

Internship Defense

M2 Astrophysics

Modeling non-linear redshift-space distortions
induced by galaxy peculiar velocities

Rocher Antoine

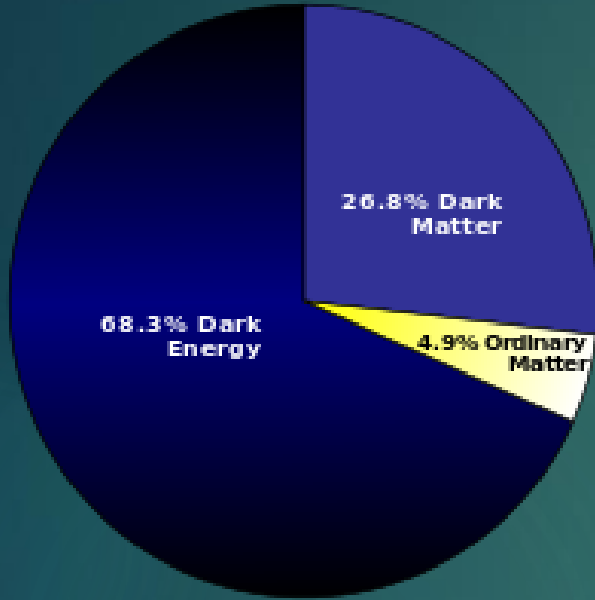
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June, 21st 2019



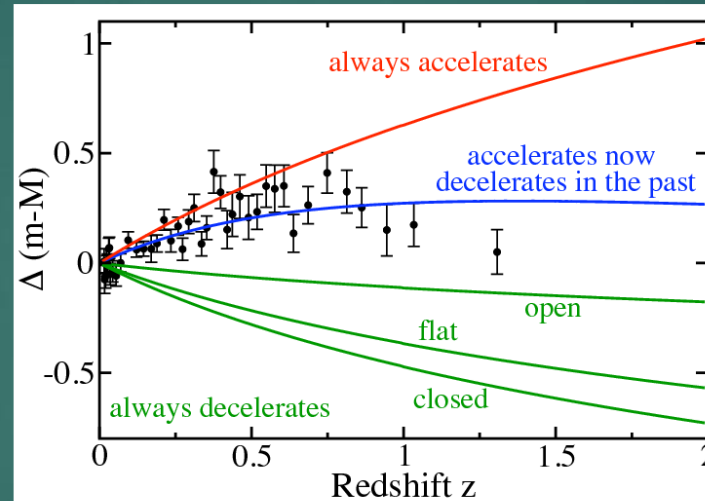
Introduction

Current cosmological model

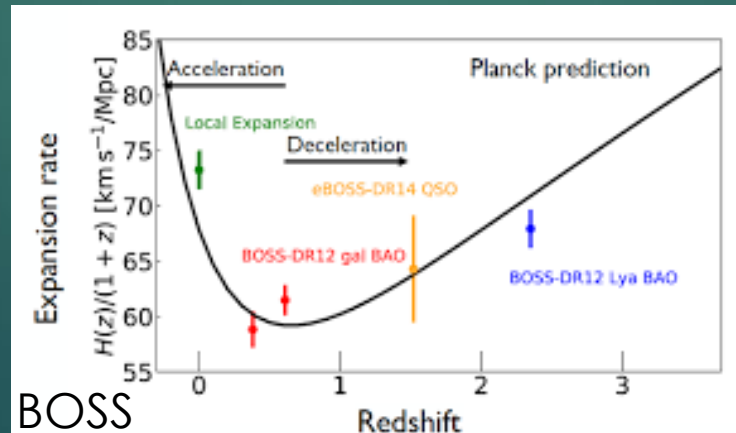


- Expanding Universe, today dominated by Dark Energy
- Two types of matter: Dark and baryonic matter
- Ruled by General Relativity (GR)
- Homogeneous and Isotropic on large scales

- Evidence of an acceleration of the expansion by Supernovae Ia and BAO

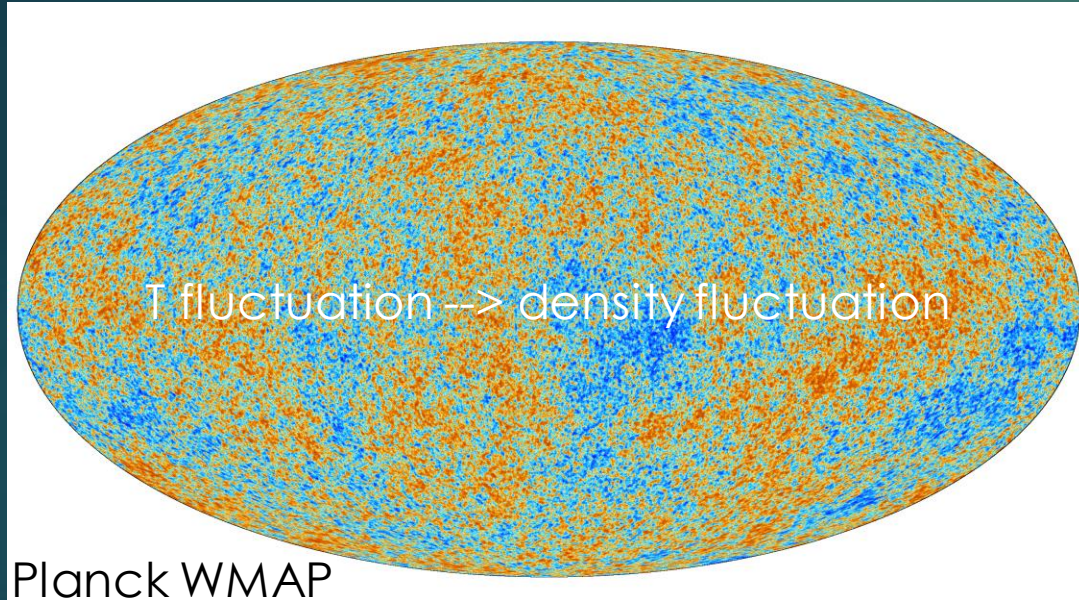


- Can be explained by Dark Energy
- Or deviation from GR ??



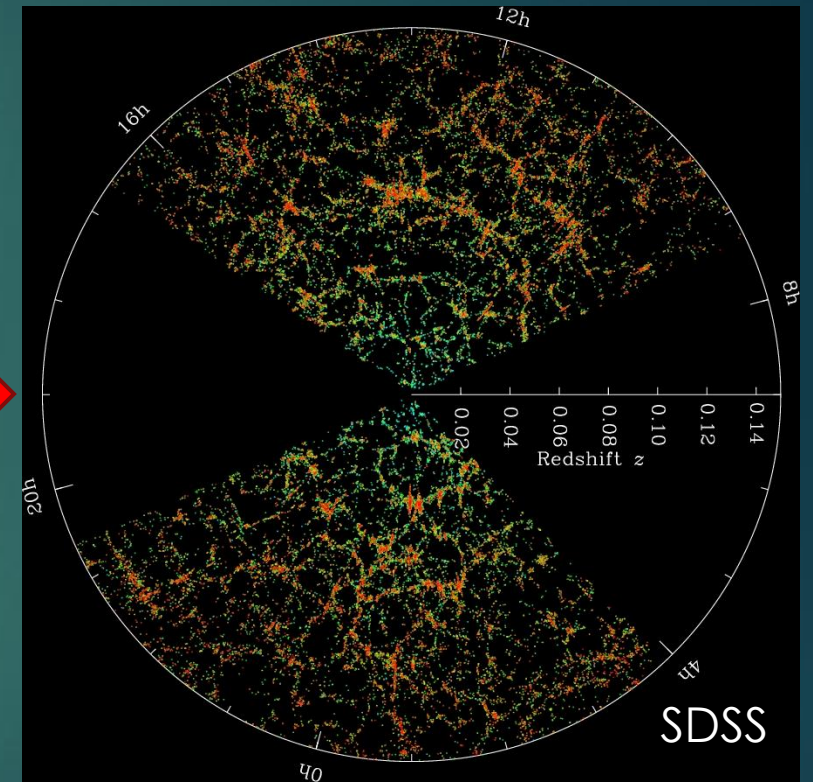
Seek probes to test gravitation and the dynamics of the Universe on large scales

Large Scales Structures (LSS)



