

Assignment 2 – Antonin Beranger

Income distribution (ECON 473)

Question 1:

1982 – 1990:

- *Total Income: TOTINC
- *After-tax income: INCAFTTX
- *Wages and Salaries: WAGSAL
- *Hours worked: HRSWRK
- *Weeks worked: WKSWRK
- *Education: EDUC
- *Age: AGE
- *Gender: SEX
- *WEIGHTS: WEIGHT

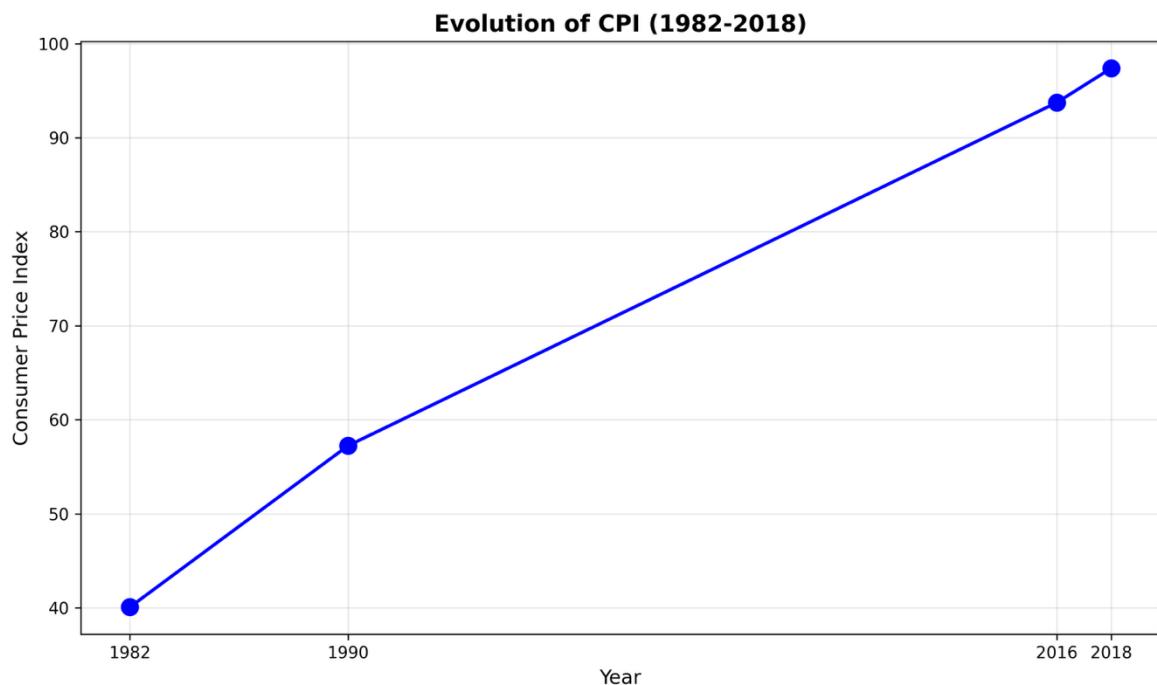
2016-2018:

- *Total Income: TTINC
- *After-tax income: ATINC
- *Wages and Salaries: WGSAL
- *Hours worked: USHRWK
- *Weeks worked: WKSEM
- *Education: HLEV2G
- *Age: AGEGP
- *Gender: SEX
- *WEIGHTS: FWEIGHT

Hourly wage:

→ `df['hourly_wage'] = df[wage_var] / (df[hours_var] * df[weeks_var])`

Question 2:



Real hourly wage in 2020 \$:

- `cpi = {1982: 40.07, 1990: 57.23, 2016: 93.72, 2018: 97.37}`
- for `y`, `df` in `datasets.items()`:
- `df['hourly_real_wage'] = (df['hourly_wage'] / cpi[y]) * 100`

