## Fermilab Keras Workshop

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#### What is this talk about?

- Modern implemenation, description and application of neural networks
- Currently favoured approach:
  - Keras used for high-level description of neural networks models
  - ► **High-performance implementations** provided by backends, e.g., Theano or **TensorFlow** libraries

Being able to go from idea to result with the least possible delay is key to doing good research.

theano





#### Outline

The workshop has these parts:

- 1. Brief introduction to neural networks
- 2. Brief introduction to **computational graphs** with TensorFlow
- 3. Introduction to Keras
- 4. Useful tools in combination with Keras, e.g., TMVA Keras interface
  - ▶ In parts 3 and 4, you have to possibility to follow along with the examples on your laptop.

#### **Assumptions** of the tutorial:

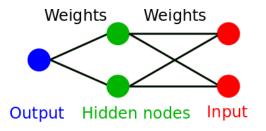
- ➤ You are not a neural network expert, but you know roughly how they work.
- You haven't used Keras before.
- You want to know why Keras is so popular and how you can use it!

## You can download the slides and code examples from GitHub: git clone

https://github.com/stwunsch/fermilab\_keras\_workshop



## A Simple Neural Network



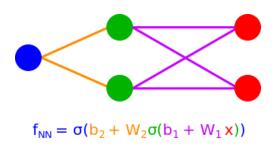
## Neural Network: f(x)

- ► **Important:** A neural network is only a mathematical function. No magic involved!
- ► **Training:** Finding the best function for a given task, e.g., separation of signal and background.

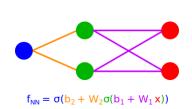
## Mathematical Representation

#### Why do we need to know this?

- $\rightarrow$  Keras backends TensorFlow and Theano implement these mathematical operations explicitely.
- ightarrow Basic knowledge to understand Keras' high-level layers



## Mathematical Representation (2)



$$\mathsf{Input}: x = \begin{bmatrix} x_{1,1} \\ x_{2,1} \end{bmatrix}$$
 
$$\mathsf{Weight}: W_1 = \begin{bmatrix} W_{1,1} & W_{1,2} \\ W_{2,1} & W_{2,2} \end{bmatrix}$$
 
$$\mathsf{Bias}: b_1 = \begin{bmatrix} b_{1,1} \\ b_{2,1} \end{bmatrix}$$

Activation :  $\sigma(x) = \tanh(x)$  (as example)

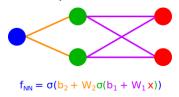
Activation is applied elementwise!

The "simple" neural network written as full equation:

$$f_{\mathrm{NN}} = \sigma_2 \left( \begin{bmatrix} b_{1,1}^2 \end{bmatrix} + \begin{bmatrix} W_{1,1}^2 & W_{1,2}^2 \end{bmatrix} \sigma_1 \left( \begin{bmatrix} b_{1,1}^1 \\ b_{2,1}^1 \end{bmatrix} + \begin{bmatrix} W_{1,1}^1 & W_{1,2}^1 \\ W_{2,1}^1 & W_{2,2}^1 \end{bmatrix} \begin{bmatrix} x_{1,1} \\ x_{2,1} \end{bmatrix} \right) \right)$$

► How many parameters can be altered during training?  $\rightarrow 1+2+2+4=9$  parameters

## Training (Short Reminder)



#### **Training:**

- 1. Forward-pass of a batch of N inputs  $x_i$  calculating the outputs  $f_{NN,i}$
- 2. Comparison of outputs  $f_{NN,i}$  with true value  $f_{Target,i}$  using the loss function as metric
- Adaption of free parameters to improve the outcome in the next forward-pass using the gradient from the back-propagation algorithm in combination with an optimizer algorithm

#### Common loss functions:

- ► Mean squared error:  $\frac{1}{N} \sum_{i=1}^{N} (f_{NN,i} f_{Target,i})^2$
- ► Cross-entropy:  $-\sum_{i=1}^{N} f_{Target,i} \log (f_{NN,i})$

### Deep Learning Textbook

Free textbook written by Ian Goodfellow, Yoshua Bengio and Aaron Courville:

http://www.deeplearningbook.org/

- Written by leading scientists in the field of machine learning
- Everything you need to know about modern machine learning and deep learning in particular.