Initial density fluctuations

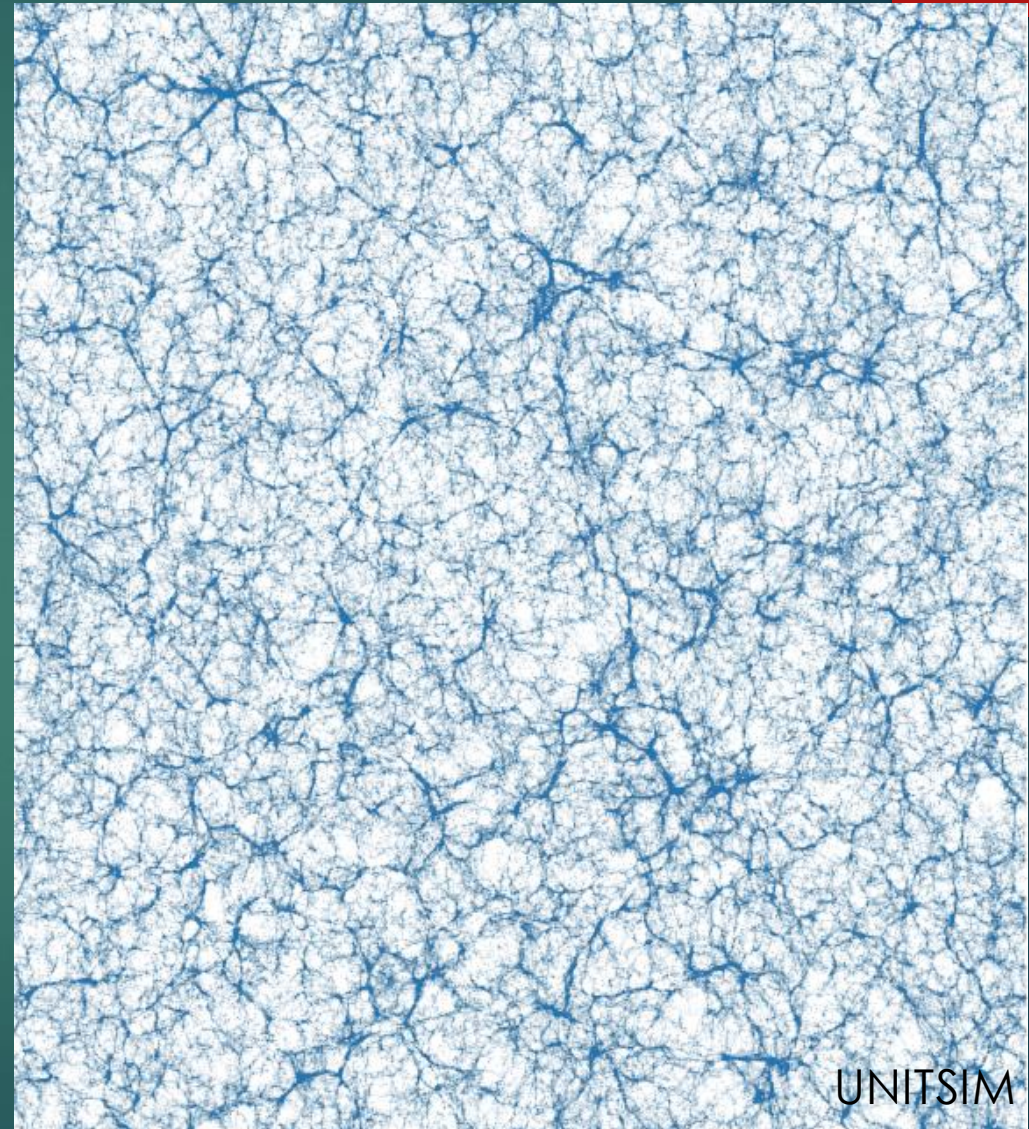
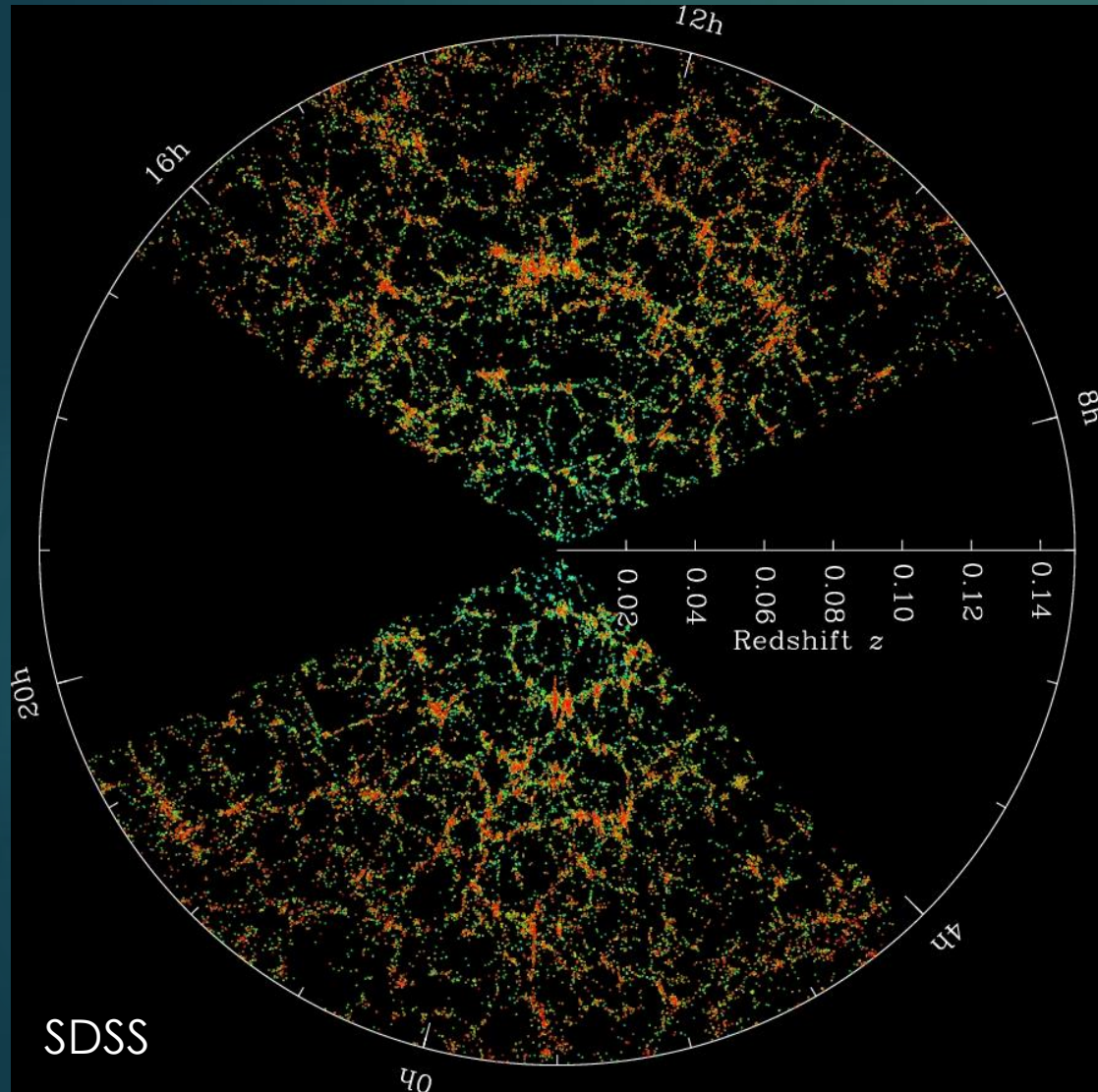
Growth under gravity



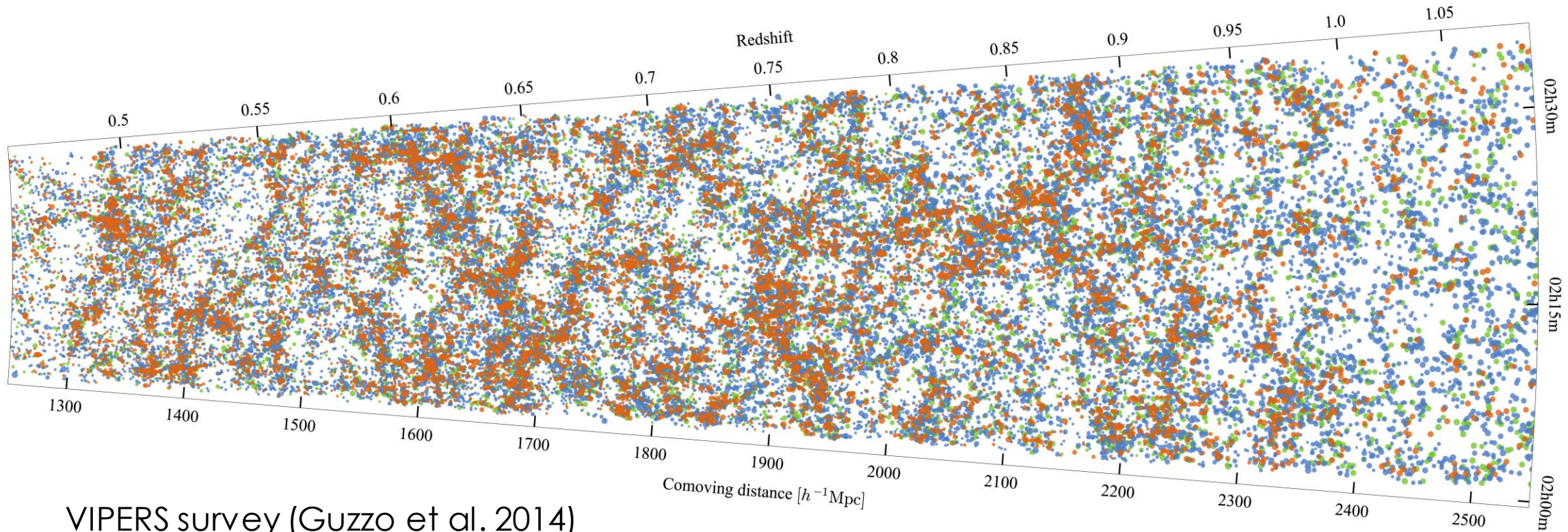
Formation of stars,
galaxies, clusters, ...

Galaxy redshift surveys

Simulation



Galaxy Redshift Surveys



VIPERS survey (Guzzo et al. 2014)



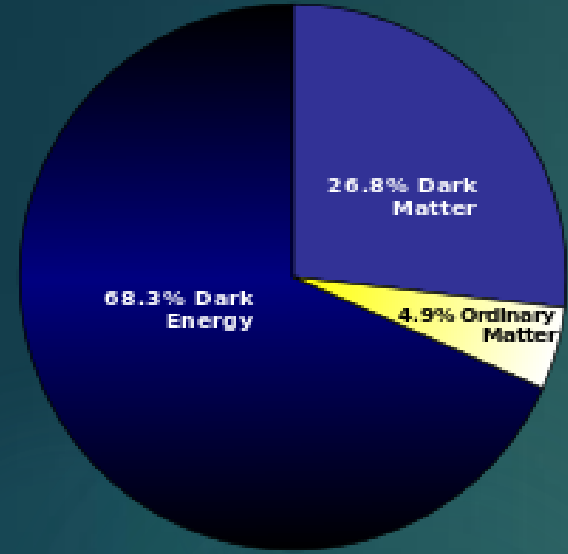
Estimation of
distances with
spectroscopic
redshift



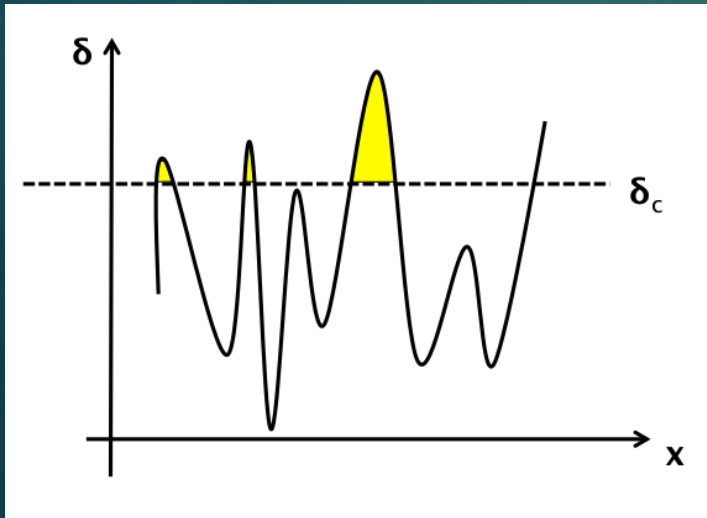
Sensitive to
galaxies peculiar
motions

$$\mathbf{s} = \mathbf{x} + \frac{\mathbf{v}(\mathbf{x}) \cdot \hat{\mathbf{x}}}{aH}$$
$$= \mathbf{x} + f[\mathbf{u}(\mathbf{x}) \cdot \hat{\mathbf{x}}], \quad \mathbf{u} \equiv \frac{\mathbf{v}}{aHf}$$

Galaxy Bias



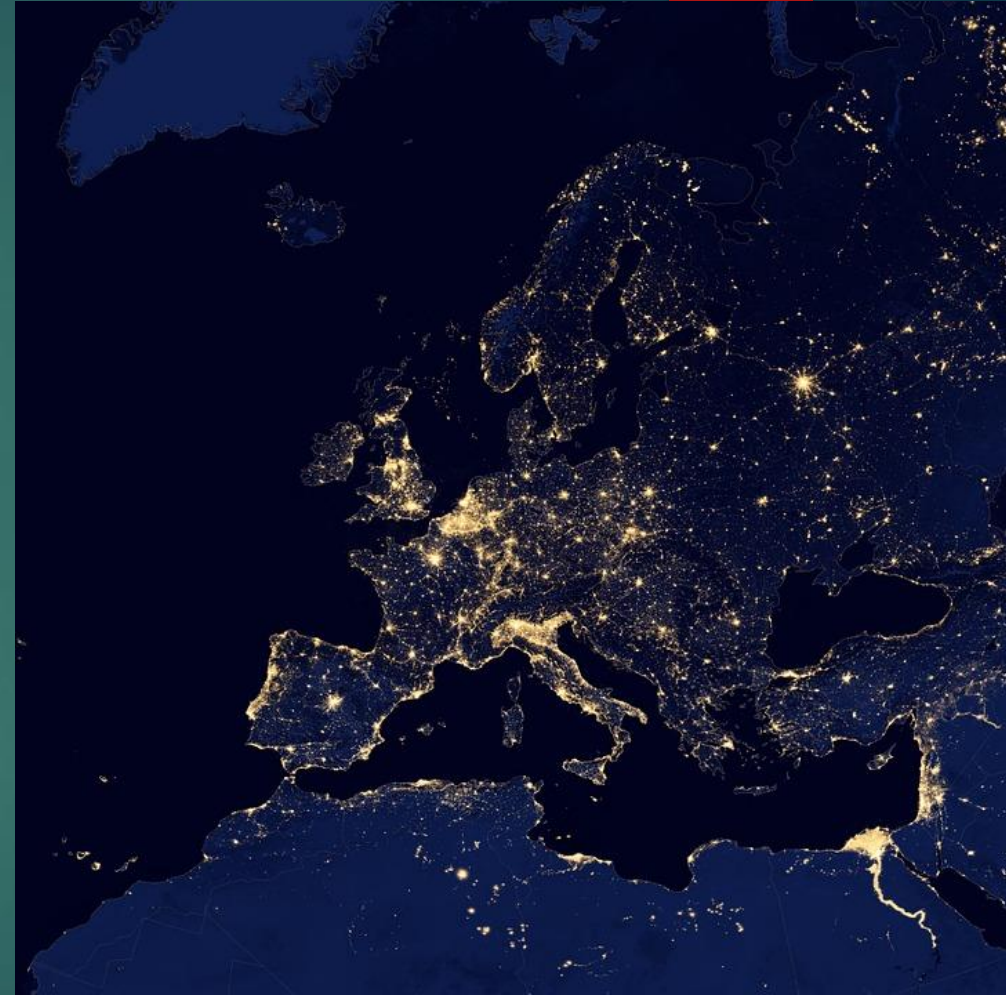
Galaxy field \neq True matter field



If $\delta > 1.68$



collapse and
create structures
(dense peaks)