Question 3:

```
#question 3 - sample selection and replication of table 1
unfiltered_datasets = {year: df.copy() for year, df in datasets.items()}

min_wage_thresholds = [3.7375*0.5, 5.0500001*0.5, 11.3*0.5, 13.4125*0.5]
years = [1982, 1990, 2016, 2018]

for year, wage in zip(years, min_wage_thresholds):
    df = datasets[year]

    print("\n" + "="*65)
    print(f"Table 1: \n Sample Selection in the {year} Dataset")
    print("="*65)

    if year in [1982, 1990]:
        hours_var, weeks_var, age_var = 'HRSWRK', 'WKSWRK', 'AGE'
    else:
        hours_var, weeks_var, age_var = 'USHRWK', 'WKSEM', 'AGEGP'

    n_total = len(df)

    # Wage & Work Filter
    df_clean = df[
        (df['hourly_wage'].notna()) &
        (df['hourly_wage'] >= wage) &
        ((df[hours_var] * df[weeks_var]) > 260)
    ]
    n_after_wage = len(df_clean)
    drop1 = n_total - n_after_wage

    # Age Filter
    if year in [1982, 1990]:
        df_clean = df_clean[(df_clean[age_var] >= 25) & (df_clean[age_var] <= 60)]
    else:
        df_clean = df_clean[(df_clean[age_var] >= 7) & (df_clean[age_var] <= 14)]

    n_after_age = len(df_clean)
    drop2 = n_after_wage - n_after_age

    # table 1 replication
    summary = pd.DataFrame({
        'Step': ['Initial data', 'After wage filtering', 'After age filtering'],
        'Observations': [n_total, n_after_wage, n_after_age],
        'Dropped': [0, drop1, drop2],
        'Cumulative Dropped': [0, drop1, drop1 + drop2]
    })
    print(summary.to_string(index=False))
    print("="*65)

    datasets[year] = df_clean
```

Table 1 reproduction from HPV

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Table 1:
Sample Selection in the 1982 Dataset
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	Step	Observations	Dropped	Cumulative	Dropped
	Initial data	42570	0		0
	After wage filtering	34256	8314		8314
	After age filtering	25940	8316		16630

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Table 1:
Sample Selection in the 1990 Dataset
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	Step	Observations	Dropped	Cumulative	Dropped
	Initial data	46510	0		0
	After wage filtering	38145	8365		8365
	After age filtering	31350	6795		15160

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Table 1:
Sample Selection in the 2016 Dataset
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	Step	Observations	Dropped	Cumulative	Dropped
	Initial data	34287	0		0
	After wage filtering	28327	5960		5960
	After age filtering	23517	4810		10770

