

```
ics
& (depth < MAXDEPTH)
{
    if (nt < 0)
        nt = inside ? 1 : -1;
    nt = nt / nc; ddn = dot(N, Nt);
    if (ddn < 0)
        cos2t = 1.0f - nnt * nnt;
    else
        cos2t = 1.0f - nnt * nnt;
    D, N );
    if (D < 0)
        D = -D;
    if (a = nt - nc, b = nt + nc,
        at Tr = 1 - (R0 + (1 - R0) *
        Tr) R = (D * nnt - N * (ddn < 0)
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &lightPdf,
    e.x + radiance.y + radiance.z) > 0) && (dot(N, L) > 0)
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;
```

3

Ray Tracing for Games

Dr. Jacco Bikker - IGAD/BUAS, Breda, January 31

Welcome!



Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache

```
ics
& (depth < MAXDEPTH)
{
    if ( ! inside )
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    Tr) R = (D * nnt - N * (ddn * nnt));

    E * diffuse;
    = true;

    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightPdf );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z);
    }

    random walk - done properly, closely following Small's
    (survive)

    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```



Ray Tracing for Games

YOU ARE HERE

GLOBAL GAME JAM

Thursday
09:00 – 14:00

advanced Whitted
audio, AI & physics
faster Whitted
Heaven7

Wednesday
13:00 – 17:00

course intro
LH2
template
Whitted
refactoring
RT-centric games

LAB 1

LAB 2



work @ home

End result day 2:

A solid Whitted-style
ray tracer, as a basis
for subsequent work.

Friday
09:00 – 17:00

optimization
profiling, rules of
engagement
threading

LAB 3



SIMD
applied SIMD
SIMD triangle
SIMD AABB

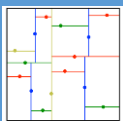
LAB 4

End result day 3:
A 5x faster tracer.

Monday
09:00 – 17:00

acceleration
grid, BVH, kD-tree
SAH
binning

LAB 5



refitting
top-level BVH
threaded building

LAB 6

End result day 4:
A real-time tracer.

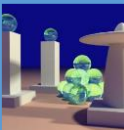
Tuesday
09:00 – 17:00

Monte-Carlo
Cook-style
glossy, AA
area lights, DOF

LAB 7



path tracing



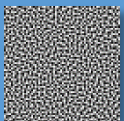
LAB 8

End result day 5:
Cook or Kajiya.

Thursday
09:00 – 17:00

random numbers
stratification
blue noise

LAB 9



importance
sampling
next event
estimation

LAB 10

End result day 6:
Efficiency.

Friday
09:00 – 17:00

future work

LAB 11



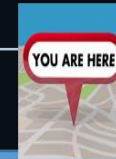
path guiding



LAB 10



End result day 6:
Great product.



Towards the End product:

1. Path tracer that produces pretty images in a few minutes.

You have a clean ray tracer with a solid API, you implemented most or all of the Whitted-style features.

2. Real-time ray tracer on the CPU or GPU.

You have finished the functionality that you want to run in real-time, graphics-wise. Animation is still to be done.

3. Raytraced game or demo.

You have a minimalistic game engine that allows you to build the game, while the engine is being completed.

4. RTX port of an existing game.

You have basic output from the original game engine using the custom ray tracing renderer.

Wednesday
13:00 – 17:00

course intro
LH2
template
Whitted
refactoring
RT-centric games

LAB 1

Thursday
09:00 – 14:00

advanced Whitted
audio, AI & physics
faster Whitted
Heaven7


LAB 2

work @ home

End result day 2:
A solid Whitted-style
ray tracer, as a basis
for subsequent work.

Friday
09:00 – 17:00

optimization
profiling, rules of
engagement
threading



LAB 3

SIMD
applied SIMD
SIMD triangle
SIMD AABB

LAB 4

End result day 3:

A 5x faster tracer.

Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache

```
ics
& (depth < MAXDEPTH)
{
    if (nt > 0)
    {
        nt = inside ? 1 + 1.2f * nt : 1 + 1.2f * nt;
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    Tr) R = (D * nnt - N * (ddn > 0) ? 1 : -1);

    E * diffuse;
    = true;

    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

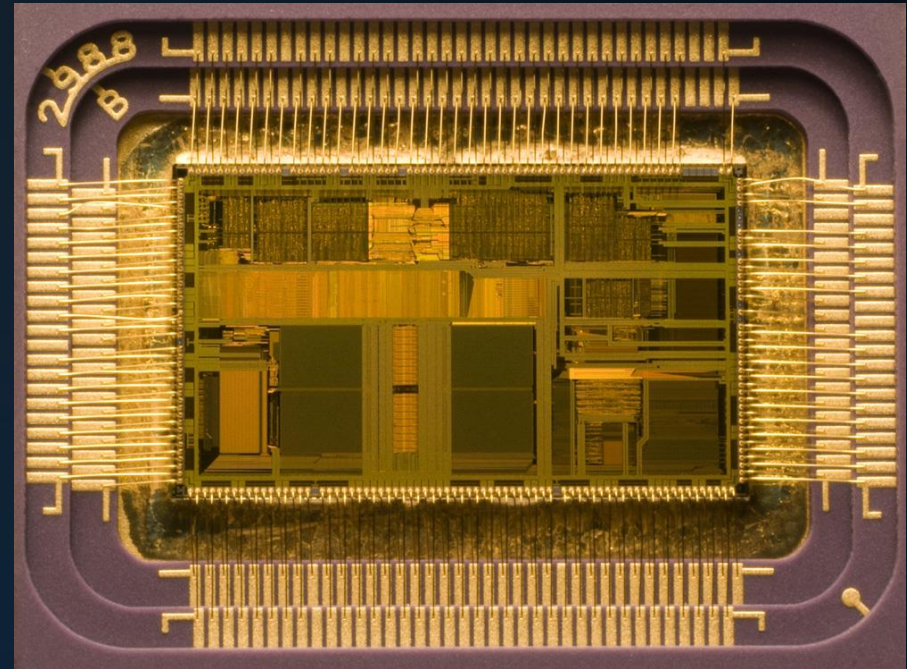
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightPdf,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```



What is optimization?

Think like a CPU

- Instruction pipelines
- Latencies
- Dependencies
- Bandwidth
- Cycles
- Floating point versus integer
- SIMD



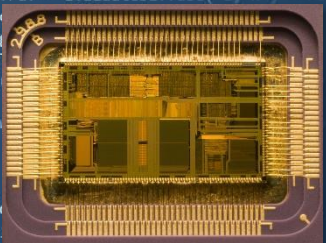
What is optimization?

Work smarter, not harder: algorithm scalability

- Big O
- Research: not reinventing the wheel
- Data characteristics & algorithm choice
- STL, Boost: Trust No One
- As accurate as necessary (but not more)
- Balancing accuracy, speed and memory



```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        ps2t = 1.0f - nnt * ddn;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ps2t);
        (Tr) R = (D * nnt - N * (ddn * ps2t));
    }
    E * diffuse;
    = true;
    {
        refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &align,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psum;
    at3 fa
    at wei
    at cos
    E * (
    random
    ive)
    ;
    at3 br
    survive
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```



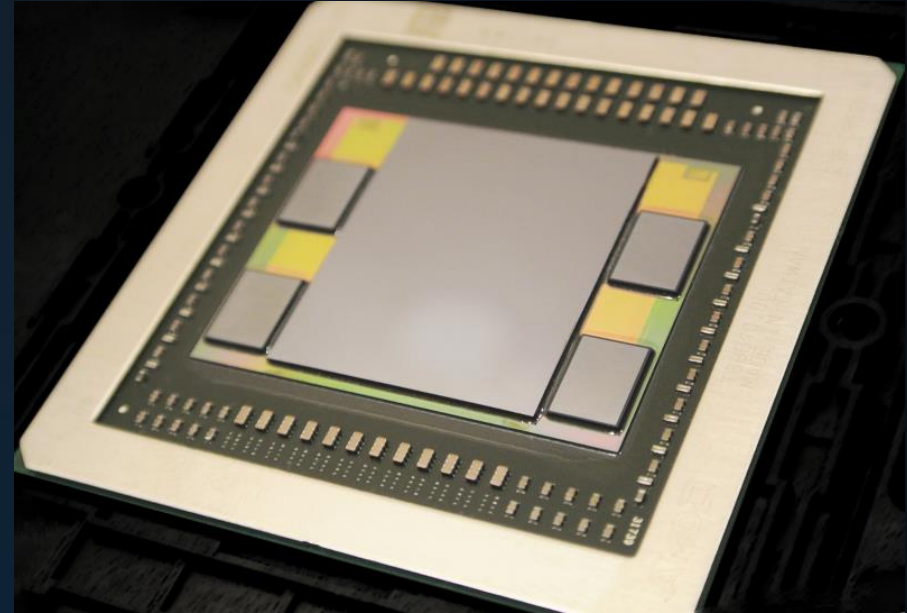
- Instruction pipelines
- Latencies
- Dependencies
- Bandwidth
- Cycles
- Floating point versus integer
- SIMD



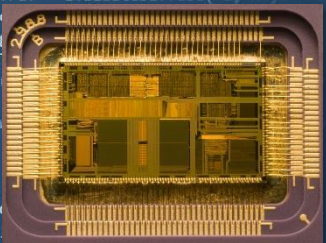
What is optimization?

Memory hierarchy: caches

- Cache architecture
- Cache lines
- Hits, misses and collisions
- Eviction policies
- Prefetching
- Cache-oblivious
- Data-centric programming