Observed LSS with redshift surveys

Real space

Redshift space

Galaxies peculiar velocities

$$z = (1 + z_{cosmo}) \left(1 + \frac{v \cdot \hat{l}}{c} \right)$$

$$\begin{aligned} \mathbf{s} &= \mathbf{x} + \frac{\mathbf{v}(\mathbf{x}) \cdot \hat{l}}{aH} \\ &= \mathbf{x} + f[\mathbf{u}(\mathbf{x}) \cdot \hat{l}], \quad \mathbf{u} \equiv \frac{\mathbf{v}}{aHf} \end{aligned}$$

Affects the
apparent
distances along
the line of sight
(los)

Distortions in redshift space



Observed LSS with redshift surveys

Real space

Redshift space

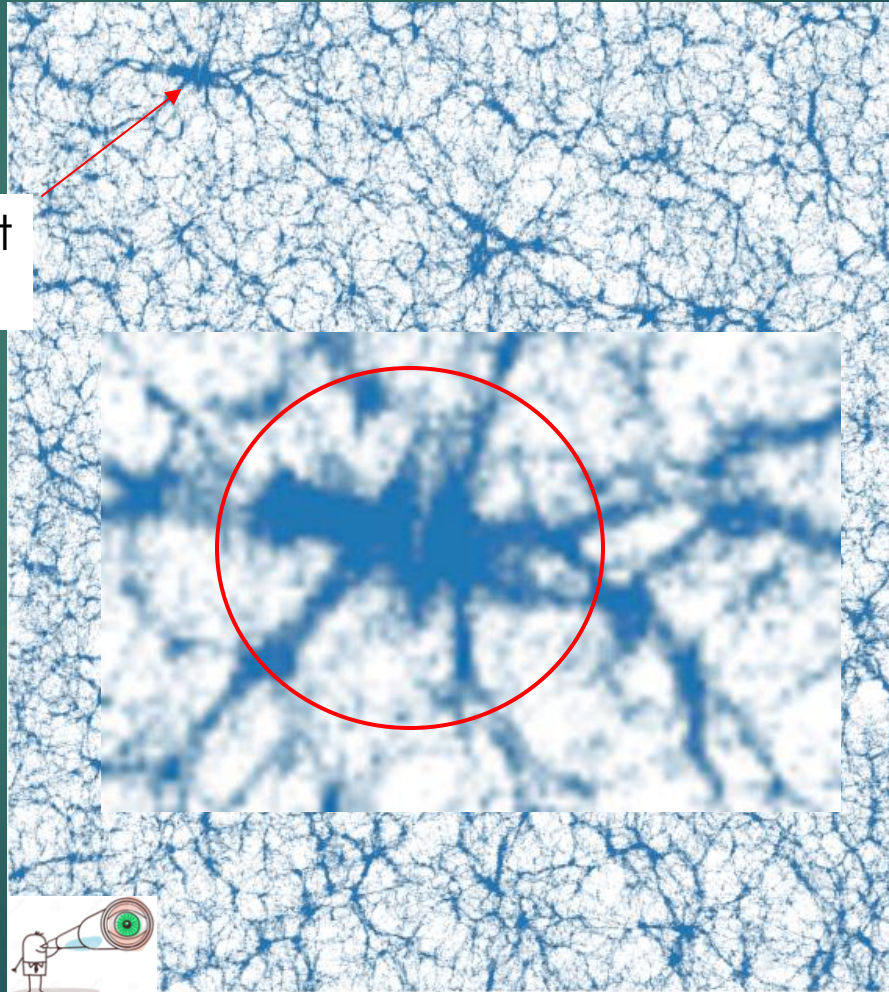
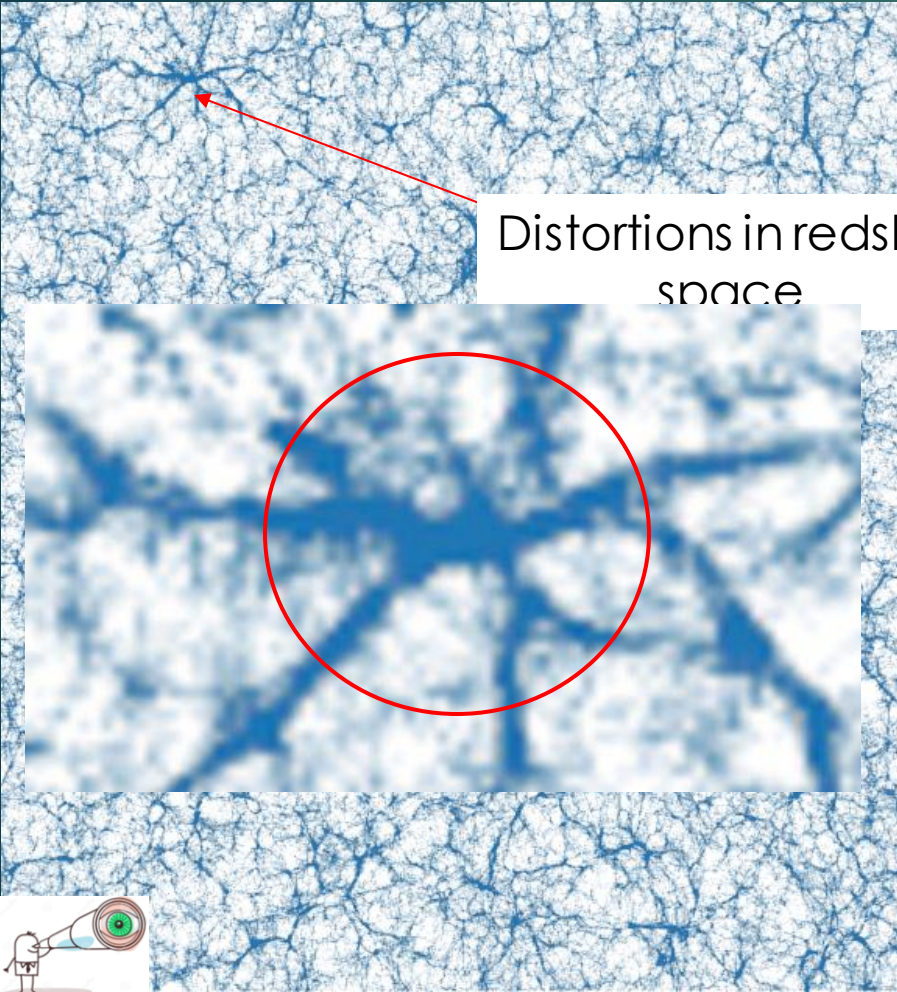
Galaxies peculiar velocities

$$z = (1 + z_{\text{cosmo}}) \left(1 + \frac{v \cdot \hat{l}}{c} \right)$$

$$\mathbf{s} = \mathbf{x} + \frac{\mathbf{v}(\mathbf{x}) \cdot \hat{l}}{aH}$$
$$= \mathbf{x} + f[\mathbf{u}(\mathbf{x}) \cdot \hat{l}], \quad \mathbf{u} \equiv \frac{\mathbf{v}}{aHf}$$

Affects the
apparent
distances along
the line of sight
(los)

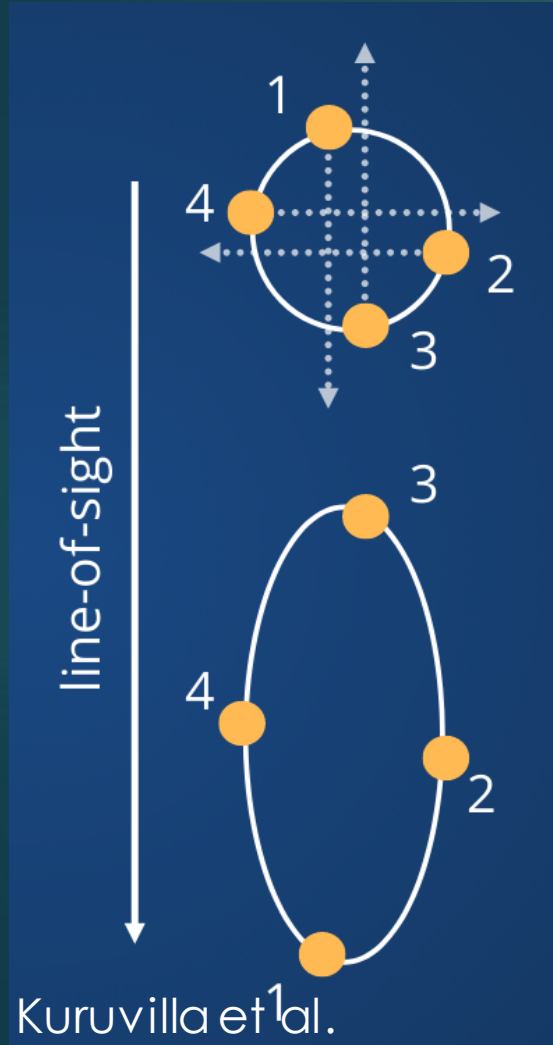
Distortions in redshift space



RSD EFFECT

Small scales : Fingers of God
~Mpc (haloes)

Large scales : Kaiser effect
> ~10 Mpc

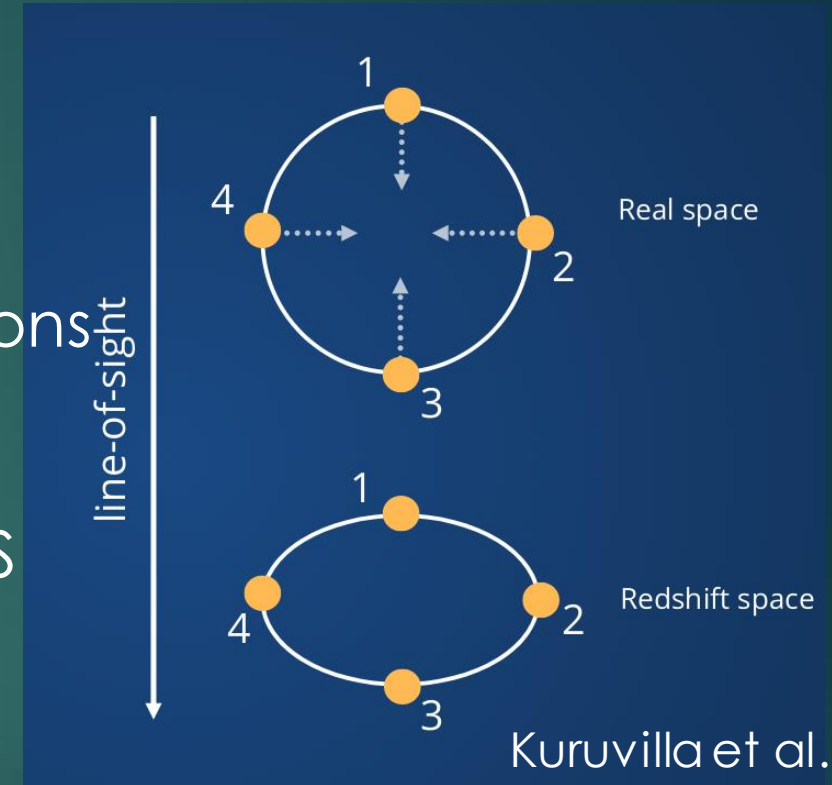


Non linear effect:

- Random motions
- Elongation along LOS

Linear effect:

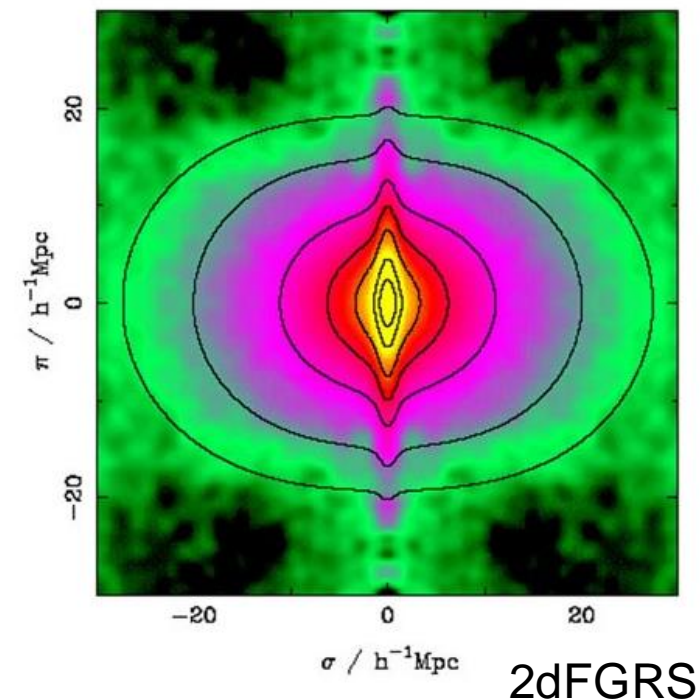
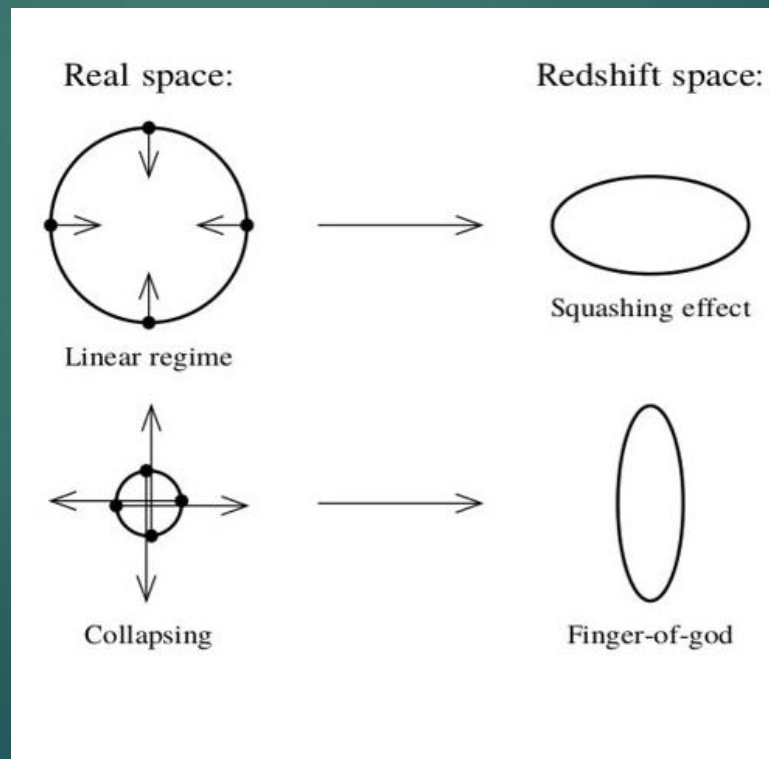
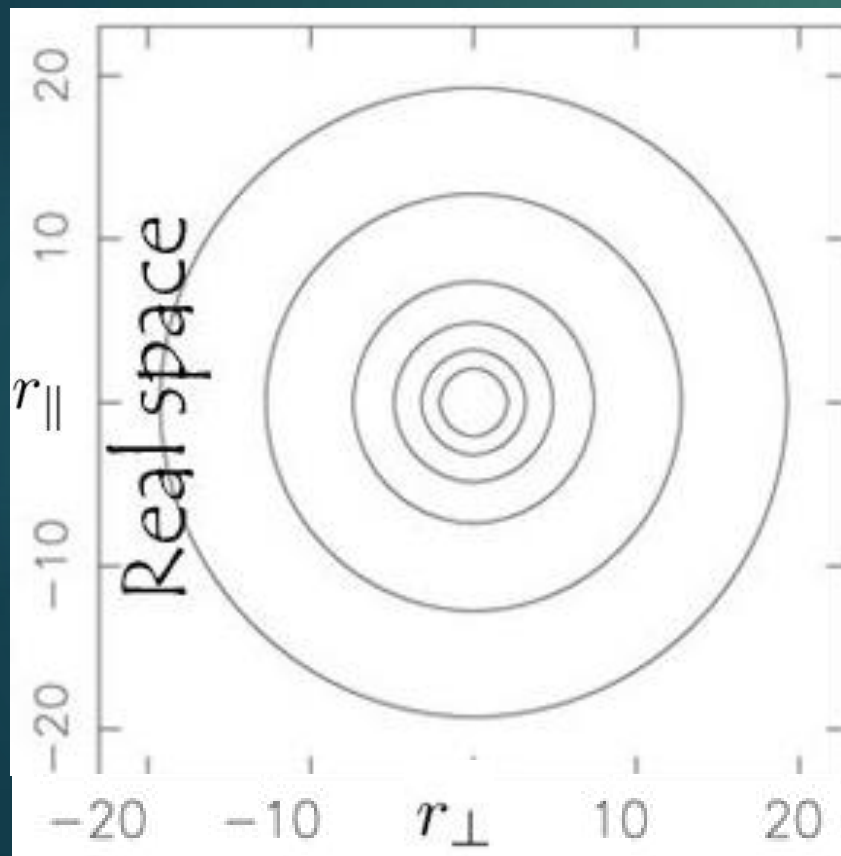
- Coherent motions
- Squashing effect along LOS



=> Anisotropies between parallel and perpendicular component
=> Characterize in redshift spectroscopic surveys

Two-points correlation function

$$dP(\mathbf{r}) = \bar{n}^2 (1 + \xi(\mathbf{r})) dV_1 dV_2$$



Growth rate

In linear theory:

$$\nabla \mathbf{u} = -aH f \delta$$

$$f(a) = \frac{d \ln D}{d \ln a}$$

Growth rate

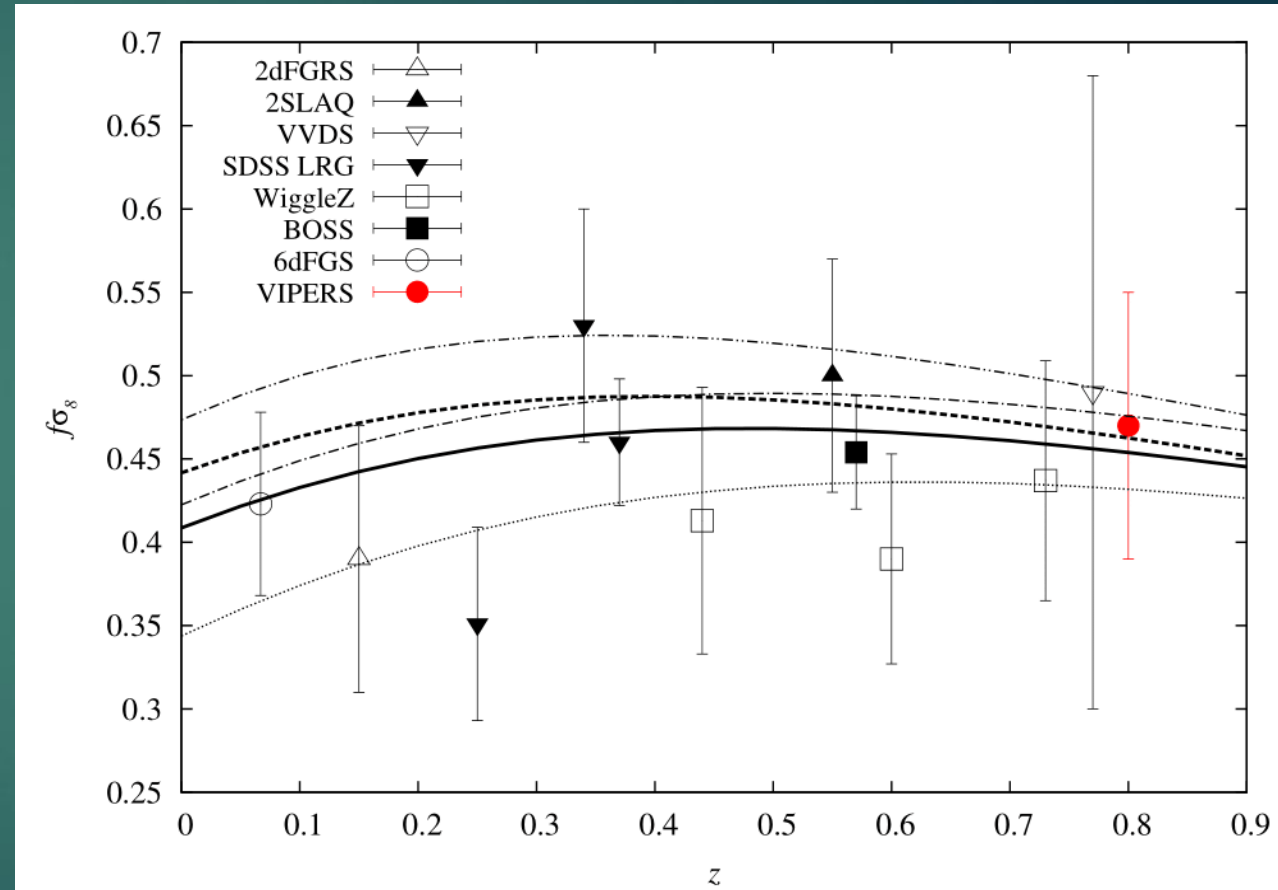
Growth Factor

$f(a)$ describes a which speed structure growth

Predicted by GR: $f(z) \approx \Omega_M(z)^{0.55}$



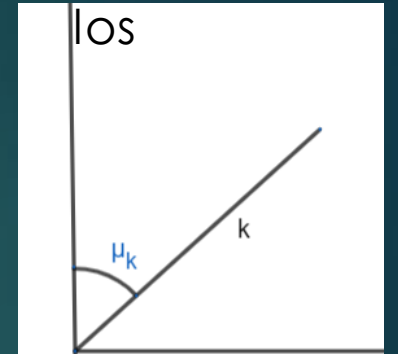
Test RG a large scale



Kaiser linear model

Number of galaxies is conserved

$$n^s(\mathbf{s}) d^3 s = n(\mathbf{r}) d^3 r$$



Small perturbation

$$\delta^s(\mathbf{k}) = (1 + f\mu^2) \delta(\mathbf{k})$$

Small velocity variation

Characteristic scale perturbations is small regarding the distance from us

$$P(k) = \langle \delta(\mathbf{k}_1) \delta(\mathbf{k}_2) \rangle$$

$$P^s(k, \mu) = (1 + f\mu^2)^2 P(k)$$

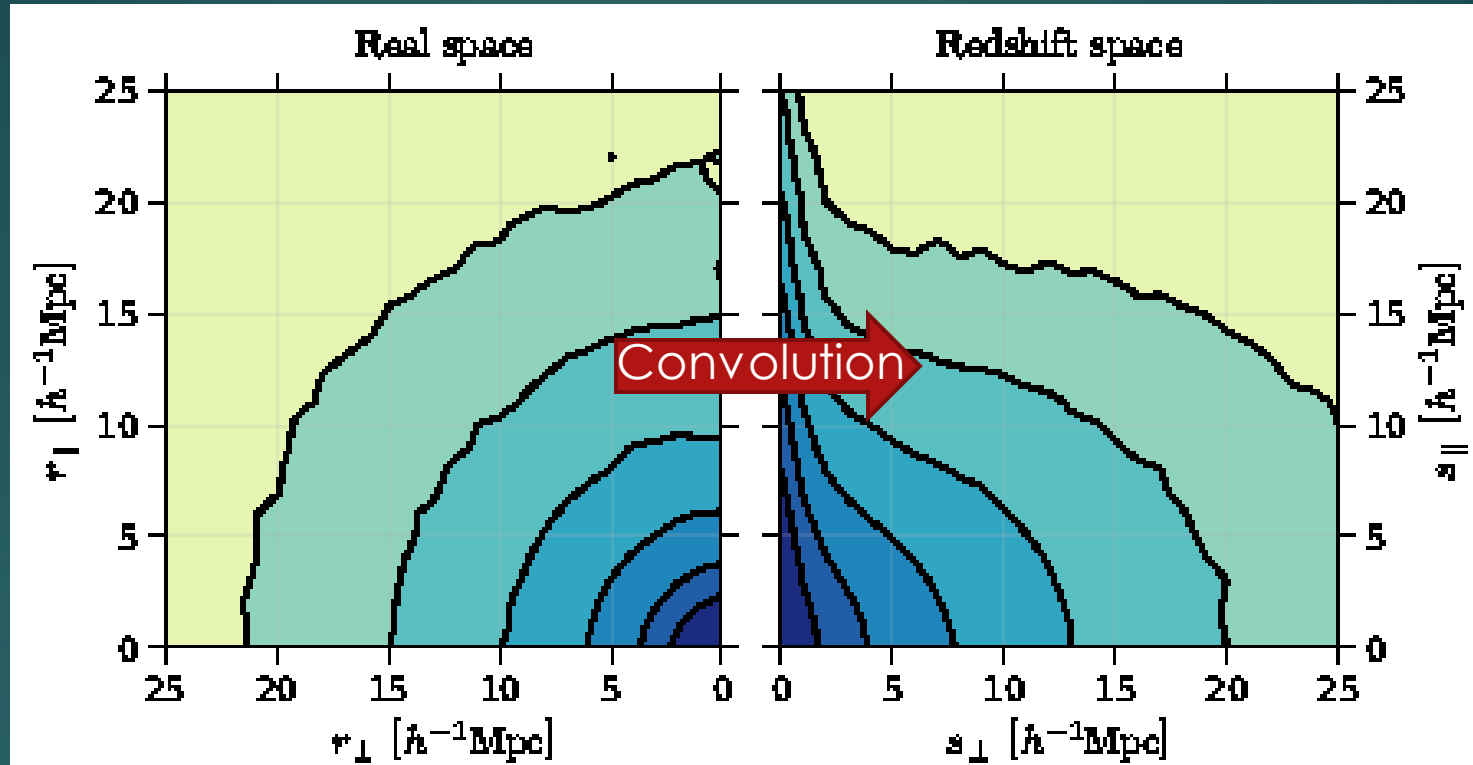
Assuming a linear bias

$$P_g^s(\mathbf{k}) = (1 + \beta\mu^2)^2 P(k)$$

$$\beta = f/b$$

Streaming model

Scoccimaro 2004, Fisher 1995, Peebles 1980



$$1 + \xi_s(s_{\parallel}, s_{\perp}) = \int_{-\infty}^{\infty} dr_{\parallel} [1 + \xi(r)] \mathcal{P}(r_{\parallel} - s_{\parallel}, \mathbf{r})$$

2PCF in redshift space

2PCF in real space

Convolution Kernel
varying with scale

Gaussian streaming model

This model assumes P is Gaussian:

$$1 + \xi_s(s_{\parallel}, s_{\perp}) = \int_{-\infty}^{\infty} dr_{\parallel} [1 + \xi(r)] \mathcal{P}(r_{\parallel} - s_{\parallel}, \mathbf{r})$$

$$\mathcal{P}(v_{12} = s_{\parallel} - r_{\parallel}, \mathbf{r}) = \frac{1}{\sqrt{2\pi\sigma_{12}(\mathbf{r}, \mu_r)}} \exp \left[-\frac{s_{\parallel} - r_{\parallel} - \mu_r v_{12}(\mathbf{r})}{2\sigma_{12}^2(\mathbf{r}, \mu_r)} \right]$$

pairwise velocity probability distribution function

But need to evaluate its moments !

$$\mu_r v_{12}(\mathbf{r})$$

$$\sigma_{12}^2(\mathbf{r}, \mu_r)$$

Fisher 1995 linear prediction

Velocity/density coupling

$$\langle (\vec{v}' - \vec{v}) (1 + \delta) (1 + \delta') \rangle$$

Velocity/Velocity coupling

$$\langle \vec{v}_i \vec{v}_j' \rangle$$

$$v_{12}(\mathbf{r}) = -\hat{r} \frac{fb}{\pi^2} \int_0^\infty dk \, k \, P_m^r(k) j_1(kr)$$

$$\Psi_{\parallel}(\mathbf{r}) = \frac{f^2}{2\pi^2} \int_0^\infty dk P_m^r(k) \left[j_0(kr) - \frac{2j_1(kr)}{kr} \right]$$

$$\Psi_{\perp}(\mathbf{r}) = \frac{f^2}{2\pi^2} \int_0^\infty dk P_m^r(k) \frac{j_1(kr)}{kr}$$

$$\sigma_{12}^2(\mathbf{r}, \mu_r^2) = 2 \left[\sigma_v^2 - \mu_r^2 \Psi_{\parallel}(r) - (1 - \mu_r^2) \Psi_{\perp}(r) \right]$$

Convolution Lagrangian Perturbation Theory

Eulerian (\mathbf{x})– Lagrangian (\mathbf{q}) mapping

$$\mathbf{x}(\mathbf{q}, t) = \mathbf{q} + \Psi(\mathbf{q}, t) \rightarrow \text{Displacement field}$$

Conservation equation

$$[1 + \delta_m(\mathbf{x}, t)] d^3x = [1 + \delta_m(\mathbf{q}, t_0)] d^3q$$

$$1 + \delta_m(\mathbf{x}, t) = [1 + \delta_m(\mathbf{q}, t_0)] \left| \frac{d^3\mathbf{x}}{d^3\mathbf{q}} \right|^{-1}$$

$$1 + \delta(\mathbf{x}, t) = \int d^3q \delta_D^3[\mathbf{x} - \mathbf{q} - \Psi(\mathbf{q}, t)]$$

$$1 + \xi(\mathbf{r}) = \int d^3q M_0(\mathbf{r}, \mathbf{q})$$

$$v_{12,n}(\mathbf{r}) = [1 + \xi(r)]^{-1} \int d^3q M_{1,n}(\mathbf{r}, \mathbf{q})$$

$$\sigma_{12,nm}^2(\mathbf{r}) = [1 + \xi(r)]^{-1} \int d^3q M_{2,nm}(\mathbf{r}, \mathbf{q})$$

M_1 et M_2 are 1st and 2nd derivative of M_0

$$1 + \xi_X(\mathbf{r}) = \int d^3q \int \frac{d^3k}{(2\pi)^3} e^{i\mathbf{k} \cdot (\mathbf{q} - \mathbf{r})} \int \frac{d\lambda_1}{2\pi} \frac{d\lambda_2}{2\pi} \tilde{F}_1 \tilde{F}_2 K(\mathbf{q}, \mathbf{k}, \lambda_1, \lambda_2)$$

$$K(\mathbf{q}, \mathbf{k}, \lambda_1, \lambda_2) = \left\langle e^{i(\lambda_1 \delta_1 + \lambda_2 \delta_2 + \mathbf{k} \cdot \vec{\Delta})} \right\rangle \quad \text{and} \quad \Delta \equiv \vec{\Psi}_2 - \vec{\Psi}_1$$

CLPT Predictions

Cumulant expansion

$$\langle e^{iX} \rangle = \exp \left[\sum_{N=1}^{\infty} \frac{i^N}{N!} \langle X^N \rangle_c \right]$$

$$M_0 = \frac{1}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 1 + \langle F' \rangle^2 \xi_R - 2 \langle F' \rangle U_i g_i + \frac{1}{2} \langle F'' \rangle^2 \xi_R - 2 \langle F' \rangle \langle F'' \rangle \xi_R U_i g_i \right. \\ \left. - [\langle F'' \rangle + \langle F' \rangle^2] \underline{U_i U_j G_{ij}} + \frac{1}{6} \underline{W_{ijk} \Gamma_{ijk}} - \langle F' \rangle \underline{A_{ij}^{10} G_{ij}} - \langle F'' \rangle U_i^{20} g_i - \langle F' \rangle^2 U_i^{11} g_i + O(P_L^3) \right\} \quad (76)$$

$$M_{1,n} = \frac{f^2}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 2 \langle F' \rangle \dot{U}_n - g_i \dot{A}_{in} + \langle F'' \rangle \dot{U}_n^{20} + \langle F' \rangle^2 \dot{U}_n^{11} + 2 \langle F' \rangle \langle F'' \rangle \xi_L \dot{U}_n \right. \\ \left. - 2 \langle F' \rangle g_i \dot{A}_{in}^{10} - \frac{1}{2} G_{ij} \dot{W}_{ijn} - 2[\langle F'' \rangle + \langle F' \rangle^2] g_i U_i \dot{U}_n - \langle F' \rangle^2 \xi_L g_i \dot{A}_{in} - 2 \langle F' \rangle G_{ij} U_i \dot{A}_{in} + O(P_L^3) \right\} \quad (77)$$

$$M_{2,nm} = \frac{f^2}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 2[\underline{\langle F' \rangle^2} + \underline{\langle F'' \rangle}] \dot{U}_n \dot{U}_m - 2 \langle F' \rangle (\dot{A}_{in} g_i \dot{U}_m + \dot{A}_{im} g_i \dot{U}_n) \right. \\ \left. - \dot{A}_{im} \dot{A}_{jn} G_{ij} + [1 + \langle F' \rangle^2 \xi_L - 2 \langle F' \rangle U_i g_i] \ddot{A}_{nm} + 2 \langle F' \rangle \ddot{A}_{nm}^{10} - \ddot{W}_{inm} g_i + O(P_L^3) \right\} \quad (78)$$

