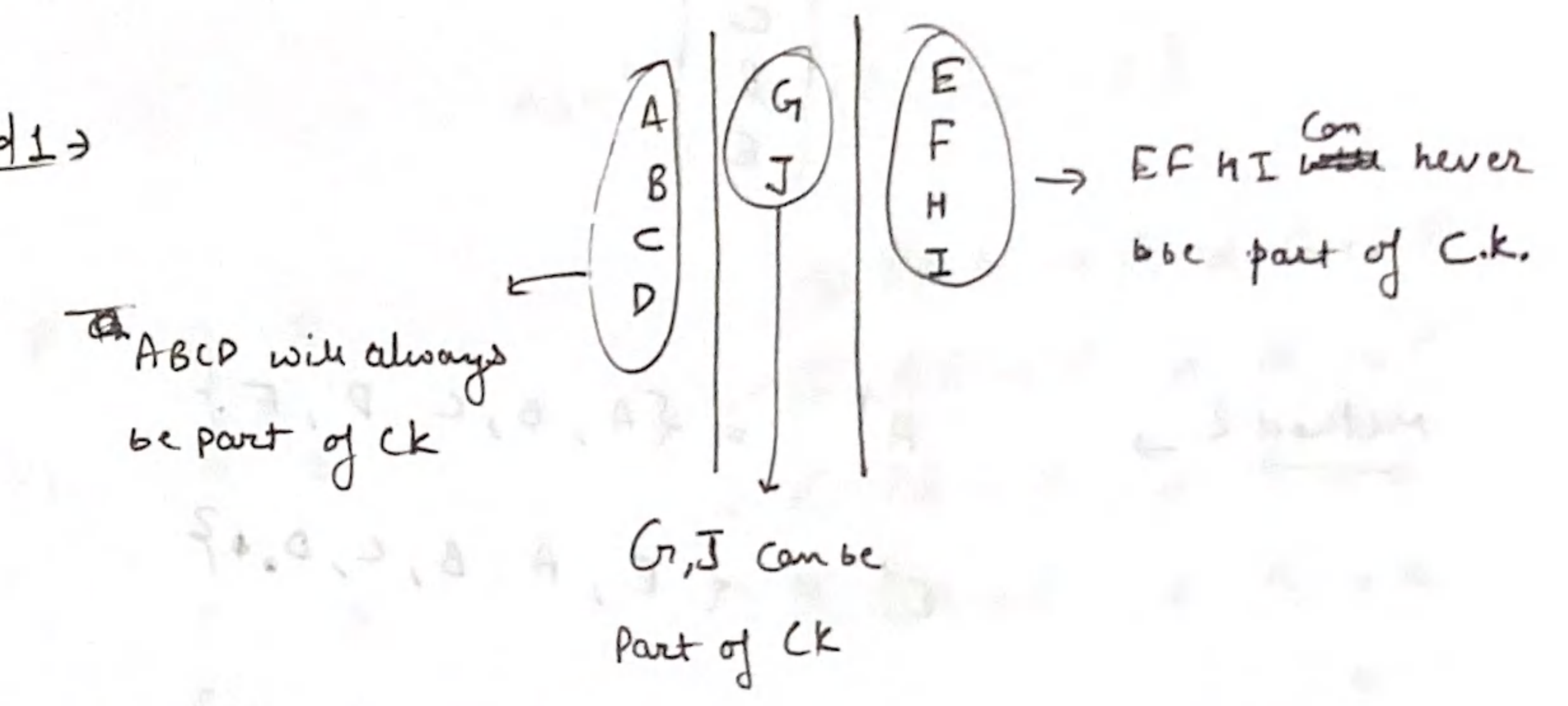
FD ⇒ $ABD \rightarrow E, AB \rightarrow G, B \rightarrow F, C \rightarrow J, CJ \rightarrow I$

$G \rightarrow H$

find C.K. ⇒

- (a) ABCD (b) ABGF (c) ABCI (d) ABC

Method 1 →



$$ABCD^+ = \{A, B, C, D, E, F, G, H, I, J\}$$

If we add G or J with ABCD even though ABCD is enough to determine whole Relation it would become Superkey $\{ABCDG \text{ or } ABCDJ \text{ or } ABCDGJ\}$ will be Super Key.

Q → R(A B C D E)

FD ⇒ $A \rightarrow BC$, $CD \rightarrow E$, $B \rightarrow D$, $E \rightarrow A$

CK?

✓ (A) A, E, CD, BE ✓ (B) AB, CD, EB, BC

✗ (C) A, E, C, B, D ✗ (D) A, E, CD, BD

Method 1

A
B
C
D
E

Method 2 →

$A^+ = \{A, B, C, D, E\}$

$E^+ = \{E, A, B, C, D\}$

$CD^+ = \{C, D, E, A, B\}$

$BE^+ = \{B, D, E, A, C\}$

⇒

$BD^+ = \{B, D\}$

Q → $AB \rightarrow C$, $CD \rightarrow E$, $DE \rightarrow B$

Key?

(A) AB

(B) ABD

(C) ABC

(D) none of Above

Ans →

A	B
	C
	D
	E

$AB^+ = \{A, B, C\}$

$ABD^+ = \{A, B, C, D, E\}$

Q

P	Q	R
1	4	2
1	5	3
1	6	3
3	2	2

✗ (A) $PR \rightarrow Q$ & $Q \rightarrow P$

✓ (B) $QR \rightarrow P$ & $Q \rightarrow P$

✗ (C) $PQ \rightarrow R$ & $R \rightarrow Q$

✗ (D) $QR \rightarrow P$ & $Q \rightarrow R$

which FD holds. ↑

↑

{ Only on option B our FD is not failing }
so, it is correct.