Radar cross section detection calculator

ANSYS, Inc.

This tutorial demonstrates how to determine a radar's ability to track differently sized targets with varying radar cross sections using Python and PySTK. It is inspired by this tutorial.

What is radar cross section?

One important property of a potential radar target is its radar cross section (RCS), which measures how easily the object can be detected by a radar, with a higher RCS corresponding to a more easily detected target. How easily an object can be detected has to do with its echo, which is a function of its size, shape, and orientation. RCS is the projected area of a metal sphere that would return the same echo signal as the target if it were substituted for the target. Through STK, it is possible to either specify the RCS of all targets at the scenario level, or to specify the RCS individually for each target. It is also possible to select different RCS computation methods, including directly using a constant value, using output files from Ansys HFSS, and using aspect dependent RCS files. Finally, STK supports the use of Swerling cases, which account for RCS fluctuations considering a range of fluctuation values and possible correlations between radar scans.

Problem statement

A radar site which surveils aircraft flying over it is located at latitude 35.75174° and longitude 139.35621°. The site's antenna is located 50 ft above the ground. The radar site has a servo system for antenna positioning, modeled by a sensor with a simple conic field of view with a 2° half angle. The sensor locks onto aircraft. The sensor can track aircraft with an elevation angle from 0° to 30°, and a range of up to 150 km. Anything higher than 30° is the cone of silence in which the radar cannot track the aircraft. The sensor has a monostatic aircraft surveillance radar on it with a search/track mode. The radar has a waveform with a fixed pulse repetition frequency of 1000 Hz and a pulse width of 1 microsecond. The radar's antenna is modeled by the cosine squared aperture rectangular antenna pattern, with an antenna transmit frequency between 2.7 and 2.9 GHz. The antenna also has an X dimension beamwidth of 5°, a Y dimension beamwidth of 1.4°, a design frequency of 2.8 GHz, a main-lobe gain of 34 dB, and an efficiency of 55%. The radar's transmitter has a frequency range of 2.7 – 2.9 GHz, a peak

power of 20 kW, and uses linear polarization. The radar's receiver uses linear polarization, and computes system noise temperature taking into account Sun and cosmic background noise.

Using a test aircraft, determine if the aircraft surveillance radar can see a large aircraft (RCS: 19 dBsm), a medium aircraft (RCS: 10 dBsm), a small aircraft (RCS: 0 dBsm), and a bird (RCS: -20 dBsm).

Launch a new STK instance

```
Start by launching a new STK instance. In this example, STKEngine is used.
```

```
from ansys.stk.core.stkengine import STKEngine
```

```
stk = STKEngine.start_application(no_graphics=False)
print(f"Using {stk.version}")
```

Create a new scenario

RFBOutputContext()

Using STK Engine v12.10.0

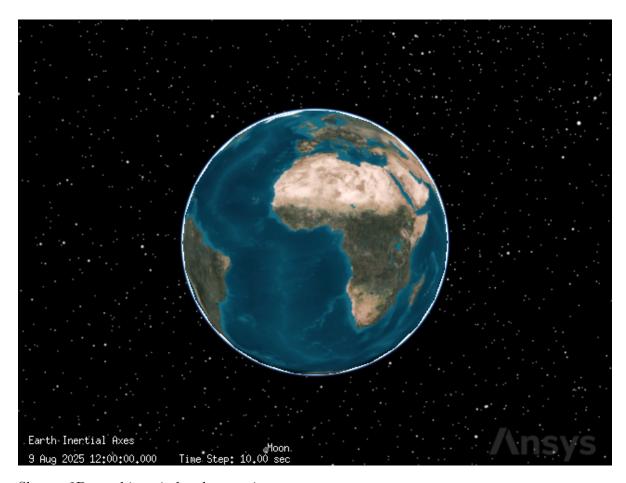
Create an STK scenario using the STK Root object:

```
root = stk.new_object_root()
root.new_scenario("IntroductionToRadar")
```

Once the scenario is created, it is possible to show a 3D graphics window by running:

from ansys.stk.core.stkengine.experimental.jupyterwidgets import GlobeWidget

```
globe_widget = GlobeWidget(root, 640, 480)
globe_widget.show()
```



