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Functional Dependencies

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Database Systems I. Seminar

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Recap

- Notion of Functional dependency
- Key definitions with FDs
- Legal and illegal instances
- Armstrong axioms
 - Reflexivity
 - Augmentation
 - Transitivity
- Derivation rules
 - Union
 - Decomposition
 - Pseudotransitivity
- Formal proof for Pseudotransitivity
 - With the tuple function
 - From the Armstrong axioms
- Logical consequence (implication)
- Closure of the dependency set F^+
- Closure of the attribute set A^+
- Find keys with FD-s



Examples

- For which FD-s is the following instance legal?

$A \rightarrow B$

$B \rightarrow A$

$A \rightarrow C$

$B \rightarrow C$

$A \rightarrow BC$

$B \rightarrow AC$

$AB \rightarrow C$

A	B	C
1	2	3
6	7	3
10	11	12
1	4	3
7	7	3

- Check if the particular FD holds on the given instance!

$A \rightarrow B$

$BC \rightarrow A$

$B \rightarrow C$

A	B	C
1	2	3
4	2	3
5	3	3



Keys

- Given $R(A, B, C, D)$ and the following FDs. For each case, find the possible candidate keys!
 - $F1 = \{ C \rightarrow D, C \rightarrow A, B \rightarrow C \}$
 - $F2 = \{ B \rightarrow C, D \rightarrow A \}$
 - $F3 = \{ ABC \rightarrow D, D \rightarrow A \}$
 - $F4 = \{ A \rightarrow B, BC \rightarrow D, A \rightarrow C \}$
 - $F5 = \{ AB \rightarrow C, AB \rightarrow D, C \rightarrow A, D \rightarrow B \}$