```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &align;
    e.x + radiance.y + radiance.z > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psum;
    at3 fa;
    at wei;
    at cos;
    E * (
    random
    ive)
    at3 br;
    survive
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
```



- Instruction pipelines
- Latencies
- Dependencies
- Bandwidth
- Cycles
- Floating point versus integer
- SIMD



- Big O
- Research: not reinventing the wheel
- Data characteristics & algorithm choice
- STL: Trust No One
- As accurate as necessary (but not more)
- Balancing accuracy, speed and memory

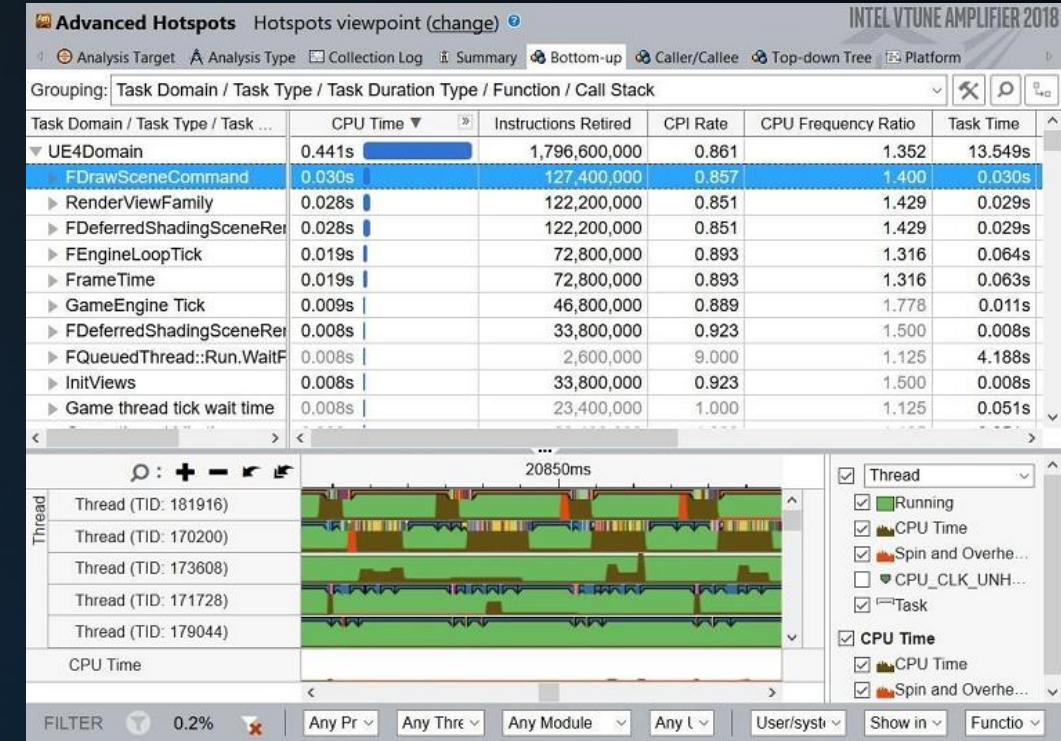


Ray Tracing for Games

What is optimization?

Don't assume, measure

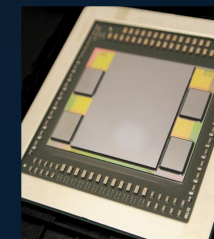
- Profilers
- Interpreting profiling data
- Instrumentation
- Bottlenecks
- Steering optimization effort



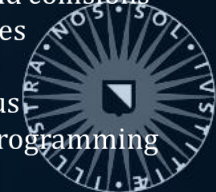
- Instruction pipelines
- Latencies
- Dependencies
- Bandwidth
- Cycles
- Floating point versus integer
- SIMD



- Big O
- Research: not reinventing the wheel
- Data characteristics & algorithm choice
- STL: Trust No One
- As accurate as necessary (but not more)
- Balancing accuracy, speed and memory



- Cache architecture
- Cache lines
- Hits, misses and collisions
- Eviction policies
- Prefetching
- Cache-oblivious
- Data-centric programming



What is optimization? – Project Management

Keeping code maintainable

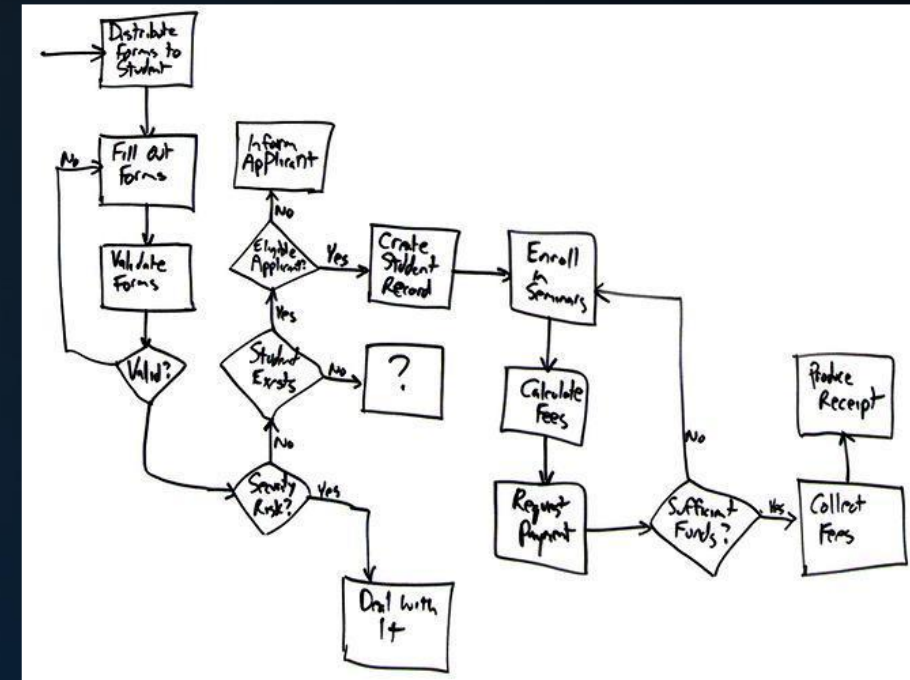
- Pareto principle / 80-20 rule: roughly 80% of the effects are caused by 20% of the causes.
- 1% of the code takes 99% of the time.

“The curse of premature optimization”

- Optimization, rule 1: “Don’t do it”.
- Rule 2 (for experts only!), “Don’t do it yet”.

Optimization as a deliberate process

- *Get predictable gains using a consistent approach.*



What is optimization?

“Perceived Performance”

1. Wait for user input
2. Respond to user input *as quickly as possible*
3. Execute requested operation.



Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache

```
ics
& (depth < MAXDEPTH)
{
    if (nt > 0)
    {
        nt = inside ? 1 + 1.2f * nt : 1 + 1.2f * nt;
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    Tr) R = (D * nnt - N * (ddn > 0) ? 1 : -1);

    E * diffuse;
    = true;

    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightPdf,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)

    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
```



Consistent Approach

- (0.) Determine optimization requirements
1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
5. Parallelize / vectorize / use GPGPU
6. Profile again.
7. Apply low level optimizations to hotspots
8. Repeat step 6 and 7 until time runs out
9. Report.

