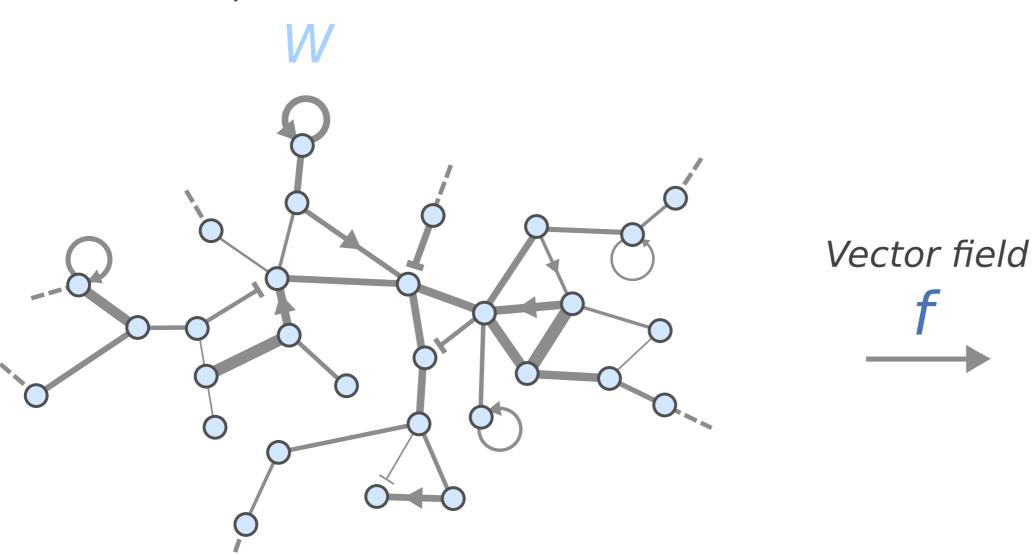
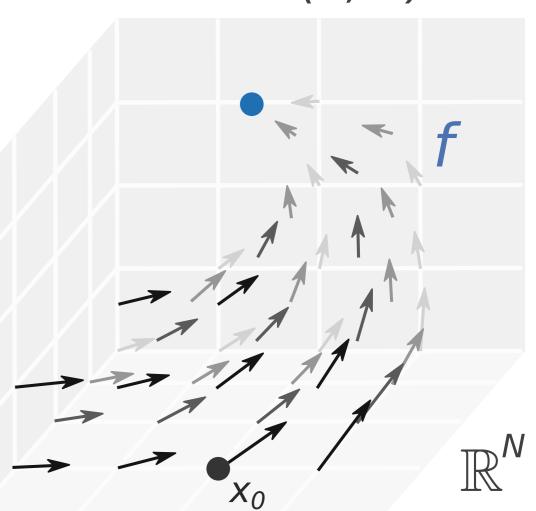
Complex network



High-dimensional dynamics

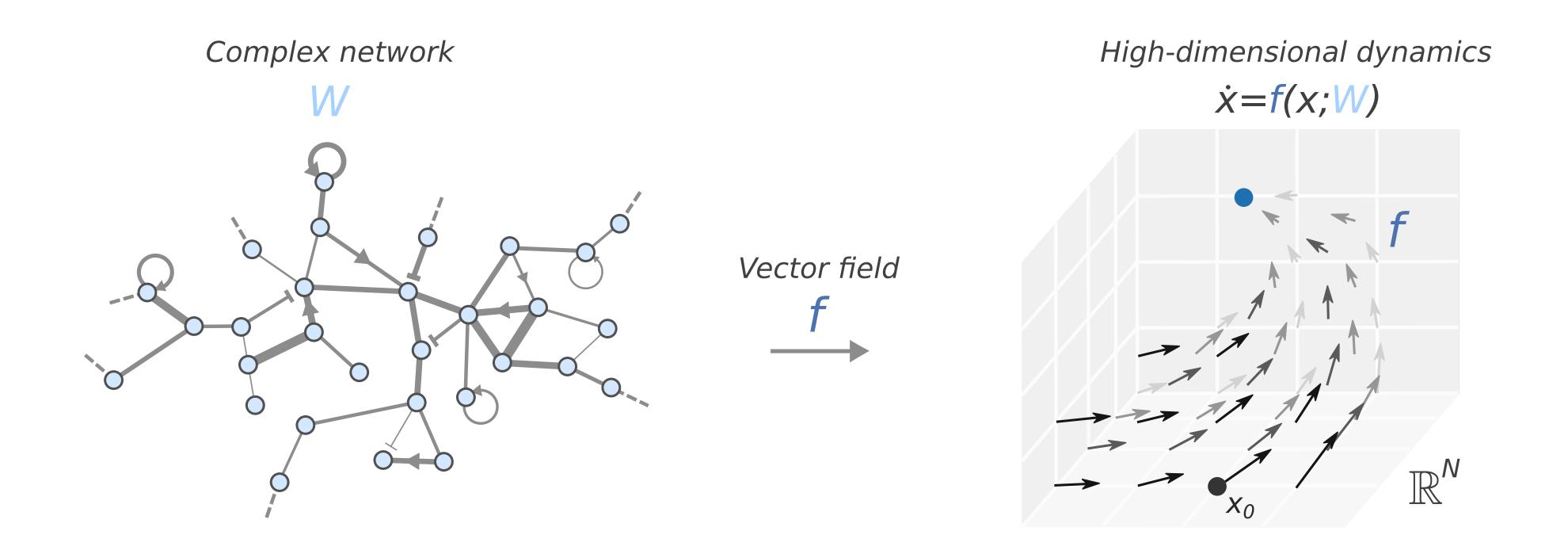
$$\dot{x} = f(x; W)$$



## Modeling the dynamics of complex systems

High-dimensional dynamics are hard to analyze and extracting meaningful intuitions from them is difficult. Most mathematical models involve low-dimensional representations of the networks and/or dynamical observables. Can we justify such a low-dimensional approach beyond mathematical and/or conceptual convenience?

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## The rank of adjacency matrices

Rank r of a matrix

- > number of linearly independent rows/columns
- ▷ dimension of the vector space generated by its rows/columns
- > number of nonzero singular values