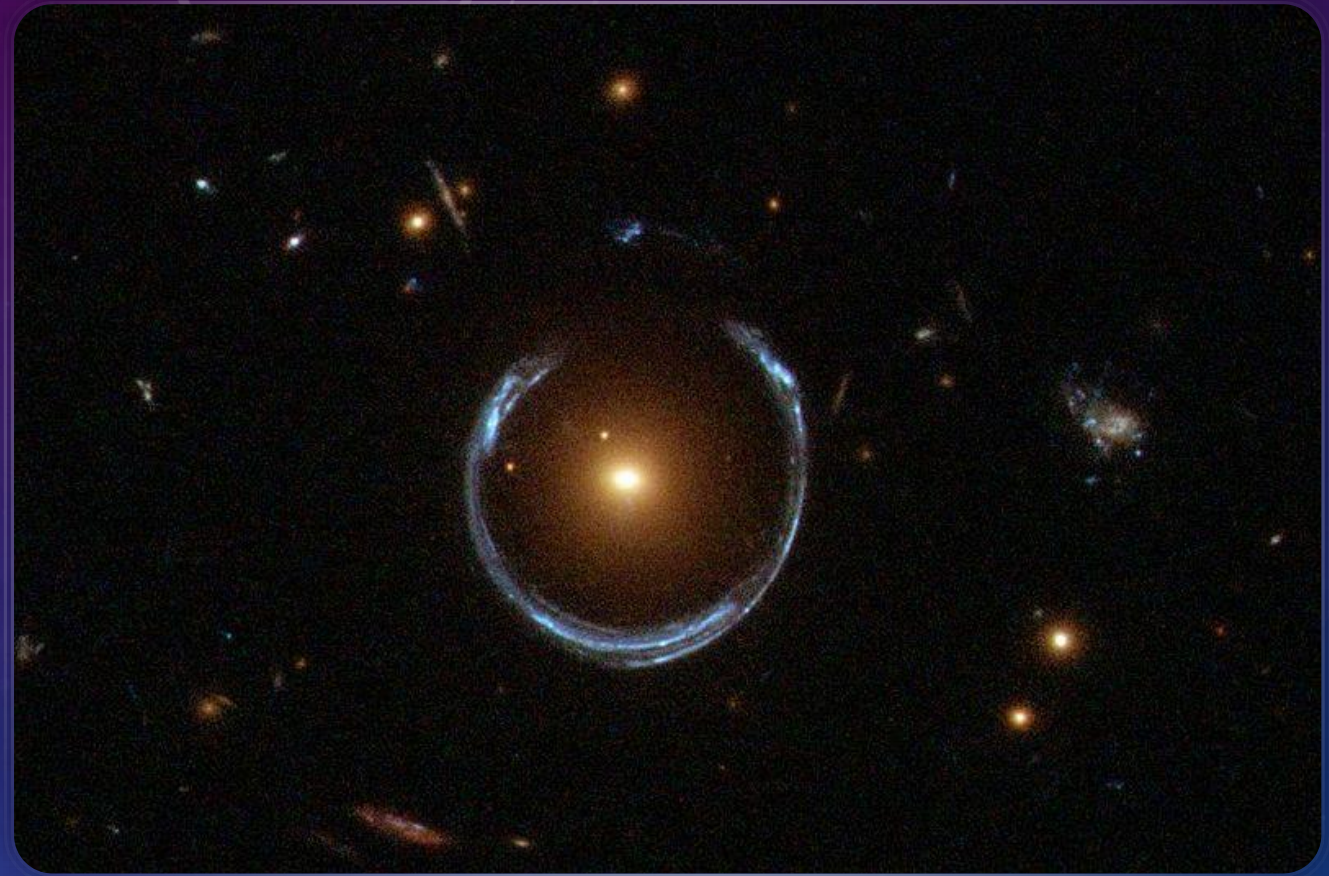
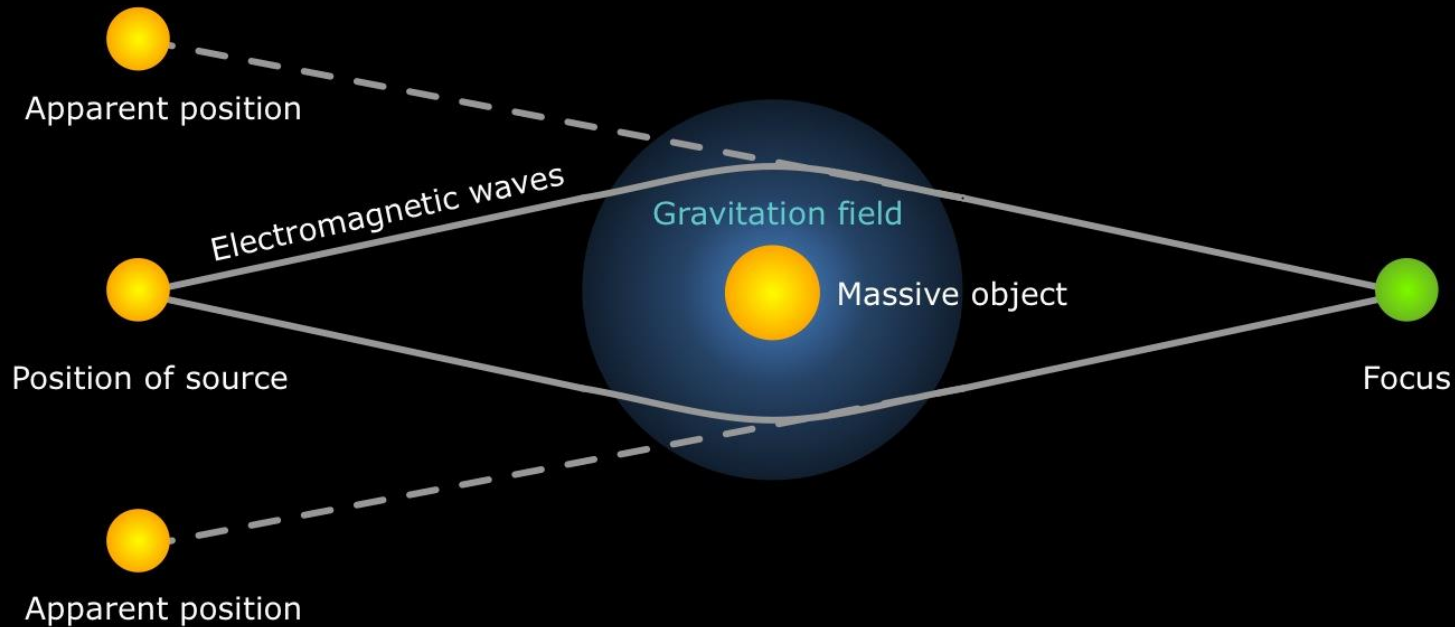


# NUMERICAL PROJECT : LENSTOOL

M2 ASTROPHYSICS - ROCHER ANTOINE  
SUPERVISED BY RICHARD JOHAN



# GRAVITATIONAL LENSING EFFECT



- Source behind a massive object
- Massive object deflects light rays
- Observer sees several images





## SLACS: The Sloan Lens ACS Survey

[www.SLACS.org](http://www.SLACS.org)

A. Bolton (U. Hawai'i IfA), L. Koopmans (Kapteyn), T. Treu (UCSB), R. Gavazzi (IAP Paris), L. Moustakas (JPL/Caltech), S. Burles (MIT)

Image credit: A. Bolton, for the SLACS team and NASA/ESA



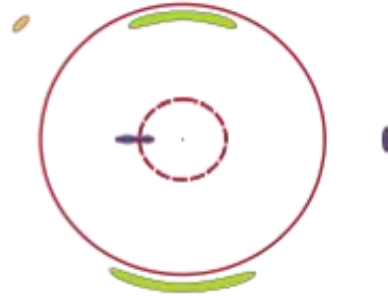
# GRAVITATIONAL LENSING

**Source Plane**

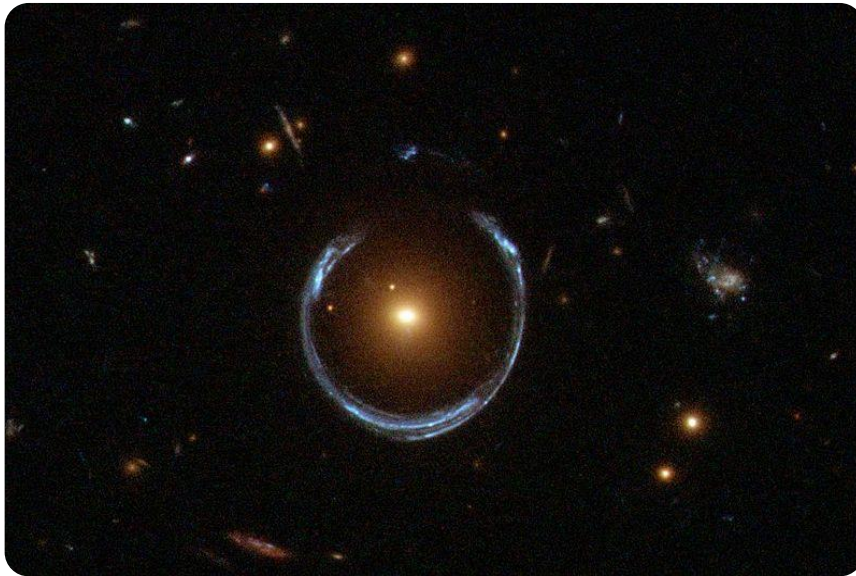


Caustic curves

**Image Plane**



Critical curves



Gravitationslinsen (IV)