- Part I: Applied Math and Machine Learning
  Basics
  - 2 Linear Algebra
  - 3 Probability and Information Theory
  - 4 Numerical Computation
  - 5 Machine Learning Basics
- ► II: Modern Practical Deep Networks
  - 6 Deep Feedforward Networks
  - 7 Regularization for Deep Learning
  - 8 Optimization for Training Deep Models
  - 9 Convolutional Networks
  - 10 Sequence Modeling: Recurrent and Recursive Nets
    - 11 Practical Methodology
  - 12 Applications
- III: Deep Learning Research
  - 13 Linear Factor Models
  - 14 Autoencoders
  - ▶ 15 Representation Learning
    - 16 Structured Probabilistic Models for Deep Learning
  - ▶ 17 Monte Carlo Methods
  - 18 Confronting the Partition Function
  - ▶ 19 Approximate Inference
  - 20 Deep Generative Models

# Brief Introduction to Computational Graphs With TensorFlow

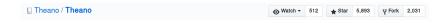
#### Motivation

► Keras wraps and simplifies usage of libraries, which are optimized on efficient computations, e.g., TensorFlow.

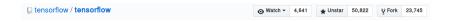
► How do modern numerical computation libraries such as Theano and TensorFlow work?

#### Theano? TensorFlow?

- Libraries for large-scale numerical computations
- ► TensorFlow is growing much faster and gains more support (Google does it!).

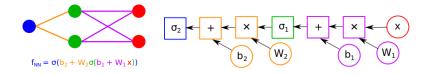


Theano is a Python library that allows you to define, optimize, and evaluate mathematical expressions involving multi-dimensional arrays efficiently.



**TensorFlow** is an open source software library for **numerical computation using data flow graphs**. Nodes in the graph represent mathematical operations, while the graph edges represent the multidimensional data arrays (tensors) communicated between them.

## Computational Graphs

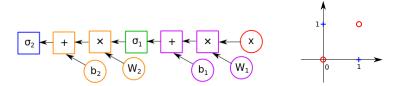


#### **Example neural network**

- → According computational graph
- ► TensorFlow implements all needed mathematical operations for multi-threaded CPU and multi GPU environments.
- Computation of neural networks using data flow graphs is a perfect match!

**TensorFlow** is an open source software library for numerical computation using data flow graphs. **Nodes** in the graph **represent mathematical operations**, while the **graph edges represent the multidimensional data arrays (tensors)** communicated between them.

## TensorFlow Implementation of the Example Neural Network



#### fermilab\_keras\_workshop/tensorflow/xor.py:

 $\rightarrow$  Already quite complicated for such a simple model!

# TensorFlow Implementation of the Example Neural Network (2)

- Plain TensorFlow implements only the mathematical operations.
- Combination of these operations to a neural network model is up to you.
- ► Already quite complicated for a simple neural network model without definition of loss function, training procedure, . . .

- ► **Solution 1:** Write your own framework to simplify TensorFlow applications
- ► **Solution 2:** Use wrapper such as Keras with predefined layers, loss functions, . . .

## Introduction to Keras

#### What is Keras?

- Most popular tool to train and apply (deep) neural networks
- ► Python wrapper around multiple numerical computation libaries, e.g., TensorFlow
- ► Hides most of the low-level operations that you don't want to care about.
- ► Sacrificing little functionality for much easier user interface
- ▶ Backends: TensorFlow, Theano
- ▶ NEW: Microsoft Cognitive Toolkit (CNTK) added as backend



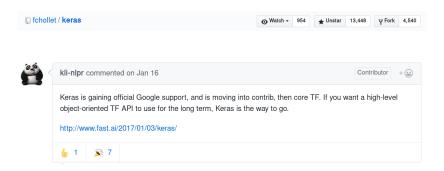






## Why Keras and not one of the other wrappers?

- ▶ There are lot of alternatives: TFLearn, Lasagne, . . .
- None of them are as popular as Keras!
- Will be tightly integrated into TensorFlow and officially supported by Google.
- ► Looks like a safe future for Keras!



