Exercise 1

A study looking at breast cancer in women compared cases with non-cases, and found that 75/100 cases did not use calcium supplements compared with 25/100 of the non-cases.

(a) Develop a 2 x 2 table to display the data.

	Case ("Diseased")	Control ("Healthy")
Exposed		
Not Exposed		

- (b) Calculate the odds ratio (OR) based on the 2×2 table.
- (c) Interpret the odds ratio.
- (d) Define the following data frame in R and fit the binary logistic regression model by using the below glm() function.

(e) How can you extract the (same) odds ratio as calculated in b) from the glm() model?

Exercise 2

The CHFLS data set from package **HSAUR2** is a subset of the Chinese Health and Family Life Survey (cf. Exercise 3, Worksheet 1).

We want to study the impact of age and income on happiness in a proportional odds logistic model. For this, the following polr() model is fitted:

```
library("MASS")
data("CHFLS", package = "HSAUR2")
polr.mod <- polr(R_happy ~ R_age + R_income, data = CHFLS)</pre>
```

(a) What are the characteristics of the response variable R_happy?

Apply the following commands to the previously defined R object polr.mod.

```
summary(polr.mod)
c(polr.mod$zeta, coef(polr.mod))
exp(c(polr.mod$zeta, coef(polr.mod)))
```

- (b) Do the coefficients from a porportional odds logistic regression model have a multiplicative or an additive effect?
- (c) Interpret $\exp(\beta_{\text{age}})$ and $\exp(\beta_{\text{income}})$.
- (d) How do you interpret the polr.mod\$zeta coefficients?

Exercise 3

The model studying the impact of age and income on happiness from the previous exercise can also be used to predict outcome probabilities.

(a) Based on the polr.mod, predict the probabilities of the self-reported happiness groups (R_happy) by changing the values of R_age while keeping the R_income variable constant.

```
age <- c(min(CHFLS$R_age), mean(CHFLS$R_age), max(CHFLS$R_age))
nd.age <- expand.grid(R_age = age, R_income = mean(CHFLS$R_income))</pre>
```

(b) Based on the polr.mod, predict the probabilities of the self-reported happiness groups (R_happy) by changing the values of R_income while keeping the R_age variable constant.

```
income <- c(min(CHFLS$R_income), mean(CHFLS$R_income), max(CHFLS$R_income))
nd.income <- expand.grid(R_age = mean(CHFLS$R_age), R_income = income)</pre>
```

(c) Are the predicted probabilities in alignment with the regression model coefficients? Why?

Exercise 4

Show that

(a) In the model where

$$F_Y(y) = \mathbb{P}(Y \le y) = \operatorname{expit}(h(y)),$$

it holds that

$$h(y) = \log\left(\frac{F(y)}{1 - F(y)}\right).$$

(b) In the model where

$$F_Y(y) = \mathbb{P}(Y \le y) = 1 - \exp(-\exp(h(y))),$$

it holds that

$$h(y) = \log (\Lambda(y))$$
,

where $\Lambda(y)$ is the cumulative hazard function.