Cumulants

$$\langle \delta_1^m \delta_2^n \Delta_{i_1} \dots \Delta_{i_r} \rangle$$

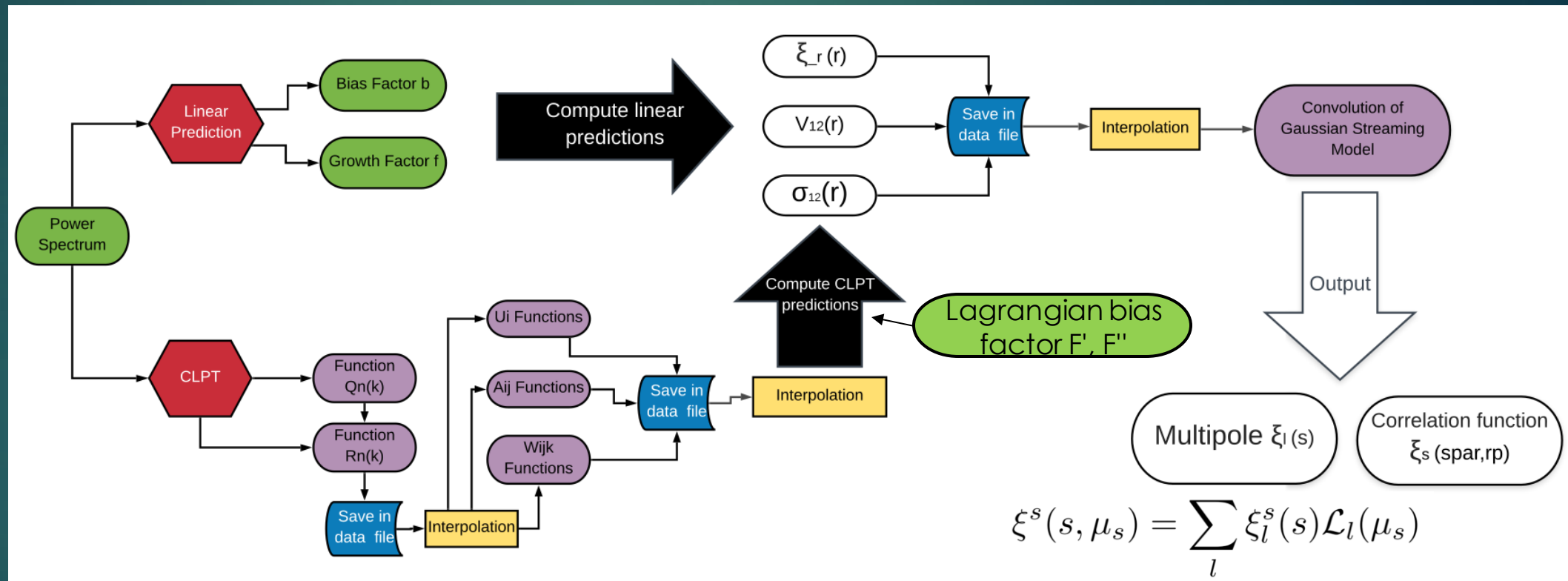
Quasi linear regime
Cut at order 2

Lagrangian bias

My work

I Wrote a C code of the GSM with linear and CLPT predictions

Cosmo
 Ω_m, h, σ_8



My work

$$M_0 = \frac{1}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 1 + \langle F' \rangle^2 \xi_R - 2 \langle F' \rangle U_i g_i + \frac{1}{2} \langle F'' \rangle^2 \xi_R - 2 \langle F' \rangle \langle F'' \rangle \xi_R U_i g_i \right. \\ \left. - [\langle F'' \rangle + \langle F' \rangle^2] U_i U_j G_{ij} + \frac{1}{6} W_{ijk} \Gamma_{ijk} - \langle F' \rangle A_{ij}^{10} G_{ij} - \langle F'' \rangle U_i^{20} g_i - \langle F' \rangle^2 U_i^{11} g_i + O(P_L^3) \right\} \quad (76)$$

$$M_{1,n} = \frac{f^2}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 2 \langle F' \rangle \dot{U}_n - g_i \dot{A}_{in} + \langle F'' \rangle \dot{U}_n^{20} + \langle F' \rangle^2 \dot{U}_n^{11} + 2 \langle F' \rangle \langle F'' \rangle \xi_L \dot{U}_n \right. \\ \left. - 2 \langle F' \rangle g_i \dot{A}_{in}^{10} - \frac{1}{2} G_{ij} \dot{W}_{ijn} - 2[\langle F'' \rangle + \langle F' \rangle^2] g_i U_i \dot{U}_n - \langle F' \rangle^2 \xi_L g_i \dot{A}_{in} - 2 \langle F' \rangle G_{ij} U_i \dot{A}_{in} + O(P_L^3) \right\} \quad (77)$$

$$M_{2,nm} = \frac{f^2}{(2\pi)^{3/2}|A|^{1/2}} e^{-\frac{1}{2}(r-q)^T \mathbf{A}^{-1}(r-q)} \times \left\{ 2[\langle F' \rangle^2 + \langle F'' \rangle] \dot{U}_n \dot{U}_m - 2 \langle F' \rangle (\dot{A}_{in} g_i \dot{U}_m + \dot{A}_{im} g_i \dot{U}_n) \right. \\ \left. - \dot{A}_{im} \dot{A}_{jn} G_{ij} + [1 + \langle F' \rangle^2 \xi_L - 2 \langle F' \rangle U_i g_i] \ddot{A}_{nm} + 2 \langle F' \rangle \ddot{A}_{nm}^{10} - \ddot{W}_{inm} g_i + O(P_L^3) \right\} \quad (78)$$

My work

Finally...

$$U_i = U_i^{(1)} + U_i^{(3)} + \dots, \quad U_i^{20} = U_i^{20(2)} + \dots, \quad U_i^{11} = U_i^{11(2)} + \dots, \\ A_{ij} = A_{ij}^{(11)} + A_{ij}^{(22)} + A_{ij}^{(13)} + A_{ij}^{(31)} + \dots, \quad A_{ij}^{10} = A_{ij}^{10(12)} + A_{ij}^{10(21)} + \dots \\ W_{ijk} = W_{ijk}^{(112)} + W_{ijk}^{(121)} + W_{ijk}^{(211)} + \dots.$$

$$\dot{U}_n = \frac{\langle \delta_1 \dot{\Delta}_n \rangle}{f} = U_n^{(1)} + 3U_n^{(3)} + \dots, \quad \dot{U}_n^{20} = \frac{\langle \delta_1^2 \dot{\Delta}_n \rangle}{f} = U_n^{20(2)} + \dots, \quad \dot{U}_n^{11} = \frac{\langle \delta_1 \delta_2 \dot{\Delta}_n \rangle}{f} = U_n^{11(2)} + \dots \\ \dot{A}_{in} = \frac{\langle \Delta_i \dot{\Delta}_n \rangle}{f} = A_{in}^{(11)} + 3A_{in}^{(13)} + A_{in}^{(31)} + 2A_{in}^{(22)} + \dots, \quad \dot{A}_{in}^{10} = \frac{\langle \delta_1 \Delta_i \dot{\Delta}_n \rangle}{f} = 2A_{in}^{10(12)} + A_{in}^{10(21)} + \dots \\ \dot{W}_{ijn} = \frac{\langle \delta_1 \Delta_i \Delta_j \dot{\Delta}_n \rangle}{f} = 2W_{ijn}^{(112)} + W_{ijn}^{(121)} + W_{ijn}^{(211)} + \dots$$

$$U_i^{mn(p)} = \langle \delta_1^m \delta_2^n \Delta_i^{(p)} \rangle_c, \quad A_{ij}^{mn(pq)} = \langle \delta_1^m \delta_2^n \Delta_i^{(p)} \Delta_j^{(q)} \rangle_c \\ W_{ijk}^{mn(pqr)} = \langle \delta_1^m \delta_2^n \Delta_i^{(p)} \Delta_j^{(q)} \Delta_k^{(r)} \rangle_c,$$

$$R_n(k) = \frac{k^3}{4\pi^2} P_L(k) \int_0^\infty dr P_L(kr) \tilde{R}_n(r)$$

$$Q_n(k) = \frac{k^3}{4\pi^2} \int_0^\infty dr P_L(kr) \int_{-1}^1 dx P_L(k\sqrt{y}) Q_n(r, x),$$

$$\ddot{A}_{nm} = \frac{\langle \dot{\Delta}_n \dot{\Delta}_m \rangle}{f^2} = A_{nm}^{(11)} + 3A_{nm}^{(13)} + 3A_{nm}^{(31)} + 4A_{nm}^{(22)}, \\ \ddot{A}_{10,nm} = \frac{\langle \delta_1 \dot{\Delta}_n \dot{\Delta}_m \rangle}{f^2} = 2A_{nm}^{10(12)} + 2A_{nm}^{10(21)}, \\ \ddot{W}_{inm} = \frac{\langle \delta_1 \Delta_i \dot{\Delta}_n \dot{\Delta}_m \rangle}{f^2} = 2W_{inm}^{(112)} + 2W_{inm}^{(121)} + W_{inm}^{(211)}.$$

$$Q_1 = \frac{r^2(1-x^2)^2}{y^2}, \quad Q_2 = \frac{(1-x^2)rx(1-rx)}{y^2}, \\ Q_5 = \frac{rx(1-x^2)}{y}, \quad Q_8 = \frac{r^2(1-x^2)}{y},$$

$$\tilde{R}_1(r) = \int_{-1}^{+1} dx \frac{r^2(1-x^2)^2}{1+r^2-2rx}$$

$$\tilde{R}_2(r) = \int_{-1}^{+1} dx \frac{(1-x^2)rx(1-rx)}{1+r^2-2rx}$$

$$\xi_L(q) = \frac{1}{2\pi^2} \int_0^\infty dk k^2 P_L(k) j_0(kq)$$

$$V_1^{(112)}(q) = \frac{1}{2\pi^2} \int_0^\infty \frac{dk}{k} \left(-\frac{3}{7}\right) R_1(k) j_1(kq)$$

$$V_3^{(112)}(q) = \frac{1}{2\pi^2} \int_0^\infty \frac{dk}{k} \left(-\frac{3}{7}\right) Q_1(k) j_1(kq)$$

$$S^{(112)}(q) = \frac{1}{2\pi^2} \int_0^\infty \frac{dk}{k} \frac{3}{7} [2R_1(k) + 4R_2(k) + Q_1(k) + 2Q_2(k)] \frac{j_2(kq)}{kq}$$

$$T^{(112)}(q) = \frac{1}{2\pi^2} \int_0^\infty \frac{dk}{k} \left(-\frac{3}{7}\right) \times \\ [2R_1 + 4R_2 + Q_1 + 2Q_2] j_3(kq)$$

$$U^{(1)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk k (-1) P_L(k) j_1(kq)$$

$$U^{(3)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk k \left(-\frac{5}{21}\right) R_1(k) j_1(kq)$$

$$U_{20}^{(2)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk k \left(-\frac{3}{7}\right) Q_8(k) j_1(kq)$$

$$U_{11}^{(2)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk k \left(-\frac{6}{7}\right) [R_1(k) + R_2(k)] j_1(kq)$$

$$X_{10}^{(12)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \frac{1}{14} \left\{ 2[R_1(k) - R_2(k)] + 3R_1(k) j_0(kq) \right. \\ \left. - 3[3R_1(k) + 4R_2(k) + 2Q_5(k)] \frac{j_1(kq)}{kq} \right\}$$

$$Y_{10}^{(12)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \left(-\frac{3}{14}\right) [3R_1(k) + 4R_2(k) + 2Q_5(k)] \times \left[j_0(kq) - 3 \frac{j_1(kq)}{kq} \right]$$

$$X^{(11)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk P_L(k) \left[\frac{2}{3} - 2 \frac{j_1(kq)}{kq} \right]$$

$$X^{(22)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \frac{9}{98} Q_1(k) \left[\frac{2}{3} - 2 \frac{j_1(kq)}{kq} \right]$$

$$X^{(13)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \frac{5}{21} R_1(k) \left[\frac{2}{3} - 2 \frac{j_1(kq)}{kq} \right]$$