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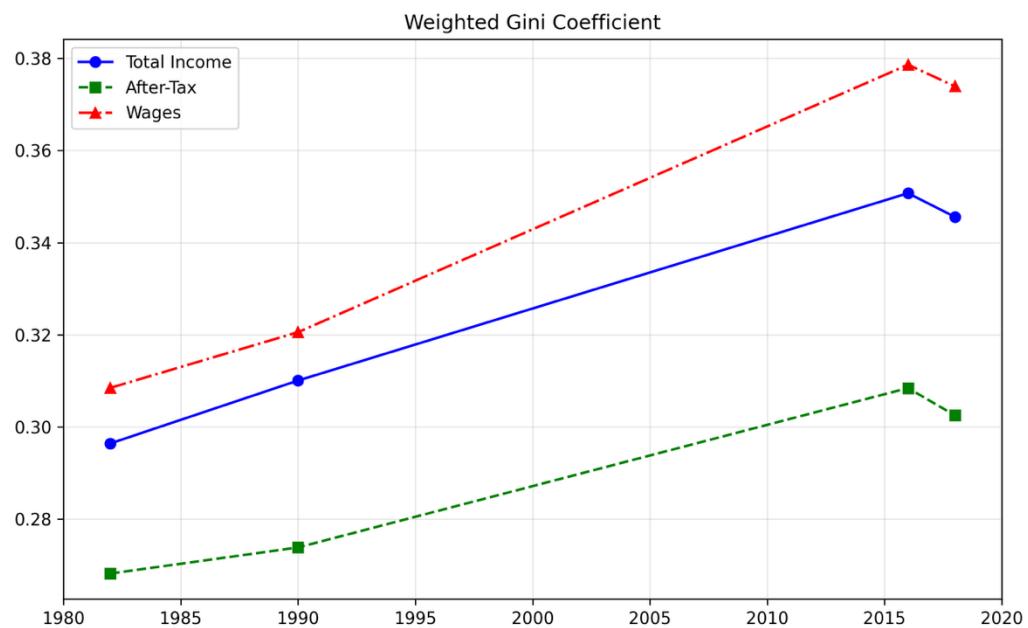
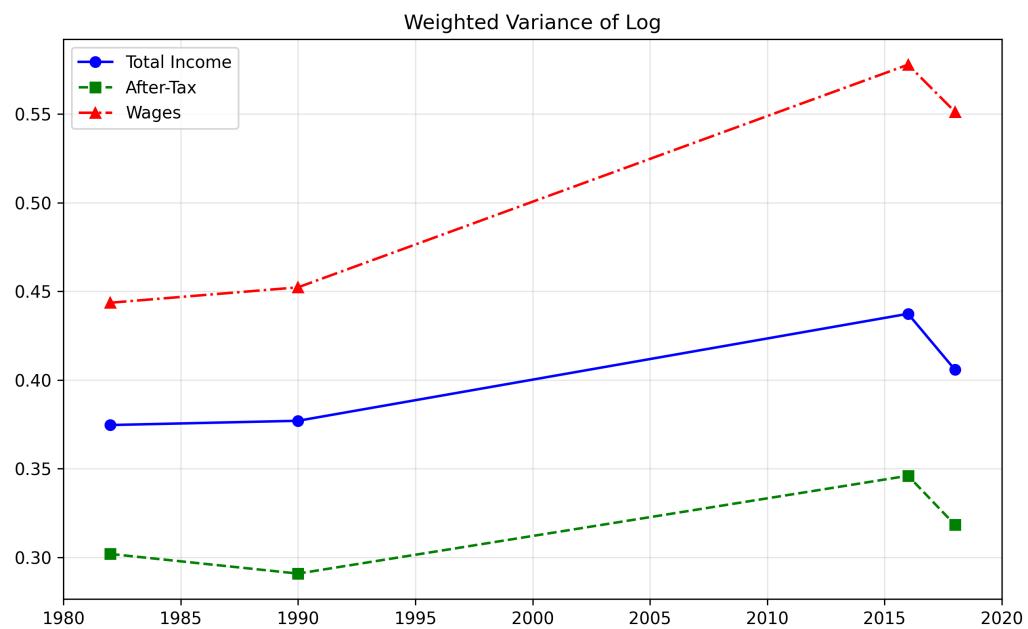
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Table 1:
Sample Selection in the 2018 Dataset
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	Step	Observations	Dropped	Cumulative	Dropped
	Initial data	50588	0		0
	After wage filtering	41807	8781		8781
	After age filtering	32469	9338		18119

