

1. For each of the following estimated models provide the simplest possible explanation of the effect of IQ (intelligent quotient has mean of 100) on EARN\$ (annual earnings in \$). Hint: For models with logs use elasticities or semi-elasticities.

(a) $EARN\$ = 1000 + 500 \times IQ$.

(b) $EARN\$ = 20000 + 200 \times IQ + 2 \times IQ^2$

(c) $EARN\$ = -20000 + 50000 \times \ln(IQ)$

(d) $EARN\$ = 45000 + 10000 \times d$, where $d = 1$ if $IQ > 100$ and $d = 0$ if $IQ \leq 100$.

(e) $\ln(EARN\$) = 10 + 0.010 \times IQ$.

(f) $\ln(EARN\$) = 5 + 0.90 \times \ln(IQ)$.

(g) For the model in (c) give the marginal effect at the mean if $\bar{IQ} = 110$.

2. Use data in file ADVERTISING.DTA at the course website.

In answering the following it can be helpful (though not necessary) to use **estimates store** and **estimates table** to present model results side by side. Here is a generic example:

```
quietly regress y x estimates store MODEL1  quietly regress y
z estimates store MODEL2  quietly regress y w estimates store
MODEL3  estimates table MODEL*, b(%6.3g) t(%4.2f) p(%4.3f)
stat(N r2)
```

You will need to modify this code so that it is appropriate for the dataset at hand and includes all the regressions you wish to run

(a) Fit linear, linear-log, log-linear and log-log models for regression of sales on tv.

(b) Which model, if any, do you prefer? Explain.

(c) Compute the average marginal effect (AME) and the marginal effect at the mean (MEM) for the linear-log model.

(d) Use command **predict** after the linear regression to predict sales from the linear model. Does the prediction on average equal sales on average?

(e) Use command `predict` after the log-linear regression to predict log-sales from the log-linear model.

Then create a crude prediction of sales as follows. `predict plnsales, xb` generate `psales = exp(plnsales)`

Does the prediction on average equal sales on average?

(f) The notes in Chapter 12.5 suggest multiplying the preceding prediction by $\exp(s_e^2/2)$ where s_e is

the standard error of the regression of $\ln y$ on x . Does this lead to a better prediction? Explain.

(g) Plot the three different predictions from parts (d), (e) and (f) against `tv` on the same graph. Comment on these plots. Suppose the predictions are called `p1`, `p2` and `p3`. Then the Stata commands to use are

```
sort tv
scatter p1 tv, c(l) || scatter p2 tv, c(l) || scatter
p3 tv, c(l)
```

3. Use data in file `ADVERTISING.DTA` at the course website.

(a) Obtain summary statistics for `sales`, `tv`, `radio`, and `newspaper`. Are the data in the expected ranges?
HINT: Use command `describe` to get variable descriptions.

(b) Test the claim that the population mean sales are less than 13000 at level 0.05. (Use command `ttest sales=13000`).

(c) Give command `graph matrix sales tv radio newspaper, half`

Which variable(s) do you think will be important predictors of sales?

(d) Give command `correlate sales tv radio newspaper`

Which variables are most highly correlated with sales? Are there any surprises?

(e) Give command `regress sales tv radio newspaper`

Which variables are statistically significant (two-sided test at 5%)? Use the individual p-values.

(f) State which, if any, of the regressors do not have the sign you expect a priori, and give an explanation for why you expected a different sign.