Show a 2D graphics window by running:

from ansys.stk.core.stkengine.experimental.jupyterwidgets import MapWidget

```
map_widget = MapWidget(root, 640, 480)
map_widget.show()
```

RFBOutputContext()



Set the scenario time period

Using the newly created scenario, set the start and stop times. Rewind the scenario so that the graphics match the start and stop times of the scenario:

```
scenario = root.current_scenario
scenario.set_time_period("5 May 2024 03:00:00.000", "5 May 2024 03:30:00.000")
root.rewind()
```

Create the target aircraft

A test aircraft is used to analyze the airfield surveillance radar. Insert the aircraft:

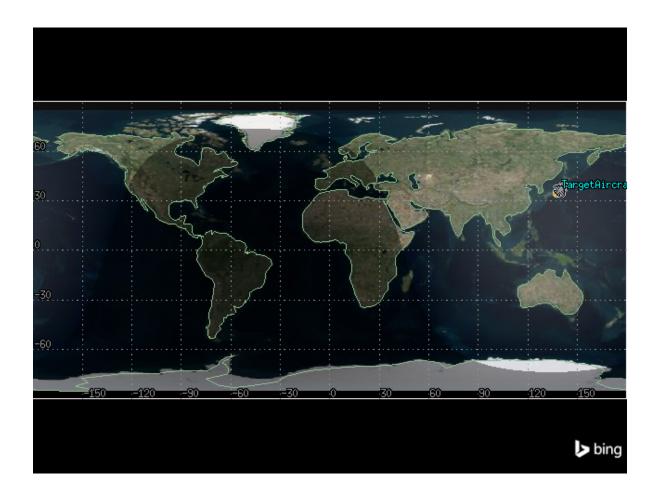
from ansys.stk.core.stkobjects import STKObjectType

```
aircraft = root.current_scenario.children.new(STKObjectType.AIRCRAFT, "TargetAircraft")
```

The aircraft's route is designated by a great arc propagator, which uses waypoints to calculate how the aircraft flies. The aircraft flies between two waypoints. The first is located at latitude 37° and longitude 139.7°, and the second is located at latitude 34° and longitude 139.1°. The aircraft flies at an altitude of 25000 ft (7.62 km) and a speed of 330 nm/hr at both waypoints.

Insert the first waypoint:

```
waypoint1 = aircraft.route.waypoints.add()
waypoint1.latitude = 37
waypoint1.longitude = 139.7
waypoint1.altitude = 7.62
waypoint1.speed = 330
Insert the second waypoint:
waypoint2 = aircraft.route.waypoints.add()
waypoint2.latitude = 34
waypoint2.longitude = 139.1
waypoint2.altitude = 7.62
waypoint2.speed = 330
Then, propagate the aircraft's route:
aircraft.route.propagate()
It is now possible to view the aircraft's route in the 2D graphics window:
map\_widget.camera.position = [-12290, 32850, 0.0]
map_widget.show()
```



Specify the radar cross section

Before setting up and constraining a radar system, STK allows the specification of a potential radar target's radar cross section. Use the RCS of a popular four-engined turboprop transport aircraft.

First, set the radar cross section's inherit property to False. When the inherit property is set to True, the RCS is inherited from the scenario. In this case, set the property to False to specify the RCS for only the aircraft:

```
aircraft.radar_cross_section.inherit = False
```

Get the model's first frequency band:

Configure the band to use a constant frequency:

band1.set_compute_strategy("Constant Value")

Set the constant frequency to 19 dBsm:

band1.compute_strategy.constant_value = 19

Next, configure the radar 3D graphics. Enable the visualization of RCS volume for the aircraft:

aircraft.graphics_3d.radar_cross_section.volume_graphics.show = True

It is now possible to see the aircraft's constant RCS in the 3D graphics window:

globe_widget.camera.position = [3435.3329, 3789.8112, 3815.5677]
globe_widget.show()



Insert the radar site

```
The radar site is modeled by a place object. Insert the site:
```

```
from ansys.stk.core.stkobjects import Place
```

```
radar_site = Place(root.current_scenario.children.new(STKObjectType.PLACE, "RadarSite"))
```

The site is located at latitude 35.75174° and longitude 139.35621°. The site's antenna is located 50 ft above the ground. Assign the site's position:

```
radar_site.use_terrain = False
radar_site.position.assign_geodetic(35.75174, 139.35621, 0.01524)
```

Insert the antenna servo system

Insert a sensor to simulate a servo system for antenna positioning. In STK, it is possible to create a spinning sensor to simulate a spinning radar antenna normally seen at an airfield. However, in this case, the sensor locks onto the aircraft and is constrained to point in a limited area. This simulates the actual field of view of the airfield surveillance radar both horizontally and vertically.

