Assignment 5: Results/Description

Problem 1

For this problem I have written two programs (myFTCS and myCN) to solve the following problem. These may be compiled all together with a make all as shown below.

```
aburrow@schooner1:~/NumericalMethods/hw5
                                                                                              [aburrow@schooner1 hw5]$ [aburrow@schooner1 hw5]$
[aburrow@schooner1 hw5]$ pwd
/home/aburrow/NumericalMethods/hw5
[aburrow@schooner1 hw5]$ ls
           Makefile plot.py README.md run_full src
[aburrow@schooner1 hw5]$ make all
mkdir -p bin
mkdir -p output
mkdir -p doc/figs
icpc -mkl -c src/myFTCS.cpp -o bin/myFTCS.o
icpc -mkl -c src/io.cpp -o bin/io.o
icpc -mkl -c src/ftcs.cpp -o bin/ftcs.o
icpc -mkl bin/myFTCS.o bin/io.o bin/ftcs.o -o bin/myFTCS
icpc -mkl -c src/myCN.cpp -o bin/myCN.o
icpc -mkl -c src/crankNicholson.cpp -o bin/crankNicholson.o
icpc -mkl -c src/tridiag.cpp -o bin/tridiag.o
icpc -mkl bin/myCN.o bin/io.o bin/crankNicholson.o bin/tridiag.o -o bin/myCN
[aburrow@schooner1 hw5]$
```

This generates executables myFTCS and myCN in the "./bin" directory, which may be run one at a time. There is also a plot.py in the root which may be run to generate plots from the output of the executables. However, to run all these programs at once, I have also included a run_full bash script that may be executed for convenience.

In this problem, I use (a) the FTCS method and (b) the Crank-Nicholson method to solve the diffusion equation

$$\frac{\partial n}{\partial t} = \frac{\partial^2 n}{\partial x^2}.$$

(a)

Below I run the program that demonstrates solving our differential equation using the FTCS method:

```
aburrow@schooner1:~/NumericalMethods/hw5

[aburrow@schooner1 hw5]$ [aburrow@schooner1 hw5]$

[aburrow@schooner1 hw5]$ pwd

/home/aburrow/NumericalMethods/hw5

[aburrow@schooner1 hw5]$ ls

bin config doc Makefile output plot.py README.md run_full src

[aburrow@schooner1 hw5]$ ./bin/myFTCS

Reading from parameter file: ./config/params

D: 1

dt: 0.02

dx: 0.2

x min: -20

x max: 20

Left bound: 0

Right bound: 0

Evolution time: 20

Using r = 0.5

Calculating solution...

Writing to ./output/ftcs.dat

[aburrow@schooner1 hw5]$ ■
```

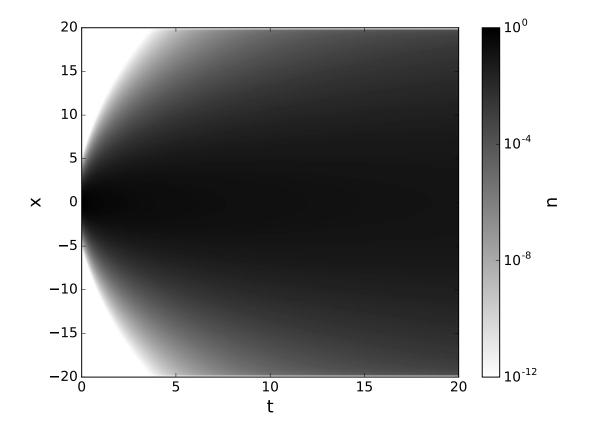


Figure 1: Solution using the FTCS method.

(b)

Below I run the program that demonstrates solving our differential equation using the Crank-Nicholson method:

```
aburrow@schooner1:~/NumericalMethods/hw5
                                                                                                               [aburrow@schooner1 hw5]$ [aburrow@schooner1 hw5]$ pwd
/home/aburrow/NumericalMethods/hw5
[aburrow@schooner1 hw5]$ ls
                                          plot.py README.md run_full src
                     Makefile
[aburrow@schooner1 hw5]$ ./bin/myCN
Reading from parameter file: ./config/params
  dt: 0.02
  dx: 0.2
  x min: -20
  x max: 20
  Left bound: 0
  Right bound: 0
  Evolution time: 20
Using r = 0.5
Calculating solution...
Writing to ./output/crankNicholson.dat
[aburrow@schooner1 hw5]$
```

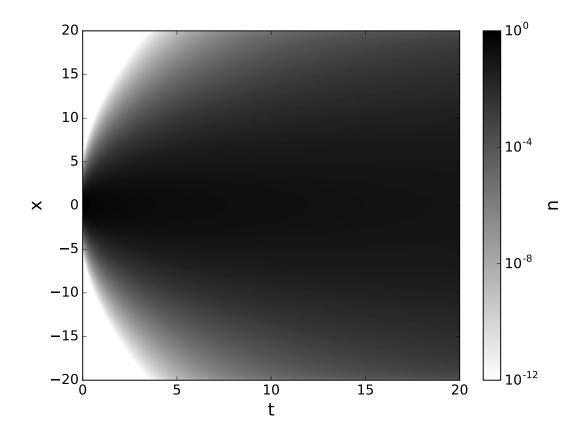


Figure 2: Solution using the Crank-Nicholson method.