- 1. For each of the following estimated models provide the simplest possible explanation of the effect of IQ (intelligent quotient has mean of 100) on EARNS (annual earnings in \$). Hint: For models with logs use elasticities or semi-elasticities.
- (a) $EARNS = 1000 + 500 \times IQ$.
- (b) $EARNS = 20000 + 200 \times IQ + 2 \times IQ^2$
- (c) $EARNS = -20000 + 50000 \times ln(IQ)$
- (d) $EARNS = 45000 + 10000 \times d$, where d = 1 if IQ > 100 and d = 0 if $IQ \le 100$.
- (e) $ln(EARNS) = 10 + 0.010 \times IQ$.
- (f) $ln(EARNS) = 5 + 0.90 \times ln(IQ)$.
- (g) For the model in (c) give the marginal effect at the mean if IQ = 110.
- Use data in file ADVERTISING.DTA at the course website.

In answering the following it can be helpful (though not necessary) to use **estimates store** and **estimates table** to present model results side by side.

- (a) Fit linear, linear-log, log-linear and log-log models for regression of sales on tv.
- (b) Which model, if any, do you prefer? Explain.
- (c) Compute the average marginal effect (AME) and the marginal effect at the mean (MEM) for the linear-log model.
- (d) Use command **predict** after the linear regression to predict sales from the linear model. Does the prediction on average equal sales on average?
- (e) Use command predict after the log-linear regression to predict log-sales from the log-linear model.

 Then create a crude prediction of sales. Does the prediction on average equal sales on average?
- (f) The notes in Chapter 12.5 suggest multiplying the preceding prediction by $\exp{(S_{e^2}/2)}$ where s_e is

the standard error of the regression of lny on x. Does this lead to a better prediction? Explain.

- (g) Plot the three different predictions from parts (d), (e) and (f) against tv on the same graph. Comment on these plots. Suppose the predictions are called p1, p2 and p3.
- 3. Use data in file ADVERTISING.DTA at the course website.
- (a) Obtain summary statistics for sales, tv, radio, and newspaper. Are the data in the expected ranges? HINT: Use command describe to get variable descriptions.
- (b) Test the claim that the population mean sales are less than 13000 at level 0.05.
- (c) Which variable(s) do you think will be important predictors of sales?
- (d) Which variables are most highly correlated with sales? Are there any surprises?
- (e) Which variables are statistically significant (two-sided test at 5%)? Use the individual p-values.
- (f) State which, if any, of the regressors do not have the sign you expect a priori and give an explanation for why you expected a different sign.