Insert a sensor on the radar site:

```
antenna_sensor = radar_site.children.new(STKObjectType.SENSOR, "AntennaSensor")
```

Assign a simple conic field of view with a 2° half angle to the sensor:

from ansys.stk.core.stkobjects import SensorPattern

```
antenna_sensor.common_tasks.set_pattern_simple_conic(2, 1)
```

<ansys.stk.core.stkobjects.SensorSimpleConicPattern at 0x7f9b501b72f0>

The sensor points at the aircraft, so set the sensor's pointing type to targeted:

from ansys.stk.core.stkobjects import SensorPointing

```
antenna_sensor.set_pointing_type(SensorPointing.TARGETED)
```

Finally, set the aircraft as the sensor's target:

antenna_sensor.pointing.targets.add(aircraft.path)

Set range and elevation angle constraints

A typical airport surveillance radar's nominal range is 60 miles and the elevation angle of the beam can track from 0° to 30°. Anything higher than 30° is the cone of silence in which the radar cannot track the aircraft. Extend the sensor's maximum range to 150 km in order to lock onto the aircraft when it's above the horizon.

First, insert an elevation angle constraint on the sensor:

```
from ansys.stk.core.stkobjects import AccessConstraintType
elevation_constraint = antenna_sensor.access_constraints.add_constraint(
          AccessConstraintType.ELEVATION_ANGLE
)
```

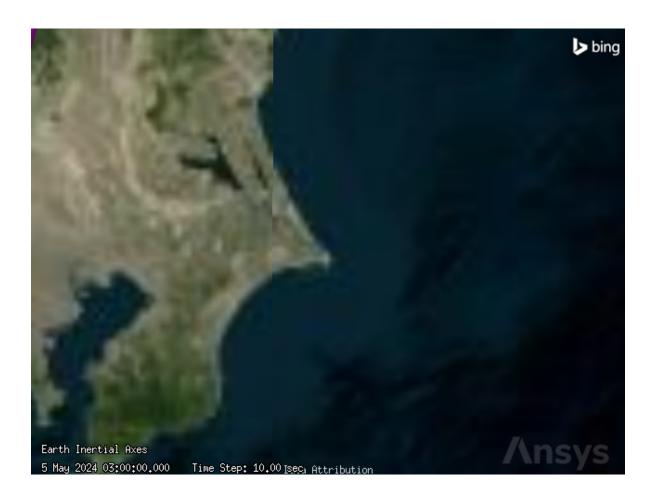
The elevation angle constraint is represented by an AccessConstraintMinMax object, through which it is possible to enable a minimum and/or maximum amount on the constraint, and designate what those amounts are. Use the constraint to enable a maximum elevation angle and set the maximum angle to 30°:

The range constraint is also represented by an AccessConstraintMinMax object. Use this object to set a maximum range of 150 km:

```
range_constraint.enable_maximum = True
range_constraint.maximum = 150
```

View the sensor's field of view using the 3D graphics window:

```
globe_widget.camera.position = [3555, 4084, 3861]
globe widget.show()
```



Calculate access

Next, get and compute the access between the sensor and the aircraft:

```
basic_access = antenna_sensor.get_access_to_object(aircraft)
basic_access.compute_access()
```

Generate an azimuth-elevation-range report to see the effect the constraints have on the accesses:

```
aer_df = (
    basic_access.data_providers.item("AER Data")
    .group.item("Default")
    .execute(scenario.start_time, scenario.stop_time, 60)
    .data_sets.to_pandas_dataframe()
)
aer_df
```

	access number	time	azimuth	elevation	range
0	1	5 May 2024 03:00:00.0000000000	12.45404734722865	2.4262391541155717	142.1935465
1	2	5 May 2024 03:00:00.465588995	155.33552870842385	28.14590949842654	16.08790699
2	1	5 May 2024 03:00:00.196816962	15.13110298811972	5.266574186930059	77.72474540
3	2	5 May 2024 03:00:00.673142400	183.62283078311037	5.031611184073533	80.8918491
4	1	5 May 2024 03:00:00.393633923	42.73106714577967	27.862184658609007	16.23764310
5	2	5 May 2024 03:00:00.880695806	186.21207013940705	2.2570199217615854	148.923511

Notice that the first access ends and the second access begins at an approximate elevation angle of 30 degrees. There is a break in access when the elevation angle exceeds 30 degrees due to the modeled cone of silence.