Read the full story here: Link

#### Let's start!

- ▶ How does the tutorial works? You have the choice:
  - You can just listen and learn from the code examples on the slides.
  - 2. You can follow along with the examples on your own laptop.
- ▶ **But** you'll learn most by taking the examples as starting point and play around at home.

#### Download all files:

```
git clone https://github.com/stwunsch/fermilab_keras_workshop
```

#### **Set up the Python virtual environment:**

```
cd fermilab_keras_workshop
bash init_virtualenv.sh
```

#### **Enable the Python virtual environment:**

```
# This has to be done in every new shell!
source py2_virtualenv/bin/activate
```

## Keras Basics

## Configure Keras Backend

- Two ways to configure Keras backend (Theano, TensorFlow or CNTK):
  - 1. Using environment variables
  - 2. Using **Keras config file** in \$HOME/.keras/keras.json

#### Example setup using environment variables: Terminal:

```
export KERAS_BACKEND=tensorflow
python your_script_using_keras.py
```

#### Inside a Python script:

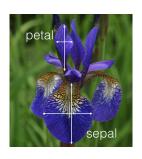
```
# Select TensorFlow as backend for Keras using environment variable `KERAS_BACKEND`
from os import environ
environ['KERAS_BACKEND'] = 'tensorflow'
```

#### Example Keras config using TensorFlow as backend:

```
$ cat $HOME/.keras/keras.json
{
    "image_dim_ordering": "th",
    "epsilon": 1e-07,
    "floatx": "float32",
    "backend": "tensorflow"
}
```

## Example Using the Iris Dataset

- Next slides will introduce the basics of Keras using the example fermilab\_keras\_workshop/keras/iris/train.py.
- ▶ Iris dataset: Classify flowers based on their proportions
- ▶ **4 features:** Sepal length/width and petal length/wdith
- ▶ 3 targets (flower types): Setosa, Versicolour and Virginica



#### Model Definition

- ▶ Two types of models: Sequential and the functional API
  - Sequential: Simply stacks all layers
  - ► Funktional API: You can do everything you want (multiple inputs, multiple outputs, ...).

## Model Summary

- model.summary() prints a description of the model
- ► Extremely useful to keep track of the number of free parameters

Layer (type)	Output Shape	Param #
dense_1 (Dense)	(None, 8)	40
dense_2 (Dense)	(None, 3)	27
Total params: 67 Trainable params: 67 Non-trainable params: 0		

## Define Loss Function, Optimizer, Validation Metrics. . .

- ► Everything is set in a single function, called the **compile** step of the model.
- ▶ Validation is performed after each training epoch (next slides).

## **Data Preprocessing**

- Some preprocessing steps are included in Keras, but mainly for text and image inputs.
- ▶ Better option: Using scikit-learn package (Link to preprocessing module)
- ▶ **Single input** (4 features): [5.1, 3.5, 1.4, 0.2]
  - Needs to be scaled to the order of 1 to fit the activation function.
- ► Single output (3 classes): [1 0 0]
- ► Common preprocessing: Standardization of inputs
  - ightarrow Operation:  $\frac{\text{input-mean}}{\text{standard deviation}}$

#### # Set up preprocessing

```
from sklearn.preprocessing import StandardScaler
preprocessing = StandardScaler()
preprocessing.fit(inputs)
inputs = preprocessing.transform(inputs)
```

## Training

Training is again a single call of the model object, called fit.

