

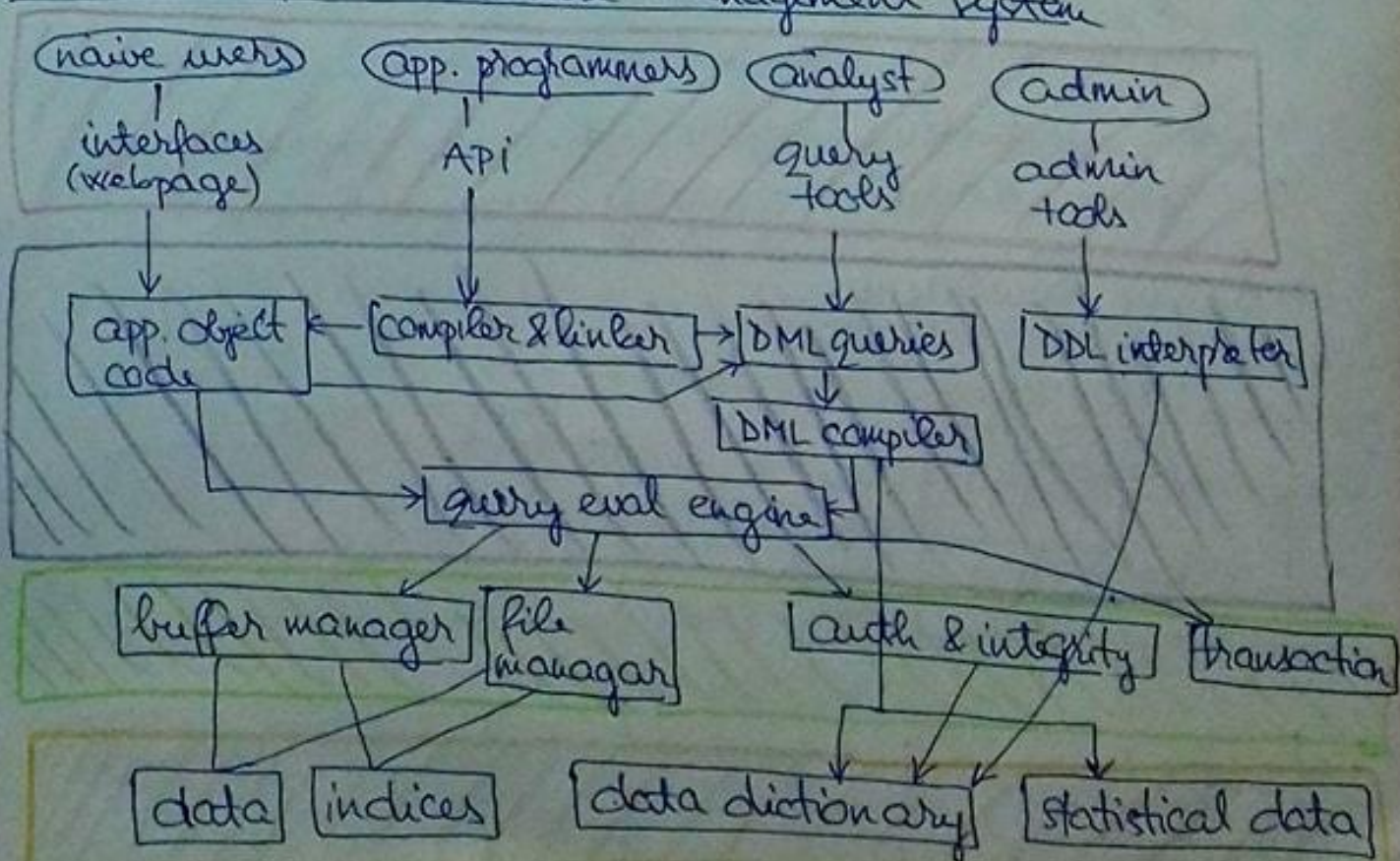
# Database systems

## FÉLÉVES ÖSSZEFOGLALÓ VIZSGÁRA

### 1. Introduction, course outline

- What is a DBMS? ✓
- What is data modelling? ✓
- Abstraction levels of a database ✓
- Creating databases (abstraction levels, logical struct., DDL) ✓
- Getting data from database: QL → RELATIONAL ALGEBRA ✓
- Manipulating data in database: DML → SQL ✓
- Storing data: authorization, recovery → UNDO/REDO LOGGING SHADOWING
- Multiuser environment: transaction management, concurrency control  
↓  
LOCKING MECHANISMS  
TIMESTAMPING
- Development lifecycle ✓
- Active elements: constraints, triggers
- Database architectures ✓
- Functional dependencies and normalisation ✓

### 2. Structure of a database management system





## What is a database :

- structured data in relational storage (properties)
- serves multiple users :