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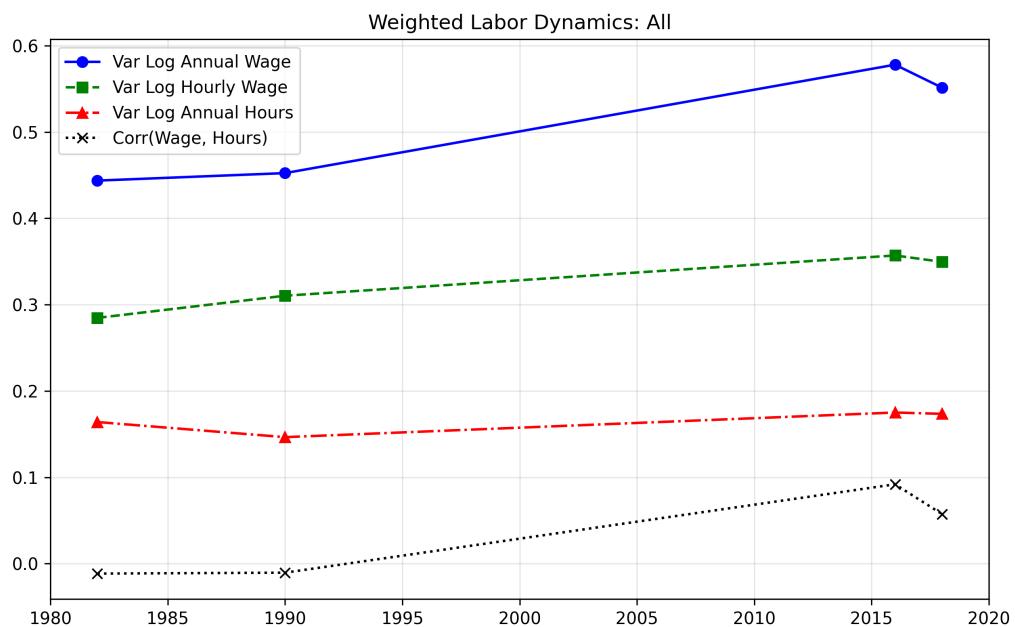
Question 4:

Part A)

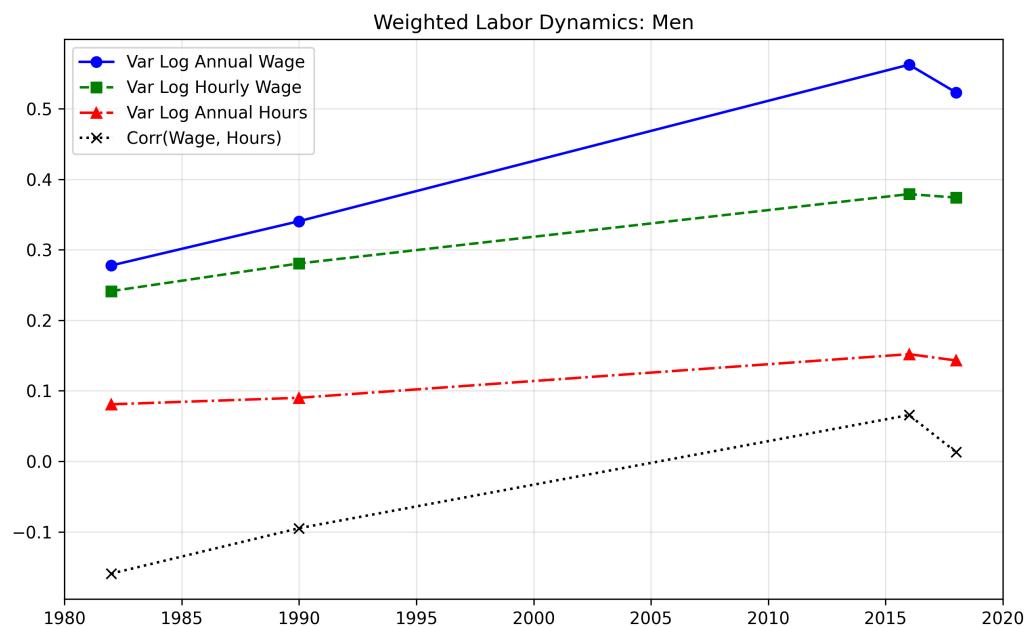


Part B)