Eine asymmetrische Linse

Matthias Bartelmann, MPA Garching



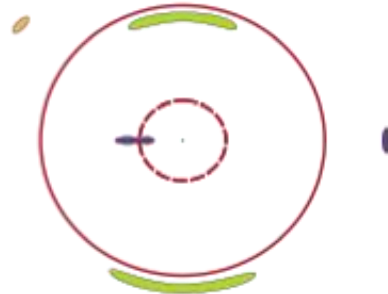
# GRAVITATIONAL LENSING

Source Plane

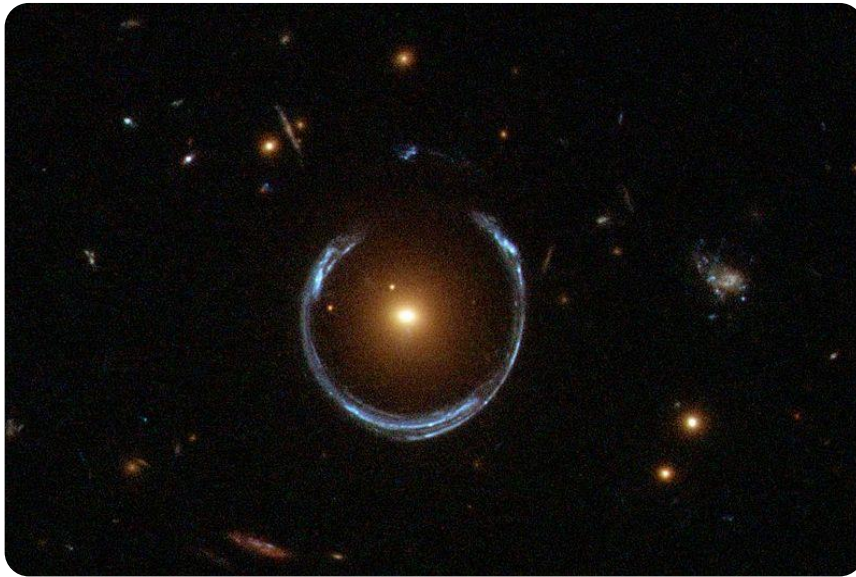


Caustic curves

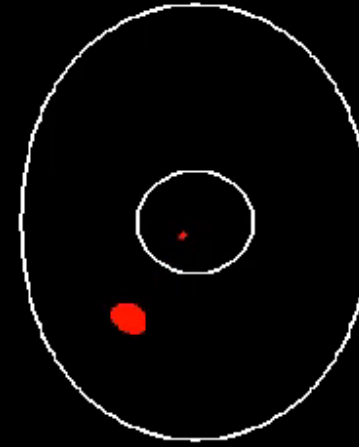
Image Plane



Critical curves



Bilder



Quellen

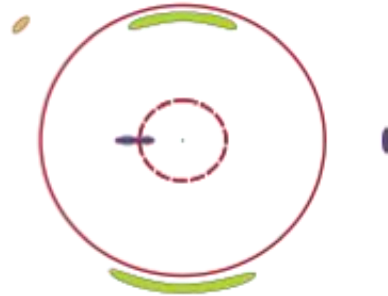
# GRAVITATIONAL LENSING

Source Plane

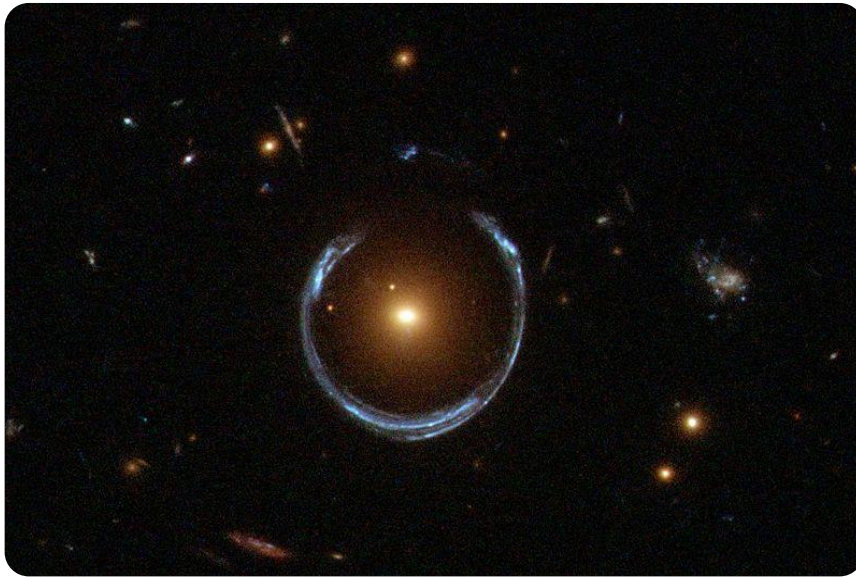


Caustic curves

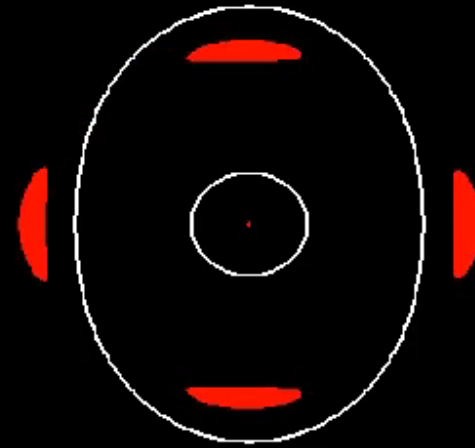
Image Plane



Critical curves



Bilder



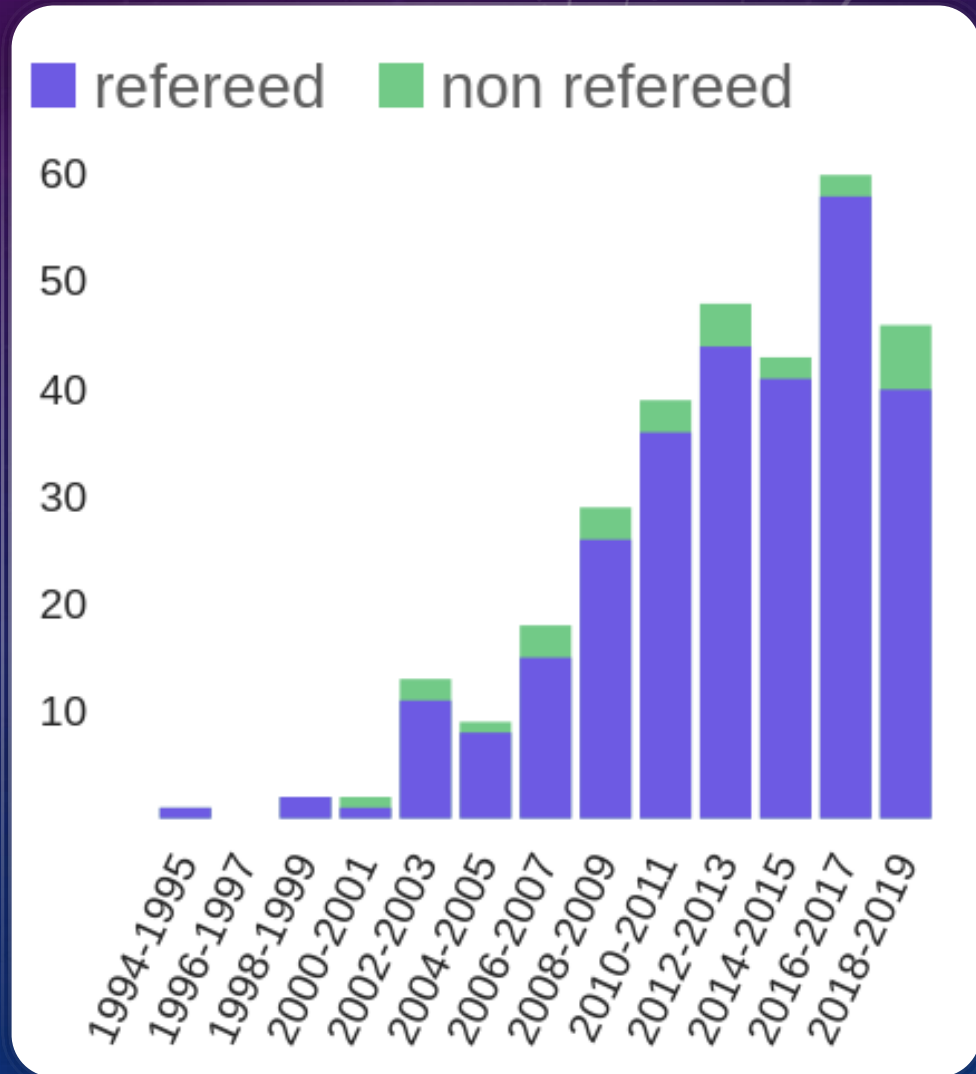
Quellen





# LENSTOOL: INFORMATIONS

- Gravitational lensing simulation program
- Created by J.P. Kneib (1993)
- Public, open source, multi developers
- French collaboration : Toulouse, Marseille, Lyon
- Used by about 10 research teams around the world

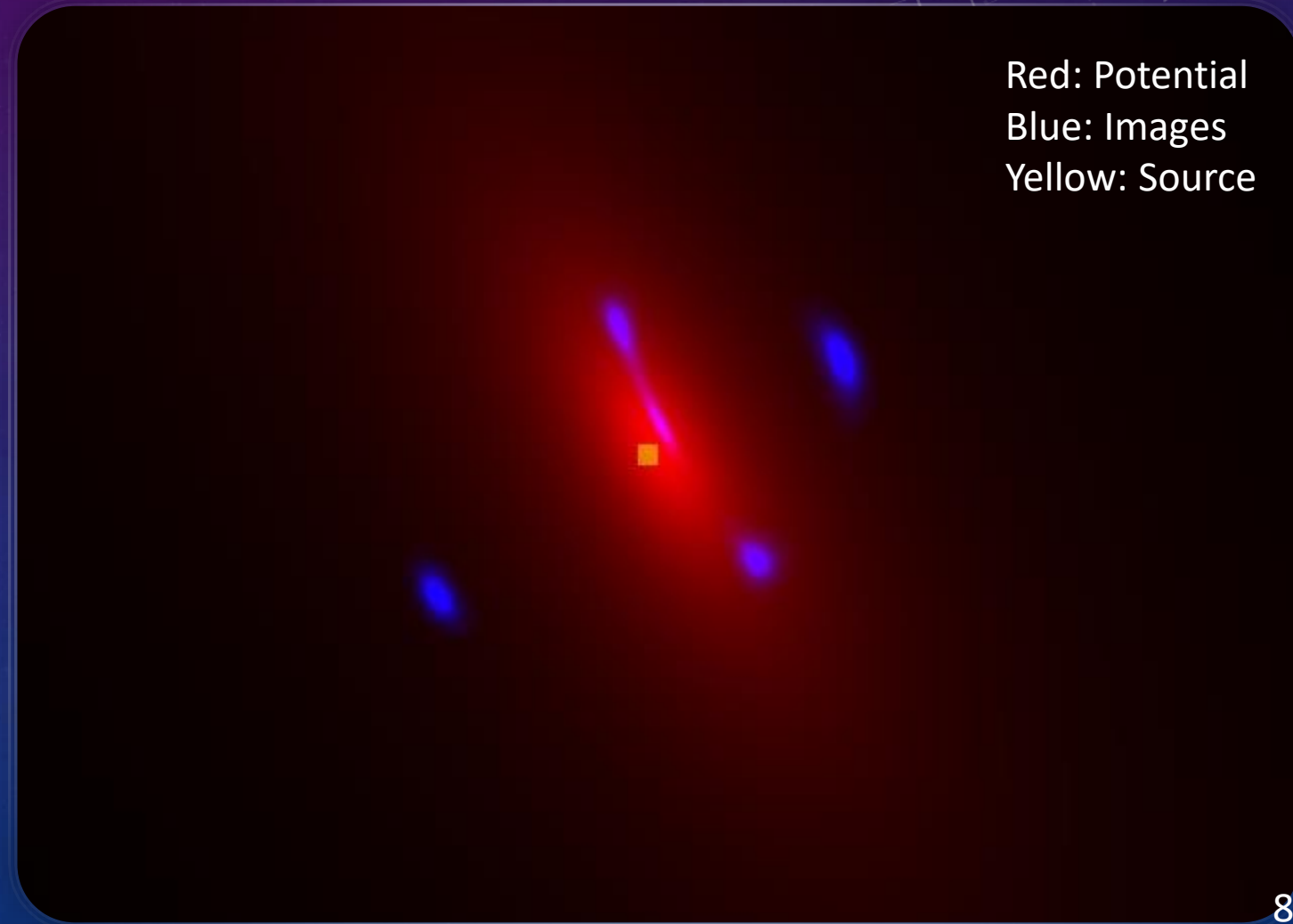


# LENSTOOL: RUNNING

**INPUT** : source / image positions  
+ lens parameters

```
runmode
  reference      3 133.69 -1.36|
  image         0 image_wcs.cat
end
grille
  nombre        100
  polaire       0
  nlentille     1
end
potentiel 01
  profil        81
  x_centre      0.0
  y_centre      0.0
  ellipticite   0.65
  angle_pos     120.0
  core_radius_kpc 16.11
  cut_radius_kpc 1343.23
  v_disp        800.0
  z_lens        0.4000
end
```