  - access, insert, modify data  $\rightarrow$  QL, DML  $\rightarrow$  authority management
  - simultaneous access  $\rightarrow$  transaction manager
- history (recovery)
- File Management (physical layer)

## Data modelling, abstraction levels

WORLD  $\rightarrow$  abstraction : no values, just relations  
database INSTANCE  $\rightarrow$  satisfying model

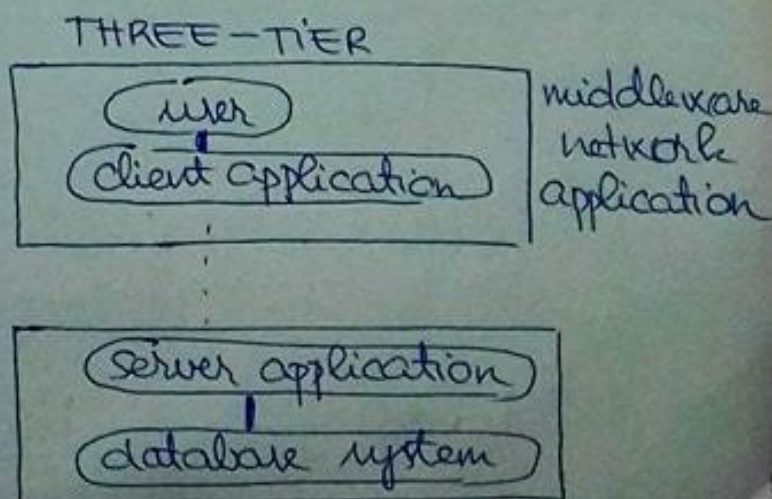
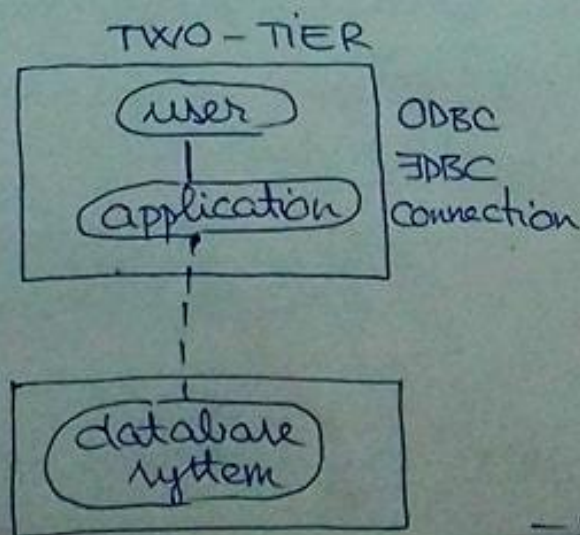
Levels :

- view level : accessible by naive users and apps
- logical / conceptual level : DB admins
- physical level : DBMS programmers : P

## Creating databases / development lifecycle

1. ~~specification~~ (~~high level design~~) : requirements, constraints
2. high level design : entity-relationship model
3. implementation design : relational model
4. low level design : files, indices  $\rightarrow$  ~~implementation~~
5. system model : complete documentation  $\rightarrow$  implement.

