

Math 244 Midterm 1

Names: _____

1. Let $A = \begin{bmatrix} 1 & 1 & 1 & 1 \\ -2 & 1 & 1 & 4 \end{bmatrix}$ and let $S = \{\mathbf{x} \text{ in } \mathbb{R}^4 : A\mathbf{x} = \mathbf{0}\}$. Find a basis for S and the dimension of S .

2. Write the system $\begin{cases} x - z = 1 \\ y - z = -2 \\ -y + 2z = 0 \end{cases}$ as a matrix multiplication of the form $A\mathbf{x} = \mathbf{b}$. Solve using A^{-1} .

3. Find all eigenvalues and eigenvectors for $\begin{bmatrix} 1 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$.

4. Are the vectors $\begin{bmatrix} 1 \\ 1 \\ 0 \\ 1 \end{bmatrix}$, $\begin{bmatrix} 1 \\ 0 \\ -1 \\ 1 \end{bmatrix}$, $\begin{bmatrix} 0 \\ 2 \\ 1 \\ 1 \end{bmatrix}$ linearly independent? Why or why not?

5. Let $S = \text{span}\{x + 1, x - 1, x^2 + 1, x^2 - 1\}$. Find a basis for S and the dimension of S .