It is also possible to see this cone of silence on a plot of the aircraft's elevation when it is accessed by the sensor:

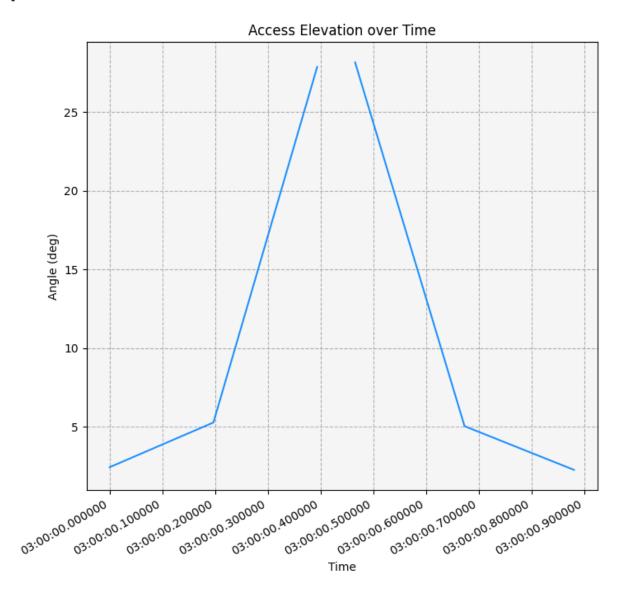
```
import matplotlib.dates as md
import matplotlib.pyplot as plt
import pandas as pd
# Convert columns to correct types
aer_df["time"] = pd.to_datetime(aer_df["time"])
aer_df["elevation"] = aer_df["elevation"].apply(pd.to_numeric)
# Create a plot
fig, ax = plt.subplots(figsize=(8, 8))
# Group by access number, then plot elevation
aer_df.groupby("access number").plot(x="time", y="elevation", ax=ax, color="dodgerblue")
# Set title and axes labels
ax.set title("Access Elevation over Time")
ax.set_xlabel("Time")
ax.set_ylabel("Angle (deg)")
# Configure style
ax.set_facecolor("whitesmoke")
ax.grid(visible=True, which="both", linestyle="--")
# Improve x-axis formatting
formatter = md.DateFormatter("%H:%M:%S.%f")
ax.xaxis.set_major_formatter(formatter)
```

Set major and minor locators

xlocator_major = md.MicrosecondLocator(interval=100000)
ax.xaxis.set_major_locator(xlocator_major)

Remove axis

ax.get_legend().remove()
plt.show()



Insert an airport surveillance radar

Insert the airport surveillance radar on the sensor:

```
airport_radar = antenna_sensor.children.new(STKObjectType.RADAR, "Radar")
```

In this scenario, the radar is a monostatic radar with a search/track mode. A monostatic radar uses a common antenna for both transmitting and receiving. A search/track radar detects and tracks point targets. Both the monostatic radar type and the search/track mode are default when a radar is inserted, so there is no need to designate either.

Define the waveform

Radar systems often use multiple pulse integration to increase the signal-to-noise ratio. The fixed pulse repetition frequency (PRF) is the number of pulses of a repeating signal in a specific time unit. After producing a brief transmission pulse, the transmitter is turned off in order for the receiver to hear the reflections of that signal off of targets. The default waveform for radars in STK uses a fixed PRF with a default value of 0.001 MHz. In this case, the airport surveillance radar uses a fixed PRF of 1000 Hz, so the defaults can be used directly.

