Reasoning

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Chapter 1

Electric Cars

1. If an electric car uses electricity generated by coal does it produce less carbon emissions per unit of energy then an ICE? Consider the mass of carbon emmitted per unit distance driven by an electric car and an ICE denoted $\eta_{\rm e}$ and $\eta_{\rm ICE}$ respectively. The dimensions are:

$$[\eta_{\rm e}] = \frac{[M]}{[L]} = \underbrace{\frac{[M]}{[E]}}_{a} \underbrace{\frac{[E]}{[L]}}_{1/b}$$

where a is the mass of carbon produced per kWh by a coal plant, and b is the number of km's per kWh of charge. The U.S Energy Information Administration estimates a=0.42 kg/kWh. For a Tesla Model 3:

$$b = \frac{50}{400} \frac{\text{kWh}}{\text{km}} = \frac{5}{40} \frac{\text{kWh}}{\text{km}}$$

giving:

$$\eta_e = 2.1 \frac{\text{kg}}{\text{km}}$$

For the ICE:

$$[\eta_{ ext{ICE}}] = rac{[M]}{[L]} = \underbrace{rac{[M]}{[L^3]}}_{c} \underbrace{rac{[L^3]}{[L]}}_{d}$$

where c is the number of kg's of carbon per litre and d is the number of litres per km. The National Resources of Canada estimates c=2.3 kg/L and d=9.0 L/km. Therefore:

$$\eta_{\rm ICE} = 20.7 \frac{\rm kg}{\rm km}$$

So an electric car produces 10 times less carbon emission even if the fuel is generated by coal.