

HW4

1)

A1: 10x20
A2: 20x25
A3: 25x15
A4: 15x10
A5: 10x30
A6: 30x12

$m[1,3]$

$(A_1 A_2) A_3$
5,625 10,250 25,5
8,750

$A_1 (A_2 A_3)$
5,625 10,250 25,5
10,500

$m[2,4]$

$(A_2 A_3) A_4$
20,250 15,150 10
10,500

$A_2 (A_3 A_4)$
25,250 15,150 10
8,750

$m[3,5]$

$(A_3 A_4) A_5$
25,150 15,100 30
11,250

$A_3 (A_4 A_5)$
25,150 15,100 30
15,750

$((A_1 \cdot A_2) \cdot A_3) \cdot A_4 \cdot (A_5 \cdot A_6)$

m	1	2	3	4	5	6
1	○	5000	8,750	10,250	13,250	15,050
2		○	7,500	8,750	14,750	14,750
3			○	3,750	11,250	9,000
4				○	4,500	5,400
5					○	3,600
6						○

s	1	2	3	4	5	6
1		1	2	3	4	4
2			2	3	4	4
3				3	4	3
4					4	4
5						5
6						

$m[4, 6]$

$$(A_4 \ A_5) \ A_6 \ 12$$

$$15 \ 10 \ 15 \ 30 \ 30 \ 12$$

$$9900$$

$$A_4 (A_5 \ A_6)$$

$$15 \ 10 \ 15 \ 30 \ 30 \ 12$$

$$8400$$

$m[3, 6]$

$$A_3 (A_4 \ A_5 \ A_6)$$

$$25 \ 15 \ 15 \ 10 \ 10 \ 30 \ 12$$

$$9400$$

$$(A_3 \ A_4) (A_5 \ A_6)$$

$$25 \ 15 \ 15 \ 10 \ 10 \ 30 \ 12$$

$$10,350$$

$$(A_3 \ A_4 \ A_5) \ A_6$$

$$25 \ 15 \ 15 \ 10 \ 10 \ 30 \ 12$$

$$11,250$$

$m[1, 4]$

$$A_1 (A_2 \ A_3 \ A_4)$$

$$10 \ 20 \ 20 \ 25 \ 15 \ 10$$

$$10,750$$

$$(A_1 \ A_2) (A_3 \ A_4)$$

$$10 \ 20 \ 20 \ 25 \ 15 \ 10$$

$$11,250$$

$$(A_1 \ A_2 \ A_3) \ A_4$$

$$10 \ 20 \ 20 \ 25 \ 15 \ 10$$

$$1500 + 8750 = 10,250$$

$m[2, 5]$

$$A_2 (A_3 \ A_4 \ A_5)$$

$$20 \ 25 \ 25 \ 15 \ 15 \ 10 \ 30$$

$$26,250$$

$$(A_2 \ A_3) (A_4 \ A_5)$$

$$20 \ 25 \ 25 \ 15 \ 15 \ 10 \ 30$$

$$21,000$$

$$(A_2 \ A_3 \ A_4) \ A_5$$

$$20 \ 25 \ 25 \ 15 \ 15 \ 10 \ 30$$

$$14,750$$

$m[1,5]$

$$10 \quad A_1 \quad \begin{pmatrix} A_2 & A_3 & A_4 & A_5 \end{pmatrix} \quad \begin{matrix} 20 & 20 & 30 & 30 \\ +14,750 \\ (6,000) \end{matrix}$$

$20,750$

$$10 \quad \begin{pmatrix} A_1 & A_2 \end{pmatrix} \quad \begin{pmatrix} A_3 & A_4 & A_5 \end{pmatrix} \quad \begin{matrix} 25 & 25 & 30 \\ +5,000 + 11,250 \\ (7,500) \end{matrix}$$

$23,750$

$$\begin{pmatrix} A_1 & A_2 & A_3 \end{pmatrix} \quad \begin{pmatrix} A_4 & A_5 \end{pmatrix} \quad \begin{matrix} 10 & 15 & 30 \\ +8,750 + 4,500 \\ (4,500) \end{matrix}$$

$17,750$

$$\begin{pmatrix} A_1 & A_2 & A_3 & A_4 \end{pmatrix} \quad A_5 \quad \begin{matrix} 10 & 10 & 30 & 30 \\ +10,250 \\ (3,000) \end{matrix}$$

$13,250$

M[2,6]

$$\begin{matrix} A_2 & (A_3 & A_4 & A_5 & A_6) \\ 20 & 25 & 25 & & \\ & & & 15,900 & 12 + 9900 \\ & & & & (6,000) \end{matrix}$$

$$\begin{matrix} (A_2 & A_3) & (A_4 & A_5 & A_6) \\ 20 & 15 & 15 & & \\ & & & 12 + 7500 + 5400 \\ & & & & (36,000) \end{matrix}$$

$$\begin{matrix} (A_2 & A_3 & A_4) & (A_5 & A_6) \\ 20 & & 10 & 10 & \\ & & & & 12 + 8750 + 3600 \\ & & & & & (2,400) \end{matrix}$$

$$\begin{matrix} (A_2 & A_3 & A_4 & A_5) & A_6 \\ 20 & & 30 & 30 & 12 + 14,750 \\ & & & & (7200) \end{matrix}$$

M[1,6]

$$\begin{matrix} A_1 & (A_2 & A_3 & A_4 & A_5 & A_6) \\ 10 & 20 & 20 & & & \\ & & & 17,150 & 12 + 14750 \\ & & & & (2,400) \end{matrix}$$

$$\begin{matrix} (A_1 & A_2) & (A_3 & A_4 & A_5 & A_6) \\ 10 & 25 & 25 & & & \\ & & & 17,900 & 12 + 5000 + 9900 \\ & & & & (3000) \end{matrix}$$

$$\begin{matrix} (A_1 & A_2 & A_3) & (A_4 & A_5 & A_6) \\ 10 & 15 & 15 & & & \\ & & & 15,950 & 12 + 8750 + 5400 \\ & & & & (1800) \end{matrix}$$

$$\begin{matrix} (A_1 & A_2 & A_3 & A_4) & (A_5 & A_6) \\ 10 & 10 & 10 & & & \\ & & & 12 + 10,250 + 3600 \\ & & & & (1200) \end{matrix}$$

$$\begin{matrix} (A_1 & A_2 & A_3 & A_4 & A_5) & A_6 \\ 10 & 30 & 30 & 12 + 13250 \\ & & & & (3600) \end{matrix}$$