Linear Analysis II Exercise Set 6

1. Solve the differential equations below using series. Write solutions in the form

$$y(x) = a_0 y_1(x) + a_1 y_2(x)$$

where $y_1(x)$ and $y_2(x)$ are series. It is acceptable to only write down the first three nonzero terms in the series for $y_1(x)$ and $y_2(x)$ followed by "···". For example, instead of writing $y_1(x) = \sin x$, it is acceptable to write

$$y_1(x) = \frac{x^1}{1!} - \frac{x^3}{3!} + \frac{x^5}{5!} - \cdots$$

a.
$$y'' - 2xy' - 2y = 0$$

b.
$$y'' + xy' + 3y = 0$$

c.
$$y'' - y' - xy = 0$$

d.
$$(1+x^2)y'' + 4xy' + 2y = 0$$

e.
$$(x^2 - 1)y'' - 6xy' + 12y = 0$$