## Database architectures





# Creating databases, modeling data (E-R)

HIGH LEVEL DESIGN

DATABASE  
SYSTEMS  
VIZSGA  
OSSZEFoglaló

Entity: object distinguishable from others in the microworld, through its attributes

Entity set: group of similar objects, sharing the same properties called attributes

Relationship: logical connection between two or more entity sets (association among entities)

Relationship (set): mathematical relation:

$$R = \{(e_1, e_2, \dots, e_n) \mid e_1 \in E_1, e_2 \in E_2, \dots, e_n \in E_n\}$$

where  $(e_1, e_2, \dots, e_n)$  is a relationship (n-ary tuple)

Relation:  $r(R) \subseteq E_1 \times E_2 \times \dots \times E_n \rightarrow$  table

Relation schema:  $R(E_1, E_2, \dots, E_n) \rightarrow$  table header

Types of relationship (based on degree - number of elements)

- one to one relationship
- one to many relationship
- many to many relationship

FOREIGN KEY:  
- PK of another entity set  
- must exist in the other (constraint)

Keys:  
- total participation  
- partial participation

SUPERKEY: set of attributes uniquely identifying the entity

CANDIDATE KEY: minimal set of attributes, forming an SK

PRIMARY KEY: Chosen CK.

Weak entity set: has not enough attributes for identification

- joined by so-called weak one to many, to a strong set.
- discriminator: unique in context.

Generalization, specialization (ISA): the sub entity inherits all properties of its ancestor

- may or may not be a partition of the superset



Domain constraint: set of ~~all~~ values an attribute can take

## NULL values and three-valued logic

NULL value: data is not known, not available (permission contr.)  
or has no meaning in the given context.

Arithmetic interpretation: operations are undefined

Logical operations:

TRUE - 1

NULL - 1/2

FALSE - 0

AND:  $\min(\dots)$

OR:  $\max(\dots)$

## Relational model: IMPLEMENTATION DESIGN

- transformation of the high-level design
- entity sets  $\Rightarrow$  tables, attributes  $\Rightarrow$  columns
- binary relationships  $\Rightarrow$ 
  - one-to-one: foreign key on any of the sides
  - one-to-many: foreign key on the many side
  - many-to-many: separate table with two foreign keys
- non-binary relationship  $\Rightarrow$  artificial (weak) entity set and multiple binary relations
- ISA relationship types:
  - condition-defined vs. user-defined
  - disjoint vs. overlapping
  - total or partial
  - aggregated



## Relational algebra. Getting data from database

Relation schema:  $R(A_1, A_2, \dots, A_n)$  where  $A_n$  are attributes

Relation:  $r(R) \subseteq D_1 \times D_2 \times \dots \times D_n$

Relation instance: current values of a relation (table)

Keys (revision):

SK:  $K$  is SK of  $R$  if values of  $K$  identify a unique tuple of each possible relation in  $r(R)$

CK:  $\forall$  subset of CK does not identify + is an SK  
Strong, weak and relationship entity set.

BASIC OPERATORS: SELECT, PROJECT, UNION, DIFF, PROD, RENAME

1. SELECT:  $\sigma_p(r) = \{t \mid t \in r \text{ and } p(t) \text{ is true}\}$

$p$ : selection predicate, propositional calculus

2. PROJECT:  $\pi_{A_1, A_2, \dots, A_k}(r)$ : deleted columns, removed duplicates

3. UNION:  $r \cup s = \{t \mid t \in r \text{ or } t \in s\}$

constraint:  $r, s$  compatible  $\leftarrow$  same arity  
convertible data type

4. DIFFERENCE:  $r - s = \{t \mid t \in r \text{ and } t \notin s\}$

constraint:  $r, s$  compatible

5. CARTESIAN:  $r \times s = \{(t, q) \mid t \in r \text{ and } q \in s\}$

constraint: disjoint attributes

6. RENAME:  $\rho_X(B_1, B_2, \dots, B_n)(E) \rightarrow$  returns  $E(A_1, \dots, A_n)$   
under the name/schema  $X(B_1, B_2, \dots)$