#### That's it for the training!

## Training (2)

```
Epoch 1/10
150/150 [=========== ] - 0s 998us/step - loss: 1.1936 - acc: 0.2533
Epoch 2/10
150/150 [============ ] - Os 44us/step - loss: 0.9904 - acc: 0.5867
Epoch 3/10
150/150 [============ ] - Os 61us/step - loss: 0.8257 - acc: 0.7333
Epoch 4/10
150/150 [============ ] - Os 51us/step - loss: 0.6769 - acc: 0.8267
Epoch 5/10
150/150 [============ ] - Os 49us/step - loss: 0.5449 - acc: 0.8933
Epoch 6/10
150/150 [============ ] - Os 53us/step - loss: 0.4384 - acc: 0.9267
Epoch 7/10
Epoch 8/10
150/150 [============= ] - Os 46us/step - loss: 0.3150 - acc: 0.9600
Epoch 9/10
150/150 [============ ] - Os 54us/step - loss: 0.2809 - acc: 0.9267
Epoch 10/10
```

## Save and Apply the Trained Model

#### Save model:

- Models are saved as HDF5 files: model.save("model.h5")
  - Combines description of weights and architecture in a single file
- ▶ **Alternative**: Store weights and architecture separately
  - Store weights: model.save\_weights("model\_weights.h5")
  - Store architecture: json\_dict = model.to\_json()

#### Load model:

```
from keras.models import load_model
model = load_model("model.h5")
```

#### Apply model:

```
predictions = model.predict(inputs)
```

## Wrap-Up

#### Training:

predictions = model.predict(inputs)

```
# Load iris dataset
# ...
# Model definition
model = Sequential()
model.add(Dense(8, kernel initializer="glorot normal", activation="relu", input dim=(4,)))
model.add(Dense(3, kernel initializer="glorot uniform", activation="softmax"))
# Preprocessing
preprocessing = StandardScaler().fit(inputs)
inputs = preprocessing.transform(inputs)
# Training
model.fit(inputs, targets onehot, batch size=20, epochs=10)
# Save model
model.save("model.h5")
Application:
# Load model
model = load model("model.h5")
# Application
```

That's a full training/application workflow in less than ten lines of code!

## Available Layers, Losses, Optimizers, ...

- There's everything you can imagine, and it's well documented.
- Possible to define own layers and custom metrics in Python!
- Check out: www.keras.io



## Advanced Usage of Keras

## Example Using the MNIST Dataset

Example in the repository: fermilab\_keras\_workshop/keras/mnist/train.py

#### MNIST dataset?

- ▶ **Task:** Predict the number on an image of a handwritten digit
- Official website: Yann LeCun's website (Link)
- ▶ Database of 70000 images of handwritten digits
- ▶ 28x28 pixels in greyscale as input, digit as label

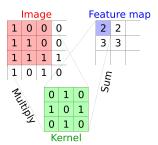


#### Data format:

- ▶ **Inputs:** 28×28 matrix with floats in [0, 1]
- ▶ **Target:** One-hot encoded digits, e.g.,  $2 \rightarrow [0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0]$

## Short Introduction to Convolutional Layers





- Kernel: Locally connected dense layer
- ▶ Convolution: Kernel moves similar to a sliding window over the image
- ▶ Feature map: Output "image" after application of the kernel

#### Model Definition

#### fermilab\_keras\_workshop/keras/mnist/train.py:

```
model = Sequential()
# First hidden layer
model.add(
    Conv2D(
        4. # Number of output filters or so-called feature maps
        (3, # column size of sliding window used for convolution
        3), # row size of sliding window used for convolution
        activation="relu". # Rectified linear unit activation
        input_shape=(28,28,1) # 28x28 image with 1 color channel
# All other hidden layers
model.add(MaxPooling2D(pool_size=(2,2)))
model.add(Flatten())
model.add(Dense(16, activation="relu"))
# Output layer
model.add(Dense(10, activation="softmax"))
# Print model summary
model.summary()
```

## Model Summary

Non-trainable params: 0

▶ Detailed summary of model complexity with model.summary()

Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 26, 26, 4)	40
max_pooling2d_1 (MaxPooling2	(None, 13, 13, 4)	0
flatten_1 (Flatten)	(None, 676)	0
dense_1 (Dense)	(None, 16)	10832
dense_2 (Dense)	(None, 10)	170
Total params: 11,042 Trainable params: 11,042		

### Training With Validation Metrics

- Validation metrics are evaluated after each training epoch.
- In compile step, multiple predefined validation metrics can be booked, e.g., accuracy.
- Custom metrics are possible.