Define the pulse width

Pulse width is the width of the transmitted pulse (the uncompressed RF bandwidth can also be taken as the inverse of the pulse width). Set the pulse width to one microsecond:

from ansys.stk.core.stkobjects import RadarModelMonostatic

```
monostatic = RadarModelMonostatic(airport_radar.model_component_linking.component)
monostatic.mode_component_linking.component.waveform.pulse_definition.pulse_width = 1e-6
```

Define the antenna model

The radar's antenna is modeled by the cosine squared aperture rectangular antenna pattern, with an antenna transmit frequency between 2.7 and 2.9 GHz. The antenna also has an X dimension beamwidth of 5°, a Y dimension beamwidth of 1.4°, a design frequency of 2.8 GHz, a main-lobe gain of 34 dB, and an efficiency of 55%.

First, set the radar's antenna model to the cosine squared aperture rectangular antenna pattern:

```
antenna_control = airport_radar.model_component_linking.component.antenna_control
antenna_control.embedded_model_component_linking.set_component(
    "Cosine Squared Aperture Rectangular"
)
antenna_model = AntennaModelApertureRectangularCosineSquared(
    antenna_control.embedded_model_component_linking.component
)
Next, configure the antenna model to use beamwidth:
from ansys.stk.core.stkobjects import RectangularApertureInputType
antenna_model.input_type = RectangularApertureInputType.BEAMWIDTHS
Set the X beamwidth to 5^{\circ}:
antenna_model.x_beamwidth = 5
Set the Y beamwidth to 1.4°
antenna_model.y_beamwidth = 1.4
Then, set the antenna's design frequency to 2.8 GHz.
antenna_model.design_frequency = 2.8
Disable the automatic computation of main-lobe gain for the antenna.
                                                                          When the
compute_mainlobe_gain property is set to True, the main-lobe gain is automatically
calculated based on beamwidth or diameter, efficiency, and design frequency. In this case,
disable the computation of main-lobe gain, and instead set the value to 34 dB:
antenna_model.compute_mainlobe_gain = False
antenna_model.mainlobe_gain = 34
Finally, set the antenna's efficiency to 55%:
antenna_model.efficiency = 55
```

Define the radar transmitter

The transmitter has a frequency range of 2.7-2.9 GHz, a peak power of 20 kW, and uses linear polarization.

First, configure the transmitter to use frequency (instead of wavelength) as its frequency specification:

from ansys.stk.core.stkobjects import RadarFrequencySpecificationType

```
radar_transmitter = airport_radar.model_component_linking.component.transmitter
radar_transmitter.frequency_specification = RadarFrequencySpecificationType.FREQUENCY
```

Then, set the transmitter's frequency to 2.8 GHz:

```
radar_transmitter.frequency = 2.8
```

Finally, set the transmitter's power to 20 kW (43.01 dBW):

```
radar_transmitter.power = 43.01
```

Polarization is a property of an electromagnetic wave that describes the orientation of the electric field vector with reference to the antenna's orientation. An aircraft surveillance radar system can use linear or circular polarization. In this case, the transmitter uses linear polarization, in which the receiver is linearly polarized with the electrical field aligned with the reference axis.

Enable the use of polarization on the transmitter:

```
radar_transmitter.enable_polarization = True
```

Linear polarization is the default value for transmitters, so there is no need to change the polarization type.

Configure the radar receiver

The radar's receiver uses linear polarization, and computes system noise temperature using the default values, and taking into account Sun and cosmic background noise.

First, enable polarization on the radar receiver:

```
radar_receiver = airport_radar.model_component_linking.component.receiver
radar_receiver.enable_polarization = True
```

Linear polarization is the default polarization type, so the default type can be used directly.

Next, add the receiver's system noise temperature. Compute system noise temperature using the default values, and take into account Sun and cosmic background noise.

Set the receiver's system noise temperature compute type to calculate:

```
{\tt from\ ansys.stk.core.stkobjects\ import\ NoiseTemperatureComputeType}
```

```
radar_receiver.system_noise_temperature.compute_type = (
    NoiseTemperatureComputeType.CALCULATE
)
```

Then, use the receiver's system noise temperature's antenna_noise_temperature property to access an AntennaNoiseTemperature object, through which it is possible to set the antenna noise temperature parameters. Set the compute type to calculate and then enable the use of Sun and cosmic background in antenna noise temperature calculations:

```
radar_receiver.system_noise_temperature.antenna_noise_temperature.compute_type = (
    NoiseTemperatureComputeType.CALCULATE
)
radar_receiver.system_noise_temperature.antenna_noise_temperature.use_sun = True
radar_receiver.system_noise_temperature.antenna_noise_temperature.use_cosmic_background = True
```

Determine the probability of detection

For this radar, the probability of detection (Pdet) is based on a value of 0.800000 or higher, with 1 being the highest value. Determine the Pdet for a large aircraft, a medium aircraft, a small aircraft, and a bird by changing the aircraft's constant RCS value to simulate different sized-targets.