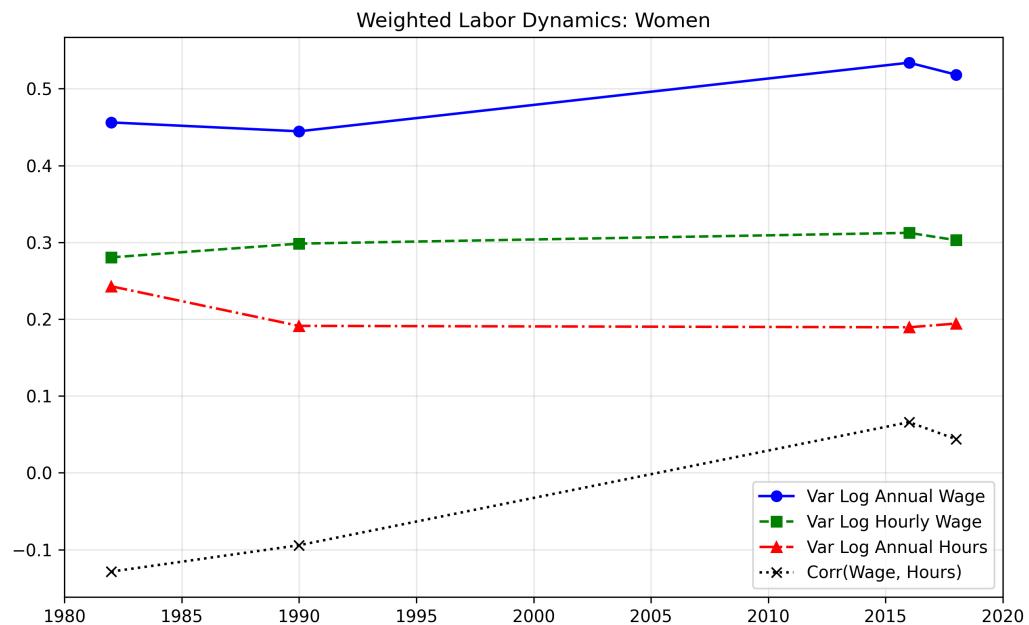
Total Population:



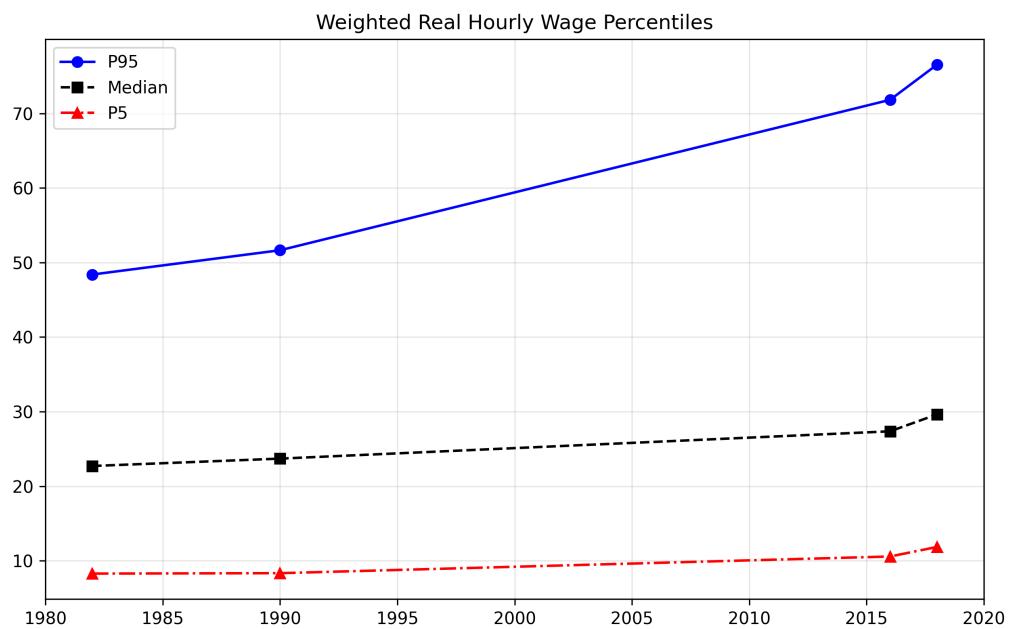
Men:



Women:



Part C)



Question 5:

- A) $df['potential_experience'] = df['age_approx'] - df['years_of_schooling'] - 6$
*all variables were defined in the function 'prep_composition_adjusted_vars(df, year)' for all datasets
B)

```
#5-B
# Verify Group Consistency
print("\nVerifying Gender x Education x Experience Groups:")
all_unique_cells = set()

for year, df in akk_datasets.items():
    # Get unique cells for this year
    unique_cells_year = set(df['akk_cell'].unique())
    all_unique_cells.update(unique_cells_year)
    df_valid_groups = df.dropna(subset=['akk_cell'])
    num_groups = df_valid_groups['akk_cell'].nunique()

    print(f"Year {year}: {num_groups} populated groups out of 40 possible.")

print(f"\nTotal unique group identifiers found across ALL years:
{len(all_unique_cells)}")
print(f"Sample Group Names: {list(all_unique_cells)[:3]}")
```

Total number of groups per year:

```
Year 1982: 24 populated groups out of 40 possible.
Year 1990: 23 populated groups out of 40 possible.
Year 2016: 30 populated groups out of 40 possible.
Year 2018: 30 populated groups out of 40 possible.
```

C & D)

```
group_stats = []

for year, df in akk_datasets.items():
    # Only keep valid wages and positive weights
    df_valid = df[(df['hourly_real_wage'] > 0) & (df['weight'] > 0)].copy()

    # Calculate log real hourly wage
    df_valid['log_wage'] = np.log(df_valid['hourly_real_wage'])
    df_valid['total_hours_weight'] = df_valid['weight'] * df_valid['annual_hours']

    total_hours_year = df_valid['total_hours_weight'].sum()

    # Group by the AKK cell
    grouped = df_valid.groupby('akk_cell')

    for cell_name, group in grouped:
        # C: Share of sample (using hours-weighted metric as per AKK)
```

```

group_hours = group['total_hours_weight'].sum()
share = group_hours / total_hours_year

# D: Compute mean log wage in group (Weighted)
mean_log_wage = np.average(group['log_wage'],
weights=group['total_hours_weight'])

# Split cell name to get gender and education back
gender, edu, exp = cell_name.split('_')

group_stats.append({
    'Year': year,
    'akk_cell': cell_name,
    'Gender': gender,
    'Education': edu,
    'Share': share,
    'Mean_Log_Wage': mean_log_wage
})

df_stats = pd.DataFrame(group_stats)

```

E)

--- Composition-Corrected vs Naive Mean Log Wages ---					
TOTAL POPULATION:					
Year	Naive	Mean	Log	Wage	Corrected
1982			3.073104		3.141894
1990			3.118680		3.126706
2016			3.342218		3.243272
2018			3.408005		3.311638
WOMEN:					
Year	Naive	Mean	Log	Wage	Corrected
1982			2.843850		2.945552
1990			2.938551		2.968465
2016			3.236435		3.115962
2018			3.307347		3.191370
MEN:					
Year	Naive	Mean	Log	Wage	Corrected
1982			3.187091		3.272802
1990			3.236770		3.238209
2016			3.424692		3.326145
2018			3.485395		3.389928
UNIVERSITY GRADUATES:					
Year	Naive	Mean	Log	Wage	Corrected
1982			3.213555		3.275485
1990			3.131780		3.131849
2016			3.427771		3.424481
2018			3.487554		3.492898
HIGH-SCHOOL GRADUATES:					
Year	Naive	Mean	Log	Wage	Corrected
1982			3.070456		3.056962
1990			3.118312		3.123708
2016			3.158992		3.148675
2018			3.212790		3.217292

F)

Over the sample period, naive wage growth consistently overstates true wage growth because they capture a workforce that became significantly older and more educated. By holding these demographics constant, composition-adjusted wages reveal much smaller “true” wage gains. This adjustment heavily dampens the apparent wage growth for women, who experienced massive educational gains and exposes severe real wage stagnation for high-school graduates, while confirming a rising premium for university graduates.