

SHRINK

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1  # attempt to shrink the stabilizer state by eliminating a part
2  # of the basis that has inner product  $\alpha$  with vector  $\xi$ 
3  def shrink(self, xi, alpha, lazy=False):
4      #  $S \leftarrow \{a \in [k] : (\xi, g) = 1\}$ 
5      # Note that a is zero-indexed.
6      S = [a for a in range(self.k) if np.inner(self.G[a], xi) % 2 == alpha]
7
8      beta = (alpha + np.inner(xi, self.h)) % 2
9      if len(S) == 0 and beta == 1: return "EMPTY"
10     if len(S) == 0 and beta == 0: return "SAME"
11
12     i = S[0] # pick any  $i \in S$ 
13     S.remove(i)
14
15     for a in S:
16         #  $g^a \leftarrow g^a \oplus g^i$ 
17         # compute shift matrix for G
18         shift = np.concatenate((np.zeros((a, self.n)), [self.G[i]],
19                                 np.zeros((self.n - a - 1, self.n))))
20         self.G = (self.G + shift) % 2
21
22         # update D, J using equations 48, 49 on page 10
23         # compute  $k \times k$  basis change matrix R (equation 47)
24         if not lazy:
25             R = np.identity(self.k)
26             R[a, i] = 1
27             self.updateDJ(R)
28
29         #  $\bar{g}^i \leftarrow \bar{g}^i + \sum_a \bar{g}^a$ 
30         self.Gbar[i] += self.Gbar[a]
31     self.Gbar = self.Gbar % 2
32
33     # swap  $g^i$  and  $g^k$ ,  $\bar{g}^i$  and  $\bar{g}^k$ 
34     # remember elements are zero-indexed, so we use k-1
35     self.G[[i, self.k-1]] = self.G[[self.k-1, i]]
36     self.Gbar[[i, self.k-1]] = self.Gbar[[self.k-1, i]]
37
38     # update D, J using equations 48, 49 on page 10
39     if not lazy:
40         R = np.identity(self.k)
41         R[[i, self.k-1]] = R[[self.k-1, i]]
42         self.updateDJ(R)
43
44     #  $h \leftarrow h \oplus \beta \cdot g^k$ 
45     self.h = (self.h + beta*self.G[self.k-1]) % 2
46
47     if not lazy:
48         # update Q, D using equations 51, 52 on page 10
49         y = np.zeros(self.k)
50         y[self.k-1] = beta
51         self.updateQD(y)
52
53         self.J = self.J[1:, 1:] # remove last row and column from J
54         self.D = self.D[1:] # remove last element from D
55
56     self.k -= 1
57
58     return "SUCCESS"
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