```
ics
& (depth < MAXDEPTH)
{
    if ( ! inside ) {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    if ( a = nt - nc, b = nt * nc,
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &lightP;
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
```



Consistent Approach

(0.) Determine optimization requirements

- Target hardware (or range of hardware)
- Target performance
- Time available for optimization
- Constraints related to maintainability / portability
- ...

1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
5. Parallelize / vectorize / use GPGPU
6. Profile again.
7. Apply low level optimizations to hotspots
8. Repeat steps 6 and 7 until time runs out
9. Report.

From here on, we will assume that:

- the code is 'done' (feature complete);
- a speed improvement is required;
- we have a finite amount of time for this.



Consistent Approach

```
ics
& (depth < MAXDEPTH)
{
    if (inside) {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    if (a < b) {
        at a = nt - nc; b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn * cos2t));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &lightPos,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Smallwood
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

(0.) Determine optimization requirements

1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
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6. Profile again.
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8. Repeat steps 6 and 7 until time runs out
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Consistent Approach

(0.) Determine optimization requirements

1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
5. Parallelize / vectorize / use GPGPU
6. Profile again.
7. Apply low level optimizations to hotspots

- caching, data-centric programming,
- removing superfluous functionality and precision,
- aligning data to cache lines, vectorization,
- checking compiler output, fixed point arithmetic,
- ...

8. Repeat steps 6 and 7 until time runs out
9. Report.



Ray Tracing for Games

Microsoft Visual Studio (Administrator) window showing the project 'tmpl83.00c' and the 'game.cpp' file. The 'Release' configuration is selected in the top toolbar.

The 'Template Property Pages' dialog is open, showing the 'Configuration: Active(Relase)' and 'Platform: Active(Win32)'. The 'Debug Information Format' is set to 'Program Database (/ZI)'.

The 'game.cpp' file content is visible in the background, showing includes for 'string.h', 'stdlib.h', 'template.h', 'surface.h', and 'game.h', and the 'using namespace Tmpl8;' statement.

The 'Template Property Pages' dialog shows the following settings:

Configuration	Platform
Active(Relase)	Active(Win32)

Additional Include Directories: lib\OpenGL\lib\sdl\include;lib\freeimage;%Additional Include Directories%

Additional #using Directories:

Debug Information Format: Program Database (/ZI)

Common Language RunTime Support: None

Consume Windows Runtime Extension: C7 compatible (/Z7)

Suppress Startup Banner: Program Database (/ZI)

Warning Level: Program Database for Edit And Continue (/ZI)

Treat Warnings As Errors: <inherit from parent or project defaults>

SDL checks:

Multi-processor Compilation:

Debug Information Format: Specifies the type of debugging information generated by the compiler. You must also change linker settings appropriately to match. (/Z7, /Zd, /ZI, /Zi)

Buttons: OK, Cancel, Apply

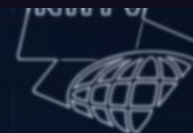


Ray Tracing for Games

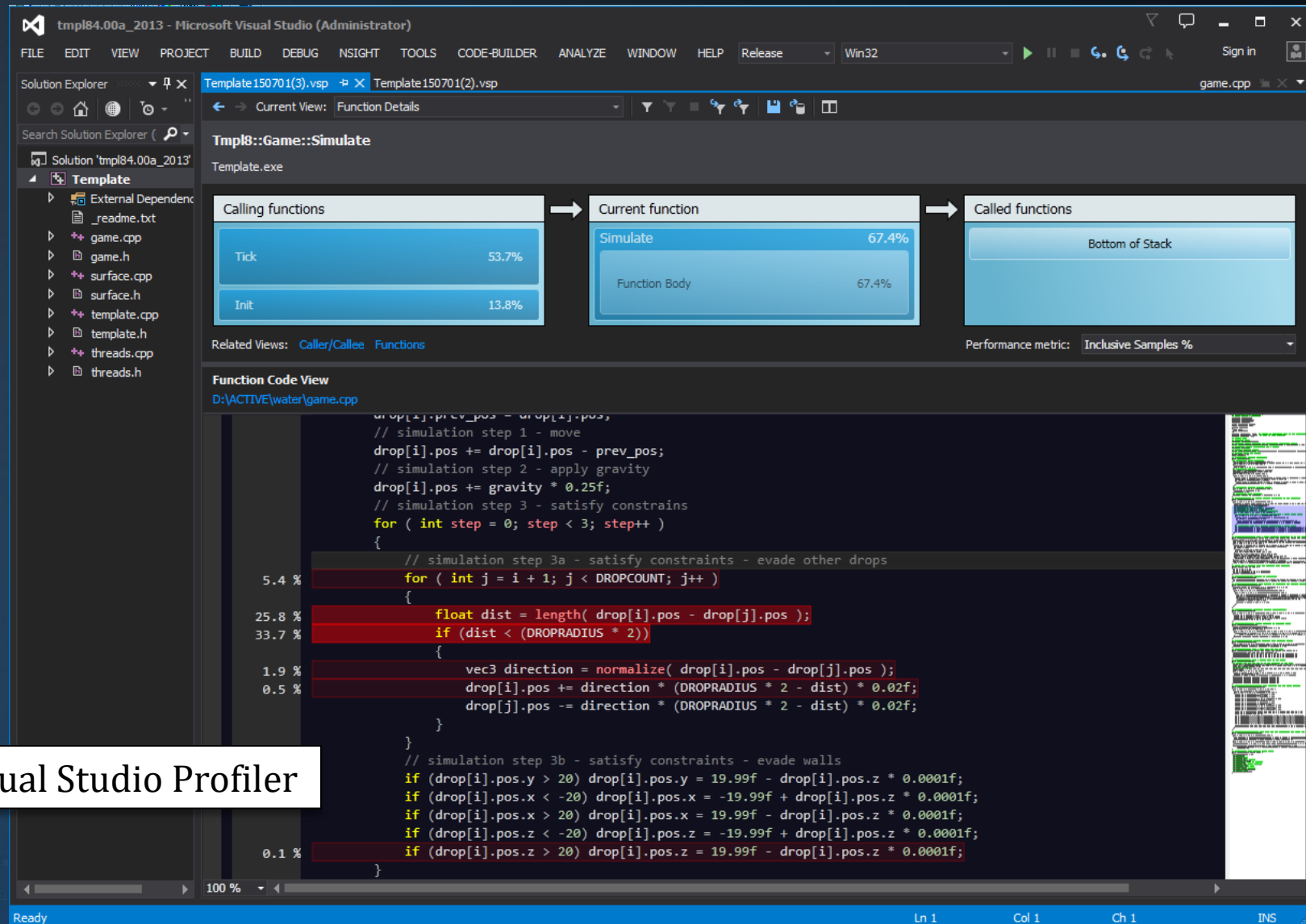
The screenshot shows the Microsoft Visual Studio (Administrator) interface. The title bar indicates the project is 'tmpl84.00a_2013'. The 'Performance and Diagnostics' window is open, displaying the 'Performance Wizard -- Page 1 of 3'. The wizard prompts the user to 'Specify the profiling method' and lists four options:

- ☒ **CPU sampling (recommended)**
Monitor CPU-bound applications with low overhead
- ☐ **Instrumentation**
Measure function call counts and timing
- ☐ **.NET memory allocation**
Track managed memory allocation
- ☐ **Resource contention data (concurrency)**
Detect threads waiting for other threads

The background shows the 'Solution Explorer' with a project named 'tmpl84.00a_2' containing files like 'game.cpp', 'game.h', 'surface.cpp', 'surface.h', 'template.cpp', 'template.h', 'threads.cpp', and 'threads.h'. The 'Code' window displays C++ code for a ray tracer, including functions for ray-sphere intersection and radiance calculation.