**OUTPUT** : All images and source(s) positions

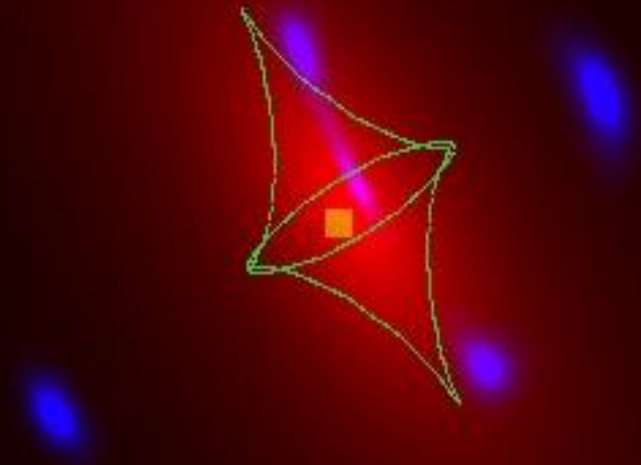




# LENSTOOL: MODEL

## Caustic lines

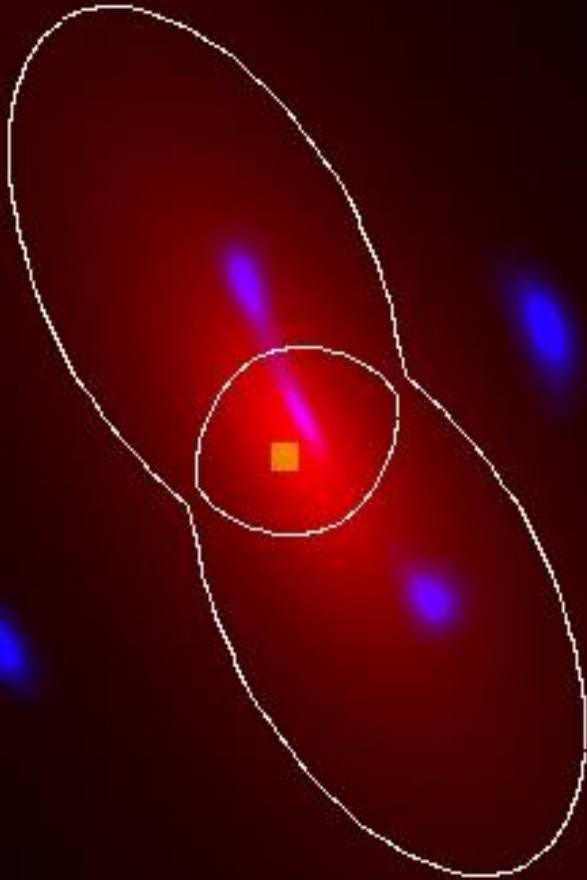
Red: Potential  
Blue: Images  
Yellow: Source



# LENSTOOL: MODEL

## Critical lines

Red: Potential  
Blue: Images  
Yellow: Source



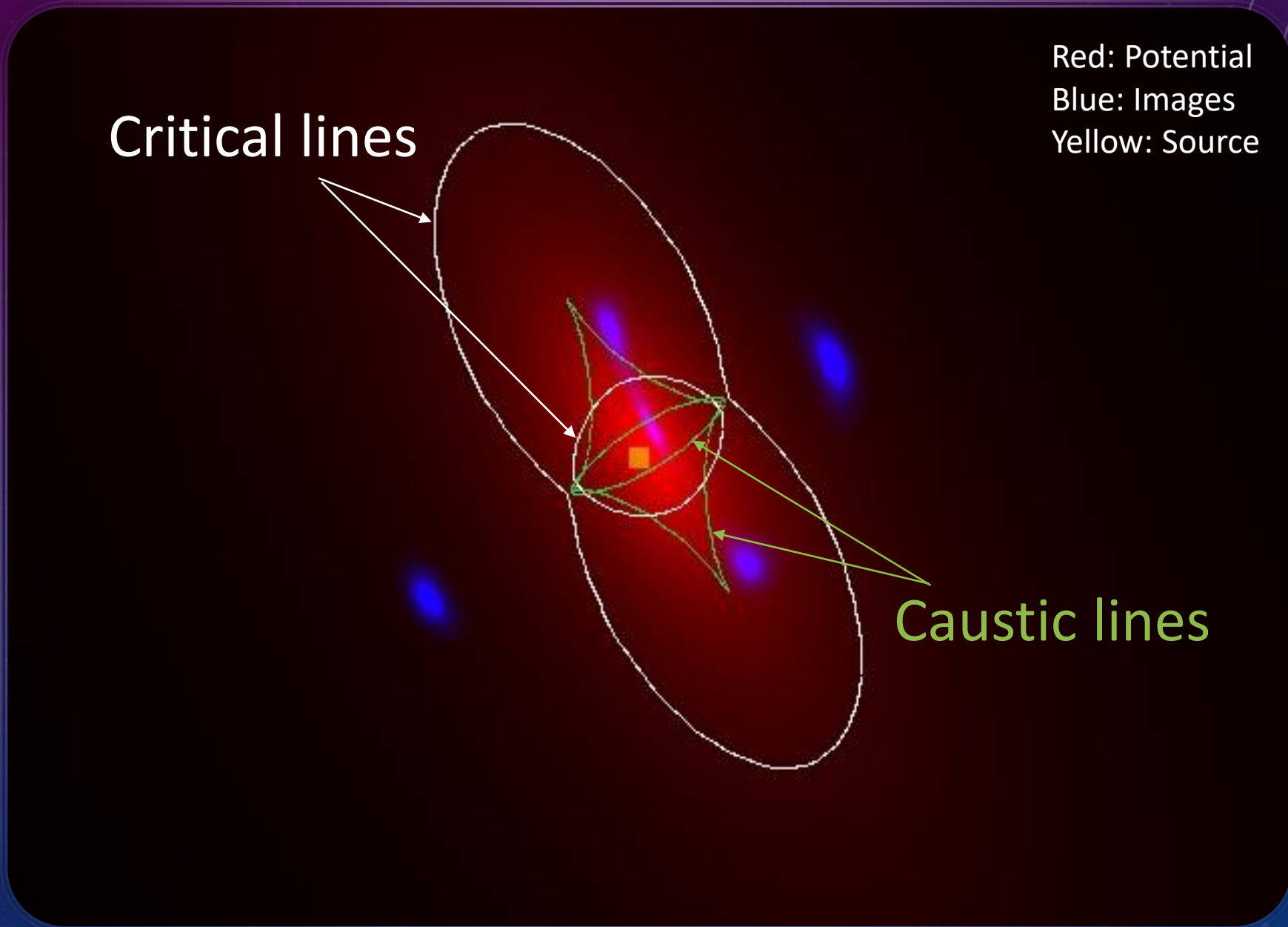


# LENSTOOL: MODEL

Critical lines

Red: Potential  
Blue: Images  
Yellow: Source

Caustic lines

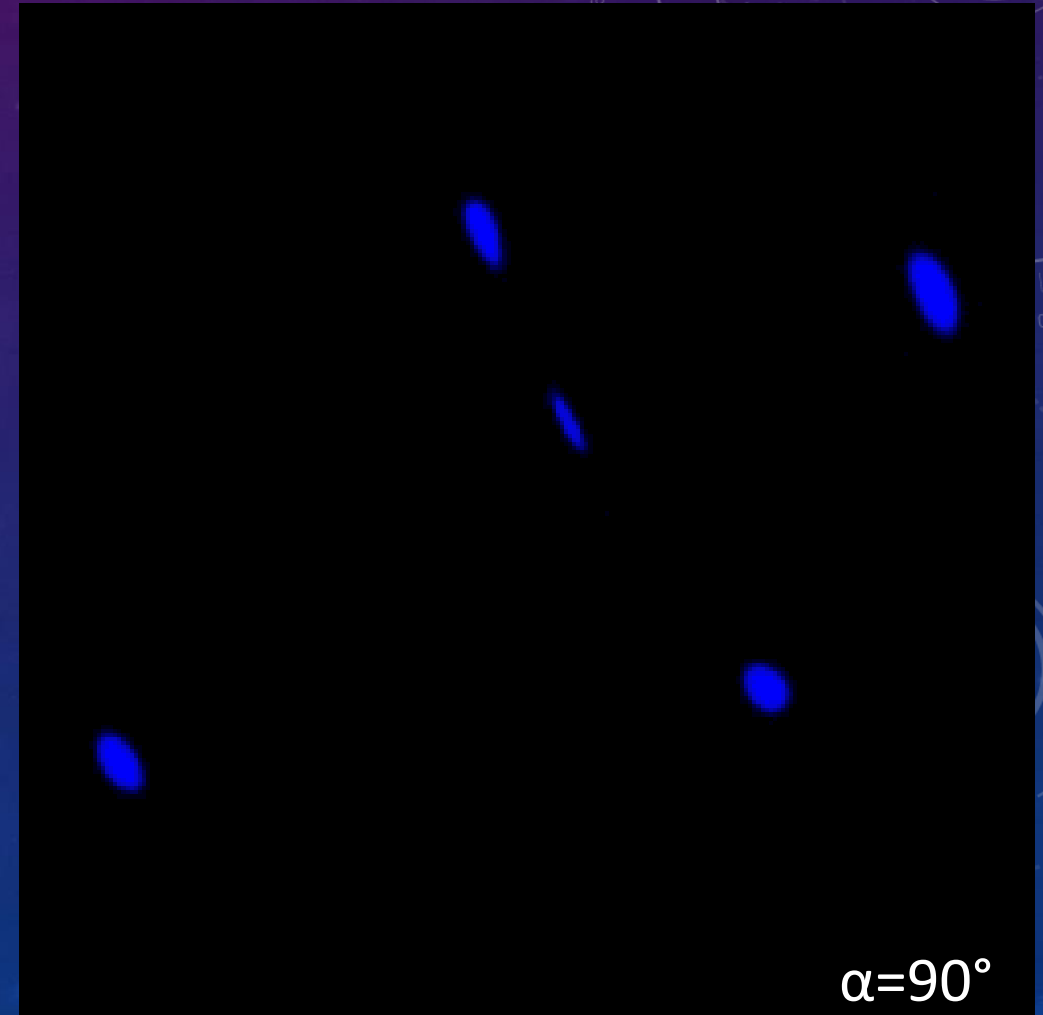


# LENSTOOL: SHEAR

Model + vertical  
shear strength up to  $\gamma=0.2$

- Environment effects create a deformation on images
- Modelisation by a shear in the image
- The Shear is described by a strength  $\gamma$  and an angle  $\alpha$