## ADDITIONAL OPERATORS

7. SET INTERSECT:  $r \cap s = r - (r - s)$



## 8. NATURAL JOIN

$$r \bowtie s = \pi_{r.A_1, r.A_2, \dots, r.A_n, s.B_{n+1}, s.B_{n+2}, \dots, s.B_k} (\pi_{\dots} (r \times s))$$

## 9. DIVISION

$$R = (A_1, \dots, A_n, B_1, \dots, B_m)$$

$$S = (B_1, \dots, B_m)$$

$$r \div s = \{t \mid t \in r \text{ and } \forall u \in s, t \in u\}$$

$$r \div s = \pi_{R-S}(r) - \pi_{R-S}((\pi_{R-S}(r) \times s) - r)$$

## 10. ASSIGNMENT : convenience, nothing else

## EXTENDED OPERATIONS

## 11. GENERALIZED PROJECTION : operations on attributes are also permitted (arithmetical, string)

## 12. AGGREGATE FUNCTIONS

$$(G_1, G_2, \dots, G_n \text{ } f \text{ } F_1(A_1), F_2(A_2), \dots, F_n(A_n)) (E)$$

$G_1, G_2, \dots, G_n$  : attributes on which to group

$F_1, F_2, \dots, F_n$  : operations (avg, min, max, sum, count)

$A_1, A_2, \dots, A_n$  : attributes

Convenience : renaming with 'as' of  $F(A_n)$  is permitted.

## 13. OUTER JOIN (inner, left, right, full)

- nonmatching ~~relatio~~ tuples filled with null values

## Manipulating data with relational algebra

1. DELETE :  $r \leftarrow r - E$

2. INSERT :  $r \leftarrow r \cup E$

3. UPDATE :  $r \leftarrow \pi_{F_1, F_2, \dots, F_k}(r)$



# Functional dependencies

## Outline

- functional dependency is a semantic concept, <sup>defined by the world, being modeled</sup> used to define formal measures on the goodness of a relational design
- can be defined as a constraint on legal relation instances
- used to define normal forms

## Formal definition

"Tuple function" :  $t: \{A_1, A_2, \dots, A_n\} \rightarrow D_{A_1} \cup D_{A_2} \cup \dots \cup D_{A_n}$   
↳ example:  $t[ID] = \text{"Bus123"}$ , ← value in the tuple

## Functional dependency:

$$\alpha = \{A_{e_1}, A_{e_2}, \dots, A_{e_n}\} \quad \beta = \{A_{e_1}, A_{e_2}, \dots, A_{e_n}\}$$

$\alpha \rightarrow \beta$  means that  $t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$

Trivial dependency: satisfied by all tuples.

Partial dependency: attributes depend on part of the key, not all attributes of it. [this should be avoided]

## Armstrong axioms

3. Transitivity :  $\alpha \rightarrow \beta$  and  $\beta \rightarrow \gamma \Rightarrow \alpha \rightarrow \gamma$

2. Augmentation :  $\alpha \rightarrow \beta \Rightarrow \alpha\gamma \rightarrow \beta$

1. Reflexivity :  $\alpha \rightarrow \beta$  if  $\beta \subseteq \alpha$  Proof: trivial

Rules derived from this:

4. Pseudotransitivity :  $\alpha \rightarrow \beta$  and  $\beta\gamma \rightarrow \delta \Rightarrow \alpha\gamma \rightarrow \delta$

5. Union :  $\alpha \rightarrow \beta$  and  $\alpha \rightarrow \gamma \Rightarrow \alpha \rightarrow \beta\gamma$

5. Decomposition :  $\alpha \rightarrow \beta\gamma \Rightarrow \alpha \rightarrow \beta$  and  $\alpha \rightarrow \gamma$



Derivation (bizonyítás, levezetés, bővítés — nem  $\frac{d}{dx} : P$ )

Implication :  $FD_1 \models FD_2$  if every instance legal under  $FD_1$  is legal under  $FD_2$  as well

Derivation : are  $FD_1, FD_2, \dots, FD_n$  sorozat are  $\alpha \rightarrow \beta$

(thú) levezetése are FD függőségi halmazból, ha  
 $FD_n = \alpha \rightarrow \beta$  (are are elvileg a cél) és  $FD_k \in FD$   
+transl. needed. (már benne volt) vagy  $\exists FD_i, i < k : FD_i \models FD_k$ ,  
are Armstrong axiomatical bizonyíthatóan.