Ray Tracing for Games



Ray Tracing for Games

Very Sleepy CS - C:\Users\Jacco\AppData\Local\Temp\F8AF.tmp

File View Help

Functions

Name	Exclu...	Inclusive	% Exclusive	% Inclusive	Module	Source File
Tmpl8::Game::Simulate		9.47s	62.76%	62.76%	water	d:\water\game...
Tmpl8::Game::SmoothWater		2.01s	13.34%	13.34%	water	d:\water\game...
Tmpl8::Game::DrawTriangle		1.33s	8.80%	8.80%	water	d:\water\game...
Tmpl8::Game::RenderZSprites		1.19s	7.86%	7.86%	water	d:\water\game...
Tmpl8::Game::RenderWaterSurface		0.43s	2.87%	11.67%	water	d:\water\game...
Tmpl8::Surface::Clear		0.11s	0.75%	0.75%	water	d:\water\surfa...
Tmpl8::Game::RenderDebugInfo		0.03s	0.19%	0.32%	water	d:\water\game...
Tmpl8::Surface::Plot		0.02s	0.13%	0.13%	water	d:\water\surfa...
Tmpl8::Game::DownScale		0.02s	0.10%	0.10%	water	d:\water\game...
Tmpl8::Game::TimeSmooth		0.00s	0.02%	0.02%	water	d:\water\game...
Tmpl8::Surface::AddLine		0.00s	0.01%	0.01%	water	d:\water\surfa...
swap		0.00s	0.01%	1.66%	water	d:\water\templa...
[006ADC00]		0.00s	0.00%	0.01%	water	
__tmainCRTStartup		0.00s	0.00%	99.93%	water	f:\dd\vctools\cr...
SDL_main		0.00s	0.00%	99.57%	water	d:\water\templa...
Tmpl8::Game::Tick		0.00s	0.00%	91.96%	water	d:\water\game...
Tmpl8::Game::DrawBoat		0.00s	0.00%	0.01%	water	d:\water\game...
Tmpl8::Game::GlowLine		0.00s	0.00%	0.01%	water	d:\water\game...

Source Log

```
for ( int step = 0; step < 3; step++ )
{
    // simulation step 3a - satisfy constraints - evade other drops
    for ( int j = i + 1; j < DROPCOUNT; j++ )
    {
        float dist = (drop[i].pos - drop[j].pos).Length();
        if (dist < (DROPRADIUS * 2))
        {
            vector3 direction = (drop[i].pos - drop[j].pos).Normalized;
            drop[i].pos += direction * (DROPRADIUS * 2 - dist) * 0.02f;
            drop[j].pos -= direction * (DROPRADIUS * 2 - dist) * 0.02f;
        }
    }
    // simulation step 3b - satisfy constraints - evade walls
    if (drop[i].pos.y > 20) drop[i].pos.y = 19.99f - drop[i].pos.z * 0.0001f;
    if (drop[i].pos.x < -20) drop[i].pos.x = -19.99f + drop[i].pos.z * 0.0001f;
    if (drop[i].pos.x > 20) drop[i].pos.x = 19.99f - drop[i].pos.z * 0.0001f;
    if (drop[i].pos.z < -20) drop[i].pos.z = -19.99f + drop[i].pos.x * 0.0001f;
    if (drop[i].pos.z > 20) drop[i].pos.z = 19.99f - drop[i].pos.x * 0.0001f;
}
```

Source file: d:\water\game.cpp Line 97

Averages Call Stacks Filters

Called From

Name	Samples	% Calls	Module
Tmpl8::Game::Tick	8.70s	91.88%	water
Tmpl8::Game::Init	0.77s	8.12%	water

