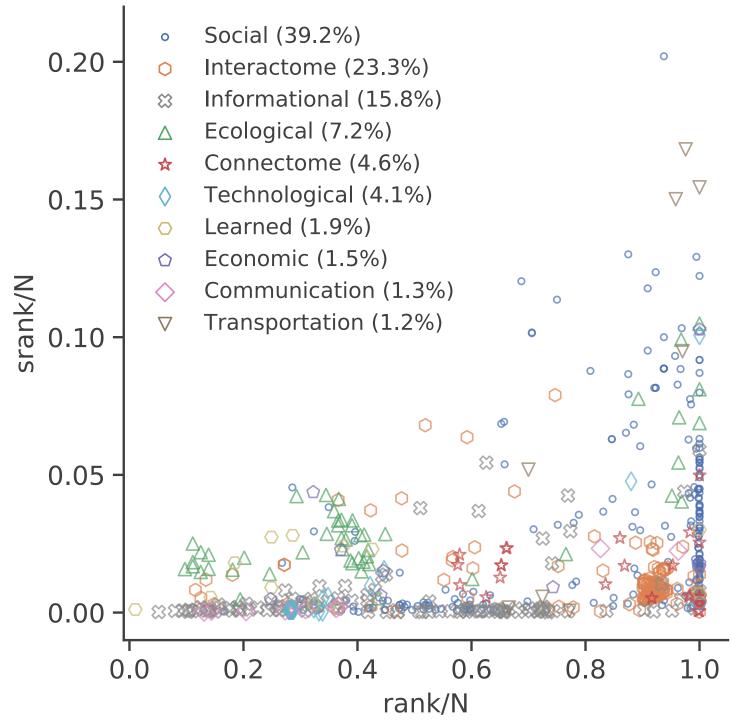
Results for 679 empirical networks (502 unweighted networks and 177 weighted networks) dowloaded from Netzschleuder.

Many empirical networks appear to have a low effective rank!

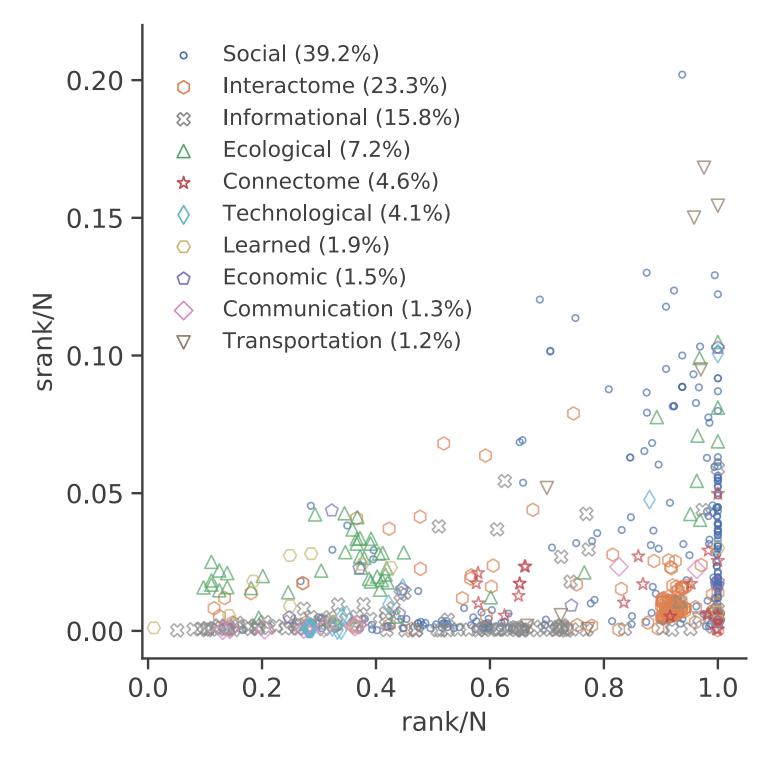


The effective ranks of adjacency matrices

But what does "low" mean?

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The impact of effective low rank on the dynamics

Many dynamics on networks have the form

$$\dot{\boldsymbol{x}} = rac{\mathrm{d} \boldsymbol{x}}{\mathrm{d} t} = \mathbf{g}(\boldsymbol{x}, \mathbf{W} \boldsymbol{x}) = \mathbf{g}(\boldsymbol{x}, \boldsymbol{y})$$

with $\boldsymbol{x} \in \mathbb{R}^N$.

Examples:

- \triangleright SIS (mean-field) : $\dot{x}_i = -d_i x_i + \gamma (1 x_i) y_i$
- $\qquad \qquad \text{Wilson-Cowan: } \dot{x}_i = -d_i x_i + (1-ax_i) \frac{1}{1+e^{-b(\gamma \, \textbf{\textit{y}}_i-c)}}$
- \triangleright Recurrent Neural Networks (RNN): $\dot{x}_i = -d_i x_i + \tanh(\gamma y_i + c_i)$
- ho Kuramoto-Sakaguchi: $\dot{z}_j=\mathrm{i}\omega_jz_j+\gamma\,e^{-\mathrm{i}lpha}\,y_j-\gamma\,e^{\mathrm{i}lpha}\,z_j^2\,ar{y}_j$ with $z_j=e^{\mathrm{i} heta_j}$
- Population dynamics: $\dot{x}_i = -dx_i + \gamma x_i y_i$ (Lotka-Volterra) $\dot{x}_i = -dx_i sx_i^2 + \gamma \frac{x_i y_i}{\alpha + y_i}$ $\dot{x}_i = a dx_i + bx_i^2 cx_i^3 + \gamma x_i y_i$
- for $i, j \in \{1, ..., N\}$ and $y_i = \sum_{j=1}^{N} W_{ij} x_j$.