

Math 241 Group Quiz 4

Names: _____

1. Find the volume of the ellipsoid $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} \leq 1$ where a, b, c are constants (it is a squished sphere).

2. Find the line integral $\int_C (x - y) \, ds$ where C is the line segment from (a, b, c) to (d, e, f) .

3. Using a line integral, find the lateral surface area of the portion of the cylinder $x^2 + y^2 = r^2$ above the plane $z = 0$ and below the graph of $z = f(x, y)$. (Leave the answer as an integral involving f).

4. Let R be the set of points in the x, y -plane which satisfy $x^2 + y^2 \leq a^2$. Use Question the previous exercise to explain why

$$\iint_R f(x, y) \, dx \, dy = \int_0^a \int_0^{2\pi} f(r \cos \vartheta, r \sin \vartheta) \, r \, d\vartheta \, dr$$