Start by determining the Pdet of the large turboprop aircraft.

Compute access between the radar and the aircraft:

```
large_aircraft_access = airport_radar.get_access_to_object(aircraft)
large_aircraft_access.compute_access()

Next, generate a radar SearchTrack report using a step value of 30 sec:
large_aircraft_df = (
    large_aircraft_access.data_providers.item("Radar SearchTrack")
    .execute(scenario.start_time, scenario.stop_time, 30)
    .data_sets.to_pandas_dataframe()
)
```

Select the report's s/t pdet1 (the Pdet for a single pulse), s/t integrated pdet (the Pdet for multiple pulses), s/t pulses integrated (the number of pulses integrated), s/t snr1 (the signal-to-noise ratio (SNR) for a single pulse), and s/t integrated snr (the SNR for multiple pulses):

	s/t pdet1	s/t integrated pdet	s/t snr1	s/t integrated snr	s/t pulses inte
0	0.004241189154789869	0.8990454122417457	0.4039825109939072	16.085999751663856	37
1	1.0	1.0	38.487444062754676	38.487444062754676	1
2	1.0	1.0	38.333965316780535	38.333965316780535	1
3	0.0005349943277871887	0.2999687378212546	-5.246222130023764	16.024825853624314	134

As can be seen by the difference between the s/t pdet1 and s/t integrated pdet columns, pulse integration improves the ability of the radar to detect targets by combining the returns from multiple pulses. Pulse integration also improves the signal-to-noise ratio.

Simulate a medium-sized aircraft

To simulate a medium-sized aircraft, change the target aircraft's RCS to 10 dBsm:

```
band1.compute_strategy.constant_value = 10
Then, compute access between the aircraft and the radar:
medium_aircraft_access = airport_radar.get_access_to_object(aircraft)
medium_aircraft_access.compute_access()

Generate a radar SearchTrack report using a step value of 30 sec:
medium_aircraft_df = (
    medium_aircraft_access.data_providers.item("Radar SearchTrack")
    .execute(scenario.start_time, scenario.stop_time, 30)
    .data_sets.to_pandas_dataframe()
)
```

Select the s/t pdet1, s/t integrated pdet, s/t pulses integrated, s/t snr1, and s/t integrated snr:

	s/t pdet1	s/t integrated pdet	s/t snr1	s/t integrated snr	s/t pulses
0	0.00025371021992869145	0.07763118319057452	-8.596017489006092	16.012960938559388	289
1	1.0	1.0	29.48744406275468	29.48744406275468	1
2	1.0	1.0	29.33396531678053	29.33396531678053	1
3	0.0001332979757668818	0.0022131674685955697	-14.24622213002376	12.846477479734546	512

The radar's ability to track this aircraft has diminished due to the aircraft's smaller RCS.

Simulate a small aircraft

To simulate a small aircraft, change the target aircraft's RCS to 0 dBsm:

```
band1.compute_strategy.constant_value = 0
```

Then, compute access between the aircraft and the radar:

```
small_aircraft_access = airport_radar.get_access_to_object(aircraft)
small_aircraft_access.compute_access()
```

Generate a radar SearchTrack report using a step value of 30 sec:

```
small_aircraft_df = (
    small_aircraft_access.data_providers.item("Radar SearchTrack")
    .execute(scenario.start_time, scenario.stop_time, 30)
    .data_sets.to_pandas_dataframe()
)
```

Select the s/t pdet1, s/t integrated pdet, s/t pulses integrated, s/t snr1, and s/t integrated snr:

	s/t pdet1	s/t integrated pdet	s/t snr1	s/t integrated snr	s/t pul
0	0.00011254140305492283	0.00034616354655054465	-18.596017489006094	8.496682120752215	512
1	1.0	1.0	19.487444062754676	19.487444062754676	1
2	1.0	1.0	19.33396531678053	19.33396531678053	1
3	0.00010345088906840799	0.00014192164338157505	-24.24622213002376	2.846477479734546	512

The radar's ability to track this aircraft has again diminished due to the aircraft's smaller RCS.