Armstrong axioms :

- sound : every FD obtained by derivation is consequence of the original one
- complete : if it is consequence, a derivation exists.

Closure of FD set :

$F^+$  contains all FD's implied by  $F$ . (derivable)

Keys as FD's :

$\beta \subseteq R$  is SUPERKEY, if  $\beta \rightarrow R$

$\alpha \subseteq R$  is CANDIDATEKEY, if  $\alpha$  is super, but  $\nexists \gamma \subset \alpha : \gamma \rightarrow R$  is true.

Closure of attribute set :  $\alpha^+ = \{A \mid \exists FD \in F^+ : FD = \alpha \rightarrow A\}$

(thú) "are are attribútumok, amit  $\alpha$  meghatároz"

"Algorithm" :  $\alpha^+(0) = \alpha ; \alpha^+(i+1) = \alpha^+(i) \cup A$  if  $\exists Y \in \alpha^+(i) : Y \rightarrow A$ .

Theorem :  $\alpha \rightarrow \beta$  is derivable from  $F$  iff  $\beta \in \alpha^+$

" $\Rightarrow$ " if  $\beta \in \alpha^+$  : algorithm constructively gives derivation

" $\Leftarrow$ " if  $\alpha \rightarrow \beta$  is derivable : by definition  $\beta \in \alpha^+$



## Normalization

Normalization : process of

- determining the normal form of a relation
- applying decomposition methods to achieve that.

Anomalies (of poorly designed systems) :

- update anomaly: caused by uncontrolled redundancy
- insert anomaly: not possible to store information unless another information is stored as well.
- delete anomaly: cannot delete information without deleting another information as well.

Normal forms (shortly) :



1NF: all attributes must have atomic domain

2NF: nonprime attribute parsidisan nem fugghet a CK-től + 1NF teljesül

3NF: nonprime attr. nem fugghet tranzitív módon CK-től + 2NF

BCNF: az attribútumok csak SK-től függhetnek

Total dependency: in the FD  $\alpha \rightarrow \beta$  attribute set  $\beta$  is totally dependent on  $\alpha$  if  $\nexists \delta \subset \alpha : \delta \rightarrow \beta$

Partial dependency: in the FD  $\alpha \rightarrow \beta$  attribute set  $\beta$  is partially dependent on  $\alpha$  if  $\exists \delta \subset \alpha : \delta \rightarrow \beta$

Prime attribute: attribute involved in (at least one) CK.

Nonprime attribute: no CK contains it.



2NF: <sup>all</sup> ~~min~~ nonprime attributes totally depend on any CK.

$\alpha \rightarrow \beta$  violates the 2NF, if  $\beta$  is nonprime, and  $\exists \delta \subset \alpha : \delta \rightarrow \beta$ .

~~XXXX~~

Transitive dependency:  $\gamma$  depends transitively on a set of attribute  $\alpha$  if  $\exists \beta : \alpha \rightarrow \beta$  and  $\beta \rightarrow \gamma$ .

3NF:

DEF 1: A relation is in 3NF, if it is in 2NF and non-prime attributes do not depend partially transitively on any CK.

$\forall \alpha$  nonprime  $\nexists \beta \subset CK, \gamma : \beta \rightarrow \gamma$  and  $\gamma \rightarrow \alpha$ .