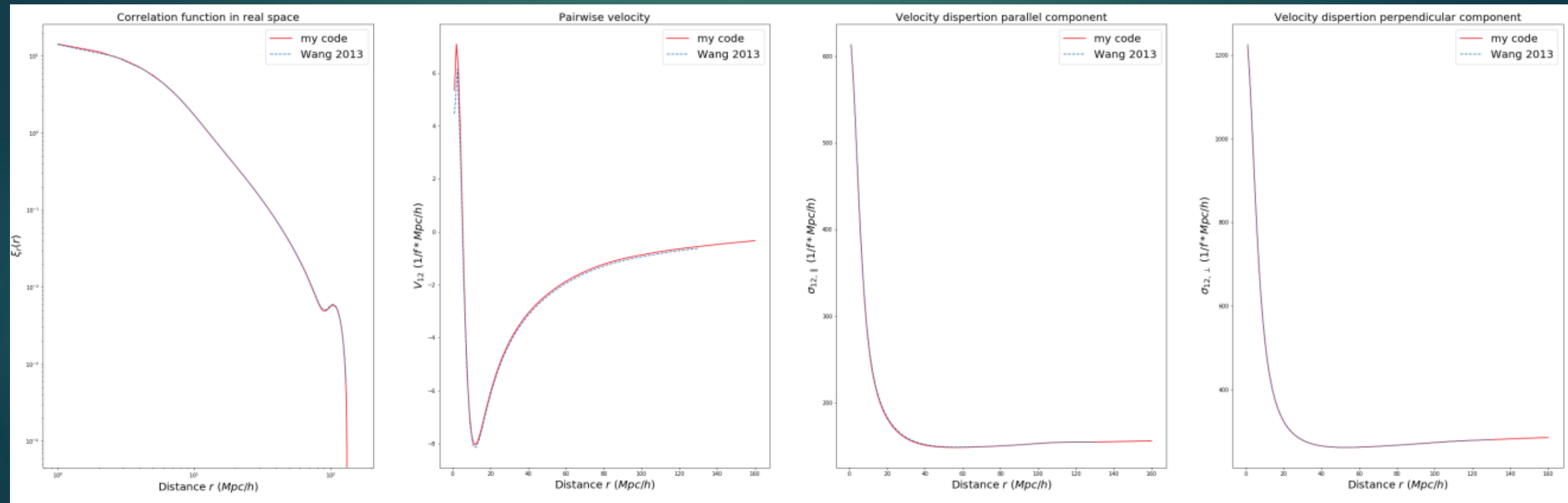
$$Y^{(11)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk P_L(k) \left[-2j_0(kq) + 6 \frac{j_1(kq)}{kq} \right]$$

$$Y^{(22)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \frac{9}{98} Q_1(k) \left[-2j_0(kq) + 6 \frac{j_1(kq)}{kq} \right]$$

$$Y^{(13)}(q) = \frac{1}{2\pi^2} \int_0^\infty dk \frac{5}{21} R_1(k) \left[-2j_0(kq) + 6 \frac{j_1(kq)}{kq} \right]$$

Code comparison results

CLPT moments comparison with code from Reid et al. 2011



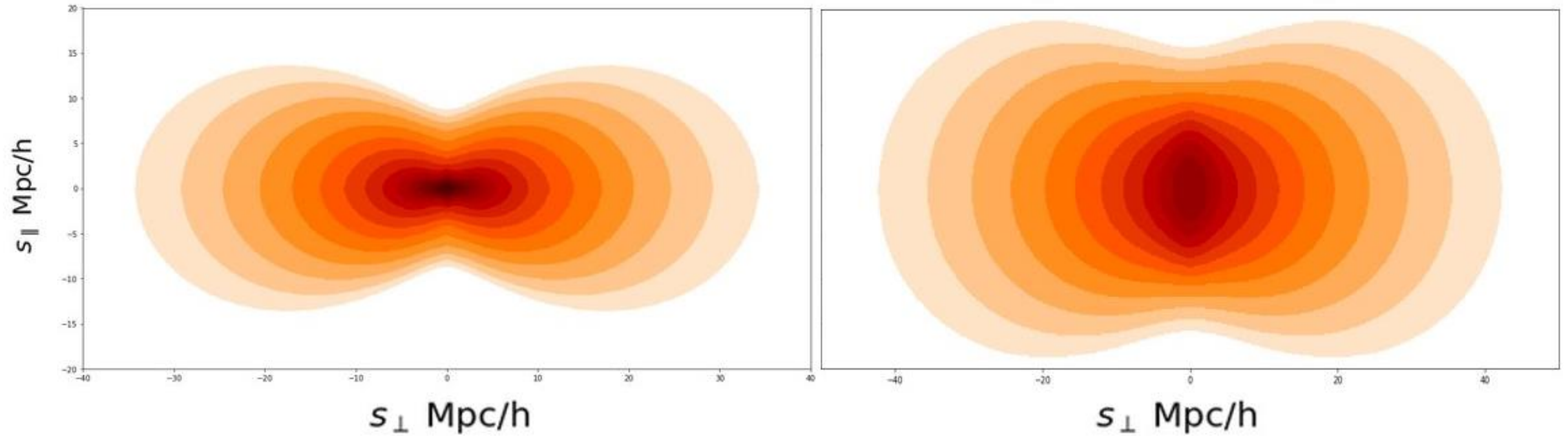
Perfect agreement when taking same inputs

Code predictions

CLPT two-point correlation function contours

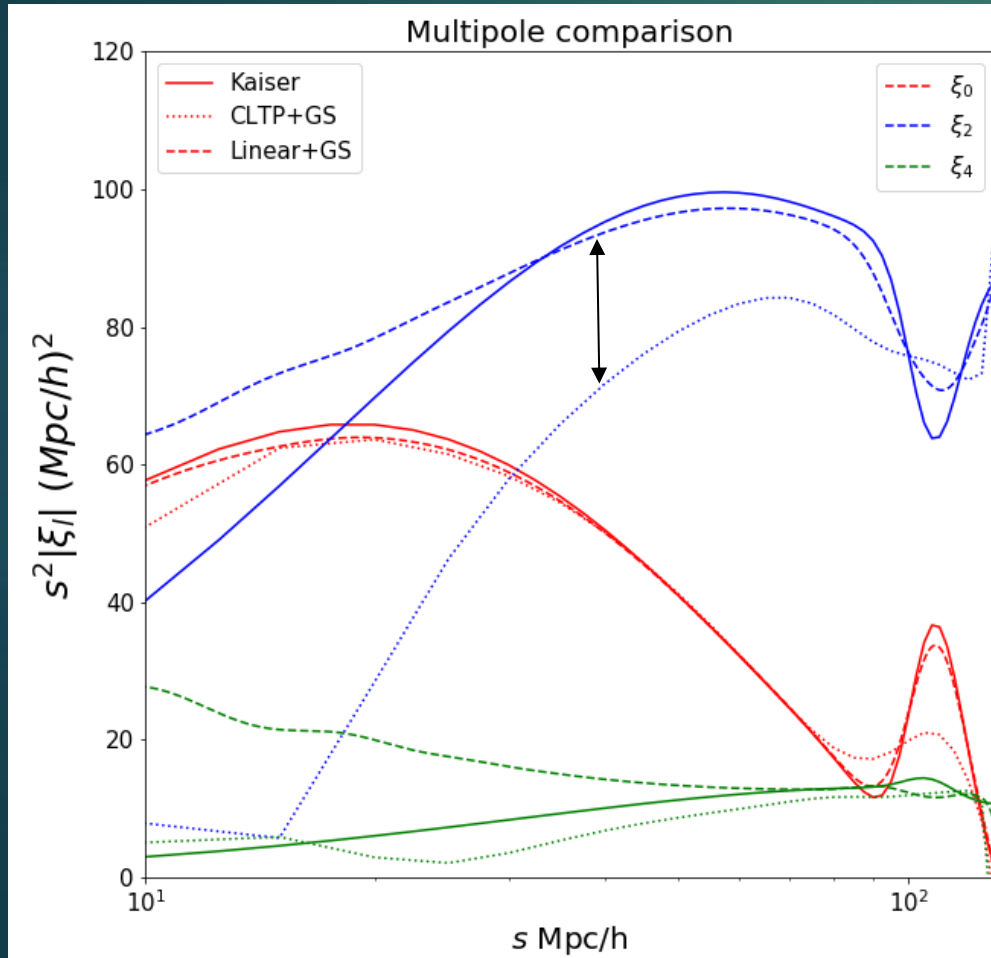
Linear GSM

CLPT GSM

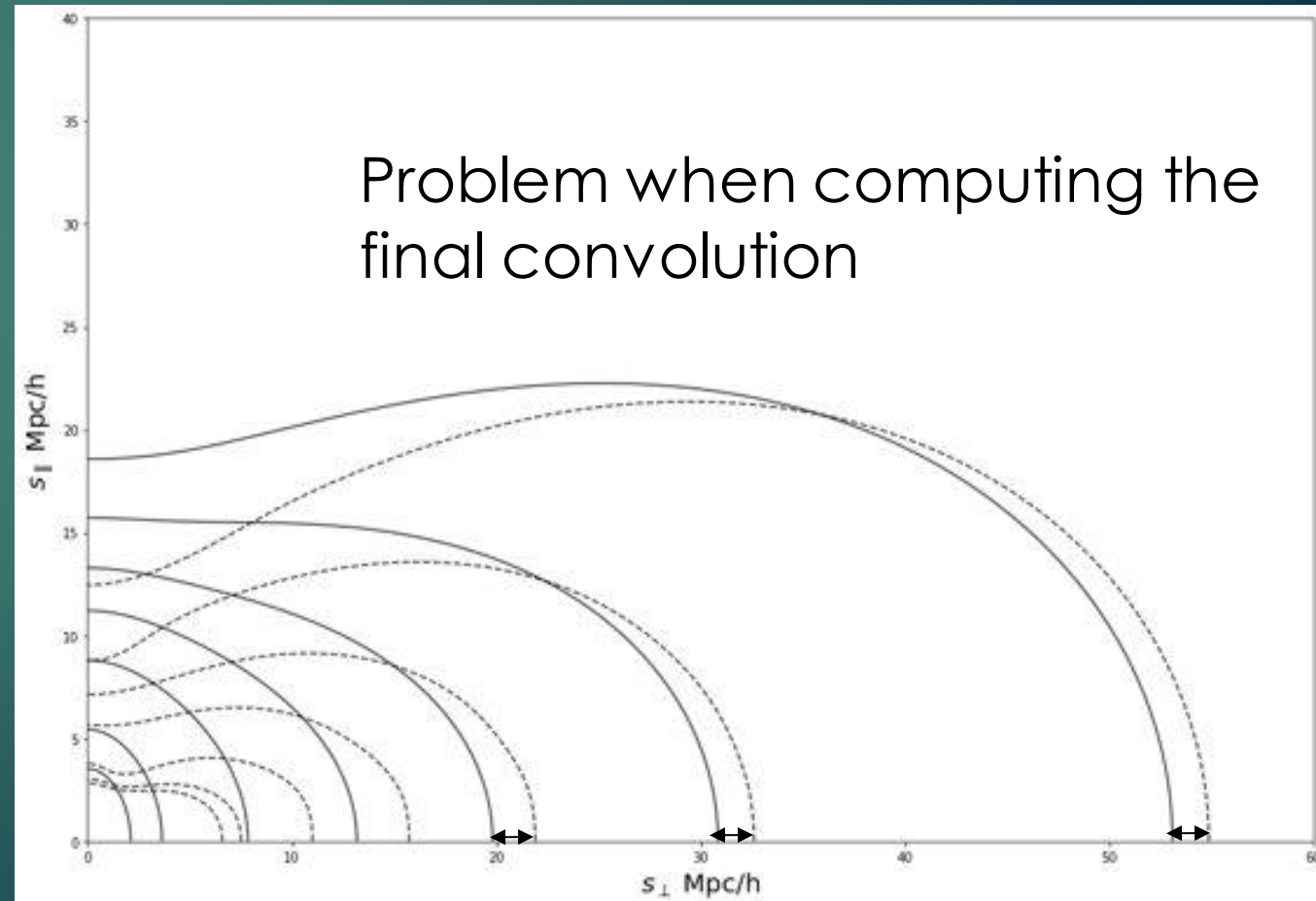


Code predictions

Multipole moments
comparison for different
predictions



2PCF comparison from linear GSM
(dashed line) and CLPT GSM (solid line)