#### Booking a predefined metric:

```
# Compile model
model.compile(loss="categorical_crossentropy",
    optimize=Adam(),
    metrics=["accuracy"])
```

#### Training with validation data:

### Training With Callbacks

- Callbacks are executed before and/or after each training epoch.
- Numerous predefined callbacks are available, custom callbacks can be implemented.

#### Definition of model-checkpoint callback:

#### Register callback:

```
model.fit(inputs, targets, # Training data
batch_size=100, # Batch size
epochs=10, # Number of training epochs
callbacks=[checkpoint]) # Register callbacks
```

# Training With Callbacks (2)

- Commonly used callbacks for improvement, debugging and validation of the training progress are implemented, e.g., EarlyStopping.
- Powerful tool: TensorBoard in combination with TensorFlow
- Custom callback: LambdaCallback or write callback class extending base class keras.callbacks.Callback

#### Callbacks

Usage of callbacks

Callback

BaseLogger

TerminateOnNaN

ProgbarLogger

History

ModelCheckn

EarlyStopping

RemoteMonitor

LearningRateScheduler

TensorBoard

ReduceLROnPlateau

CSVLogger

LambdaCallback

Create a callback

### Advanced Training Methods for Big Data

- ► The call model.fit(inputs, targets, ...) expects all inputs and targets to be already loaded in memory.
  - $\rightarrow$  Physics applications have often data on Gigabyte to Terabyte scale!

# These methods can be used to train on data that does not fit in memory.

Training on single batches, performs a single gradient step:

```
model.train_on_batch(inputs, targets, ...)
```

Training with data from a Python generator:

```
def generator_function():
    while True:
        yield custom_load_next_batch()

model.fit_generator(generator_function, ...)
```

# Application on Handwritten Digits

PNG images of handwritten digits are placed in fermilab\_keras\_workshop/keras/mnist/example\_images/, have a look!



- Let's **apply our trained model** on the images:
- ./keras/mnist/apply.py keras/mnist/example\_images/\*.png
  - ▶ If you are bored on your way home:
    - Open with GIMP your\_own\_digit.xcf
    - 2. Dig out your most beautiful handwriting
    - 3. Save as PNG and run your model on it

# Application on Handwritten Digits (2)

#### Predict labels for images:

```
keras/mnist/example_images/example_input_0.png : 7
keras/mnist/example_images/example_input_1.png : 2
keras/mnist/example_images/example_input_2.png : 1
keras/mnist/example_images/example_input_3.png : 0
keras/mnist/example_images/example_input_4.png : 4
keras/mnist/example_images/example_input_5.png : 1
keras/mnist/example_images/example_input_6.png : 4
keras/mnist/example_images/example_input_7.png : 9
keras/mnist/example_images/example_input_8.png : 6
keras/mnist/example_images/example_input_9.png : 9
```

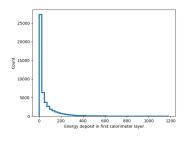


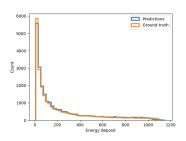
# Examples with Physics Data

### Toy Calorimeter

- Data represent measurements in a toy-calorimeter
  - ▶ Inputs: 13 calorimeter layers with energy deposits
  - ► Target: Reconstruction of total energy deposit
- Example in repository:

fermilab\_keras\_workshop/keras/calorimeter/train.py





#### Implemented regression model:

```
model = Sequential()
model.add(Dense(100, activation="tanh", input_dim=(13,)))
model.add(Dense(1, activation="linear"))
```

Source: Link

# Deep Learning on the HIGGS Dataset

One of the most often cited papers about deep learning in combination with a physics application:

Searching for Exotic Particles in High-Energy Physics with Deep Learning

Pierre Baldi, Peter Sadowski, Daniel Whiteson

- ▶ Topic: Application of deep neural networks for separation of signal and background in an exotic Higgs scenario
- ▶ **Results:** Deep learning neural networks are more powerful than "shallow" neural networks with only a single hidden layer.