Simulate a bird

To simulate a bird, change the target aircraft's RCS to -20 dBsm:

```
band1.compute_strategy.constant_value = -20
```

Then, compute access between the aircraft and the radar:

```
bird_aircraft_access = airport_radar.get_access_to_object(aircraft)
bird_aircraft_access.compute_access()
```

Generate a radar SearchTrack report using a step value of 30 sec:

```
bird_aircraft_df = (
    bird_aircraft_access.data_providers.item("Radar SearchTrack")
    .execute(scenario.start_time, scenario.stop_time, 30)
    .data_sets.to_pandas_dataframe()
)
```

Select the s/t pdet1, s/t integrated pdet, s/t pulses integrated, s/t snr1, and s/t integrated snr:

	s/t pdet1	s/t integrated pdet	s/t snr1	s/t integrated snr	s/t pul
0	$9.998618444776282 \mathrm{e}\text{-}05$	0.00010148169909176745	-38.596017489006094	-11.503317879247785	512
1	0.0028605647015461574	0.8289110078005205	-0.5125559372453223	16.019569200508116	45
2	0.0026825084239399796	0.8206050695303343	-0.6660346832194677	16.054943896137708	47
3	$9.999623842592416\mathrm{e}\text{-}05$	0.00010050601836099273	-44.24622213002376	-17.153522520265454	512

The Pdet is very low for an object with this RCS. To track objects like birds, the radar system would need a different frequency or higher power.

Load an external Aspect Dependent RCS file

Using an Aspect Dependent RCS file built for a specific target aircraft generates much more realistic data.

To use an external file, first set the target aircraft's RCS to use an external file in computations:

```
band1.set_compute_strategy("External File")
```

Then, upload the X-47B_Notional_Sample.rcs file, which is included with the STK install, by using the band's compute_strategy property, which now holds a RadarCrossSectionComputeStrategyExterna object:

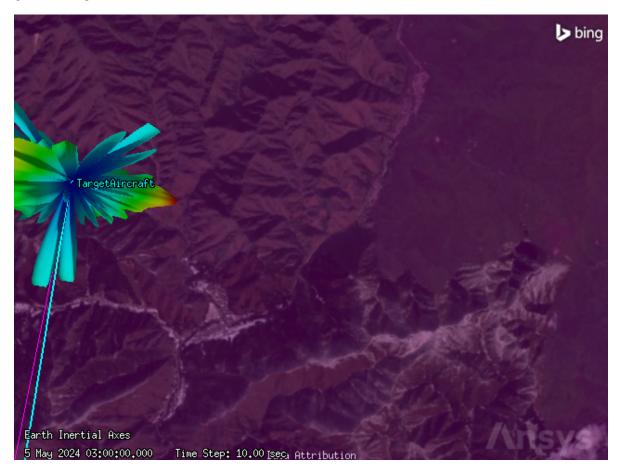
```
import pathlib
```

```
install_dir = root.execute_command("GetDirectory / STKHome")[0]
band1.compute_strategy.filename = str(
    pathlib.Path(install_dir)
    / "Data"
    / "Resources"
    / "stktraining"
```

```
/ "samples"
/ "SeaRangeResources"
/ "X-47B"
/ "X-47B_Notional_Sample.rcs"
)
```

It is now possible to see the aircraft's aspect dependent RCS pattern in the 3D graphics window:

```
globe_widget.camera.position = [3435.3329, 3789.8112, 3815.5677]
globe_widget.show()
```



Recompute the access between the aircraft and the radar:

```
aspect_dep_aircraft_access = airport_radar.get_access_to_object(aircraft)
aspect_dep_aircraft_access.compute_access()
```