DEF 2: A relation is in 3NF, if for each nontrivial FD in  $F^+$  in form of  $\alpha \rightarrow \beta$ :

a)  $\alpha$  is superkey OR:

b)  $\beta$  is prime attribute

Definition equivalency:

DEF 1  $\rightarrow$  DEF 2:

if  $\alpha \rightarrow \beta$  violates DEF 2, <sup>one</sup> ~~two~~ possible cases:

a)  $\alpha$  not superkey,  $\beta$  nonprime

if  $\alpha$  is not superkey, then:

i)  $\alpha \subset CK \Rightarrow \alpha \rightarrow \beta$  is partial dependency of nonprime attribute  $\Rightarrow$  not 2NF

ii)  $\alpha \not\subset CK \Rightarrow CK \rightarrow \alpha \rightarrow \beta$  is transitive dependency



DEF 2  $\rightarrow$  DEF 1 :

if  $\alpha \rightarrow \beta$  violates DEF 1 :

1.)  $\alpha \rightarrow \beta$  violates 2NF, meaning  $\beta$  is nonprime and  $\alpha$  is not a CK  $\Rightarrow \beta$  nonprime,  $\alpha$  not superkey

2.)  $\alpha \rightarrow \beta$  violates transitivity, meaning  $\beta \not\rightarrow \alpha$

i.)  $\beta \subset \alpha \Rightarrow \beta$  not superkey &  $\beta$  nonprime

ii.)  $\beta \not\subset \alpha \Rightarrow \beta$  not superkey (??)

BCNF: attributes may depend just on superkeys!

### Decomposition methods and conditions

Decomposition of  $R = (A_1, A_2, \dots, A_n)$  is a set of

relations  $R_1(A_{11}, A_{12}, \dots, A_{1i})$

$R_2(A_{21}, A_{22}, \dots, A_{2j})$

$\vdots$   
 $R_k(A_{k1}, A_{k2}, \dots, A_{kn})$

such that  $\cup A_{ij} = \{A_1, A_2, \dots, A_n\}$

and  $r_k = \pi_{A_{k1}, A_{k2}, \dots, A_{kn}}(r)$

Lossy decomposition  $r \bowtie r^* = r_1 \bowtie r_2 \subsetneq r$

Lossless decomposition

Theorem: if  $R_1, R_2, \dots, R_k$  is a decomposition of  $R$ ,

then  $r \subseteq r_1 \bowtie r_2 \bowtie \dots \bowtie r_k$  is true.

Definition: decomposition is lossless, if  $r = r_1 \bowtie \dots \bowtie r_k$



Theorem of lossless decomposition: decomposition is lossless iff at least one holds:

$$\left. \begin{array}{l} R_1 \cap R_2 \rightarrow R_1 \\ R_1 \cap R_2 \rightarrow R_2 \end{array} \right\} \begin{array}{l} \text{the common attribute is} \\ \text{SK in one of the parts} \end{array}$$

Lossless 2NF decomposition: if  $\alpha \rightarrow \beta$  violates the 2NF, decompose to:  $R_1(\alpha, \beta)$   
 $R_2(R - \beta)$

What ensures its really lossless:  $\alpha$  is SK in  $R_1$ .

Lossless 3NF/BCNF decomposition: always exists

1. Find CK's for R
  2. If  $\alpha \rightarrow \beta$  in  $F^+$  corresponds to 3NF/BCNF
  3. Decompose relation. (??)
- ... details later...

Projection of FD sets:

$$\pi_{R_i}(F) = \{X \rightarrow Y \mid X \rightarrow Y \in F^+ \text{ and } X \cup Y \subseteq R_i\}$$

Decomposition of schemas:

$S = (R; F)$  can be decomposed into

$$S_1 = (R_1; F_1) \quad S_2 = (R_2; F_2) \quad \dots \quad S_k = (R_k; F_k)$$

such that:

$$R = \bigcup_{i=1}^k R_i$$

$$F_i = \pi_{R_i}(F)$$

Equivalency of FD sets: E and F are equivalent iff  $E^+ = F^+$ , meaning  $E \models F$  and  $F \models E$ .