Let's reproduce this with minimal effort using Keras!

# Deep Learning on the HIGGS Dataset (2)

#### Files:

- fermilab\_keras\_workshop/keras/HIGGS/train.py
- fermilab\_keras\_workshop/keras/HIGGS/test.py

#### Dataset:

Number of events: 11MNumber of features: 28

#### Shallow model:

```
model_shallow = Sequential()
model_shallow.add(Dense(1000, activation="tanh", input_dim=(28,)))
model_shallow.add(Dense(1, activation="sigmoid"))
```

#### Deep model:

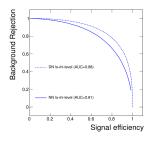
```
model_deep = Sequential()
model_deep.add(Dense(300, activation="relu", input_dim=(28,)))
model_deep.add(Dense(300, activation="relu"))
model_deep.add(Dense(300, activation="relu"))
model_deep.add(Dense(300, activation="relu"))
model_deep.add(Dense(300, activation="relu"))
model_deep.add(Dense(1, activation="relu"))
```

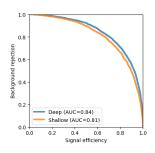
#### **Training:**

```
model.compile(loss="binary_crossentropy", optimizer=Adam(), metrics=["accuracy"])
model.fit(preprocessed_inputs, targets,
   batch_size=100, epochs=10, validation_split=0.25)
```

# Deep Learning on the HIGGS Dataset (3)

Weights of deep and shallow model are part of the repository.





- Shallow model matches performance in the paper, but deep model can be improved.
  - $\rightarrow$  Try to improve it! But you'll need a decent GPU. . .
- ► Keras allows to reproduce this result with a total of 130 lines of code:

```
# Count lines of code
$ wc -l keras/HIGGS/*.py
62 keras/HIGGS/test.py
68 keras/HIGGS/train.py
130 total
```

# Useful Tools In Combination With Keras

# TMVA Keras Interface

### Prerequisites

- Keras inteface integrated in ROOT/TMVA since v6.08
- Example for this tutorial is placed here: fermilab\_keras\_workshop/tmva/
- ➤ You need ROOT with enabled PyROOT bindings. Easiest way to test the example is using CERN's **Ixplus** machines:
  - ssh -Y you@lxplus.cern.ch
  - ▶ Source software stack LCG 91

#### How to source LCG 91 on lxplus:

source /cvmfs/sft.cern.ch/lcg/views/LCG\_91/x86\_64-slc6-gcc62-opt/setup.sh

### Why do we want a Keras interface in TMVA?

- 1. Fair comparison with other methods
  - Same preprocessing
  - Same evaluation
- 2. Try state-of-the-art DNN performance in existing analysis/application that is already using TMVA
- 3. Access data in ROOT files easily
- 4. Integrate Keras in your **application** using **C++**
- Latest DNN algorithms in the ROOT framework with minimal effort

#### How does the interface work?

- 1. Model definition done in Python using Keras
- Data management, training and evaluation within the TMVA framework
- 3. **Application** using the TMVA reader



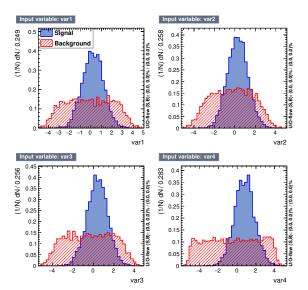
► The interface is implemented in the optional PyMVA part of TMVA:

#### # Enable PyMVA

ROOT.TMVA.PyMethodBase.PyInitialize()

### **Example Setup**

 Dataset of this example is standard ROOT/TMVA test dataset for binary classification