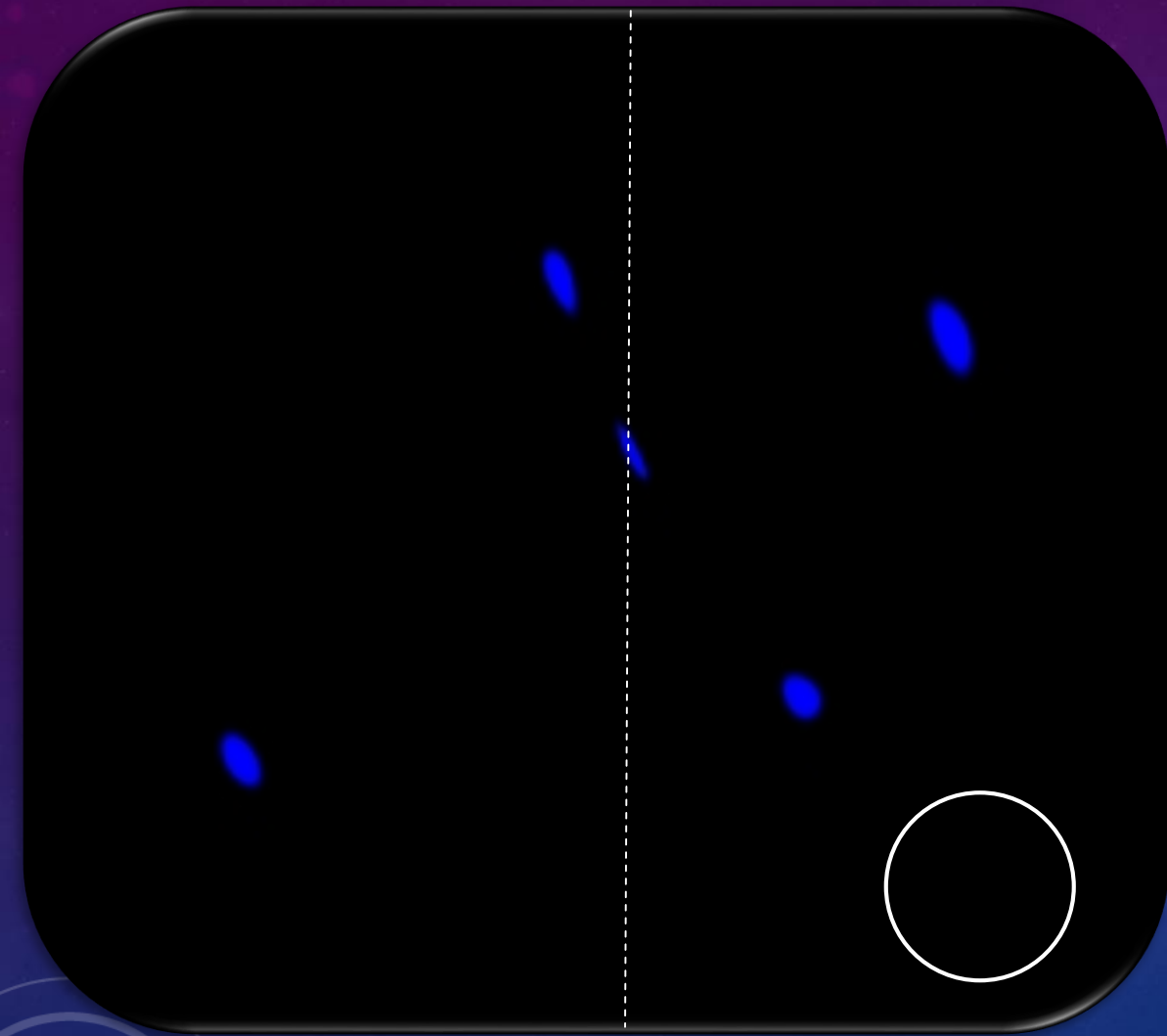
Objective  $\Rightarrow$  Find the images with no shear