Compare with simulation

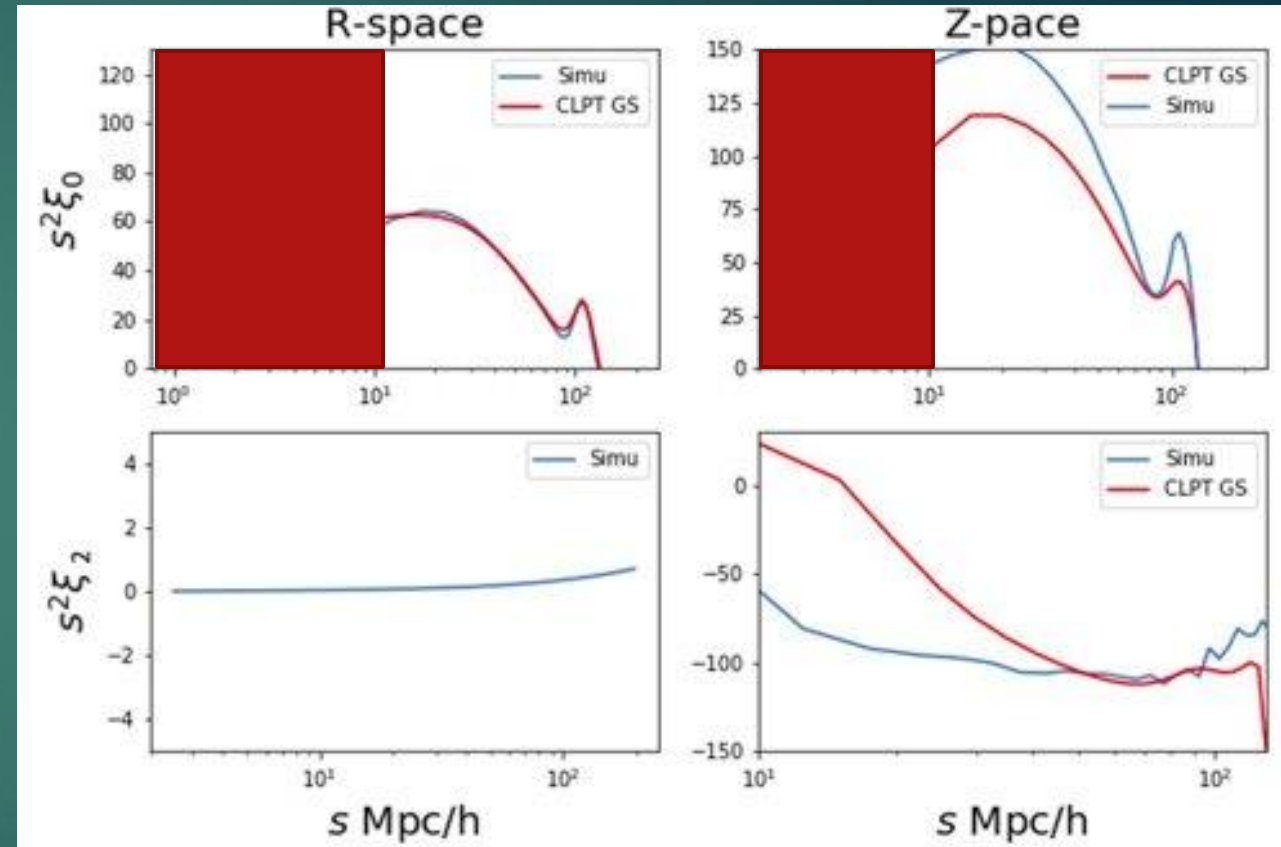
Simulation UNITS (Feng et al. 216)

$\Omega_m = 0.3089$, $h \equiv H_0/100 = 0.6774$ and $\sigma_8 = 0.8147$

Bias fitting

$$F' = 0.48$$

$$F'' = 0.05$$

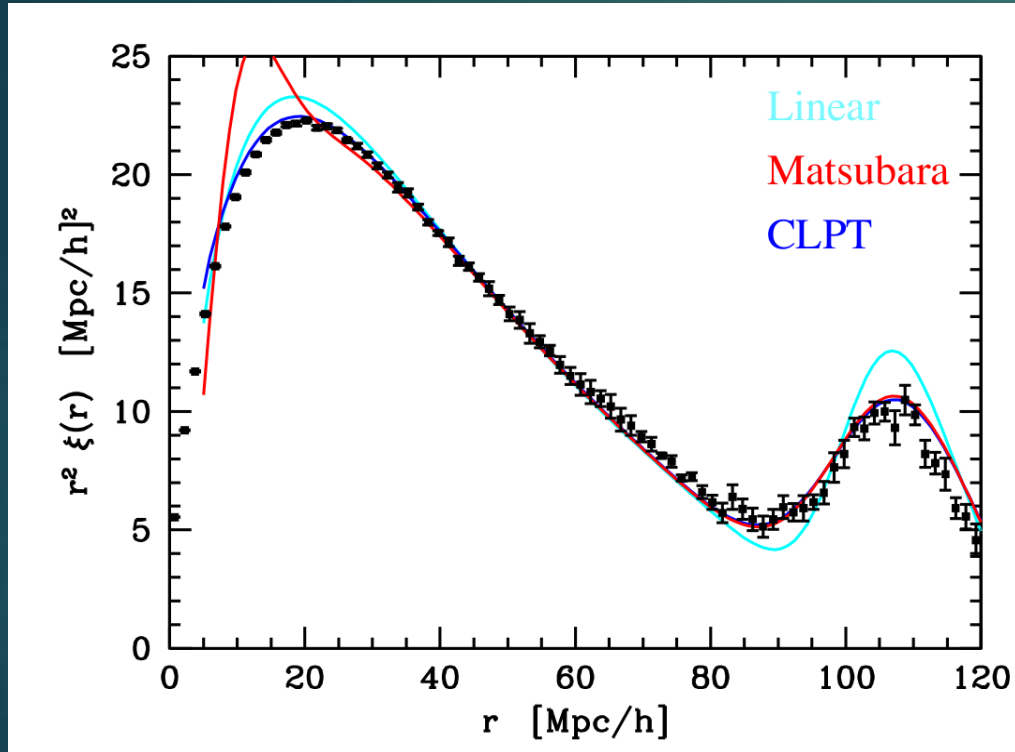


Box size 1 Gpc at $z=0$

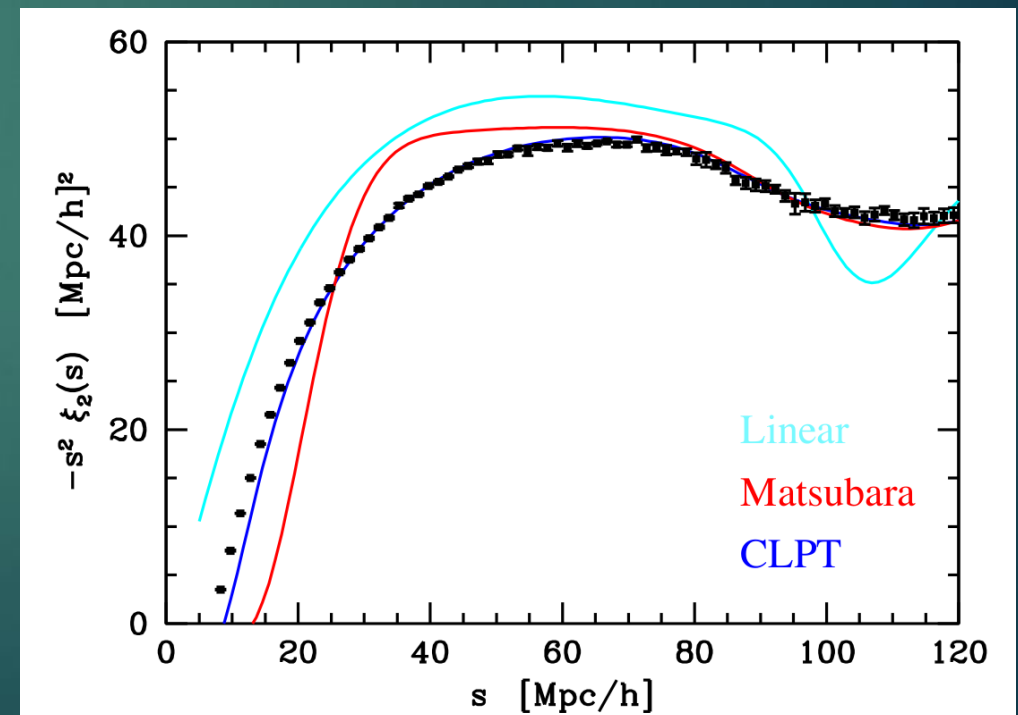
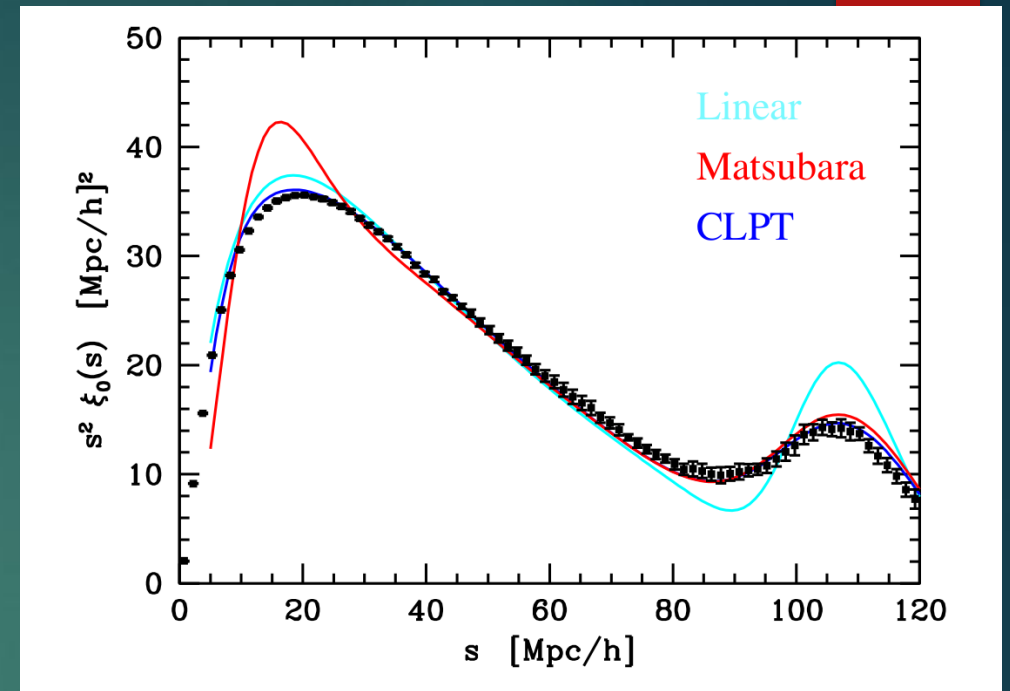
Landy-Szalay
estimator

$$\xi(r) = \frac{DD(r) - 2DR(r) + RR(r)}{RR(r)}$$

Expected results from CLPT



The GS/CLPT model allows reproducing RSD signal down to 20 Mpc/h (quasilinear regime) within 1%



Conclusion

- RSD is crucial to test gravity (on large scales) and cosmic acceleration
- Need reduce systematics from RSD non-linear modelling for precision cosmology: statistical errors under 1% for future redshift surveys such as EUCLID or DESI
- GS/CLPT is a robust RSD model that seems to meet the precision requirements for scales above 20 Mpc/h
- Still need to optimise the model with more detailed comparisons to with simulations

Thanks !