Generate a radar SearchTrack report using a step value of 30 sec:

```
aspect_dep_df = (
    aspect_dep_aircraft_access.data_providers.item("Radar SearchTrack")
    .execute(scenario.start_time, scenario.stop_time, 30)
    .data_sets.to_pandas_dataframe()
)
Select the s/t pdet1, s/t integrated pdet, s/t pulses integrated, s/t snr1, and s/t
integrated snr:
aspect_dep_df[
    "s/t pdet1",
        "s/t integrated pdet",
        "s/t snr1",
        "s/t integrated snr",
        "s/t pulses integrated",
    ]
]
```

	s/t pdet1	s/t integrated pdet	s/t snr1	s/t integrated snr	s/t pul
0	0.00010357772989095509	0.0001439764356074659	-24.088820853084524	3.003878756673781	512
1	0.7754405309015666	0.9999987492289983	10.868408484863252	16.889008398142874	4
2	0.23677011455720495	0.9997005710099416	7.734541751840621	16.18552215198319	7
3	0.00010132858779850437	0.0001147151699025594	-28.402239189069576	-1.3095395793112694	512

Depending on the reflection from the aircraft back to the radar, it is possible for there to be fluctuation in the values. This is noticeable in the S/T Pulses Integrated column.

Graph the RCS

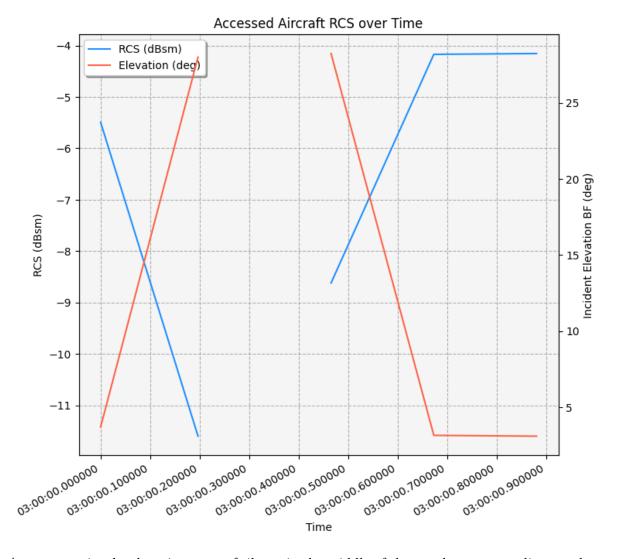
Use the Radar RCS report to get information about how the RCS changes over time:

```
rcs_df = (
    aspect_dep_aircraft_access.data_providers.item("Radar RCS")
    .execute(scenario.start_time, scenario.stop_time, 1)
    .data_sets.to_pandas_dataframe()
)
rcs_df["incident el bf"]
```

```
0
      3.709178
     28.240029
1
2
     28.006714
3
      3.161044
4
          None
       3.10671
Name: incident el bf, dtype: object
Visualize changes to the RCS and the elevation:
import matplotlib.dates as md
import matplotlib.pyplot as plt
import pandas as pd
# Convert columns to correct types
rcs_df["time"] = pd.to_datetime(aer_df["time"])
cols = ["rcs", "incident el bf"]
rcs_df[cols] = rcs_df[cols].apply(pd.to_numeric)
# Create a plot
fig, ax = plt.subplots(figsize=(8, 8))
# Duplicate axis
ax2 = ax.twinx()
# Group by access number, then plot rcs and elevation
rcs_df.groupby("access number").plot(
    x="time", y="rcs", ax=ax, color="dodgerblue", label="RCS (dBsm)"
rcs_df.groupby("access number").plot(
    x="time", y="incident el bf", ax=ax2, color="tomato", label="Elevation (deg)"
)
# Set title and axes labels
ax.set title("Accessed Aircraft RCS over Time")
ax.set_xlabel("Time")
ax.set_ylabel("RCS (dBsm)")
ax2.set_ylabel("Incident Elevation BF (deg)")
# Configure style
ax.set_facecolor("whitesmoke")
ax.grid(visible=True, which="both", linestyle="--")
```

```
# Combine legends
lines = [ax.get_lines()[0], ax2.get_lines()[0]]
labels = [line.get_label() for line in lines]
ax.legend(lines, labels, shadow=True)
ax2.get_legend().remove()

# Improve x-axis formatting
formatter = md.DateFormatter("%H:%M:%S.%f")
ax.xaxis.set_major_formatter(formatter)
# Set major and minor locators
xlocator_major = md.MicrosecondLocator(interval=100000)
ax.xaxis.set_major_locator(xlocator_major)
plt.show()
```



As seen previously, there is a cone of silence in the middle of the graph, corresponding to when the elevation angle is over 30° .