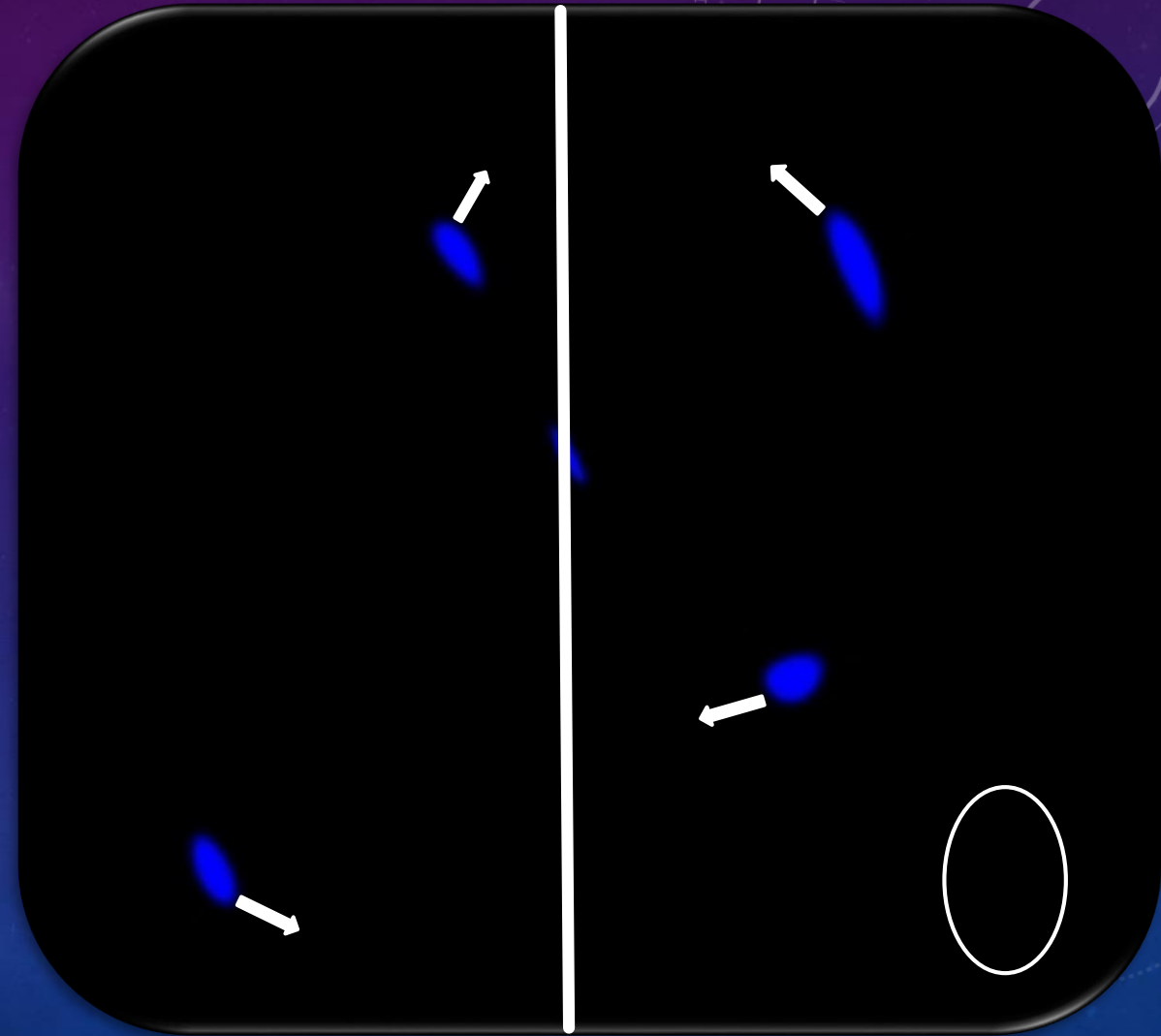


# LENSTOOL: SHEAR EFFECT

$\alpha=90^\circ$

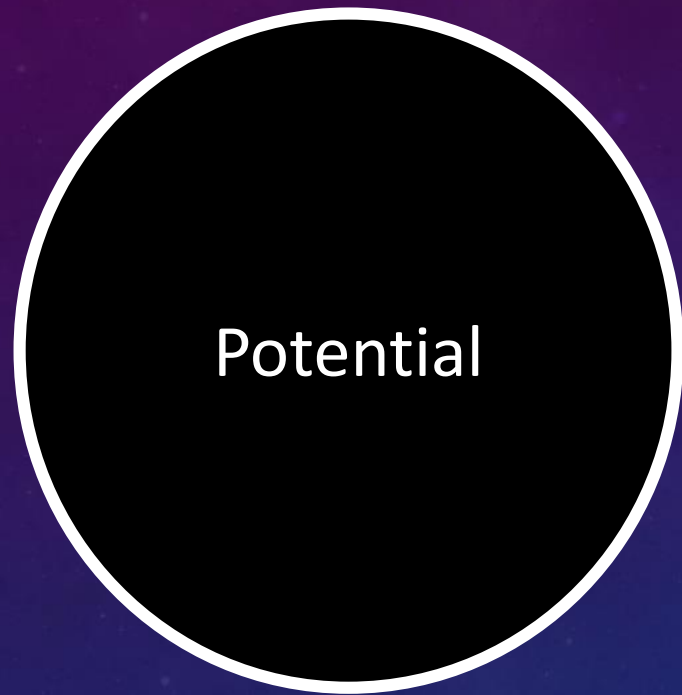


No Shear



Shear  $\gamma = 0,2$

# LENSTOOL: SHEAR EFFECT

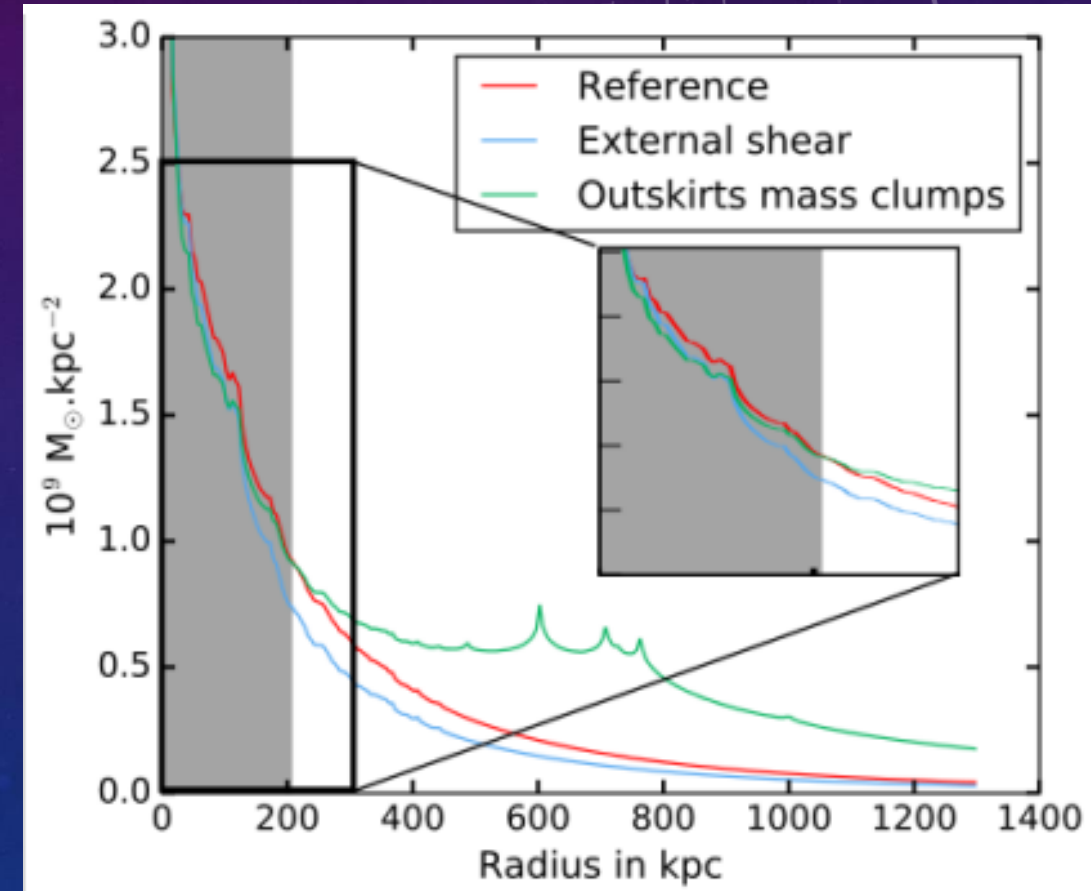
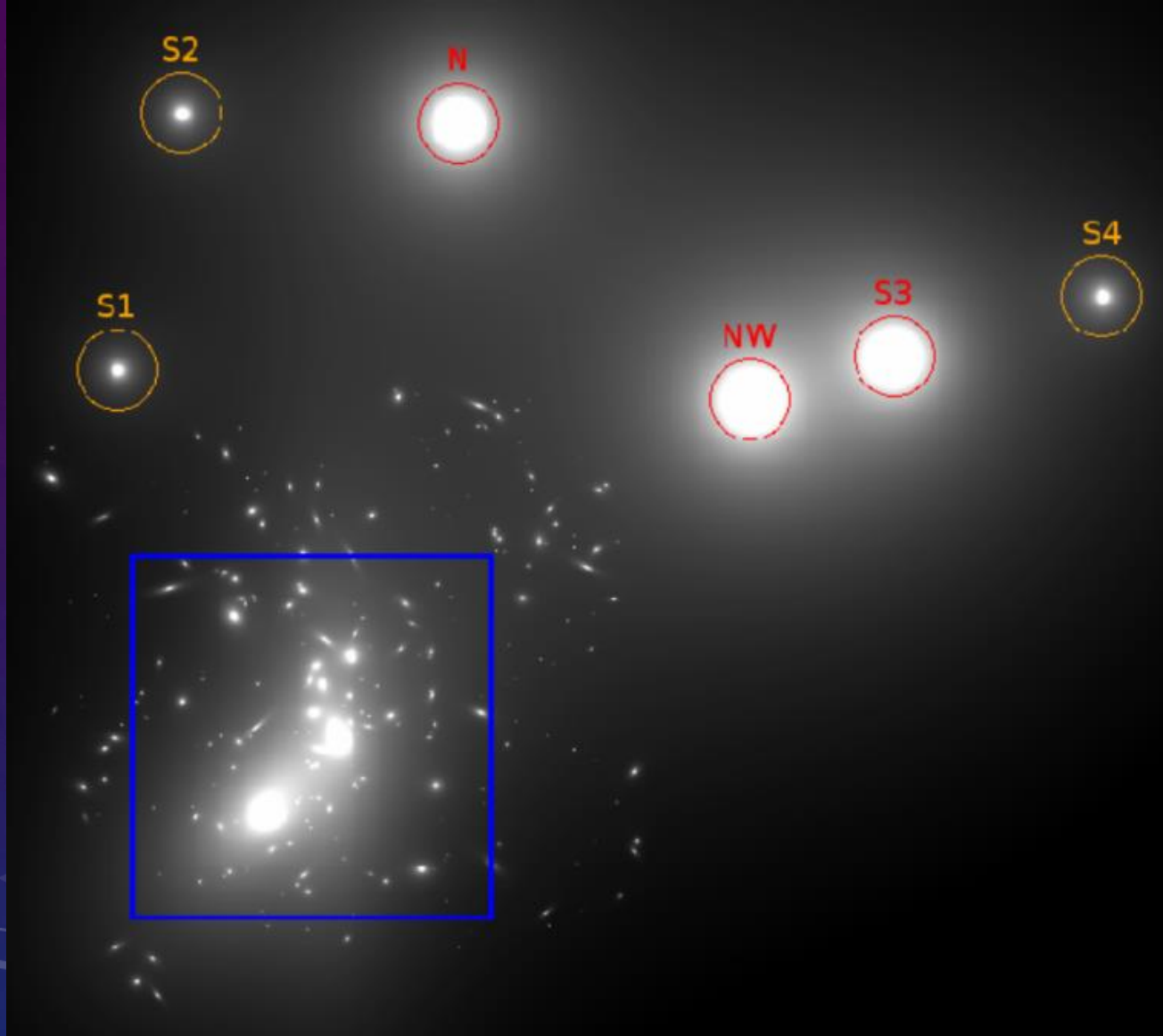


$\gamma$  decrease with the distance  
Shear is tangent to the potential





# LENSTOOL: SCIENTIFIC INTEREST



*G. Mahler et al 2018*

# LENSTOOL: POTENTIAL OPTIMISATION

```
potentiel 1
  profil      81
  x_centre    0.0
  y_centre    0.0
  ellipticite 0.65
  angle_pos   120.
  core_radius 3.0
  cut_radius  250.0
  v_disp      800.
  z_lens      0.4
end

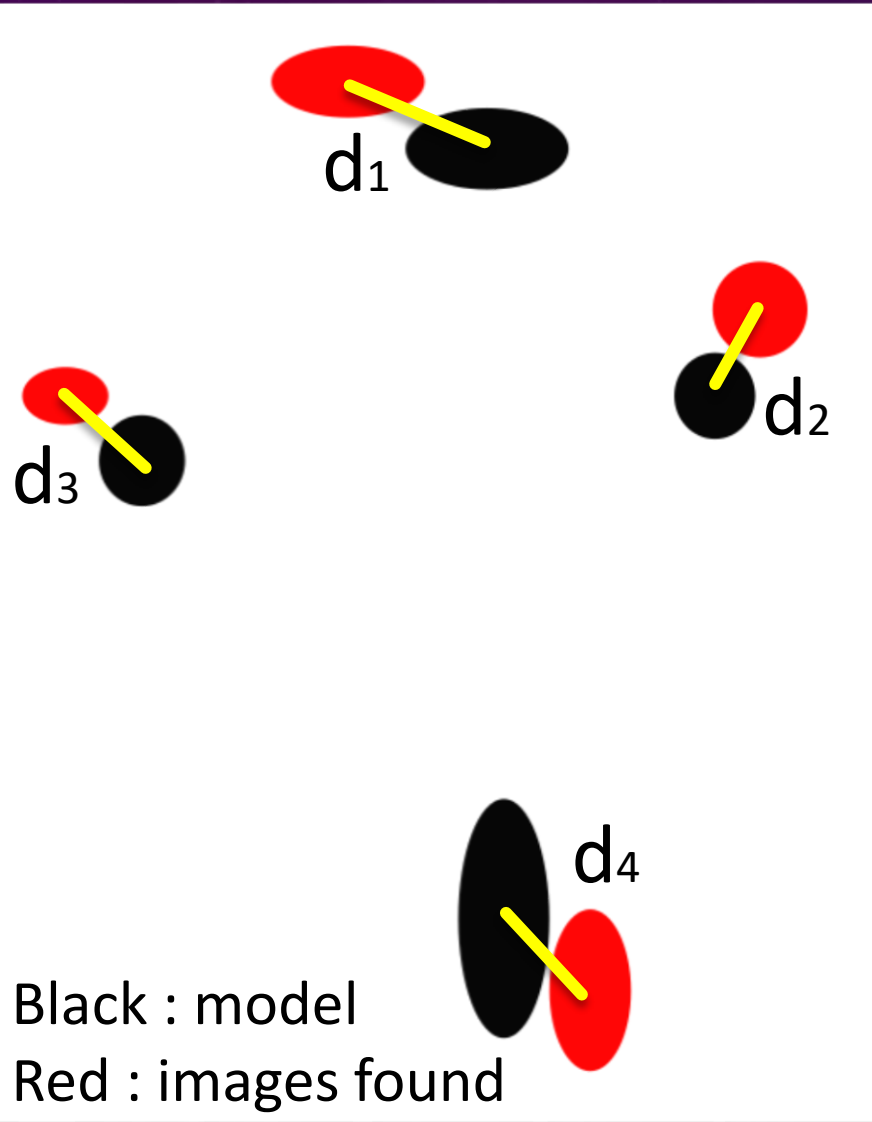
limit 1
  x_centre    0 -100.0 100.0 0.01
  y_centre    0 -1.0 1.0 0.01
  ellipticite  1 0.1 0.75 0.01
  angle_pos   1 0. 180.0 0.1
  core_radius  0 0.1 4. 0.1
  cut_radius   0 50. 500. 0.1
  v_disp       0 200. 1000. 0.1
end
```

- Prior : uniform, gaussian
- Limit : min, max
- Iteration step, deviation  $1\sigma$