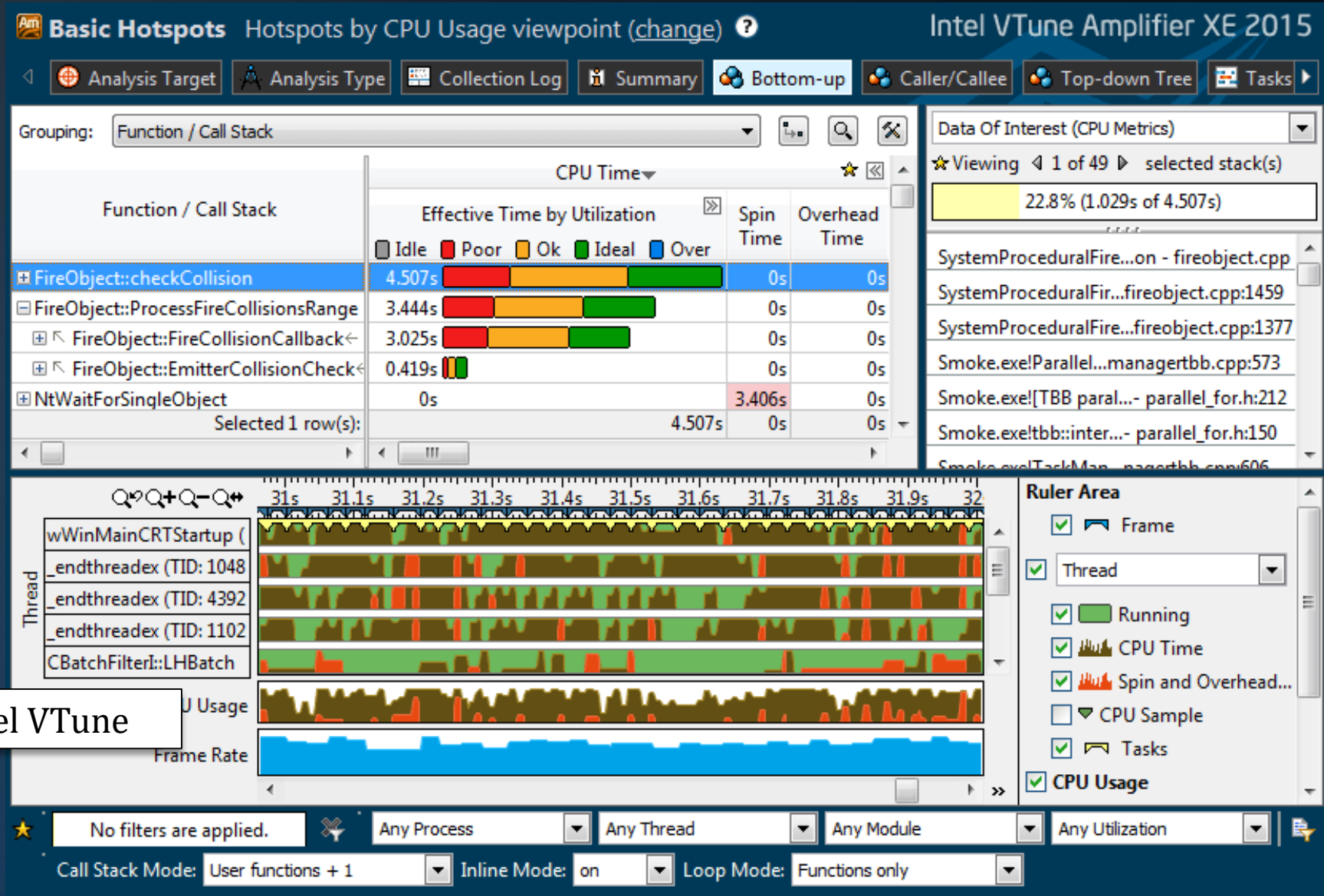
Child Calls

Name	Samples	% Calls	Module
------	---------	---------	--------

VerySleepy

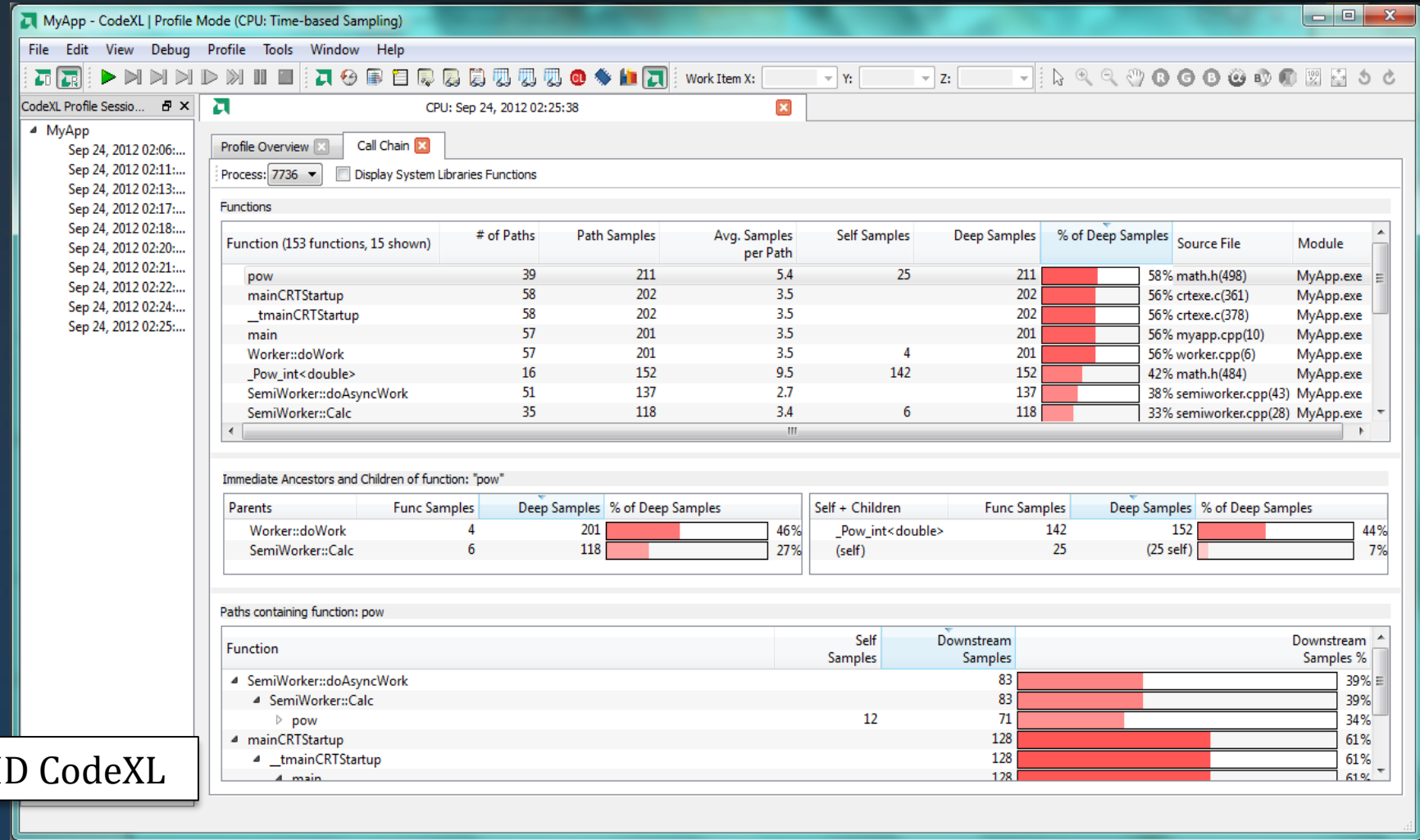


Ray Tracing for Games



Ray Tracing for Games

AMD CodeXL



Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache

```
ics
& (depth < MAXDEPTH))
{
    if (nt < 0)
        nt = inside ? 1 : 1.01;
    nt = nt / nc; ddn = ddn * nt;
    rnt = 1.0f - nnt * nnt;
    float r = 0, NdotL;
    do {
        r = rand();
        NdotL = sqrt(r);
    } while (NdotL < 0);
    float a = nt - nc, b = nt + nc;
    float Tr = 1 - (R0 + (1 - R0) * r);
    if (Tr) R = (D * nnt - N * (ddn < 0 ? 1 : -1));
    else {
        E * diffuse;
        = true;
    }
    if (refl + refr) && (depth < MAXDEPTH))
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    if (depth < MAXDEPTH)
    {
        survive = SurvivalProbability( diffuse );
        estimation - doing it properly, closely following
        if;
        radiance = SampleLight( &rand, I, &L, &lightPdf,
            e.x + radiance.y + radiance.z) && (dot(N, L) > 0);
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    (survive)
};
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
```



What is the 'cost' of a multiply?

```
starttimer();  
float x = 0;  
for( int i = 0; i < 1000000; i++ ) x *= y;  
stoptimer();
```

- Actual measured operations:
 - timer operations;
 - initializing 'x' and 'i';
 - comparing 'i' to 1000000 (x 1000000);
 - increasing 'i' (x 1000000);
 - jump instruction to start of loop (x 1000000).

■ Compiler outsmarts us!

- No work at all unless we use x
- x += 1000000 * y

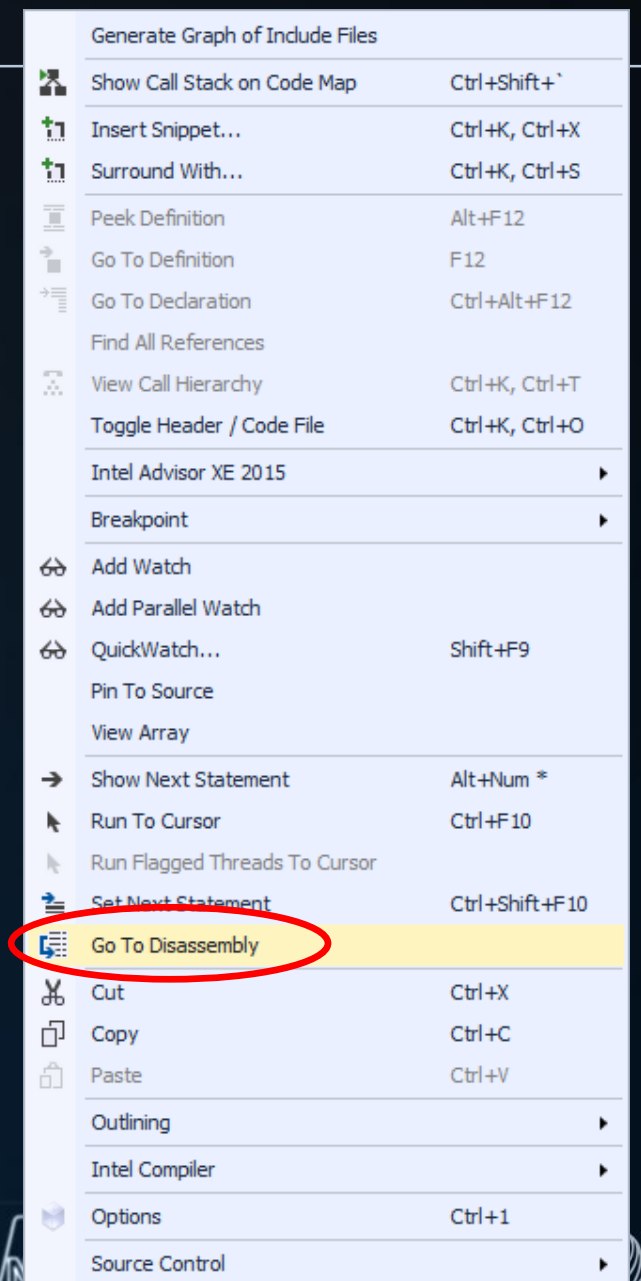
Better solution:

- Create an arbitrary loop
- Measure time with and without the instruction we want to time



What is the 'cost' of a multiply?

```
float x = 0, y = 0.1f;
unsigned int i = 0, j = 0x28929227;
for( int k = 0; k < ITERATIONS; k++ )
{
    // ensure we feed our line with fresh data
    x += y, y *= 1.01f;
    // integer operations to free up fp execution units
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    // operation to be timed
    if (with) x *= y;
    // integer operations to free up fp execution units
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    dummy = x + (float)i;
}
```



Ray Tracing for Games

x86 assembly in 5 minutes

Modern CPUs still run x86 machine code, based on Intel's 1978 8086 processor. The original processor was 16-bit, and had 8 'general purpose' 16-bit registers*:

AX ('accumulator register')	AH, AL (8-bit)	EAX (32-bit)	RAX (64-bit)
BX ('base register')	BH, BL	EBX	RBX
CX ('counter register')	CH, CL	ECX	RCX
DX ('data register')	DH, DL	EDX	RDX
BP ('base pointer')		EBP	RBP
SI ('source index')		ESI	RSI
DI ('destination index')		EDI	RDI
SP ('stack pointer')		ESP	RSP
		st0..st7	R8..R15
		XMM0..XMM7	XMM0..XMM15
			YMM0..YMM15
			ZMM0..ZMM31

* More info: <http://www.swansontec.com/sregisters.html>



x86 assembly in 5 minutes:

Typical assembler:

loop:

mov eax, [0x1008FFA0]	// read from address into register
shr eax, 5	// shift eax 5 bits to the right
add eax, edx	// add registers, store in eax
dec ecx	// decrement ecx
jnz loop	// jump if not zero
fld [esi]	// load from address [esi] onto FPU
fld st0	// duplicate top float
faddp	// add top two values, push result

More on x86 assembler: <http://www.cs.virginia.edu/~evans/cs216/guides/x86.html>

A bit more on floating point assembler: https://www.cs.uaf.edu/2007/fall/cs301/lecture/11_12_floating_asm.html

Ray Tracing for Games

What is the 'cost' of a multiply?

```
float x = 0, y = 0.1f;
unsigned int i = 0, j = 0x28929227;
for( int k = 0; k < ITERATIONS; k++ )
{
    // ...
    x += y, y *= 1.01f;
    // ...
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    // ...
    if (with) x *= y;
    // ...
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    // ...
    dummy = x + (float)i;
}
```

```
fldz
xor ecx, ecx
fld dword ptr ds:[405290h]
mov edx, 28929227h
fld dword ptr ds:[40528Ch]
push esi
mov esi, 0C350h = 50000
```

```
add ecx, edx
mov eax, 91D2A969h =  $\frac{2^{46}}{28763}$  (!!)
```

```
xor edx, 17737352h
```

```
shr ecx, 1
```

```
mul eax, edx
```

```
fld st(1)
```

```
faddp st(3), st
```

```
mov eax, 91D2A969h
```

```
shr edx, 0Eh
```

```
add ecx, edx
```

```
fmul st(1), st
```

```
xor edx, 17737352h
```

```
shr ecx, 1
```

```
mul eax, edx
```

```
shr edx, 0Eh
```

```
dec esi
```

```
jne tobetimed<0>+1Fh
```


- Compiler reorganizes code
- Compiler cleverly evades division
- Loop counter *decreases*
- Presence of integer instructions affects timing
(*to the point where the mul is free*)

- It is really hard to measure the cost of a line of code.

```

MAXDEPTH)

survive = SurvivalProbability( diffuse, L )
// estimation - doing it properly, closely following Maxwell's
// distribution
if( ! survive )
    radiance = SampleLight( &rand, I, &L, &lightDir );
radiance.x + radiance.y + radiance.z > 0) && (data.N < MAXDEPTH))
{
    w = true;
    brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    weight = Mis2( directPdf, brdfPdf );
    cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z);
} // random walk - done properly, closely following Maxwell's distribution
survive)

//
};
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
//
tion = true;
```

is really hard to measure the cost of a line of code.

Ray Tracing for Games

What is the ‘cost’ of a single instruction?

Cost is highly dependent on the surrounding instructions, and many other factors. However, there is a ‘cost ranking’:

<< >>

bit shifts

+ - & | ^

simple arithmetic, logical operands

*

multiplication

/

division

sqrt

sin, cos, tan, pow, exp

This ranking is generally true for any processor (including GPUs).

Common Opportunities in Low-level Optimization

RULE 1: Avoid Costly Operations

- Replace multiplications by bitshifts, when possible
- Replace divisions by (reciprocal) multiplications
- Avoid sin, cos, sqrt

```
ics
& (depth < MAXDEPTH))
{
    if (nt > 0)
    {
        nt = inside ? 1 : 1.0f - nt;
        nt = nt / nc; ddn = ddn * nt;
        r2 = 1.0f - nnt * nnt;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * r2);
        Tr) R = (D * nnt - N * (ddn * nnt +
        E * diffuse;
        = true;
    }
    else
    {
        refl + refr)) && (depth < MAXDEPTH))
        D, N );
        refl * E * diffuse;
        = true;
    }
}

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following Small's
if;
radiance = SampleLight( &rand, I, &L, &lightPdf );
e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0)
{
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance.x +
    random walk - done properly, closely following Small's
    vive)
};
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
```

Common Opportunities in Low-level Optimization

RULE 2: Precalculate

- Reuse (partial) results
- Adapt previous results (interpolation, reprojection, ...)
- Loop hoisting
- Lookup tables

```
ics
& (depth < MAXDEPTH) {
    if ( ! inside ) continue;
    nt = nt / nc, ddn = ddn * nc;
    ps2t = 1.0f - nnt * ddn;
    D, N );
    )
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * a);
    (Tr) R = (D * nnt - N * (ddn * a +
    E * diffuse;
    = true;
    -
    efl + refr)) && (depth < MAXDEPTH) {
    D, N );
    -refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &lightDir,
    e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0) {
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
```


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Journal compilation © 2006 Blackwell Publishing Ltd

```

k (depth < MAXDEPTH) {
    int nc = inside ? 1 : 0; // outside?
    nt = nt / nc; ddn = dot(N, D);
    float r0 = 0.7f + 0.3f * ddn; // Russian roulette
    float ps2t = 1.0f - nnt * r0; // Russian roulette
    if (D > N) {
        R = (D * nnt - N * (ddn * r0));
    } else {
        R = (-D * nnt - N * (ddn * r0));
    }
    E * diffuse;
    bool refl = true;
    if (!refl || (depth == MAXDEPTH)) {
        return Color(0, 0, 0);
    }
    D = N;
    refl * E * diffuse;
    bool w = true;
    if (!w || (depth == MAXDEPTH)) {
        survive = SurvivalProbability(diffuse);
        estimation - doing it properly, closely following survival;
    }
    radiance = SampleLight(&rand, I, &L, alignPdf, diffuse, x, y, z);
    float weight = Mis2(directPdf, brdfPdf);
    cosThetaOut = dot(N, L);
    E * ((weight * cosThetaOut) / directPdf) * (radiance);
}

// random walk - done properly, closely following survival
void RandomWalk(SampleLight *sl, Ray *r, int depth, int maxDepth) {
    if (depth >= maxDepth) {
        return;
    }
    at3 brdf = SampleDiffuse(diffuse, N, r1, r2, &R, &pdf);
    survive;
    pdf;
    n = E * brdf * (dot(N, R) / pdf);
    sion = true;

```

Common Opportunities in Low-level Optimization

RULE 4: Avoid Conditional Branches

- if, while, ?, MIN/MAX
- Try to split loops with conditional paths into multiple unconditional loops
- Use lookup tables to prevent conditional code
- Use loop unrolling
- If all else fails: make conditional branches predictable

```
ics
& (depth < MAXDEPTH)
{
    if (nt > 0)
    {
        nt = inside ? 1 : 1.0f - nt;
        nt = nt / nc; ddn = ddn * nt;
        ps2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        (Tr) R = (D * nnt - N * (ddn > 0));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        -refl * E * diffuse;
        = true;
    }
}

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following Small's
if;
radiance = SampleLight( &rand, I, &L, &lightPdf );
e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0)
{
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z)
}

random walk - done properly, closely following Small's
ive)
{
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;
}
```

Common Opportunities in Low-level Optimization

RULE 5: Early Out

```
char a[] = "abcdfghijklmnopqrstuvwxyz";
char c = 'p';
int position = -1;
for ( int t = 0; t < strlen( a ); t++ )
{
    if (a[t] == c)
    {
        position = t;
    }
}
```

```
char a[] = "abcdfghijklmnopqrstuvwxyz";
char c = 'p';
int position = -1, len = strlen( a );
for ( int t = 0; t < len; t++ )
{
    if (a[t] == c)
    {
        position = t;
        break;
    }
}
```

Common Opportunities in Low-level Optimization

RULE 6: Use the Power of Two

- A multiplication / division by a power of two is a (cheap) bitshift
- A 2D array lookup is a multiplication too – make ‘width’ a power of 2
- Dividing a circle in 256 or 512 works just as well as 360 (but it’s faster)
- Bitmasking (for free modulo) requires powers of 2

1-2-4-8-16-32-64-128-256-512-1024-2048-4096-8192-16384-32768-65536

Be fluent with powers of 2 (up to 2^{16});

learn to go back and forth for these: $2^9 = 512 = 2^9$.

