

## EXPONENTIALSUM (Partial)

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```
1 def exponentialSum(self):
2     S = [a for a in range(self.k) if self.D[a] in [2, 6]]
3     if len(S) != 0:
4         a = S[0]
5
6         # Construct R as in comment on page 12
7         R = np.identity(self.k)
8         for b in S[1:]:
9             R[b, a] += 1
10        R = R % 2
11
12        self.updateDJ(R)
13        S = [a]
14        # Now J[a, a] = 0 for all a not in S
15
16        E = [k for k in range(self.k) if k not in S]
17        M = []
18        Dimers = [] # maintain list of dimers rather than r
19
20        while len(E) > 0:
21            a = E[0]
22            K = [b for b in E[1:] if self.J[a, b] == 4]
23
24            if len(K) == 0: # found a new monomer {a}
25                M.append(a)
26                E = E[1:]
27            else:
28                b = K[0]
29
30                # Construct R for basis change
31                R = np.identity(self.k)
32                for c in [x for x in E if x != a and x != b]:
33                    if self.J[a, c] == 4: R[c, a] += 1
34                    if self.J[b, c] == 4: R[c, b] += 1
35                R = R % 2
36
37                self.updateDJ(R)
38
39                # {a, b} form a new dimer
40                Dimers.append([a, b])
41                E = [x for x in E if x != a and x != b]
42
43        if len(S) != 0:
44            # Compute W(K,q) from Eq. 63
45            raise NotImplementedError # Where exactly in reference 15?
46        else:
47            # Compute W_0, W_1 from Eq. 68
48            raise NotImplementedError
49
50        # evaluates the expression in the comment on page 12
51        def W(p, m, eps):
52            return eps * 2**(p/2) * np.exp(1j*np.pi*m/4)
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