Find images for each case and compute  $\chi^2$



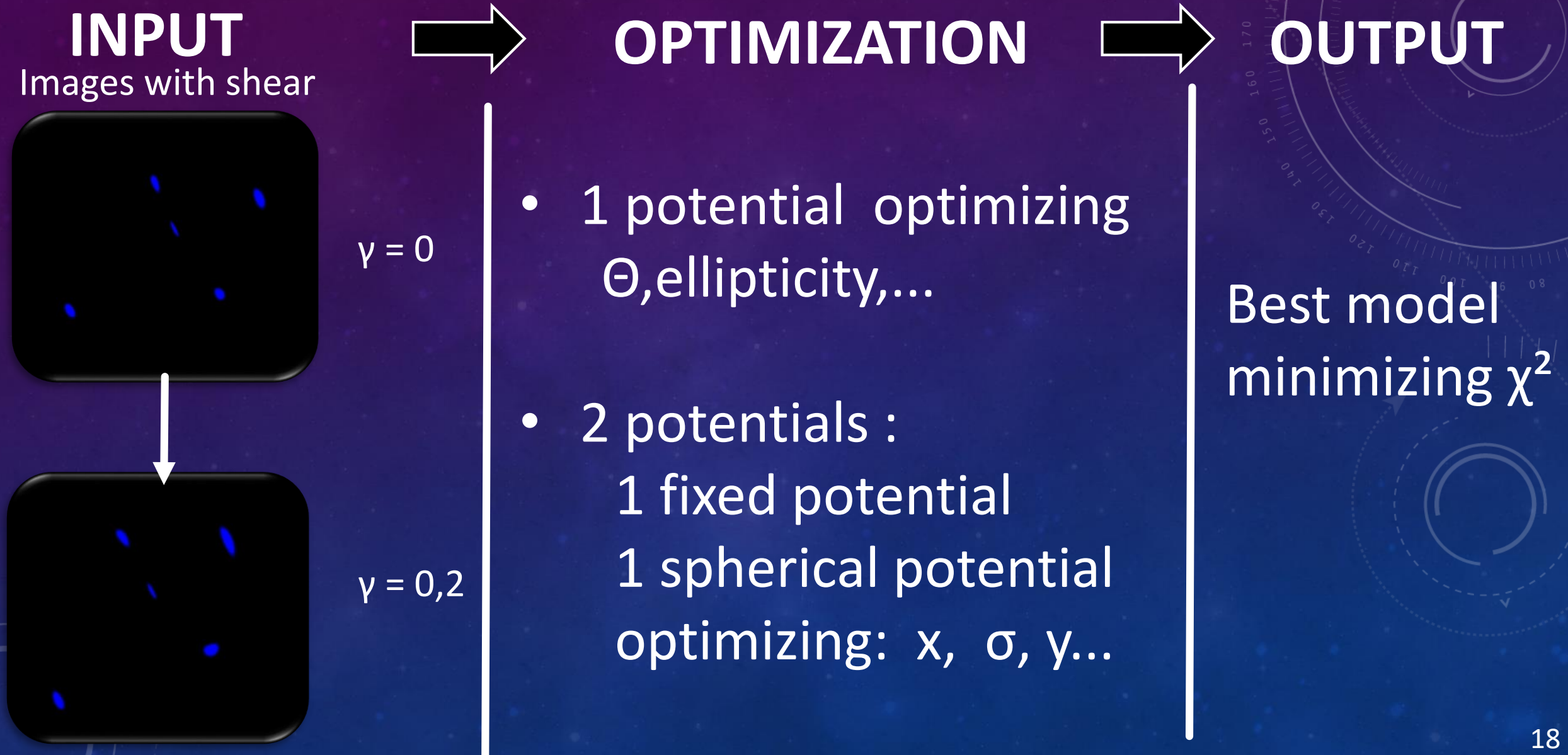
# LENSTOOL: $\chi^2$ CALCULATION



$$\chi^2 = \left( \frac{d_1}{\epsilon} \right)^2 + \left( \frac{d_2}{\epsilon} \right)^2 + \left( \frac{d_3}{\epsilon} \right)^2 + \left( \frac{d_4}{\epsilon} \right)^2$$

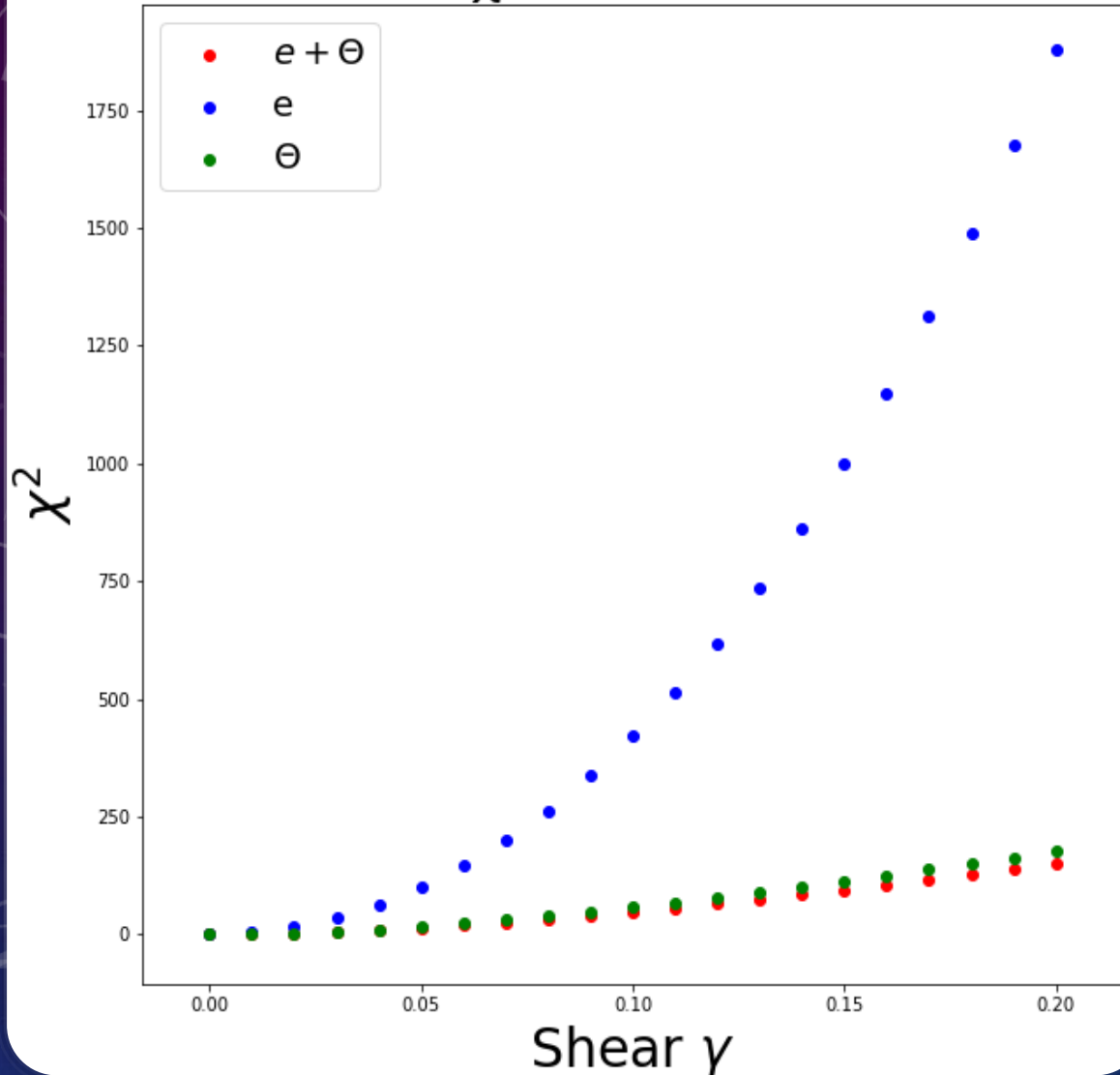
$D_i$  : separation distance in arcsec  
 $\epsilon$  : astrometric errors (0.1")