Practice counting from 0..31 on one hand in binary.

Common Opportunities in Low-level Optimization

RULE 7: Do Things Simultaneously

- Use those cores
- An integer holds four bytes; use these for instruction level parallelism
- More on this later.

```
ics
& (depth < MAXDEPTH)) {
    if (nt > 0) {
        nt = inside ? 1 + 1.0f / nt : 1.0f / nt;
        nt = nt / nc; ddn = ddn * nt;
        ps2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    Tr) R = (D * nnt - N * (ddn * nnt));
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)) {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    if;
    radiance = SampleLight( &rand, I, &L, &lightPdf );
    e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0) {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z);
    }
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;
}
```

Common Opportunities in Low-level Optimization

1. Avoid Costly Operations
2. Precalculate
3. Pick the Right Data Type
4. Avoid Conditional Branches
5. Early Out
6. Use the Power of Two
7. Do Things Simultaneously

```
ics
& (depth < MAXDEPTH)
{
    if ( ! inside ) return 0;
    nt = nt / nc; ddn = ddn * ddn;
    float r2t = 1.0f - nnt * ddn;
    float D, N );
    )
    {
        float a = nt - nc, b = nt * nc;
        float Tr = 1 - (R0 + (1 - R0) * r2t);
        float R = (D * nnt - N * (ddn * r2t));
        if (R < Tr)
        {
            E * diffuse;
            = true;
        }
        else
        {
            refl + refr)) && (depth < MAXDEPTH)
            {
                D, N );
                refl * E * diffuse;
                = true;
            }
        }
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &lightDir );
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiant
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache

```
ics
& (depth < MAXDEPTH))
{
    if (nt > 0)
    {
        nt = inside ? 1 + 1.2f * nt : 1 + 1.2f * nt;
        nt = nt / nc; ddn = ddn * nt;
        cos2t = 1.0f - nnt * nnt;
        D, N );
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    Tr) R = (D * nnt - N * (ddn > 0) ? 1 : -1);

    E * diffuse;
    = true;

    -
    refl + refr)) && (depth < MAXDEPTH))
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightPdf,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```



Ray Tracing for Games

Feeding the Beast

Let's assume our CPU runs at 4Ghz.

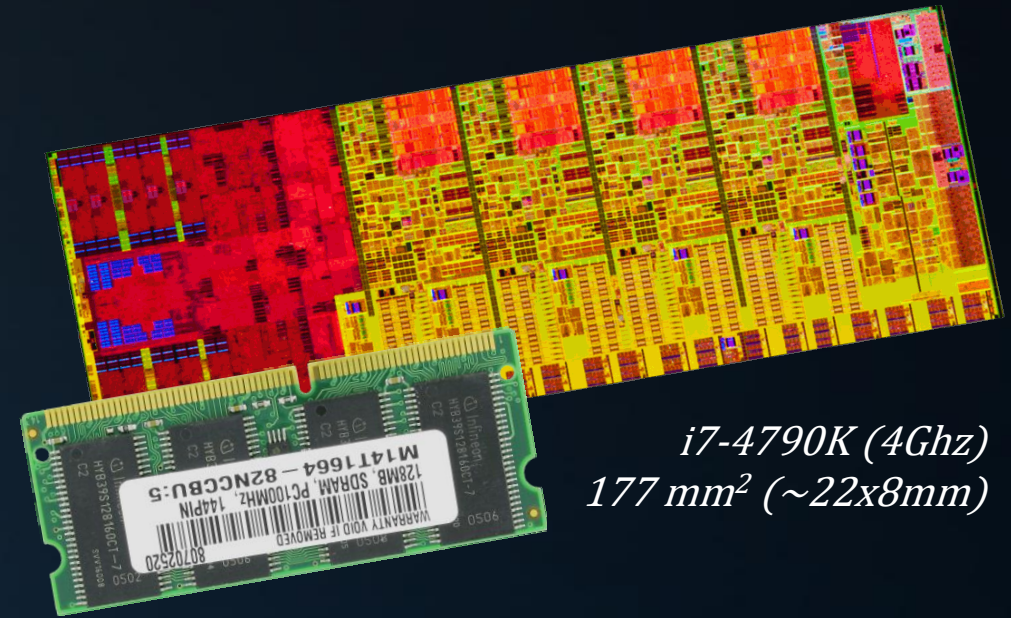
What is the maximum physical distance between memory and CPU if we want to retrieve data every cycle?

Speed of light (vacuum): 299,792,458 m/s

Per cycle: ~ 0.075 m

→ ~ 3.75 cm back and forth.

In other words: we cannot physically query RAM fast enough to keep a CPU running at full speed.



i7-4790K (4Ghz)
 177 mm^2 ($\sim 22 \times 8 \text{ mm}$)



Feeding the Beast

Sadly, we can't just divide by the physical distance between CPU and RAM to get the cycles required to query memory.

Factors include (stats for DDR4-3200/PC4-25600):

- RAM runs at a much lower clock speed than the CPU
 - 25600 here means: theoretical bandwidth in MB/s
 - 3200 is the number of transfers per second (1 transfer=64bit)
 - We get two transfers per cycle, so actual I/O clock speed is 1600Mhz
 - DRAM cell array clock is ~1/4th of that: 400Mhz.
- Latency between query and response: 20-24 cycles.



Feeding the Beast

Sadly, we can't just divide by the physical distance between CPU and RAM to get the cycles required to query memory.

Additional delays may occur when:

- Other devices than the CPU access RAM;
- DRAM must be refreshed every 64ms due to leakage.

For a processor running at 2.66GHz, latency is roughly 110-140 CPU cycles.

Details in: “What Every Programmer Should Know About Memory”, chapter 2.



Feeding the Beast

“We cannot physically query RAM fast enough to keep a CPU running at full speed.”

How do we overcome this?

We keep a copy of frequently used data in fast memory, close to the CPU: the *cache*.

```
ics
& (depth < MAXDEPTH)
{
    if ( ! inside ) return 0;
    nt = nt / nc; ddn = ddn * ddn;
    ps2t = 1.0f - nnt * nnt;
    D, N );
    )
}
```

```
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
```

```
E * diffuse;
= true;
```

```
-
efl + refr)) && (depth < MAXDEPTH)
```

```
D, N );
-refl * E * diffuse;
= true;
```

```
MAXDEPTH)
```

```
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;
```

```
radiance = SampleLight( &rand, I, &L, &lightDir,
e.x + radiance.y + radiance.z) > 0) && (dot(N, L) > 0)
{
```

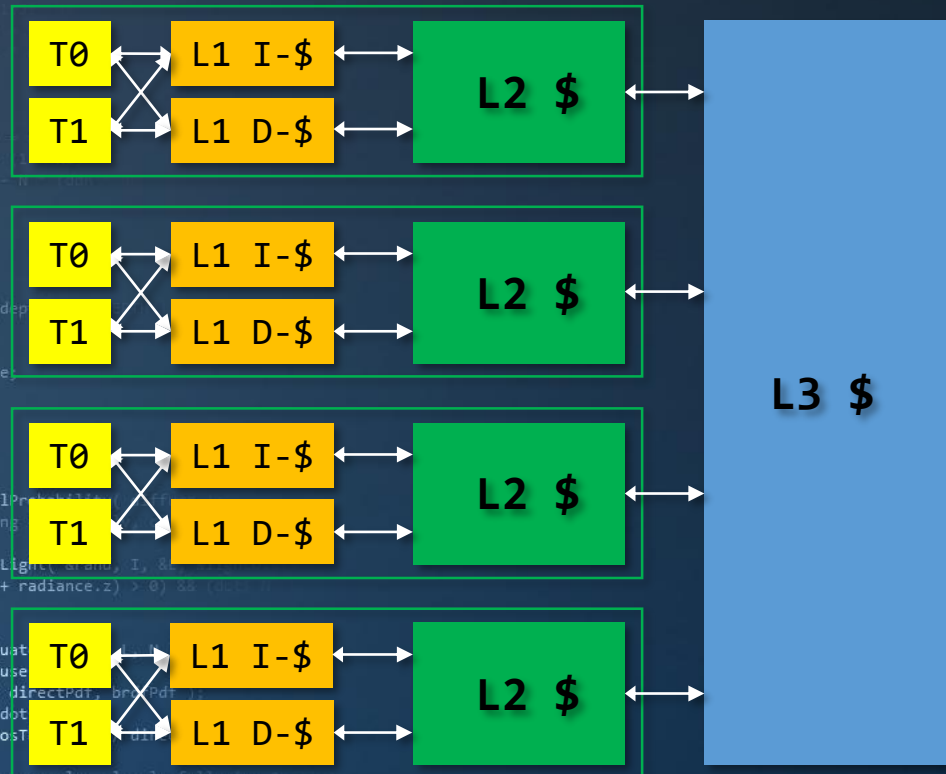
```
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
```

```
random walk - done properly, closely following Small's
ive)
```

```
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
```