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#### Model Definition

Setting up the model does not differ from using plain Keras:

```
model = Sequential()
model.add(Dense(64, init='glorot_normal', activation='relu', input_dim=4))
model.add(Dense(2, init='glorot_uniform', activation='softmax'))
model.compile(loss='categorical_crossentropy', optimizer=Adam(), metrics=['accuracy',])
model.save('model.h5')
```

► For binary classification the model needs two output nodes:

```
model.add(Dense(2, activation='softmax'))
```

► For multi-class classification the model needs two or more output nodes:

```
model.add(Dense(5, activation='softmax'))
```

► For **regression** the model needs a **single output node**:

```
model.add(Dense(1, activation='linear'))
```

#### **Training**

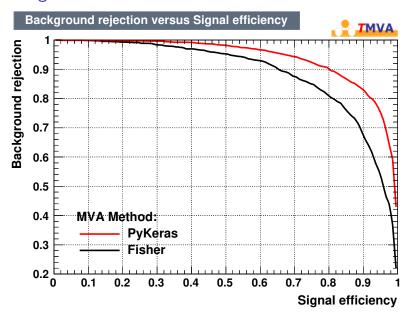
► Training options defined in the TMVA booking options:

#### That's it! You are ready to run!

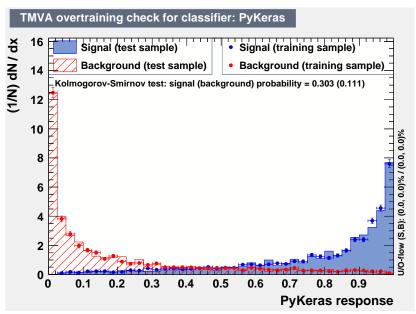
python tmva/BinaryClassification.py

Run TMVA GUI to examine results: root -1 tmva/TMVAGui.C

# Training Results: ROC



# Training Results: Overtraining Check



# Application

Does not differ from any other TMVA method!

Example application can be found here: fermilab\_keras\_workshop/ tmva/ApplicationBinaryClassification.py

# Application (2)

#### Run python tmva/ApplicationBinaryClassification.py:

```
# Response of TMVA Reader

: Booking "PyKeras" of type "PyKeras" from
: BinaryClassificationKeras/weights/TMVAClassification_PyKeras.weights.xml.

Using Theano backend.

DataSetInfo : [Default] : Added class "Signal"

DataSetInfo : [Default] : Added class "Background"
: Booked classifier "PyKeras" of type: "PyKeras"
: Load model from file:
: BinaryClassificationKeras/weights/TrainedModel_PyKeras.h5

# Average response of MVA method on signal and background
Average response on background: 0.78
Average response on background: 0.21
```

# lwtnn with Keras

#### What is lwtnn?

- Core problem: TensorFlow and others are not made for event-by-event application!
- ► C++ library to apply neural networks
  - ▶ Minimal dependencies: C++11, Eigen
  - Robust
  - Fast
- "Asymmetric" library:
  - Training in any language and framework on any system, e.g.,
     Python and Keras
  - ▶ **Application** in **C++** for real-time applications in a limited environment, e.g., high-level trigger
- ► **GitHub:** https://github.com/lwtnn/lwtnn
- ▶ IML talk about lwtnn by Daniel Guest: Link
- Tutorial can be found here: https://github.com/stwunsch/iml\_keras\_workshop

# Load and Apply Model in C++ Using lwtnn

#### Convert trained Keras model to lwtnn JSON:

 $\rightarrow$  See the tutorial and README!

// Apply model on inputs

auto outputs = model.compute(inputs);

#### Load model:

```
// Read lwtnn JSON config
auto config = lwt::parse_json(std::ifstream("lwtnn.json"));
// Set up neural network model from config
lwt::LightweightNeuralNetwork model(
        config.inputs,
        config.layers,
        config.outputs);
Apply model:
// Load inputs from argu
std::map<std::string, double> inputs;
. . .
```