

$$P(t) = e + dt$$

$$f(p) = 0 \quad f(c + dt) = 0$$

$$\text{Sphere eq: } (x - x_c)^2 + (y - y_c)^2 + (z - z_c)^2 - R^2 = 0$$

$$(P - c) \cdot (P - c) - R^2 = 0$$

$$(e + dt - c)(e + dt - c) - R^2 = 0$$

$$e^2 + e dt - ec + dt^2 + e dt - dtc + c^2 - ec - dtc - R^2 = 0$$

$$e^2 + dt^2 + c^2 + 2edt - 2ec - 2dtc - R^2 = 0$$

$$dt^2 + 2edt - 2cdt + e^2 + c^2 - R^2 = 0 \quad -2ec$$

$$(d \cdot d)t^2 + 2d(e - c)t + e^2 + c^2 - 2ec - R^2 = 0$$

$$a = d^2$$

$$b = 2d(e - c)$$

$$c = e^2 + c^2 - 2ec - R^2$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = x$$

$$\frac{-2d(e - c) \pm \sqrt{(2d(e - c))^2 - 4 \cdot d^2 \cdot (e^2 + c^2 - 2ec - R^2)}}{2 \cdot d^2} = t$$