The Memory Hierarchy – Core i7-9xx (4 cores)



32KB I / 32KB D per core

256KB per core

8MB

x GB

registers:
0 cycles

level 1 cache: 4 cycles

level 2 cache: 11 cycles

level 3 cache: 39 cycles

RAM: 100+ cycles



Caches and Optimization

Considering the cost of RAM vs L1\$ access, it is clear that the cache is an important factor in code optimization:

- Fast code communicates mostly with the caches
- We still need to get data into the caches
- But ideally, only once.

Therefore:

- The working set must be small;
- Or we must maximize *data locality*.



Data Locality

Wikipedia:

Temporal Locality – “If at one point in time a particular memory location is referenced, then it is likely that the same location will be referenced again in the near future.”

Spatial Locality – “If a particular memory location is referenced at a particular time, then it is likely that nearby memory locations will be referenced in the near future.”

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - ddn;
        D, N );
        R = (D
        at a = nt -
        at Tr = 1 -
        Tr) R = (D
        E * diffuse
        = true;
        -
        refl + refr)
        D, N );
        refl * E * diffuse;
        = true;
        MAXDEPTH)
        survive = SurvivalProbability( diffuse );
        estimation - doing it properly, closely following
        if;
        radiance = SampleLight( &rand, I, &L, &lightP,
        e.x + radiance.y + radiance.z) > 0) && (out.x +
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
        random walk - done properly, closely following Smallwood
        vive)
        ;
        at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
        survive;
        pdf;
        n = E * brdf * (dot( N, R ) / pdf);
        sion = true;
```



* More info: <http://gameprogrammingpatterns.com/data-locality.html>



Data Locality

How do we increase data locality?

Linear access – Sometimes as simple as swapping for loops *

Tiling – Example of working on a small subset of the data at a time.

Streaming – Operate on/with data until done.

Reducing data size – Smaller things are closer together.

How do trees/linked lists/hash tables fit into this?

* For an elaborate example see <https://www.cs.duke.edu/courses/cps104/spring11/lects/19-cache-sw2.pdf>



Two more issues:

1. Cache deals in lines of 64 bytes.

2. Mind ‘false sharing’.

```
ics  
& (depth < MAXDEPTH))
```

```
nt = inside ? 1 : 1.2f; // inside is darker  
nt = nt / nc; ddn = dot(N, D);  
cos2t = 1.0f - nnt * nnt;  
D, N );  
0)
```

```
at a = nt - nc, b = nt + nc;  
at Tr = 1 - (R0 + (1 - R0) * a);  
Tr) R = (D * nnt - N * (ddn < 0) * b
```

```
E * diffuse;  
= true;
```

```
-  
efl + refr)) && (depth < MAXDEPTH))
```

```
D, N );  
refl * E * diffuse;  
= true;
```

```
MAXDEPTH)
```

```
survive = SurvivalProbability( diffuse );  
estimation - doing it properly, closely following  
df;
```

```
radiance = SampleLight( &rand, I, &L, &lightPdf );  
e.x + radiance.y + radiance.z) > 0) && (dot(N, L) < 0)
```

```
w = true;  
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;  
at3 factor = diffuse * INVPI;  
at weight = Mis2( directPdf, brdfPdf );  
at cosThetaOut = dot( N, L );  
E * ((weight * cosThetaOut) / directPdf) * (radiance
```

```
random walk - done properly, closely following Small's  
vive)
```

```
;  
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );  
survive;  
pdf;  
n = E * brdf * (dot( N, R ) / pdf);  
sion = true;
```



How to Please the Cache

Or: “how to evade RAM”

1. Keep your data in registers

Use fewer variables

Limit the scope of your variables

Pack multiple values in a single variable

Use floats and ints (they use different registers)

Compile for 64-bit (more registers)

Arrays will never go in registers

Unions will never go in registers

Liefde is...



... hem het cadeau geven
dat hij écht wil.



How to Please the Cache

Or: “how to evade RAM”

2. Keep your data local

Read sequentially

Keep data small

Use tiling / Morton order

Fetch data once, work until done (streaming)

Reuse memory locations

Liefde is...



... hem het cadeau geven
dat hij écht wil.



How to Please the Cache

Or: “how to evade RAM”

3. Respect cache line boundaries

Use padding if needed

Don't pad for sequential access

Use aligned malloc / __declspec align

Assume 64-byte cache lines

Liefde is...



... hem het cadeau geven
dat hij écht wil.



How to Please the Cache

Or: “how to evade RAM”

4. Advanced tricks

Prefetch

Use a prefetch thread (theoretical...)

Use *streaming writes*

Separate mutable / immutable data

Liefde is...



... hem het cadeau geven
dat hij écht wil.



Or: “how to evade RAM”

Use the profiler!



Agenda:

- State of Affairs
- Optimization Introduction
- Profiling
- Low-level: Rules of Engagement
- The Cache



Ray Tracing for Games



GLOBAL GAME JAM

Thursday
09:00 – 14:00

advanced Whitted
audio, AI & physics
faster Whitted
Heaven7

Friday
09:00 – 17:00

optimization
profiling, rules of
engagement
threading

Monday
09:00 – 17:00

acceleration
grid, BVH, kD-tree
SAH
binning

Tuesday
09:00 – 17:00

Monte-Carlo
Cook-style
glossy, AA
area lights, DOF

Thursday
09:00 – 17:00

random numbers
stratification
blue noise

Friday
09:00 – 17:00

future work

Wednesday
13:00 – 17:00

course intro
LH2
template
Whitted
refactoring
RT-centric games

LAB 1

LAB 2



work @ home

End result day 2:

A solid Whitted-style
ray tracer, as a basis
for subsequent work.

LAB 3

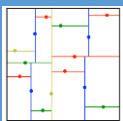


SIMD
applied SIMD
SIMD triangle
SIMD AABB

LAB 4

End result day 3:
A 5x faster tracer.

LAB 5



refitting
top-level BVH
threaded building

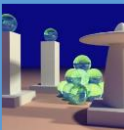
LAB 6

End result day 4:
A real-time tracer.

LAB 7



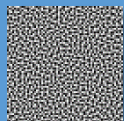
path tracing



LAB 8

End result day 5:
Cook or Kajiya.

LAB 9



importance
sampling
next event
estimation

LAB 10

End result day 6:
Efficiency.

LAB 11



path guiding



LAB 10

End result day 6:
Great product.



Take some time to speed up your ray tracer.

Low level:

Don't do more sqrt/sin/pow than you absolutely have to.

Don't trust stl, write your own code.

Limit conditionals.

Don't write values that you will later overwrite.

Rule of thumb: a single-threaded ray tracer for 3 spheres and a plane runs at 30+fps.

Cache / memory:

Reduce the amount of data you touch

- Don't new/delete anything after initialization.

- Reuse the ray.

Improve data locality

- Operate on tiles.

General guidelines:

Clean code is fast code.

It can always be made faster.

Speedups do not add up, they multiply.

End of PART 3.

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 1.01 - 0.99 * nt)
    {
        nt = nt / nc; ddn = ddn * nc;
        r2s2t = 1.0f - nnt * nnt;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * r2s2t);
        Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    if;
    radiance = SampleLight( &rand, I, &L, &lightDir );
    e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0)
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