Dependency preserving decomposition :

$S \rightarrow S_1, S_2, \dots, S_k$  is dependency preserving, if  
 $F$  is equivalent to  $\bigcup_{i=1}^k F_i$

Ullmans minimal cover (FD set)

- 1.) single attribute on the right side (decompos. rule)
- 2.) left-reduced: no partial dependency
- 3.) non-redundant: removing  $X \rightarrow Y$  ruins equivalency

Lossless dependency-preserving 3NF decomposition

- 1.) group dependencies based on the left side
- 2.) decompose everything based on groups
- 3.) add relation for the candidate keys
- 4.) decomposition ok.

What ensures losslessness?

$$R_1 \cap R_2 \rightarrow R_2$$

What ensures dependency preservation: definition of the minimal cover.

Why does lossless dep. pres BCNF always exist?

$R(\text{City, Street, Zip code}) \quad F = \{CS \rightarrow Z, Z \rightarrow C\}$

Nonprime: — Prime:  $C, S, Z$ .

1NF, 2NF, 3NF ok.

BCNF:  $Z$  is not a superkey.

$$F^- = \{CS \rightarrow Z, Z \rightarrow C\}$$

$R_1 = (Z, C) \quad Z \rightarrow C \quad \text{OK}$

$R_2 = (C, S) \quad \text{trivial}$



# Database recovery systems

Aim : restore database to a known consistent state.

Properties of database :

Atomicity : transaction completes or does not touch data

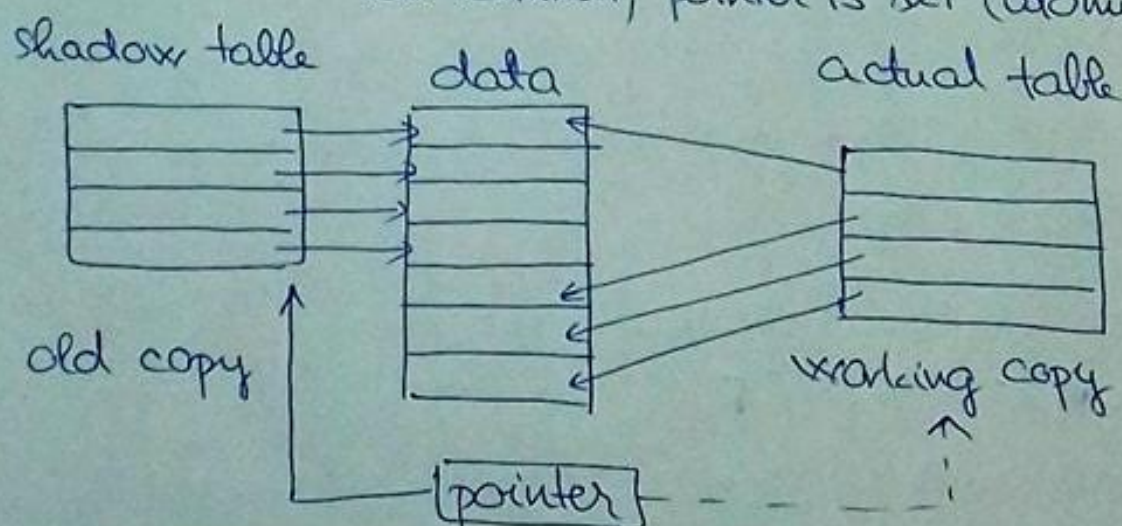
Consistency : } later in transaction manager

Isolation :

Durability : data is not lost in case of system failure  
(like hardware error, power loss, ...)

Types of recovery : LOG based or SHADOW based

SHADOW based : transactions work on a copy  
on commit, pointer is set (atomic op).



LOG based :

Deferred modification model (<sup>REDO</sup>~~UNDO~~) : uncommitted transactions are not allowed to touch database

Immediate modification (UNDO)

**REDO/UNDO** : no idea when storage is written

**CHECKPOINT** : data of committed transactions is safe

Cascading rollback caused by dirty reading

Solution : immediate modification

deferred + RIGOROUS 2-PHASE PROTOCOL