

## Math 143 Quiz 5

Names: \_\_\_\_\_

1. Show that the curvature of the graph of  $y = f(t)$  is given by  $\kappa(t) = \frac{|f''(t)|}{(1 + f'(t)^2)^{3/2}}$ .

2. Suppose  $\mathbf{r}$  is parameterized by arclength, meaning that  $\kappa = |\mathbf{r}''|$ . Show that if  $\kappa = 0$ , then  $\mathbf{r}$  is a line.

**3.** Parameterize the line that passes through the point  $(a, b, c)$  and is parallel to the vector  $\mathbf{v}$  by arclength.

**4.** Show that  $\mathbf{B}' \cdot \mathbf{B}$  and  $\mathbf{B}' \cdot \mathbf{T}$  are both 0. Why does this show that  $\mathbf{B}'$  and  $\mathbf{N}$  are parallel?