# LENSTOOL: TEST PROCEDURE

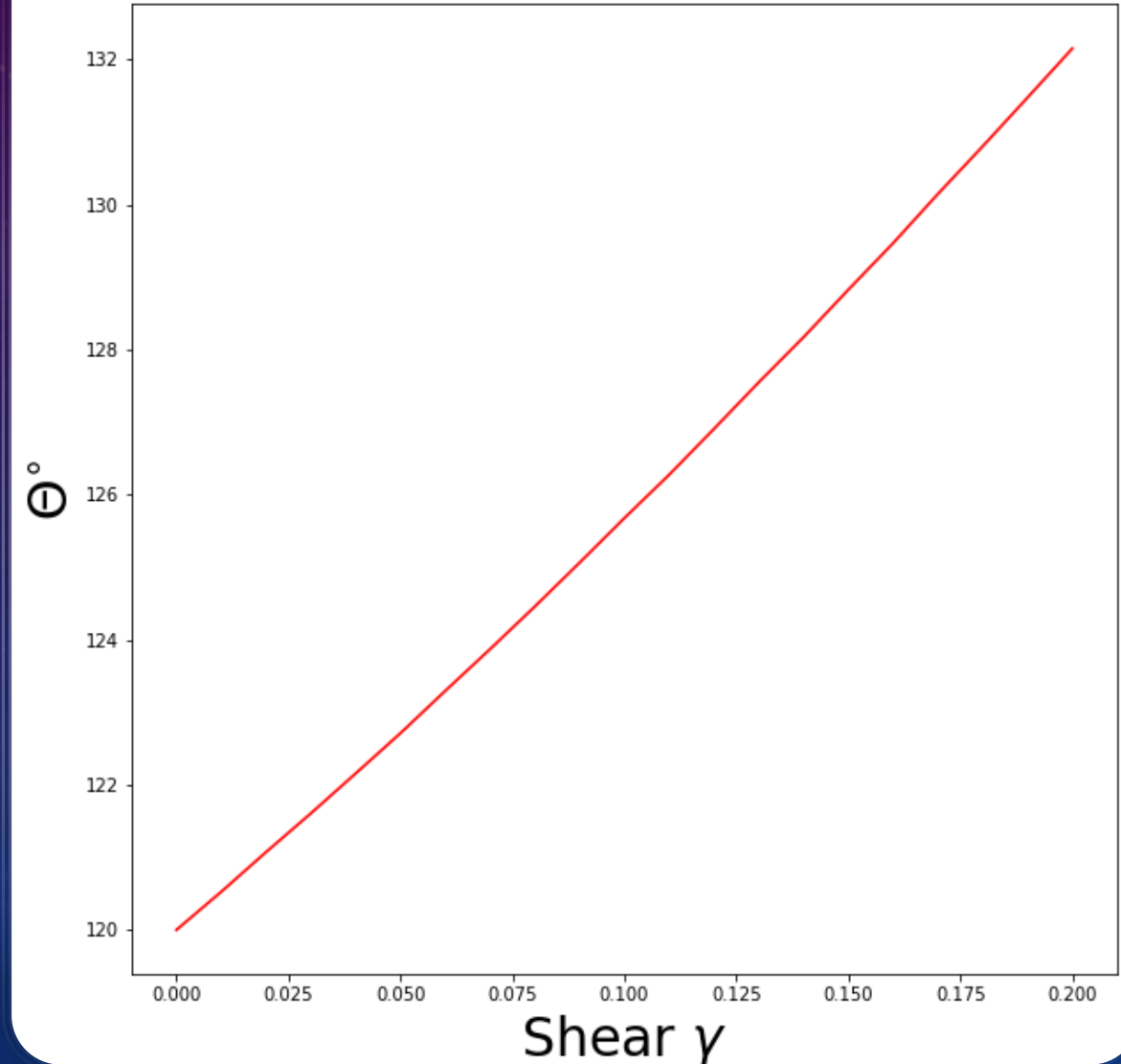


# LENSTOOL: RESULTS FOR 1 POTENTIAL

$\chi^2$  evolution



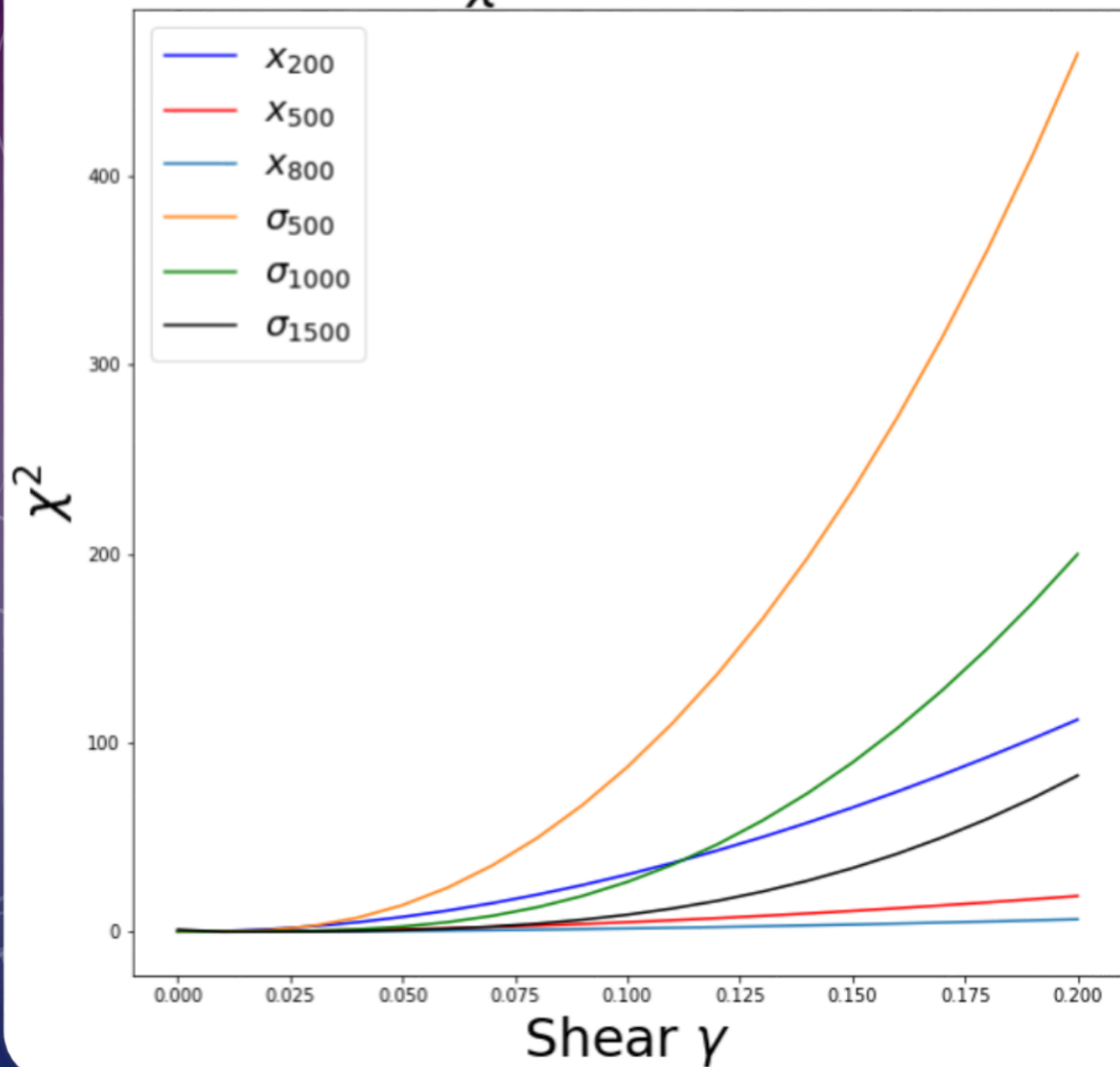
$\Theta$  evolution



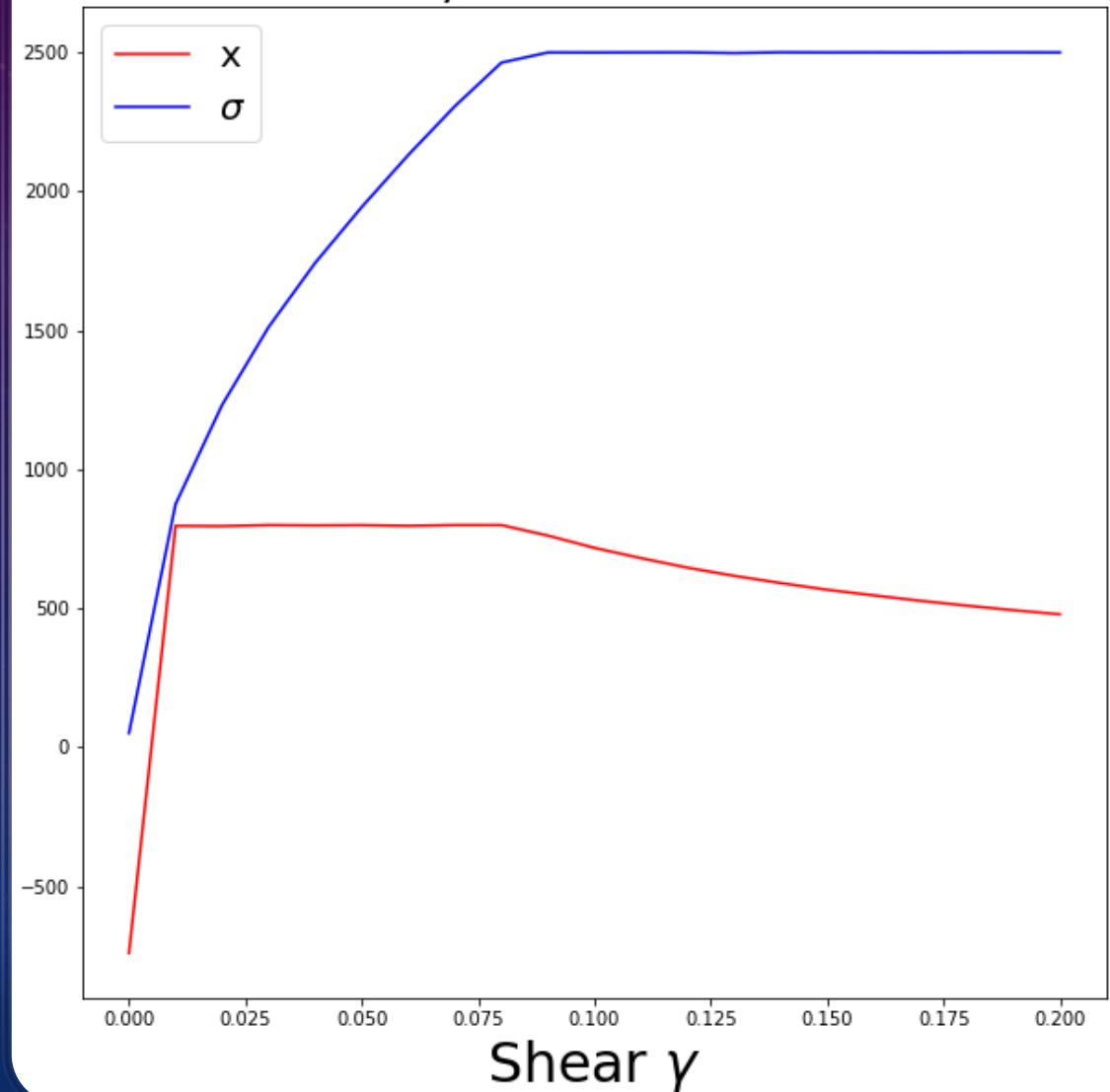


# LENSTOOL: RESULTS FOR 2 POTENTIALS

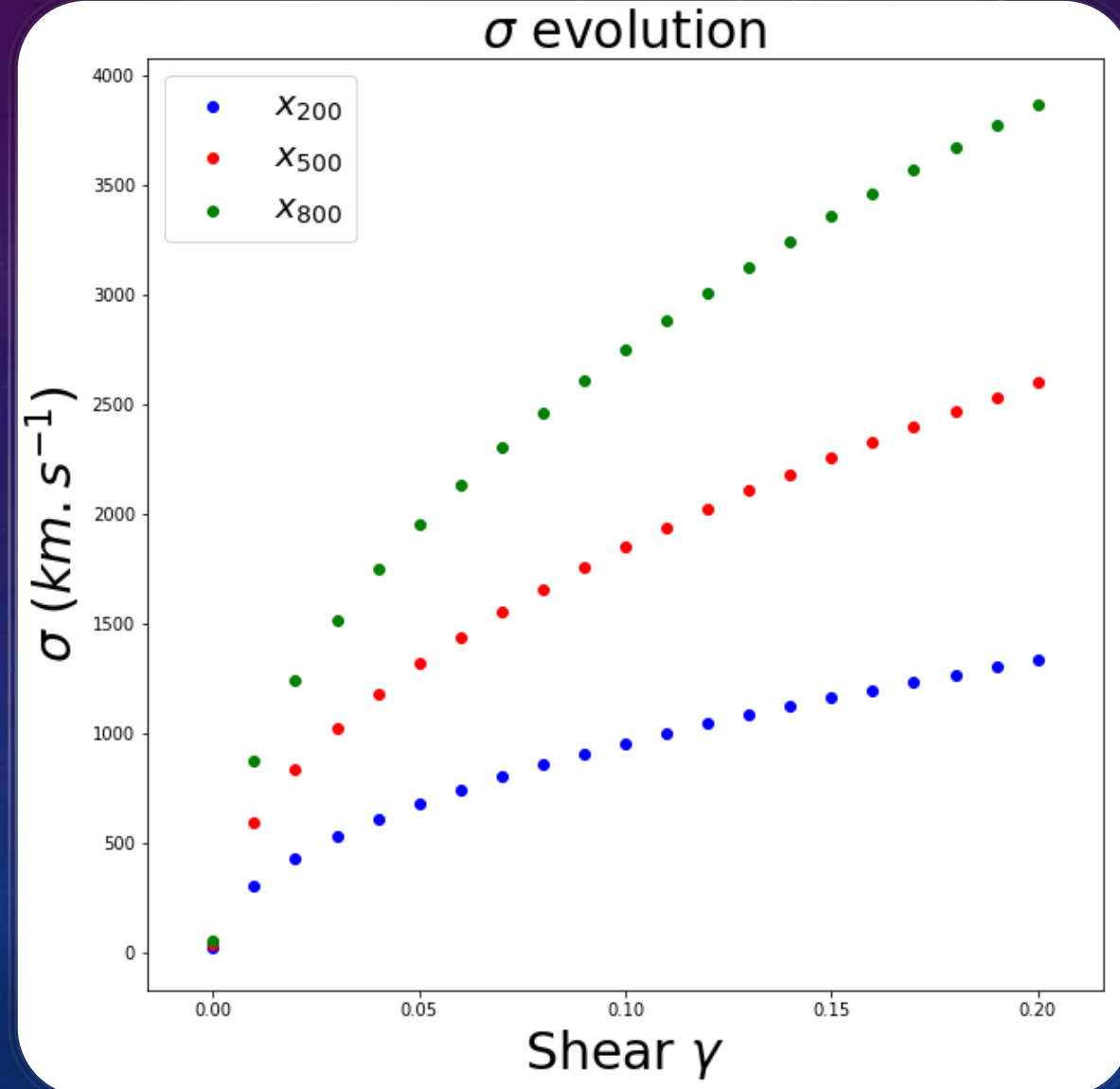
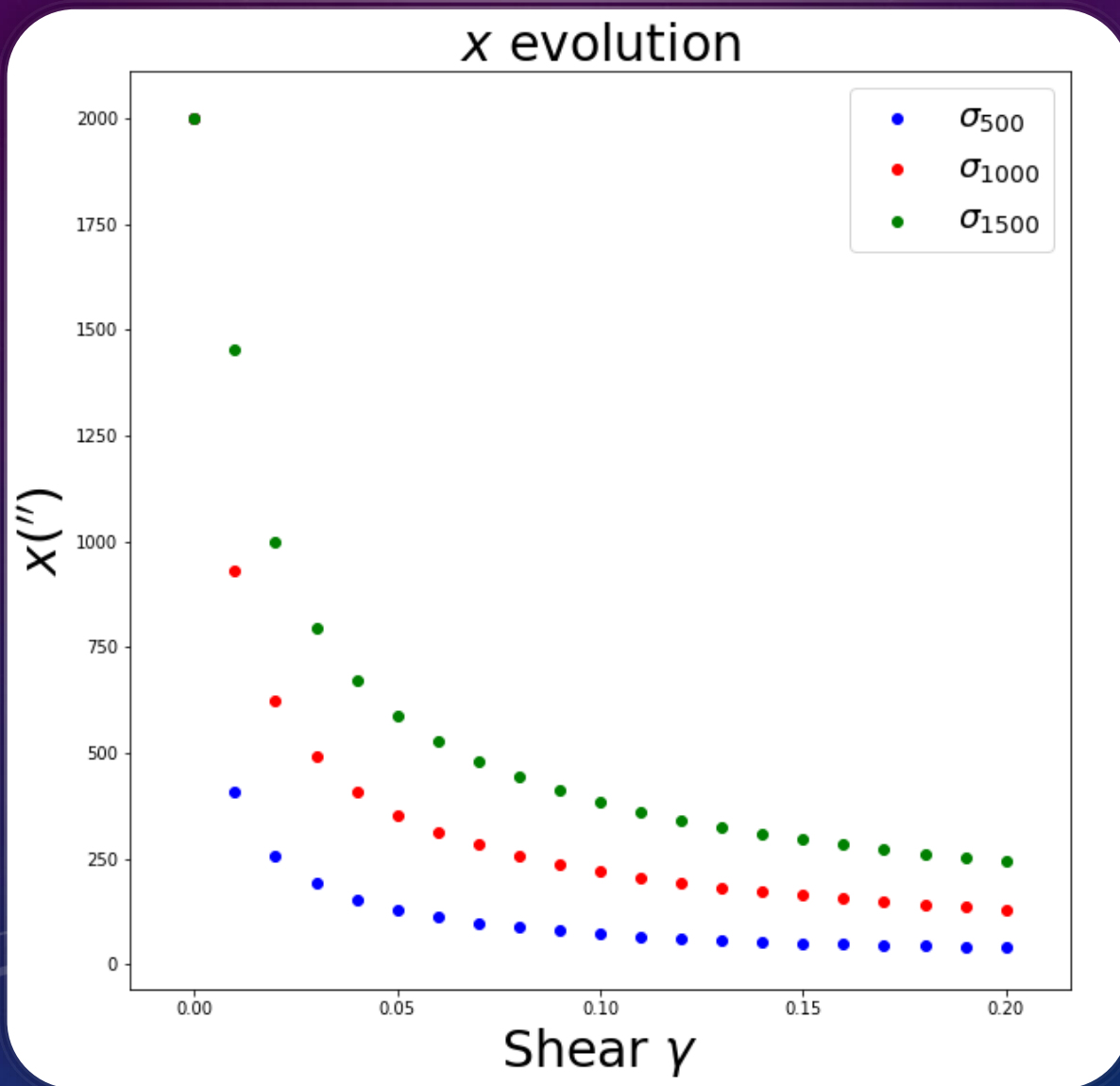
$\chi^2$  evolution



