

## Math 143 Midterm 2

Name: \_\_\_\_\_

1. Find the parametric equations for the line in  $\mathbb{R}^3$  that contains the point  $(1, 2, 3)$  and is perpendicular to both  $\langle 1, 0, 4 \rangle$  and  $\langle -1, 1, 2 \rangle$ .

2. Find the values of  $t$  for which the parametric curve  $\begin{cases} x = 2t^2 \\ y = t^4 - t^3/3 \end{cases}$  for  $t \in \mathbb{R}$  is concave down.

**3.** Square both sides of  $e^{it} = \cos t + i \sin t$ . Then use that calculation to explain why this identity is true:

$$\cos(2t) = \cos^2 t - \sin^2 t$$

4. Find the equation of the line tangent to the polar curve  $r = 1/(1 + \cos \theta)$  at  $\theta = \pi/2$ .

5. Find the area inside the polar curve  $r = \cos(3\theta)$  but outside the polar curve  $r = \sin(3\theta)$ .

*Do not evaluate the integrals, just set the integrals up!*

