

Week 3 Homework

1. Are the following formulas valid, satisfiable, or unsatisfiable?
 - $P(a) \rightarrow \exists x P(x)$
 - $\exists x P(x) \rightarrow P(a)$
 - $\exists x P(x) \vee \exists x \neg P(x) \rightarrow \forall x P(x)$
2. For each of the following sequent, give a formal proof if entailment holds.
 - $\forall x P(x) \vdash \exists x P(x)$
 - $\forall x (P(x) \rightarrow Q(x)), \forall x P(x) \vdash \forall x Q(x)$
 - $\forall x (P(x) \rightarrow Q(x)), \exists x P(x) \vdash \exists x Q(x)$
 - $\neg \exists x P(x) \vdash \forall x \neg P(x)$
 - $\neg \forall x P(x) \vdash \exists x \neg P(x)$