$x, \sigma$  evolution

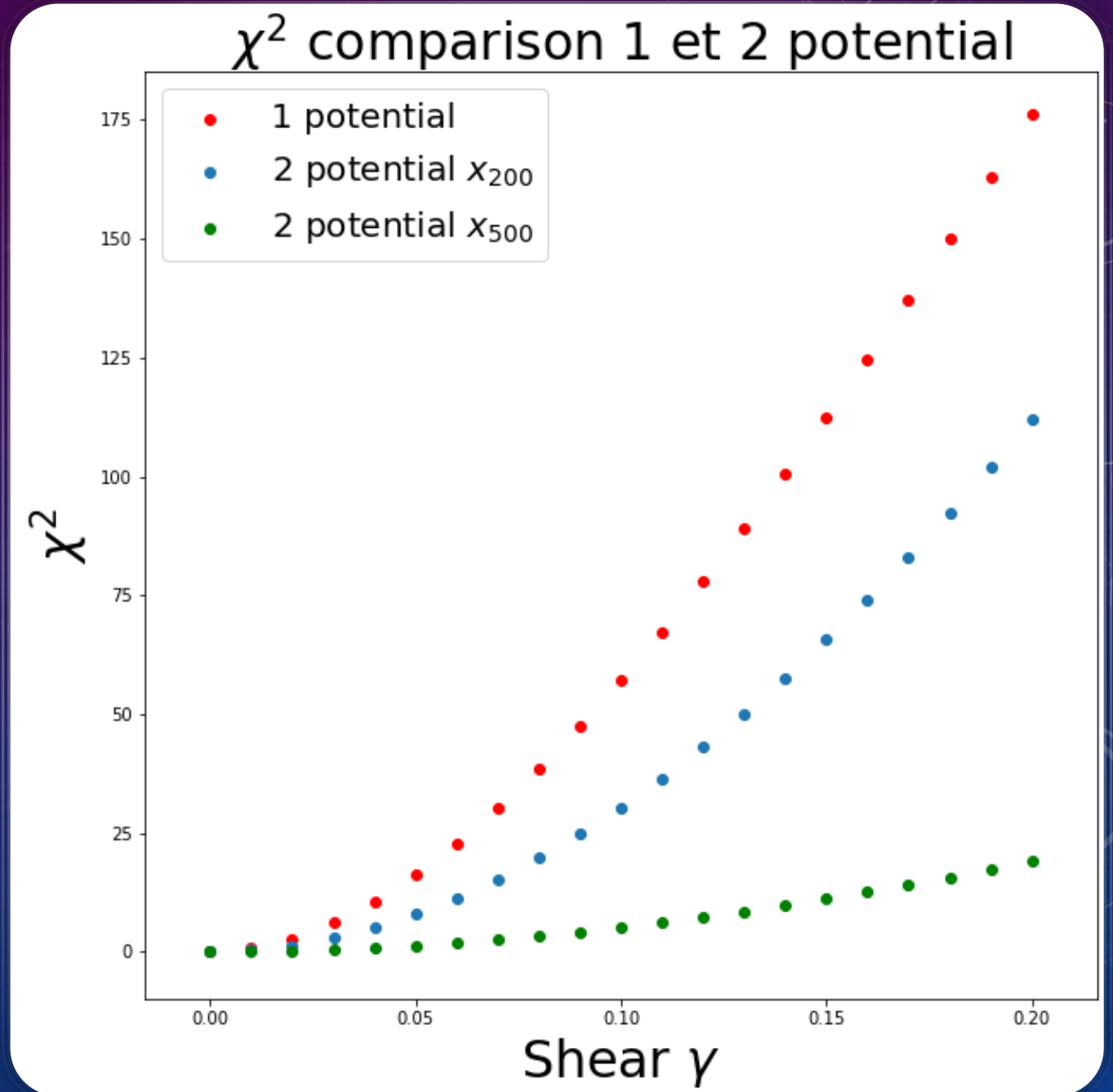


# LENSTOOL: RESULTS FOR 2 POTENTIALS



# LENSTOOL: RESULTS

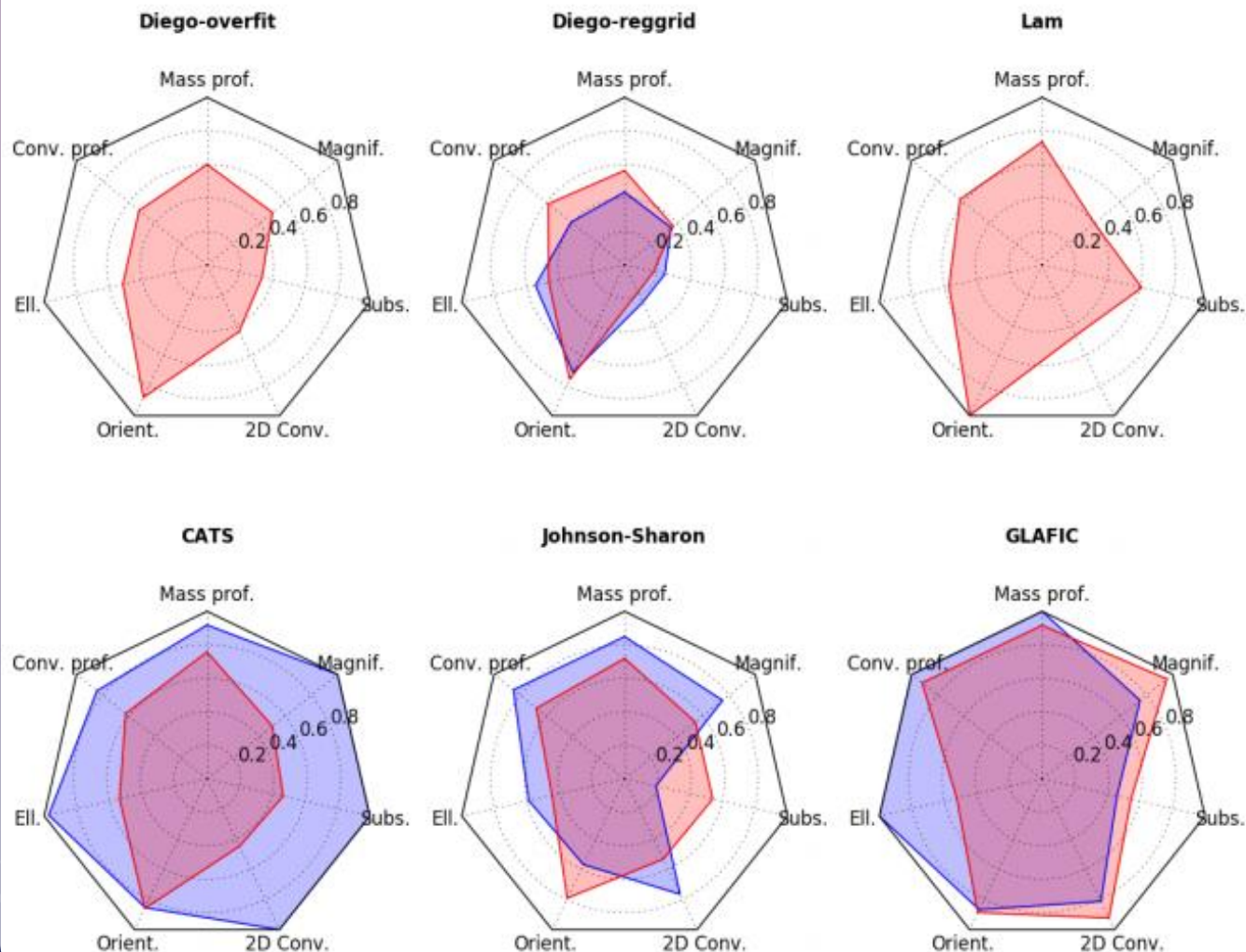
- Better results with 2 potentials
- Model is harder to reproduce with increasing shear





# LENSTOOL: CURRENT LIMIT + OTHER MODELS

## Reconstruction metrics



Red : SPH model  
Blue : Semi-analytical model

CATS uses LENSTOOL

*Meneghetti et al 2017*

# CONCLUSION

- Shear is important to understand the environment effect
- Good reproduction of images with shear when including a 2nd spherical potential
- Considering mass environment what would be the effect on the images ?

- Install C program with svn and compile with all libraries/dependencies
- Understand and use a scientific program
- Understand overall behaviour of the optimisation process for parametric model
- Data Analysis with python
- Visualisation with DS9

Thank you !